

Context-dependent host-microbe interactions in stochastic environments

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Along with increases in average temperatures, global climate change is driving increases in the variability of precipitation events, temperature extremes, and droughts (1–3). Thus discerning the effects of variability on population dynamics and species interactions is pivotal to forecasting the future of ecological systems. Classic ecological theory predicts that long-term population growth rates will be reduced by environmental variability (4, 5). This stochastic variability means that populations can expect to experience both good and bad years. The long-term stochastic growth rate (λ_s), which is the long-run geometric mean of annual growth rates, captures this variability; the geometric mean will always be less than expected from the mean growth rate alone.

Following Lewontin and Cohen (4), λ_s can be approximated as:

$$\log(\lambda_s) \approx \log(\bar{\lambda}) - \frac{\sigma^2}{2\bar{\lambda}^2} \quad [1]$$

Where $\bar{\lambda}$ is the mean of annual population growth rates (λ_t) and σ^2 is the variance (4). Populations will increase over time if λ_s is greater than 1, and can be expected to decrease if λ_s is less than 1. Here, there are two pathways to increase λ_s : (1) increasing the mean growth rate, and/or (2) reducing the variance in growth rates. That both mean and variance can determine fitness underlies understanding of which aspects of a species' life history influence its success (6) and has important implications for population viability analysis (7). The degree to which species interactions contribute to effects on the variance in growth rates is an underexplored question (8).

Microbial symbioses are ubiquitous in nature and are crucial determinants of host fitness (9, 10) but their potential influence on responses to environmental variability is under-appreciated (11). Across a broad range of taxa, mutualistic host-associated microbes provide protection from environmental stresses including drought, extreme temperatures, and enemies (12–16). The role they play may be under-appreciated, and it can be difficult to quantify the net outcome of a given interaction because they are often viewed as being context-dependent where the magnitude of benefit depends on environmental conditions (17). Rather than considering context-dependence as some unexplainable intricacy of species interactions, environmental variation opens up the possibility for interaction strength to vary through time (18, 19) and to influence the variance of population growth rates.

Symbionts may provide benefits under harsh conditions when they are needed by their hosts, but be neutral or even costly under benign conditions (cite). Over time, this may lead symbiont-associated organisms to experience a reduction in variation in vital rates by reducing the frequency of extreme years (conceptual figure). Embracing context-dependence in this way, we reveal a novel mechanism by which symbionts can act as mutualists that may come to be of increasing importance in a more variable future.

Using long-term demographic data for grass species hosting *Epichloë* fungal endophytes, we test the hypothesis that context-dependent benefits of microbial symbionts buffer hosts from the fitness consequences of environmental variability. These endophytes are common among cool-season grasses and are primarily vertically transmitted from parent to seed (20). While they have been associated with contributing to drought tolerance for their hosts, these benefits are commonly context-dependent (21–23). And so, we ask first how fungal endophytes influence the mean and interannual variance of their hosts' vital rates; next, we ask if these vital rate effects buffer variance in fitness and, if so, what is the relative importance of variance buffering vs. mean effects in the overall fitness impact of the symbiosis. To answer these questions, we use data from experimental plots originally established in 2007 to build structured, stochastic population models for seven species of grass hosts (*Agrostis perennans*, *Elymus villosus*, *Elymus virginicus*, *Festuca subverticillata*, *Lolium arundinaceum*, *Poa alsodes* and *Poa sylvestris*). These long-term plots which are censused annually contain either naturally symbiotic plants or those which have had their symbionts experimentally removed. Across 14 years, the data contain 3X,XXXX individual transition years. Each annual census is a sample of weather variation, allowing us to construct climate-explicit population models, which we use to evaluate the importance of buffering under forecasted changes in the mean and variance of climate drivers.

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75 This paragraph is mostly talking off my head about results,
 76 but my idea is to include a brief statement of our results.*
 77 Across species, we find that variance buffering by endophytes
 78 contributes (percentage) to population growth rates. While
 79 the effect is generally weaker than effects on the mean, we
 80 found that buffering was common in the most sensitive vital
 81 rates, and was most important for xxx species with xxx life
 82 history.

83 Results

84 Discussion

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Table 1. Comparison of the fitted potential energy surfaces and ab initio benchmark electronic energy calculations

Species	CBS	CV	G3
1. Acetaldehyde	0.0	0.0	0.0
2. Vinyl alcohol	9.1	9.6	13.5
3. Hydroxyethylidene	50.8	51.2	54.0

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(x+y)^3 &= (x+y)(x+y)^2 \\
&= (x+y)(x^2+2xy+y^2) \\
&= x^3+3x^2y+3xy^2+x^3.
\end{aligned}
\tag{2}$$

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Materials and Methods

Natural history of grass-endophyte symbiosis. To study the effects of context-dependent microbial symbiosis, we focused on *Epichloë* fungal endophytes, which live in the aboveground tissue of many species of cool-season grasses and grow into their hosts' seeds where they can be transmitted to the next generation. This vertical transmission couples host and symbiont fitness and leads to the expectation that the interaction be mutualistic, else the fungi cause their host to be selected out of the population (24–26). While there are demonstrated benefits against herbivory (27) and under drought stress (28) in some species, these interactions are commonly context-dependent (21, 22).

Plant propagation and endophyte removal. Seeds from naturally infected populations of seven species of cool-season grasses (*Agrostis perennans*, *Elymus villosus*, *Elymus virginicus*, *Festuca subverticillata*, *Lolium arundinaceum*, *Poa alsodes*, and *Poa sylvestris*) were collected during the 2006 growing season from Lilly Dickie Woods (39.238533, -86.218150) and the Bayles Road Teaching and Research Preserve (39.220167, -86.542683) in Brown Co. IN. Seeds with shared maternal ancestry were experimentally disinfected with heat treatments (6d in a drying oven at 60° C for *E. villosus*, *E. virginicus*, *F. subverticillata*, and *L. arundinaceum*; 7d in a drying oven at 60° C for *P. alsodes*, and *P. sylvestris*; and 12 min. in a hot water bath at 60° C for *A. perennans*)[†] or left naturally infected to reduce confounding genotype effects. Seeds were surface sterilized with bleach and cold stratified for ??? weeks, then germinated in a growth chamber before being transferred to the greenhouse at Indiana University and allowed to grow for XXXX weeks. We confirmed the endophyte status of these plants using leaf peels, where tissue from the leaf sheath is stained with aniline blue dye

and examined for the presence of fungal hyphae (29). Then, we established the experimental plots with **vegetatively propagated clones of similar sizes from the plants**[‡] to reduce the potential for negative side effects of heat treatments (30).

Experimental design and data collection. In 2007[§], we established 10 3x3 plots for *L. arundinaceum*, *F. subverticillata*, *E. virginicus*, and *E. villosus* and 18 plots for *P. alsodes* and *P. sylvestris*. For each species, an equal number of plots were randomly assigned to each endophyte status, E+ or E-, and was planted with only symbiotic or symbiont-free plants respectively. Each plot was planted with 20 evenly spaced individuals and each plant marked with aluminum tags.

During each Summer starting in 2007, we censused all original transplants and any recruits for survival, growth and reproduction. After clearing out leaf litter, for each plant alive in the previous year, we marked its survival. We measured the size of each plant as a count of the number of tillers. Further, we collected reproductive data by counting the number of reproductive tillers, and then counting the number of seed-bearing spikelets on up to three of those reproductive tillers. In 2009 year, we took additional counts of seeds per inflorescence. Together, we use these measurements to estimate seed production. In each plot, we also survey for and tag any unmarked individuals. New recruits are typically have one tiller and are non-reproductive, but we also find and tag any individuals that may have been missed in previous censuses.

We typically expect plots of each endophyte status to maintain their status as the fungus is almost entirely vertically transmitted, and plots are spaced at least XX m apart, limiting the possibility for unwanted dispersal between plots or horizontal transmission of the fungus. Seeds from reproductive individuals are opportunistically taken and scored for their endophyte status. Overall, these scores reflect a 97.5% faithfulness of recruits to their expected endophyte status across species and plots (Supplement data).

In sum, this individual-level demographic dataset covers 14 years and contains 30,XXXX individual transition-years.[¶]

Demographic modeling. Armed with this demographic data, we next constructed size-structured, stochastic population models. This demographic model describes transitions between sizes (measured as a count of tillers) from one year to the next. For all species, we include a 1 year reproductive delay in the population model following the observation that these newly recruited plants are rarely observed flowering in their first year.

$$\mathbf{n}_{t+1} = \mathbf{A}\mathbf{n}_t \tag{3}$$

where \mathbf{n}_{t+1} is a vector of abundances across sizes in year $t+1$ for each species and endophyte status.

$$\mathbf{n}_{t+1} = \begin{bmatrix} size_1 \\ \vdots \\ size_N \end{bmatrix} \tag{4}$$

and \mathbf{A} is expressed as a $N+1 \times N+1$ matrix:

$$\mathbf{A} = \begin{bmatrix} size_{sldg} & \cdot & \cdot & \cdot & size_{sldgN} \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & size_N \end{bmatrix} \tag{5}$$

[†] not sure this happened

[§] dates?

[¶] Move this earlier and also mention at the end of intro. The total number of plant-years is impressive.

Model description and estimation. We modeled the effect of endophyte symbiosis on mean and variance of vital rates by fitting generalized linear mixed models (GLMM) to the long-term data with year and plot random effects. We fit all vital rate models in a hierarchical Bayesian framework using Rstan (?), allowing us to propagate uncertainty from the vital rate estimates to our population model (31).

The probability of survival and flowering are recorded as successes or failures and consequently are modeled as Bernoulli processes. We modeled growth (measured as the number of tillers in year $t+1$), the number of flowering tillers, and the number of spikelets per inflorescence with the zero-truncated Poisson-Inverse Gaussian distribution. Where possible, each of these size dependent vital rates are modeled with the same structure of linear predictor (μ)

For example, growth ($G_{i,t1}$) of a given individual (i) in year $t+1$ is modeled as:

$$G_{i,t1} \sim P(IG(\mu_{s,e}, \lambda_{s,e})) \quad [6]$$

Similarly, survival $S_{i,t1}$ in year $t+1$ is modeled as:

$$S_{i,t1} \sim \text{Bernoulli}(\mu_{s,e}) \quad [7]$$

Where μ , for each species (s), is a linear function of the logarithm of plant size in year $t(t)$, the plot level endophyte status (e), the status as an initial experimental transplant plant(r), along with random effects to account for plot(p), and year random effects specific to each species and endophyte status. Thus μ can be written:

$$\begin{aligned} \mu_{s,e} &= \beta_s^1 + \beta_s^2 \log(\text{size}_t) + \beta_{s,e}^3 + \beta_r^4 \\ &\quad + \tau + \rho \\ \tau &\sim N(0, \sigma_{s,e}) \\ \rho &\sim N(0, \sigma_p) \end{aligned} \quad [8]$$

For all species, we account for a reproductive delay by modeling seedling growth and survival separately from adult growth and survival. Seedlings are those plants that are recruited into the plot in a given year, and typically have only one tiller. This means that they do not have size dependence. So, for seedlings, growth ($G_{1,t1}^{sdlg}$) is modelled as:

$$G_{1,t1}^{sdlg} \sim P(IG(\mu_{s,e}^{sdlg}, \lambda_{s,e})) \quad [9]$$

Similarly, survival ($S_{i,t1}^{sdlg}$) in year $t+1$ is modeled as:

$$S_{i,t1}^{sdlg} \sim \text{Bernoulli}(\mu_{s,e}^{sdlg}) \quad [10]$$

Here, $\mu_{s,e}^{sdlg}$ is the linear function for these seedling specific vital rates. It does not include size-dependence or an effect to account for the initial benefits of greenhouse rearing.

$$\begin{aligned} \mu_{s,e}^{sdlg} &= \beta_s^1 + \beta_{s,e}^3 \\ &\quad + \tau + \rho \\ \tau &\sim N(0, \sigma_{s,e}) \\ \rho &\sim N(0, \sigma_p) \end{aligned} \quad [11]$$

As a default, we ran each vital rate model for 2500 warm-up and 2500 MCMC sampling iterations with three chains using rStan. We assessed model convergence with trace plots of posterior chains and other model diagnostic statistics (). For those models that show poor convergence, we extend the MCMC sampling to include 5000 warm-up and 5000 sampling iterations; this was only necessary for seedling growth in our climate-implicit analysis. For each of these vital rate models, we graphically check model fit with posterior predictive checks using simulated data from 500 posterior draws and comparing with the observed data (See supplement?). These checks provide evidence that our models are accurately recreating size-specific growth, survival, and reproduction patterns in our data across endophyte treatments.

We calculate the effect of endophytes on mean and variance in growth rates by assembling matrix models following equation [3] with and without endophyte effects for each year based on 500 posterior draws from our vital rate models.

Stochastic growth rate simulation experiment. We decompose the contribution of endophyte to long-termThe stochastic growth rate is approximated as the long-run expectation of annual growth rates (32).

$$\log(\lambda_s) E[\log(\Sigma(\mathbf{n}_{t+1})/\Sigma(\mathbf{n}_t))] \quad [12]$$

Estimating climate drivers of environmental context-dependence.

Climate data.

Climate-explicit Model description and estimation.

Climate-explicit Model assessment.

Forecasting under alternative climate forcings. We used statistics

ACKNOWLEDGMENTS. Please include your acknowledgments here, set in a single paragraph. Please do not include any acknowledgments in the Supporting Information, or anywhere else in the manuscript.

- IPCC (Intergovernmental Panel on Climate Change). *Managing the risks of extreme events and disasters to advance climate change adaptation: special report of the intergovernmental panel on climate change. Special Report.* Cambridge University Press, 2012.
- Sonia Seneviratne, Neville Nicholls, David Easterling, Clare Goodess, Shinjiro Kanae, James Kossin, Yali Luo, Jose Marengo, Kathleen McInnes, Mohammad Rahimi, et al. Changes in climate extremes and their impacts on the natural physical environment. 2012.
- Thomas F Stocker, Dahe Qin, G-K Plattner, Lisa V Alexander, Simon K Allen, Nathaniel L Bindoff, F-M Br  on, John A Church, Ulrich Cubasch, Seita Emori, et al. Technical summary. In *Climate change 2013: the physical science basis. Contribution of Working Group I to the Fifth Assessment Report of the Intergovernmental Panel on Climate Change*, pages 33–115. Cambridge University Press, 2013.
- R. C. Lewontin and D. Cohen. On Population Growth in a Randomly Varying Environment. *Proceedings of the National Academy of Sciences*, 62(4):1056–1060, April 1969. ISSN 0027-8424, 1091-6490. . URL <https://www.pnas.org/content/62/4/1056>. Publisher: National Academy of Sciences Section: Biological Sciences: Zoology.
- Shripad D. Tuljapurkar. Population dynamics in variable environments. III. Evolutionary dynamics of r -selection. *Theoretical Population Biology*, 21(1):141–165, February 1982. ISSN 0040-5809. . URL <http://www.sciencedirect.com/science/article/pii/0040580982900107>.
- Catherine A Pfister. Patterns of variance in stage-structured populations: evolutionary predictions and ecological implications. *Proceedings of the National Academy of Sciences*, 95(1):213–218, 1998.
- Eric S Menges. Population viability analysis for an endangered plant. *Conservation biology*, 4(1):52–62, 1990.
- Christoffer H. Hilde, Marl  ne Gamelon, Bernt-Erik S  tther, Jean-Michel Gaillard, Nigel G. Yoccoz, and Christophe P  labon. The Demographic Buffering Hypothesis: Evidence and Challenges. *Trends in Ecology & Evolution*, 0(0), March 2020. ISSN 0169-5347. . URL [https://www.cell.com/trends/ecology-evolution/abstract/S0169-5347\(20\)30050-1](https://www.cell.com/trends/ecology-evolution/abstract/S0169-5347(20)30050-1). Publisher: Elsevier.
- RJ Rodriguez, JF White Jr, Anne E Arnold, and a RS and Redman. Fungal endophytes: diversity and functional roles. *New phytologist*, 182(2):314–330, 2009.
- Margaret McFall-Ngai, Michael G Hadfield, Thomas CG Bosch, Hannah V Carey, Tomislav Domazet-Lo  , Angela E Douglas, Nicole Dubilier, Gerard Eberl, Tadashi Fukami, Scott F Gilbert, et al. Animals in a bacterial world, a new imperative for the life sciences. *Proceedings of the National Academy of Sciences*, 110(9):3229–3236, 2013.
- Jennifer A Rudgers, Michelle E Afkhami, Lukas Bell-Dereske, Y Anny Chung, Kerri M Crawford, Stephanie N Kivlin, Michael A Mann, and Martin A Nu  ez. Climate disruption of plant-microbe interactions. *Annual review of ecology, evolution, and systematics*, 51(1), 2020.
- Jacob A Russell and Nancy A Moran. Costs and benefits of symbiont infection in aphids: variation among symbionts and across temperatures. *Proceedings of the Royal Society B: Biological Sciences*, 273(1586):603–610, 2006.
- Jeremy C Brownlie and Karyn N Johnson. Symbiont-mediated protection in insect hosts. *Trends in microbiology*, 17(8):348–354, 2009.
- Stephanie N Kivlin, Sarah M Emery, and Jennifer A Rudgers. Fungal symbionts alter plant responses to global change. *American Journal of Botany*, 100(7):1445–1457, 2013.
- Chris Corbin, Eleanor Rose Heyworth, Julia Ferrarri, and Gregory DD Hurst. Heritable symbionts in a world of varying temperature. *Heredity*, 118(1):10–20, 2017.
- Kenneth D Hoadley, Allison M Lewis, Drew C Wham, D Tye Pettay, Chris Grasso, Robin Smith, Dustin W Kemp, Todd C LaJeunesse, and Mark E Warner. Host-symbiont combinations dictate the photo-physiological response of reef-building corals to thermal stress. *Scientific Reports*, 9(1):1–15, 2019.
- Scott A Chamberlain, Judith L Bronstein, and Jennifer A Rudgers. How context dependent are species interactions? *Ecology letters*, 17(7):881–890, 2014.
- Pedro Jordano. Spatial and temporal variation in the avian-frugivore assemblage of prunus mahaleb: patterns and consequences. *Oikos*, pages 479–491, 1994.
- Ian Billick and Kirk Tonkel. The relative importance of spatial vs. temporal variability in generating a conditional mutualism. *Ecology*, 84(2):289–295, 2003.
- Gregory P Cheplick, Stanley Faeth, and Stanley H Faeth. *Ecology and evolution of the grass-endophyte symbiosis*. OUP USA, 2009.

21. Gregory P Cheplick. Recovery from drought stress in *Iolium perenne* (poaceae): are fungal endophytes detrimental? *American Journal of Botany*, 91(12):1960–1968, 2004.
22. S Kannadan and JA Rudgers. Endophyte symbiosis benefits a rare grass under low water availability. *Functional Ecology*, 22(4):706–713, 2008.
23. Facundo A Decunta, Luis I Pérez, Dariusz P Malinowski, Marco A Molina-Montenegro, and Pedro E Gundel. A systematic review on the effects of epichloë fungal endophytes on drought tolerance in cool-season grasses. *Frontiers in plant science*, 12:644731, 2021.
24. Paul EM Fine. Vectors and vertical transmission: an epidemiologic perspective. *Annals of the New York Academy of Sciences*, 266(1):173–194, 1975.
25. AE Douglas. Host benefit and the evolution of specialization in symbiosis. *Heredity*, 81(6):599–603, 1998.
26. Jennifer A Rudgers, Michelle E Afkhami, Megan A Rúa, Andrew J Davitt, Samantha Hammer, and Valérie M Huguet. A fungus among us: broad patterns of endophyte distribution in the grasses. *Ecology*, 90(6):1531–1539, 2009.
27. D Brem and A Leuchtman. Epichloë grass endophytes increase herbivore resistance in the woodland grass *brachypodium sylvaticum*. *Oecologia*, 126(4):522–530, 2001.
28. Cyd E Hamilton and Taryn L Bauerle. A new currency for mutualism? fungal endophytes alter antioxidant activity in hosts responding to drought. *Fungal Diversity*, 54(1):39–49, 2012.
29. Charles W Bacon and James F White. Stains, media, and procedures for analyzing endophytes. In *Biotechnology of endophytic fungi of grasses*, pages 47–56. CRC Press, 2018.
30. Jennifer A Rudgers and Angela L Swafford. Benefits of a fungal endophyte in *elymus virginicus* decline under drought stress. *Basic and Applied Ecology*, 10(1):43–51, 2009.
31. Bret D Elderder and Tom EX Miller. Quantifying demographic uncertainty: Bayesian methods for integral projection models. *Ecological Monographs*, 86(1):125–144, 2016.
32. SD Tuljapurkar and Steven Hecht Orzack. Population dynamics in variable environments i. long-run growth rates and extinction. *Theoretical Population Biology*, 18(3):314–342, 1980.

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