

Señales y Sistemas: Laboratorio Series de Fourier.

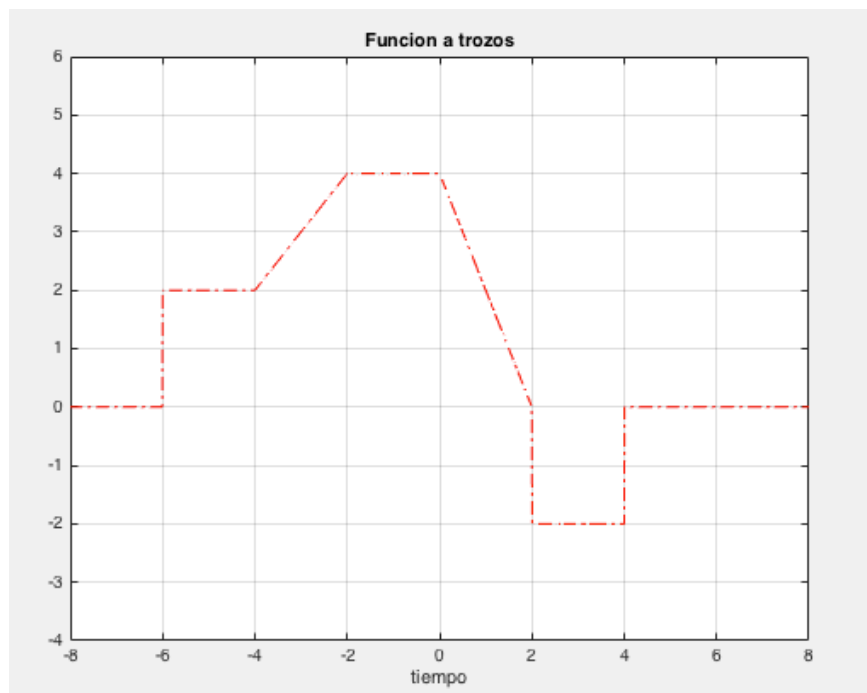
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- Graficar la función a trozos correspondiente.

$$f(x) = \begin{cases} 2; & -6 \leq t < -4 \\ t + 6; & -4 \leq t < -2 \\ 4; & -2 \leq t < 0 \\ -2t + 4; & 0 \leq t < 2 \\ -2; & 2 \leq t < 4 \\ 2; & 4 \leq t < 6 \\ 0; & \text{otro valor} \end{cases}$$

```
% Julián Esteban Nieto Díaz
clc
clear all
% 1) escribir señal x(t), como una función a trozos

t= linspace(-8,8,2000);
f= (2).*( (-6<=t) & (t<-4) ) + (t+6).*( (-4<=t) & (t<-2) ) + (4).*( (-2<=t) & (t<0) ) + (-2*t+4).*( (0<=t) & (t<2) ) + (-2).*( (2<=t) & (t<4) ) + (2).*( (4<=t) & (t<6) );
figure
plot(t,f,'-r')
xlabel('tiempo')
grid
hold on
axis([-8 8 -4 6])
```



2)Coeficientes de fourier

```
% A0
syms t
T=12;
Ao= (1/T)*(int((2),t,-6,-4)+int((t+6),t,-4,-2)+int((4),t,-2,0)+int((-2*t+4),t,0,2)+int((-2),t,2,4)+int((2),t,4,2));
% e= int((-2),t,2,4);f= int((2),t,4,2);
% s=a+b+c+d+e+f; Ao=(1/T)*s;
disp('cte Ao es:');disp(Ao);
```

cte Ao es:
7/6

Ak

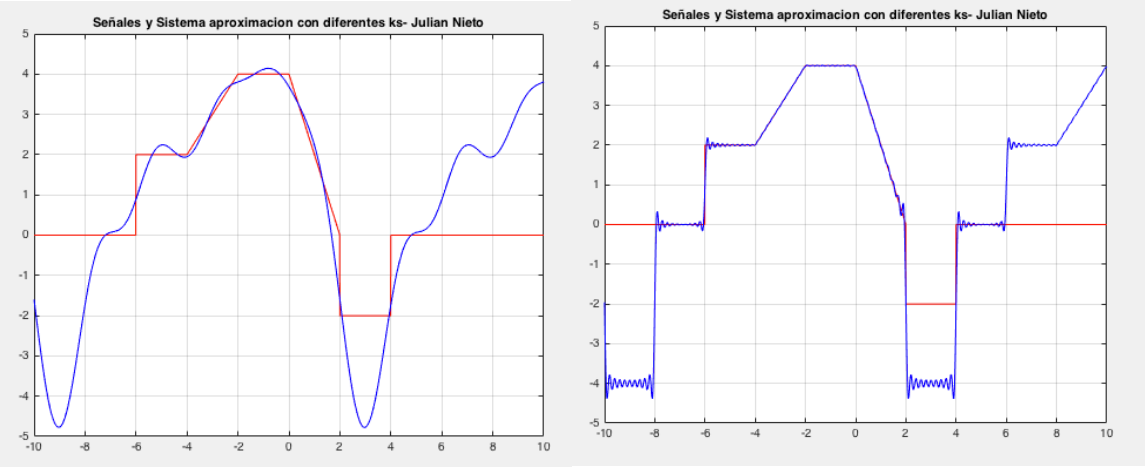
```
syms t k
T=12;
w=(2*pi)/T;
r=w*k*t;
%acos=int((2)*cos(r),t,-6,-4);bcos=int((t+6)*cos(r),t,-4,-2);ccos=int((4)*cos(r),t,-2,0);
%dcos=int((-2*t+4)*cos(r),t,0,2);ecos= int((-2)*cos(r),t,2,4);fcos= int((2)*cos(r),t,4,2);
%scos=acos+bcos+ccos+dcos+ecos+fcos;Ak=(2/T)*scos;
Ak=(2/T)*(int((2)*cos(r),t,-6,-4)+int((t+6)*cos(r),t,-4,-2)+int((4)*cos(r),t,-2,0)+int((-2*t+4)*cos(r),t,0,2)+int((-2)*cos(r),t,2,4)+int((2)*cos(r),t,4,2));
disp('cte Ak es:');disp(Ak);

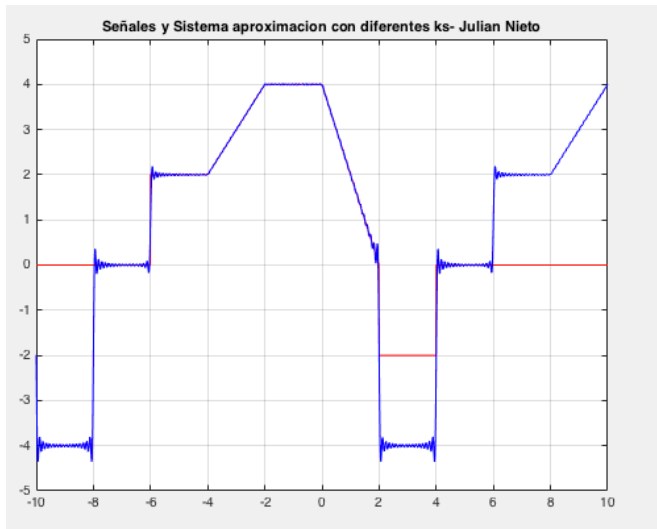
%bk
%asen=int((2)*sin(r),t,-6,-4);bsen=int((t+6)*sin(r),t,-4,-2);csen=int((4)*sin(r),t,-2,0);
%dsen=int((-2*t+4)*sin(r),t,0,2);esen= int((-2)*sin(r),t,2,4);fsen= int((2)*sin(r),t,4,2);
%ssen=asen+bsen+csen+dsen+esen+fsen;bk=(2/T)*ssen;
bk=(2/T)*(int((2)*sin(r),t,-6,-4)+int((t+6)*sin(r),t,-4,-2)+int((4)*sin(r),t,-2,0)+int((-2*t+4)*sin(r),t,0,2)+ int((-2)*sin(r),t,2,4)+ int((2)*sin(r),t,4,2));
disp('cte bk es:');disp(bk);
```

cte Ak es:
 $(4*\sin((\pi*k)/3))/(k*\pi) + (2*(\sin(\pi*k) - \sin((2*\pi*k)/3)))/(k*\pi) + (4*(\sin((\pi*k)/3) - \sin((2*\pi*k)/3)))/(k*\pi) + (12*\sin((\pi*k)/3)^2)/(k^2*\pi^2) + (12*\sin((\pi*k)/3) - \cos((2*\pi*k)/3))/(k*\pi) - (4*(3*\sin((\pi*k)/3) - \pi*k))/(k^2*\pi^2) - (36*\sin((\pi*k)/3) - 72*\cos((\pi*k)/3)*\sin((\pi*k)/3) + k*(24*\pi*\cos((\pi*k)/3) - 12*\pi*k))/k^3$

cte bk es:
 $(2*(\cos(\pi*k) - \cos((2*\pi*k)/3)))/(k*\pi) - (4*(3*\sin((\pi*k)/3) - \pi*k))/(k^2*\pi^2) - (36*\sin((\pi*k)/3) - 72*\cos((\pi*k)/3)*\sin((\pi*k)/3) + k*(24*\pi*\cos((\pi*k)/3) - 12*\pi*k))/k^3$

con k=5,60,100





```

clc
clear all
disp('Serie de Fourier- Julian Nieto')
N = input('Numero de armonicos deseados');
x=-10:0.01:10;T=12;sum=0;a0=7/6;w=(2*pi)/T;
for k=1:N
    r=k*w*x;
    a(k)=(4*sin((pi*k)/3))/(k*pi) + (2*(sin(pi*k) - sin((2*pi*k)/3)))/(k*pi) + (4*(sin((pi*k)/3) - sin((2*pi*k)/3)))/(k*pi) + (12*sin((pi*k)/3)^2)/(k^2*pi^2);
    b(k)= (2*(cos(pi*k) - cos((2*pi*k)/3)))/(k*pi) - (4*(3*sin((pi*k)/3) - pi*k))/(k^2*pi^2) - (36*sin((pi*k)/3) - 72*cos((pi*k)/3)*sin((pi*k)/3))/k^3;
    sum=sum+(a(k)*cos(r)+b(k)*sin(r));
end

sfour= a0+sum;

f= (2).*((-6<=x)&(x<-4))+(x+6).*((-4<=x) &(x<-2))+(4).*((-2<=x)&(x<0))+(-2*x+4).*((0<=x)&(x<2))+(-2).*((2<=x)&(x<4))+(2).*((4<=x)&(x<8));
plot(x,f,'r',x,sfour,'b')
grid on
title('Señales y Sistema aproximacion con diferentes ks- Julian Nieto')

% a0= 7/6
%ak=(4*sin((pi*k)/3))/(k*pi) + (2*(sin(pi*k) - sin((2*pi*k)/3)))/(k*pi) + (4*(sin((pi*k)/3) - sin((2*pi*k)/3)))/(k*pi) + (12*sin((pi*k)/3)^2)/(k^2*pi^2);
%bk=(2*(cos(pi*k) - cos((2*pi*k)/3)))/(k*pi) - (4*(3*sin((pi*k)/3) - pi*k))/(k^2*pi^2) - (36*sin((pi*k)/3) - 72*cos((pi*k)/3)*sin((pi*k)/3))/k^3;

```

en el command prompt

```

Serie de Fourier- Julian Nieto
Numero de armonicos deseados60
>> |

```

```

Serie de Fourier- Julian Nieto
Numero de armonicos deseados100
>>

```