



Sienna



**SOLVING THE MARKET-TO-MARKET  
PROBLEM IN LARGE SCALE POWER SYSTEMS**

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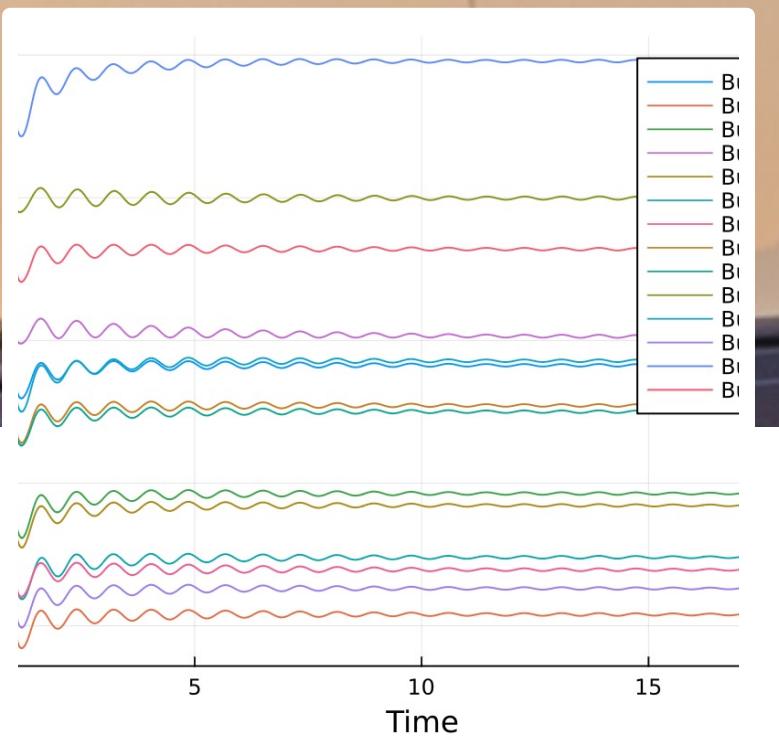
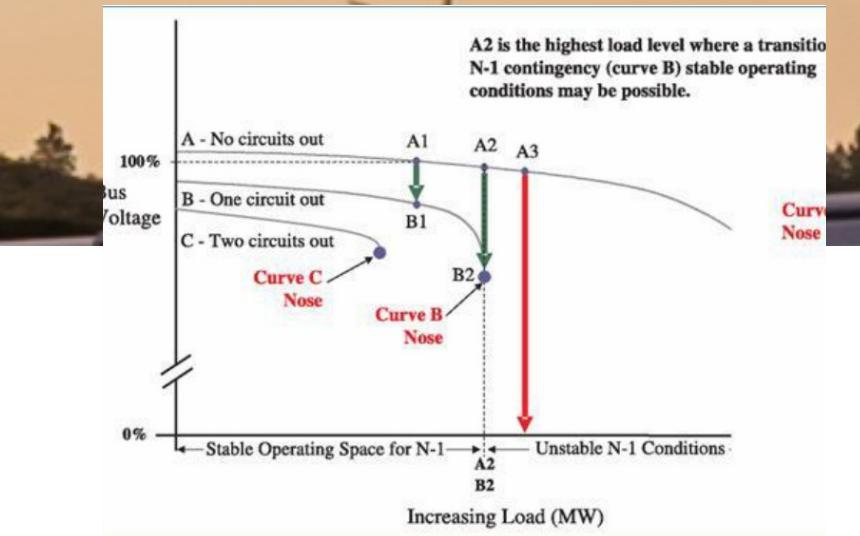
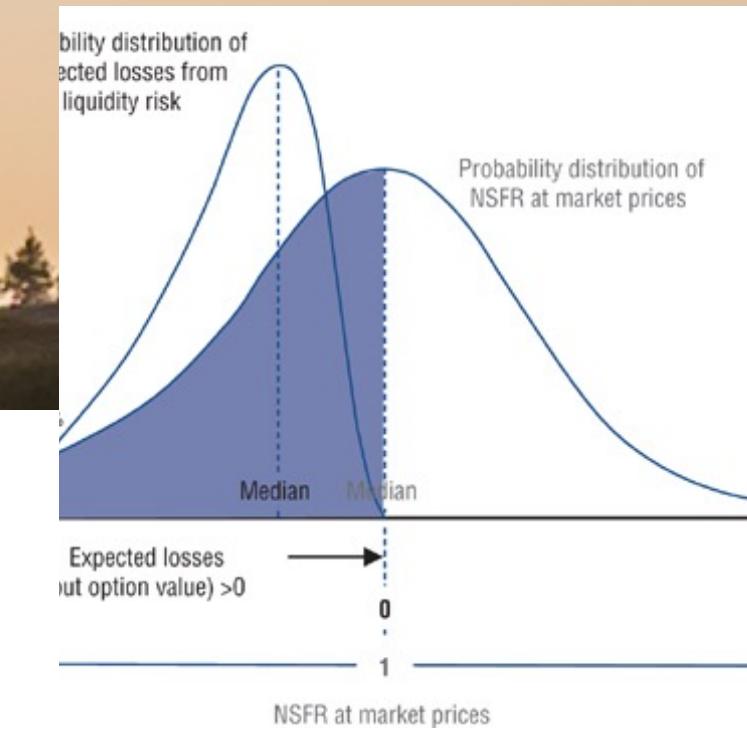
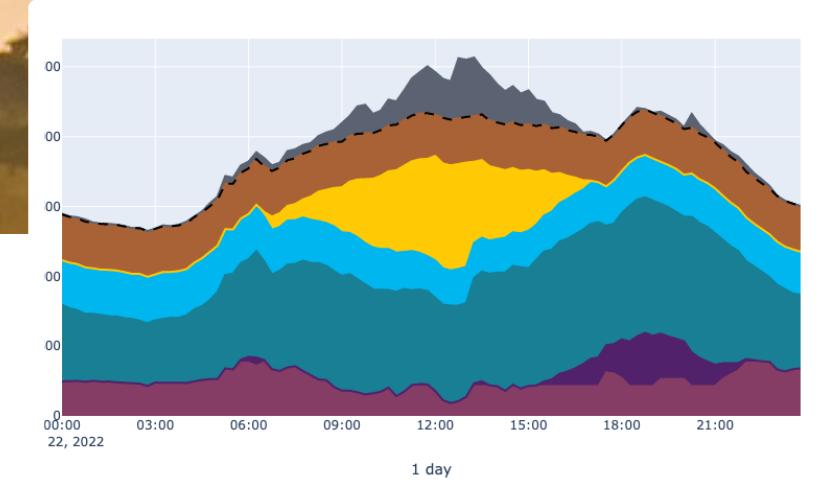
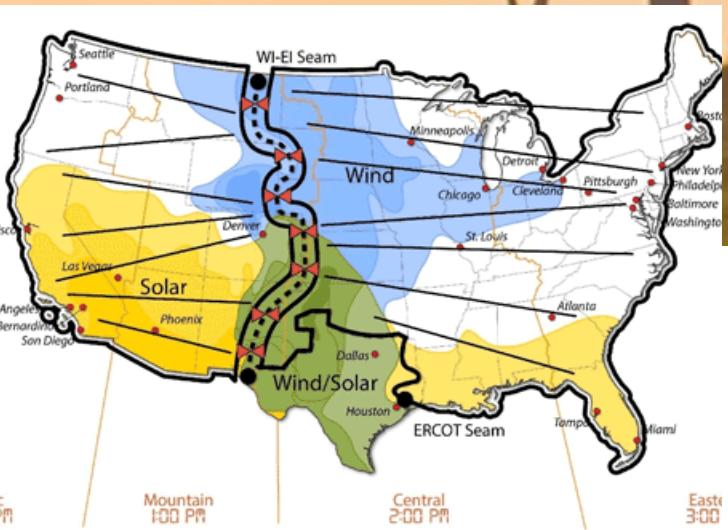


NREL's Grid Planning and Analysis Center

bridges engineering, economics, and equity

to advance the grid of the future

# Bulk Power Systems Modeling for Decision Making



Build

What to build?  
Where and When

Operate

Can the planned  
system operate?

Adequate

Is supply sufficient  
under all conditions?

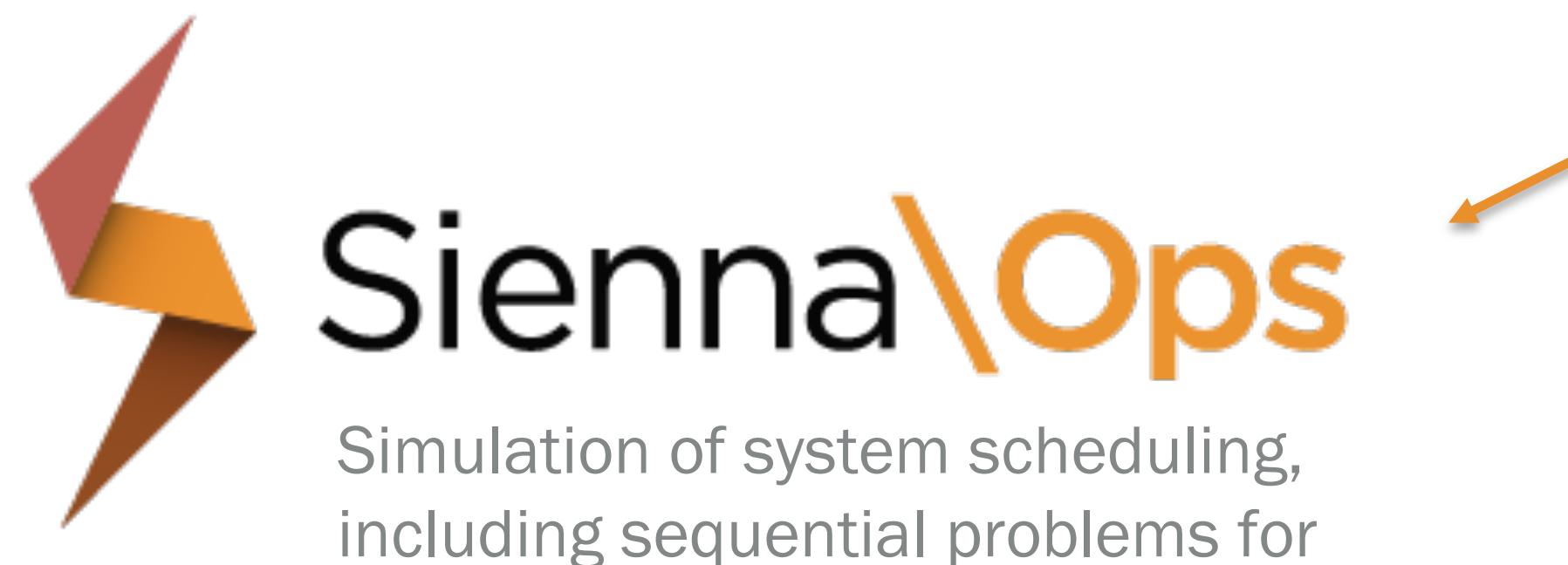
Statically  
Stable

Can the system be stable under contingencies?  
Can the transmission system operate correctly  
following the physical representation of the assets?

Dynamically  
Stable

# Open-source ecosystem for power system modeling, simulation and optimization

Sienna's three core applications use combinations of packages in the [Julia Programming Language](#)



Developed to support  
modeling with large shares  
of renewable energy  
technologies

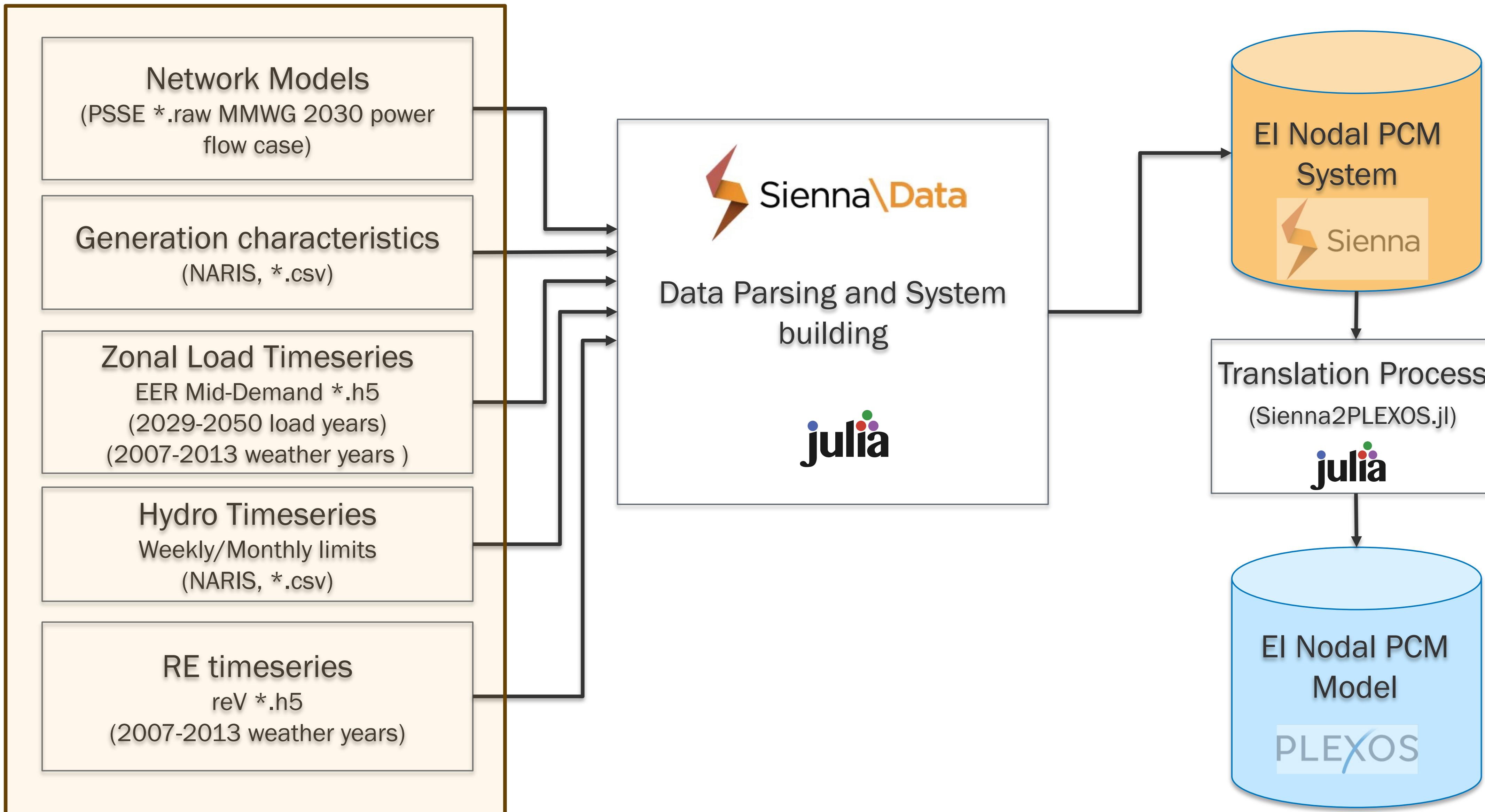


Formerly known as SIPP



<https://github.com/NREL-Sienna>

# Dataset Building Process



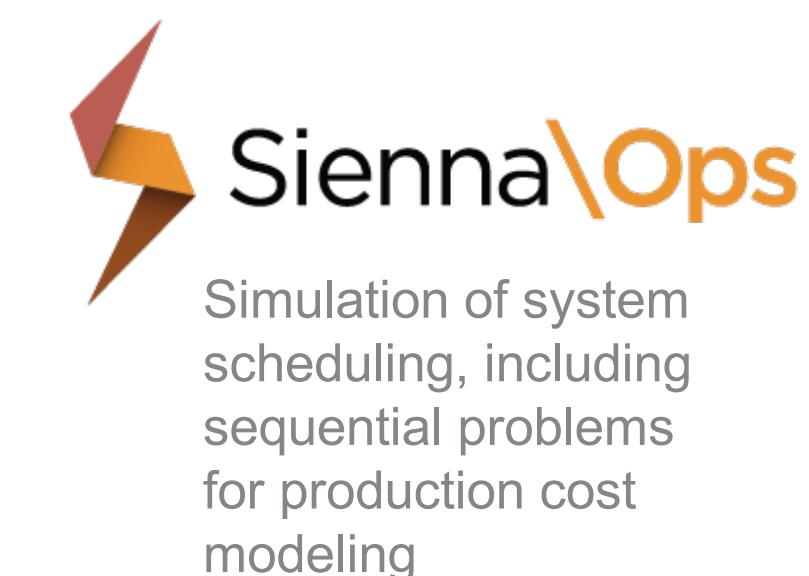
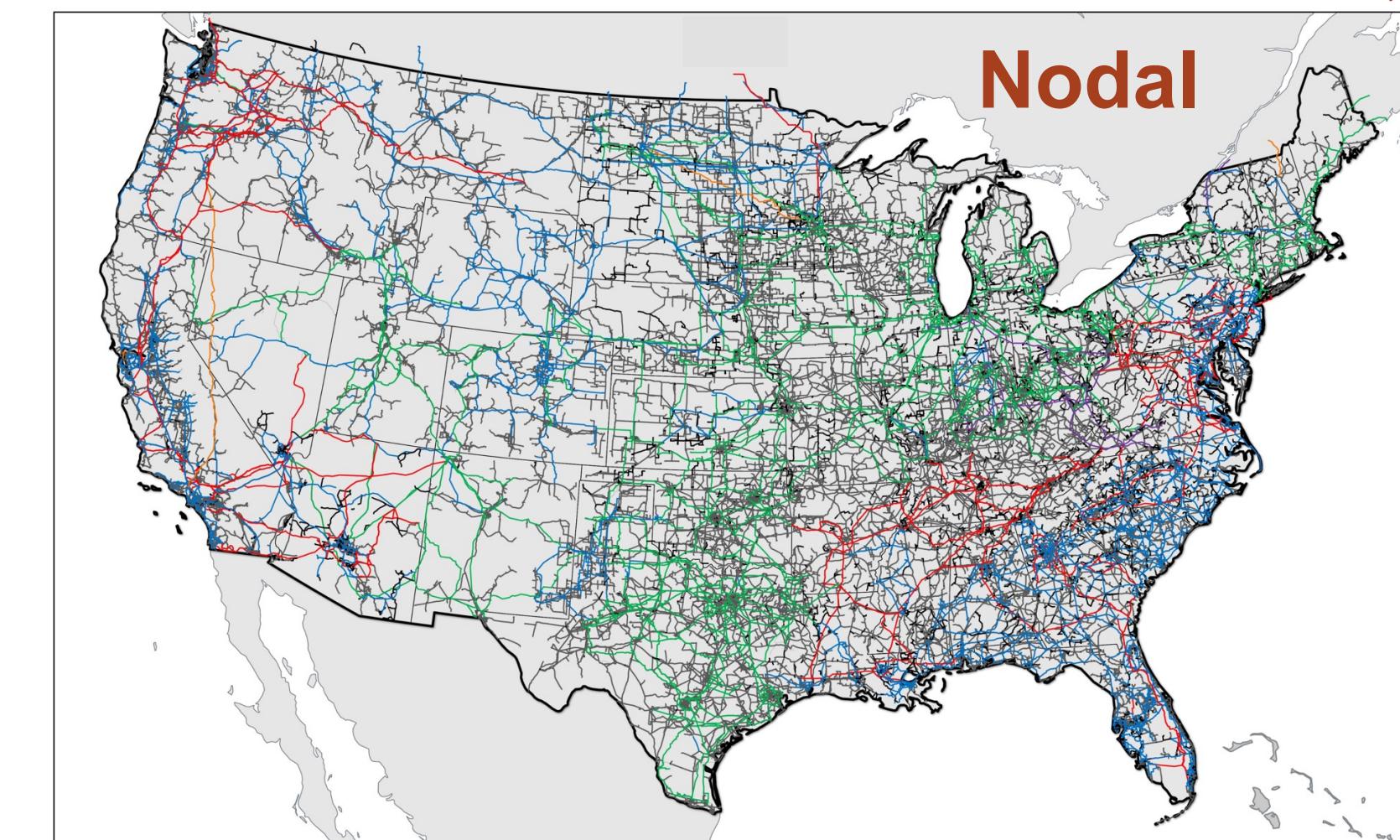
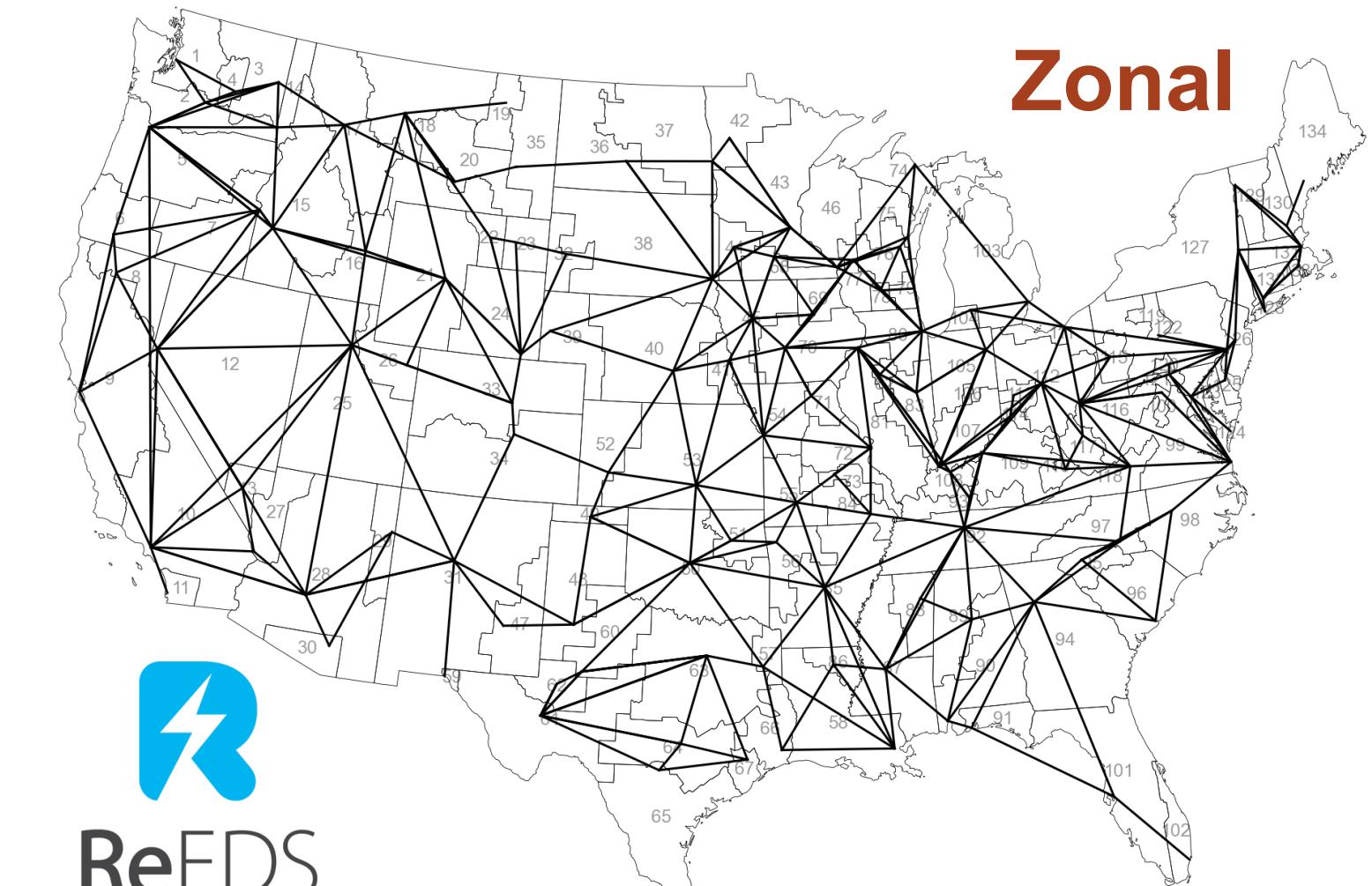
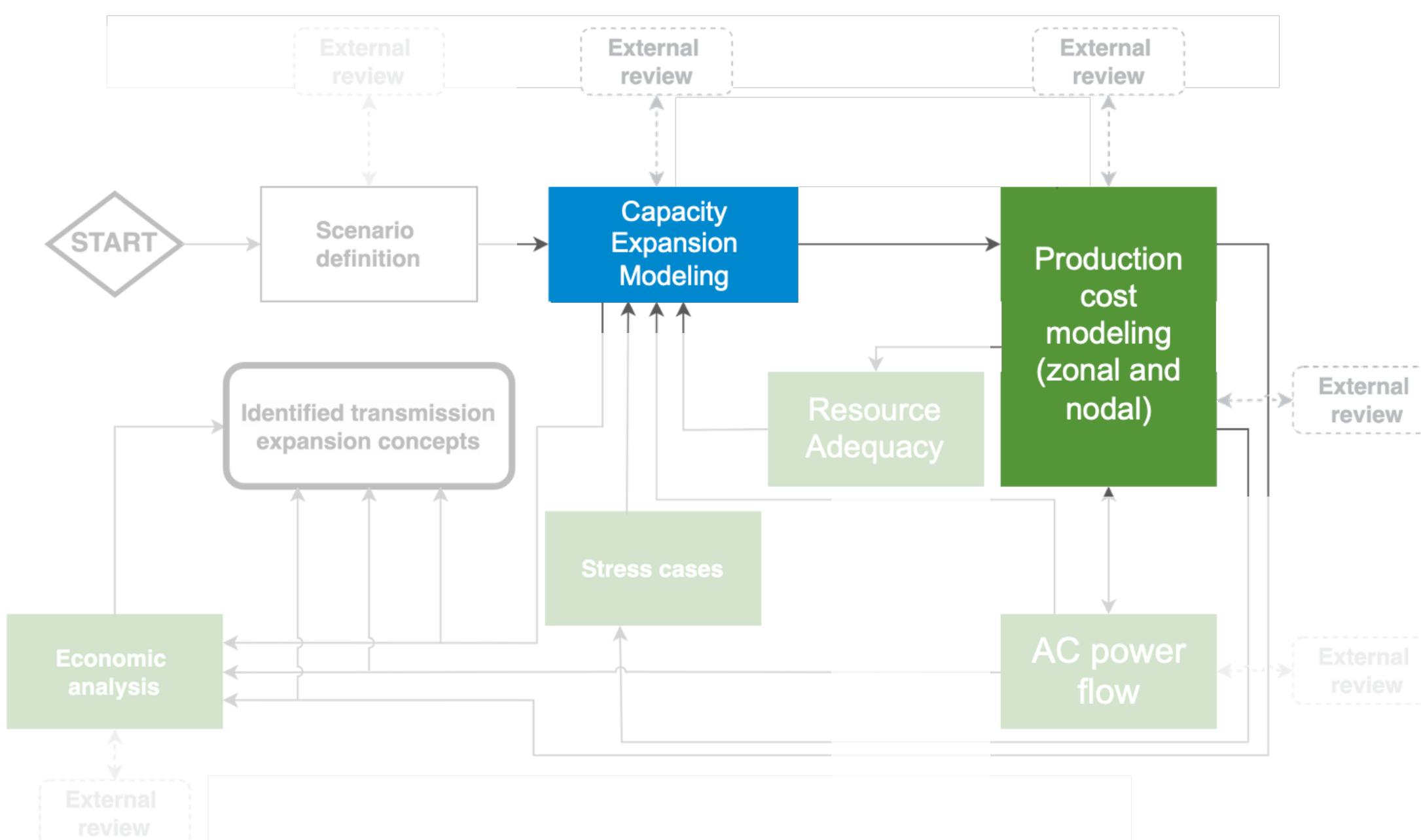


# Use Case: National Transmission Planning Study

(<https://www.energy.gov/gdo/national-transmission-planning-study>)

## Objectives

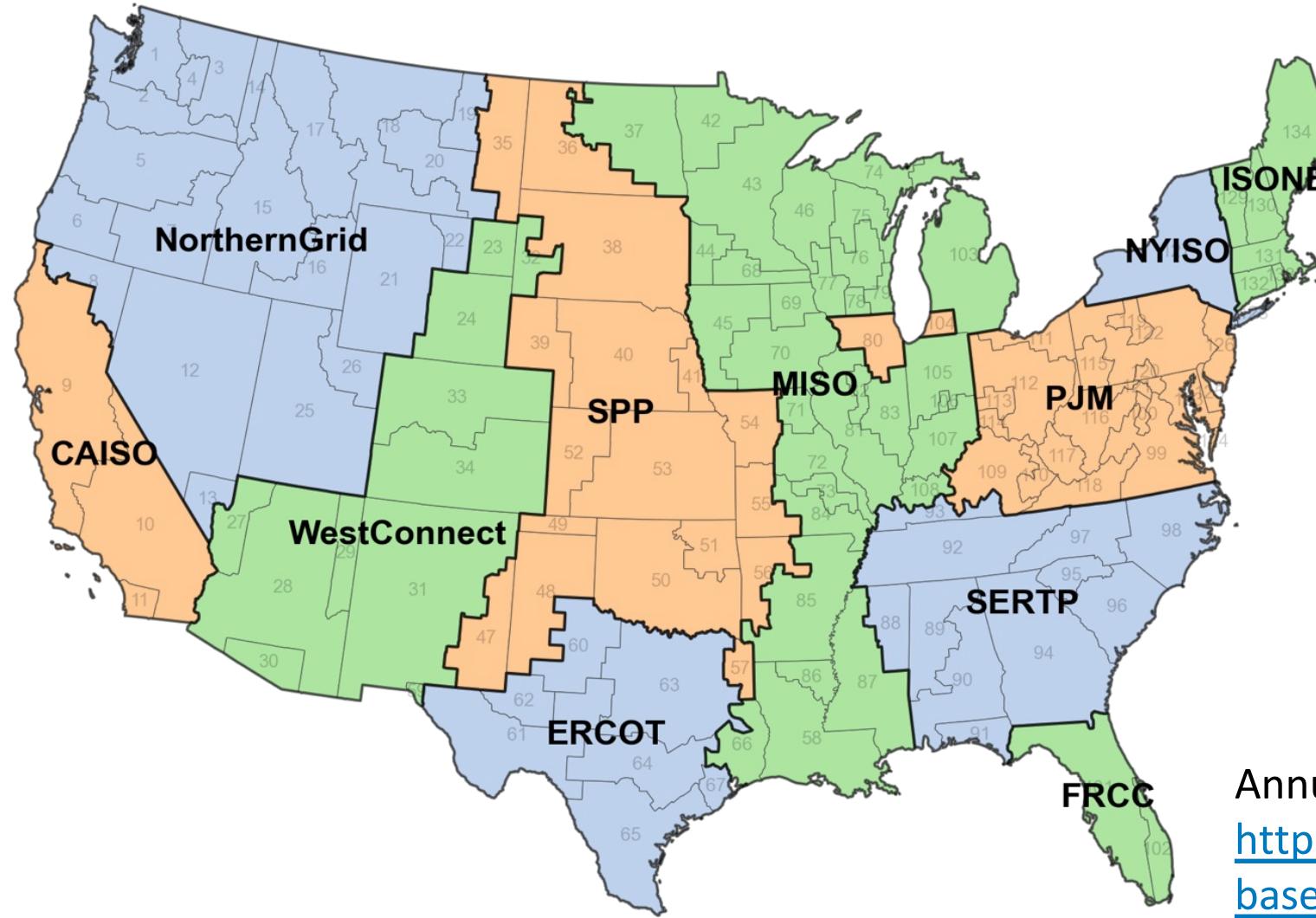
- Identify **interregional and national strategies** to accelerate cost-effective **decarbonization** while maintaining system reliability
- Inform regional and interregional transmission planning processes, particularly by **engaging stakeholders** in dialogue
- Results help **inform future DOE funding** for transmission infrastructure support



# Four interregional transmission frameworks

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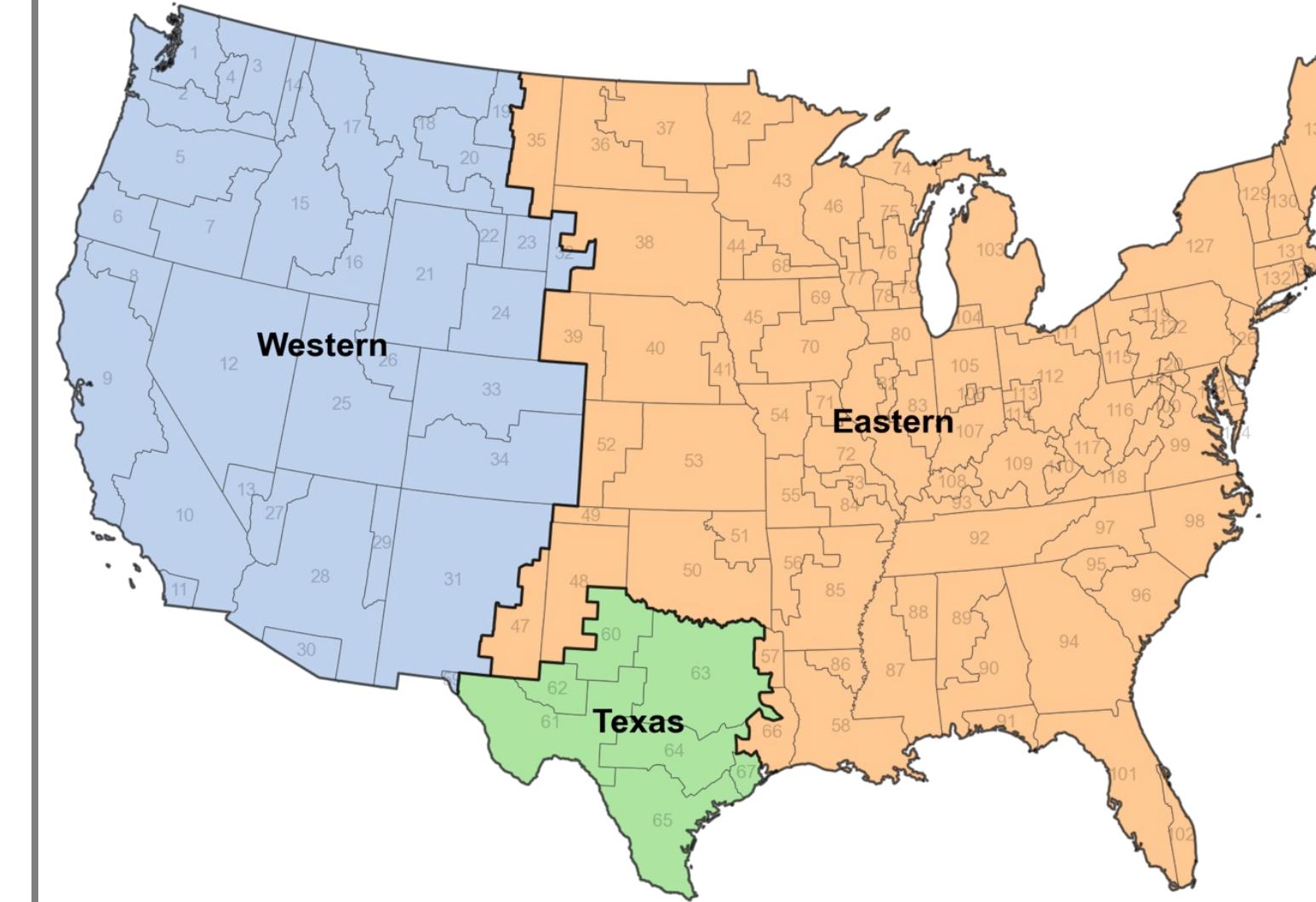
## Limited



- AC and existing HVDC expansion allowed within “transmission regions” (FERC order 1000 + ERCOT)
- Annual transmission additions (all types)  $\leq$  1.83 TW-miles/year

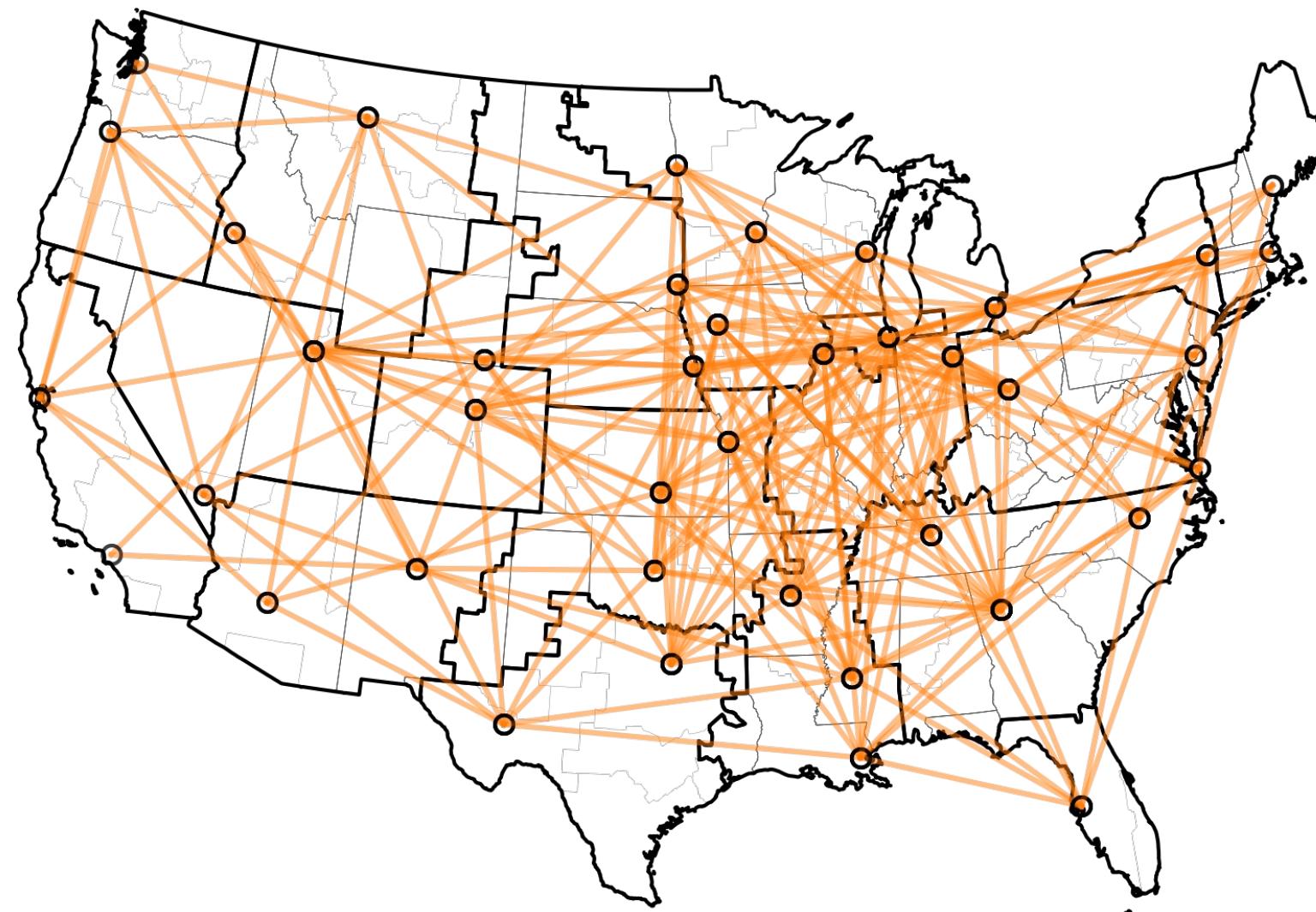
Annual US high-voltage transmission additions:  
<https://www.energy.gov/eere/wind/articles/land-based-wind-market-report-2023-edition>

## AC



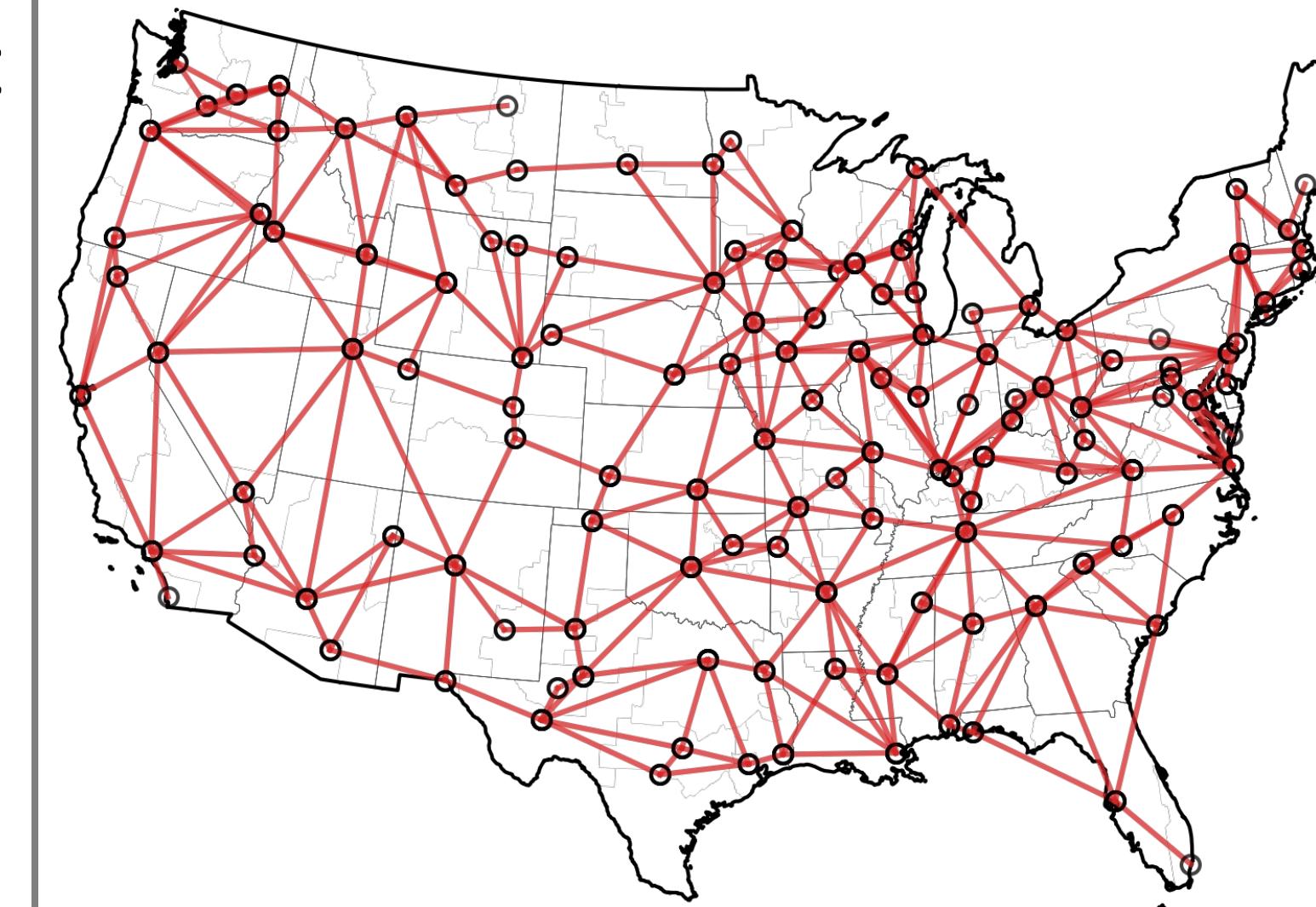
- AC and existing HVDC expansion allowed within interconnections
- No limit on total annual transmission additions

## P2P (“point-to-point”)



- AC and existing HVDC expansion allowed within interconnections
- Expansion of B2B interties allowed
- HVDC expansion along 195 new corridors allowed

## MT (“multi-terminal”)



- AC and existing HVDC expansion allowed within interconnections
- Multi-terminal HVDC expansion allowed between adjacent regions

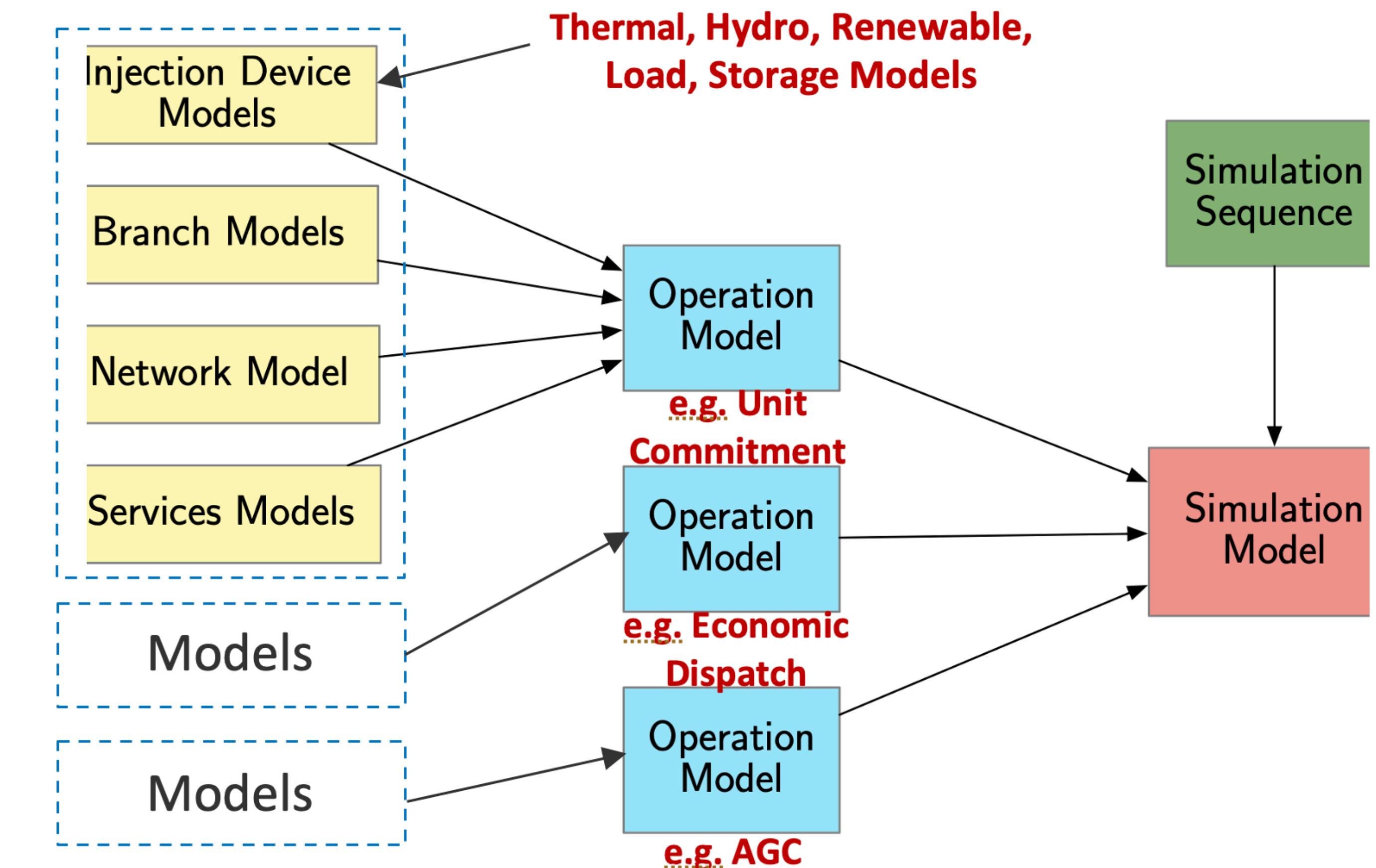
# MODEL LIMITED CHOICE<sup>®</sup>

**Structural exclusion of certain  
forms of simulation and analysis**  
**&**  
**Formulation limitations due to  
restrictions in underlying models or  
data availability**



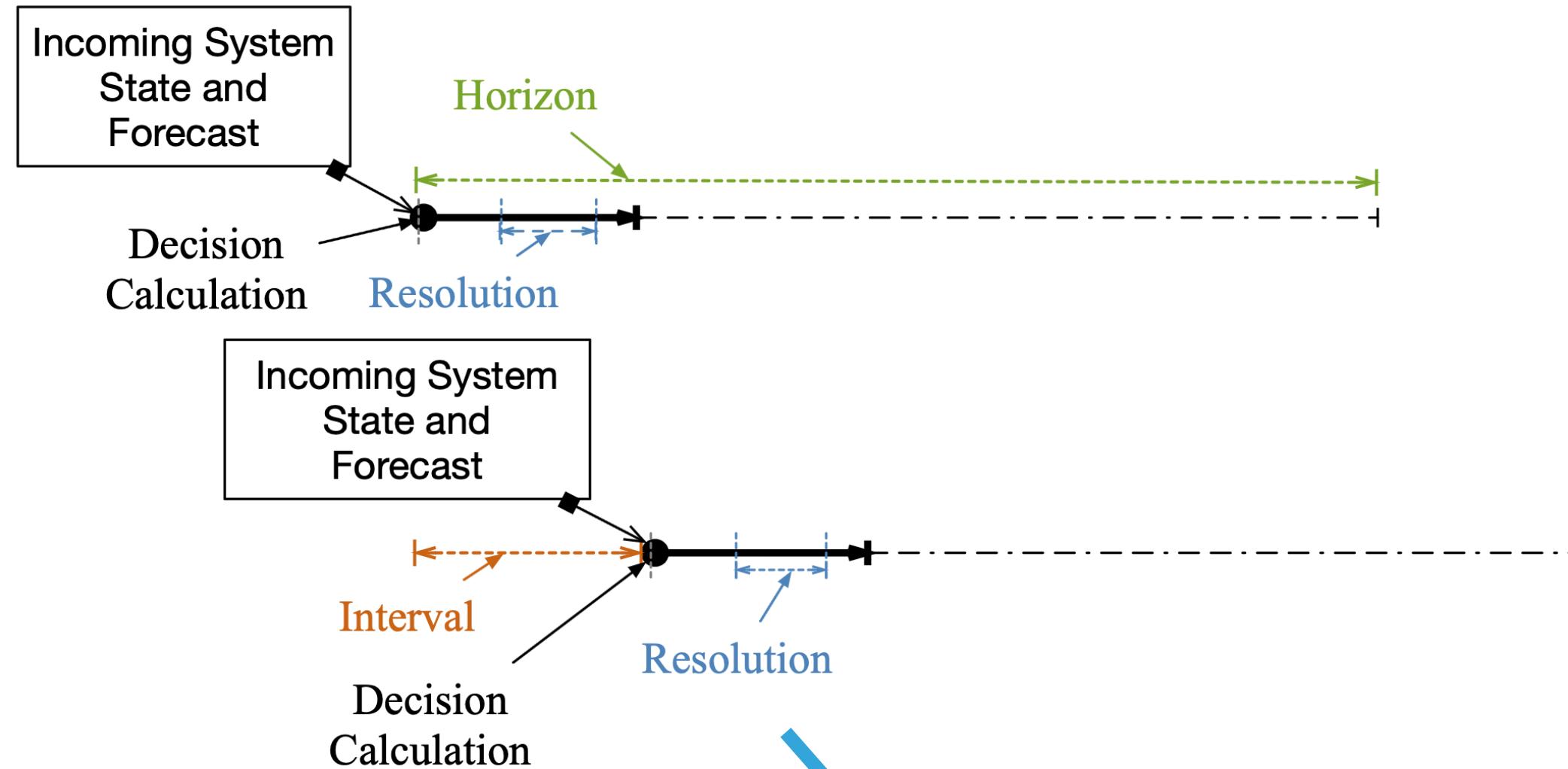
## CUSTOMIZATION OF THE UNDERLYING SIMULATION

- ▶ Employ a tree-type structure to store the optimization models and related information.
- ▶ Define the sequence of solution separately from the problem definitions.
- ▶ Support problem level customization of the solution technique and details.

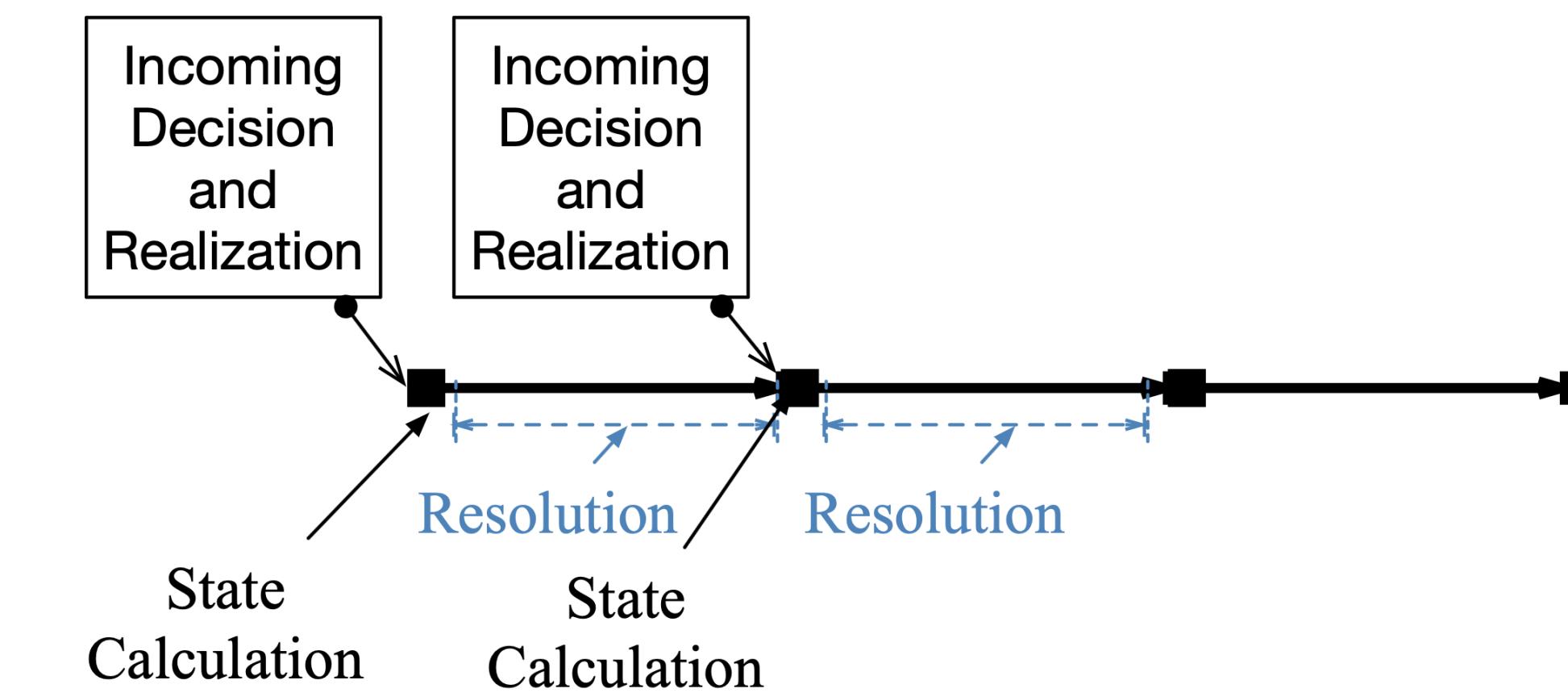


# FORMALIZING SIMULATING OPERATIONS

## DECISION MODEL



## EMULATION MODEL

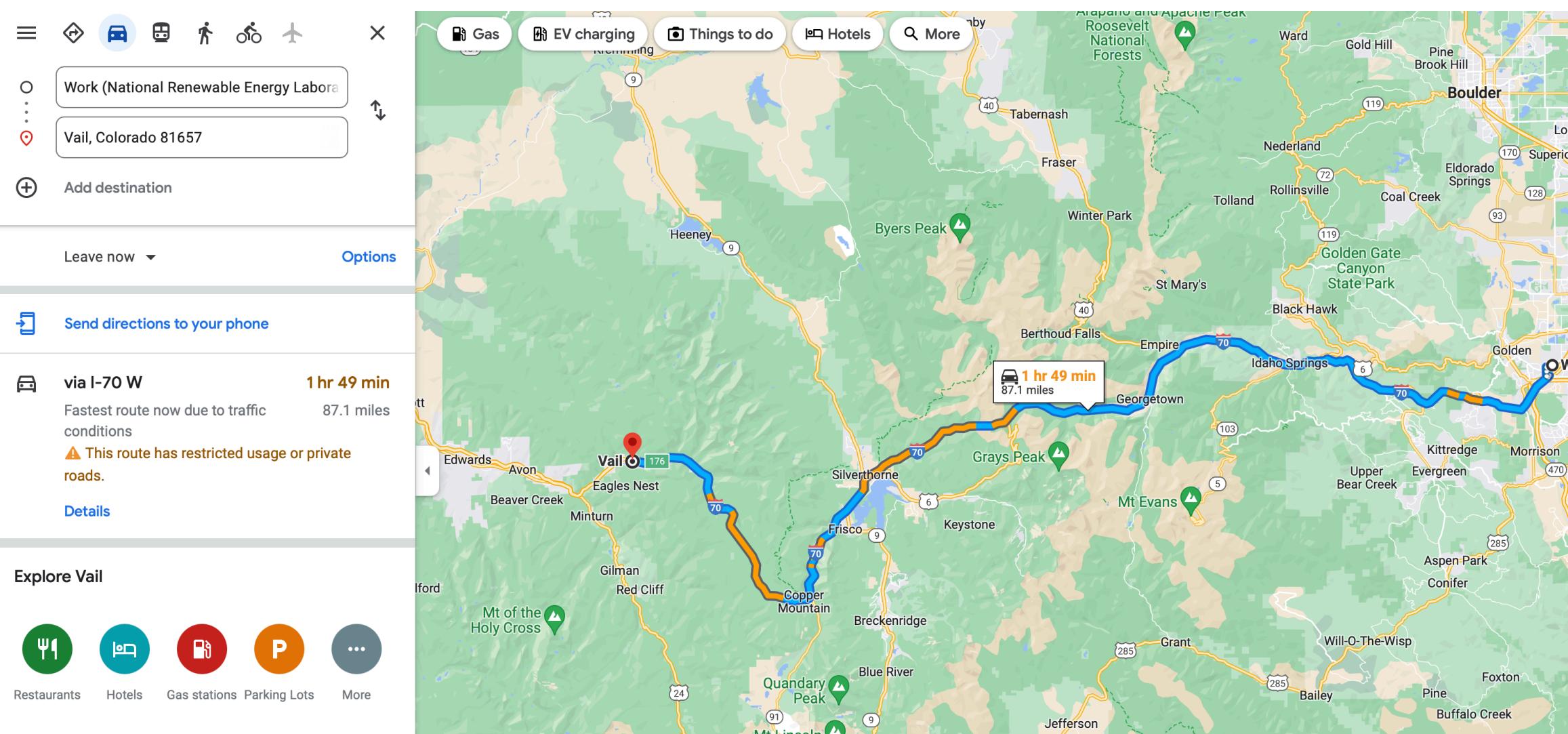


$$\vec{u}_t = F_t(\vec{x}_{t-1}, \vec{u}_{t-1}, \vec{\rho}_t, \Phi | t), \quad \vec{u}_{t_0} = \vec{u}_0$$

$$G_t(\vec{x}_t, \vec{x}_{t-1}, \vec{u}_t, \vec{\psi}_t) = 0, \quad \vec{x}_{t_0} = \vec{x}_0$$

# EVERYDAY ANALOGOUS PROCESS

## DECISION MODEL

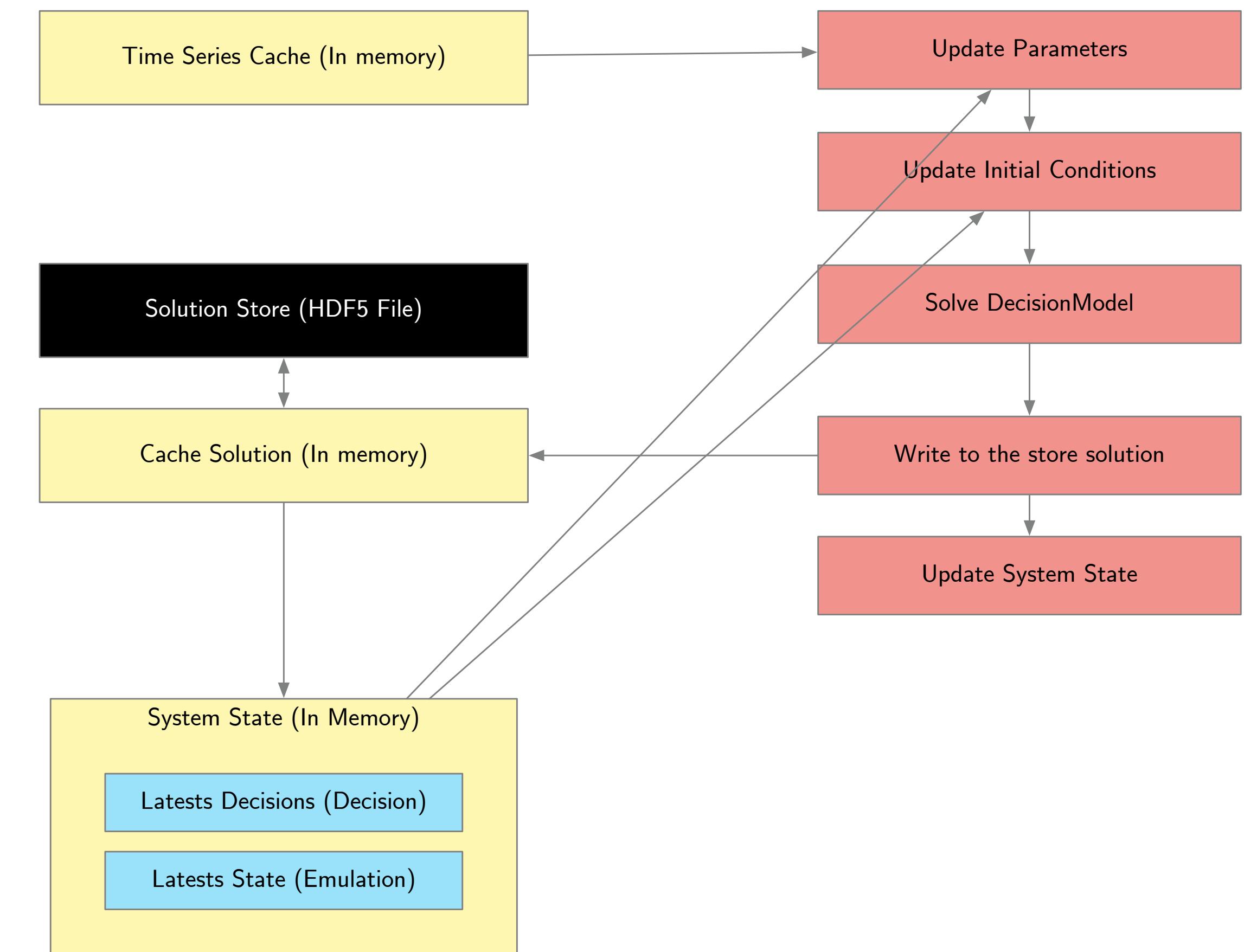


## EMULATION MODEL



## SOLVE MODEL FOR MULTI-STAGE SIMULATIONS

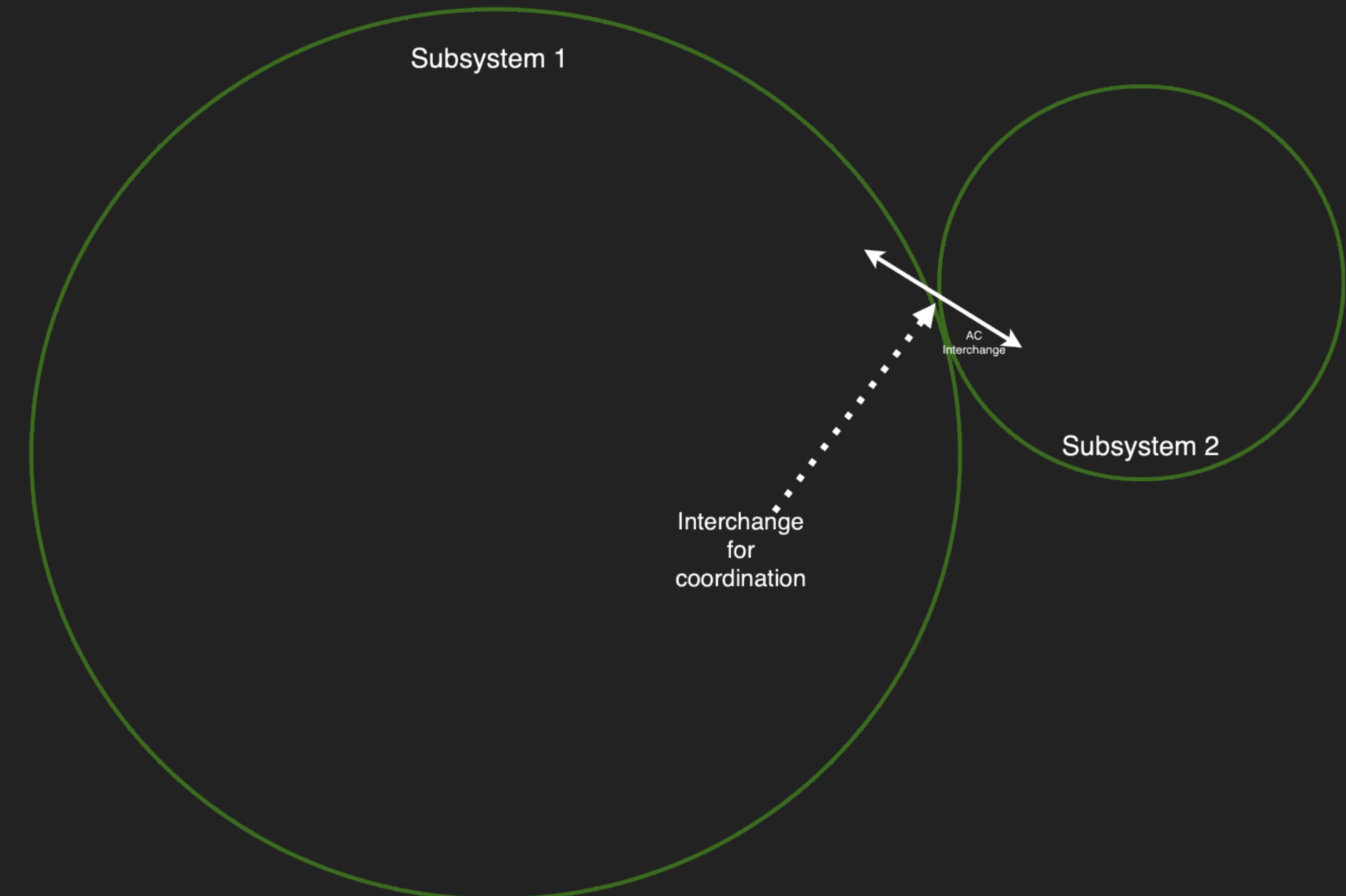
- ▶ The simulation has a store for the solution of each stage of the decision making problem.
- ▶ The simulator keeps track of the latest value of the decision variables and the system variables in a given state.
- ▶ An incumbent solution also speeds up finding the solution for the next step.
- ▶ Information written to disk is not retrieved back for the purpose of modeling. I.e., no write-read of LP files for every run.



# DEVELOPMENTS FOR M2M SIMULATION ON LARGE SCALE NETWORKS

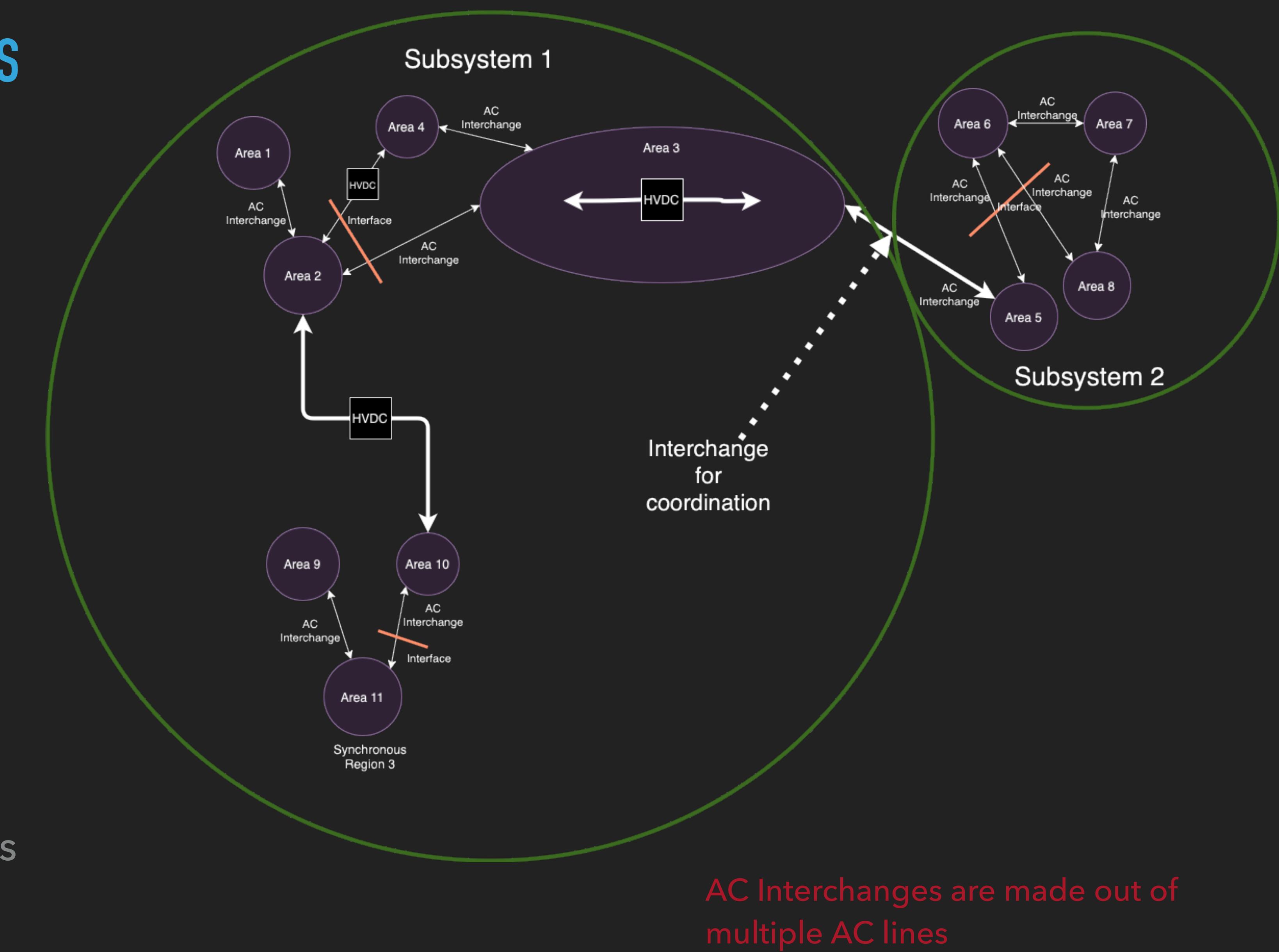
## 2-SUBSYSTEMS

- ▶ We define two Subsystems in an interconnected area that share an interchange.
- ▶ The objective is to develop a modeling/simulation platform to assess different techniques to coordinate over this interconnection efficiently.
- ▶ Several works have looked at this problem; however, these have not considered other topological challenges



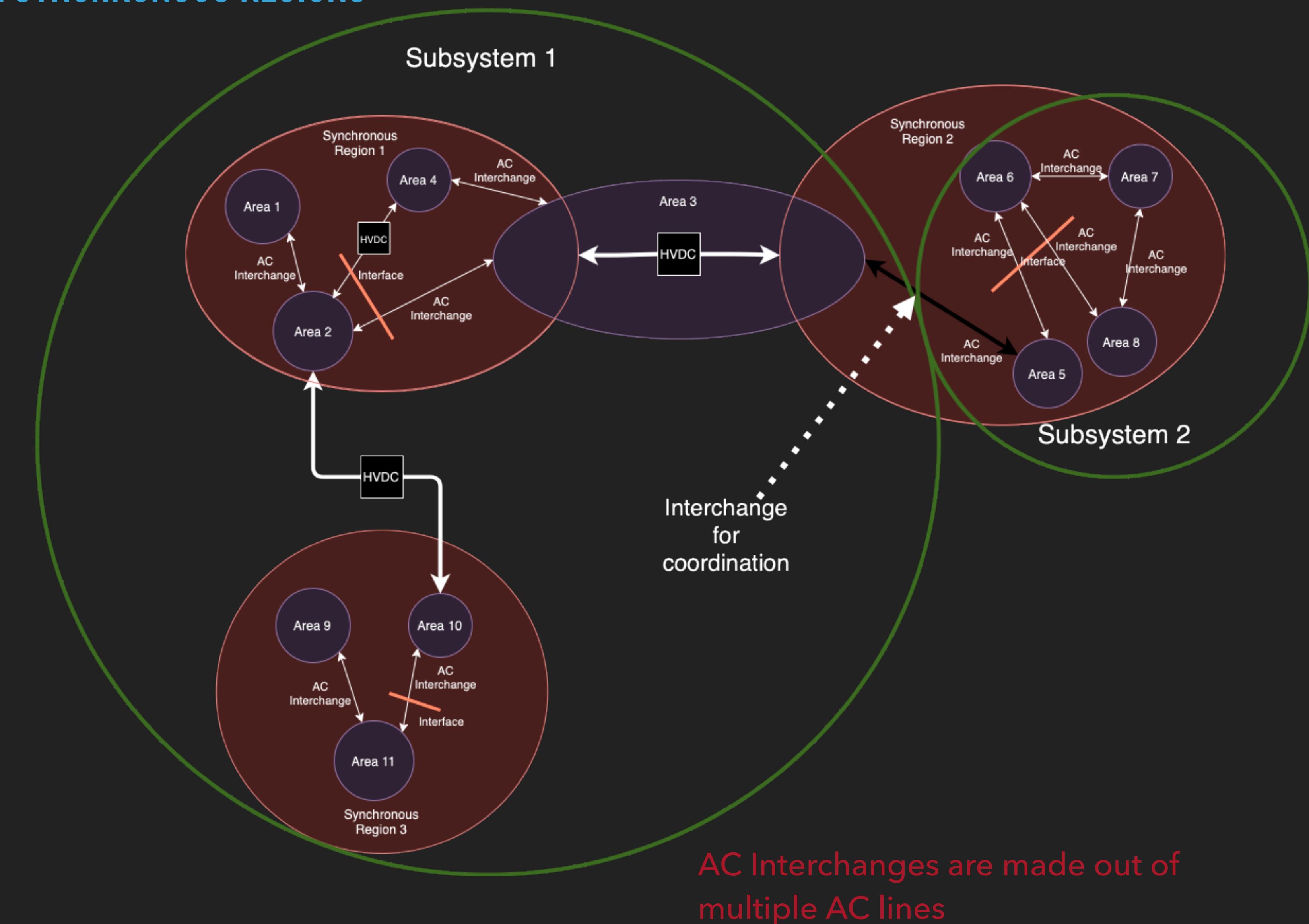
## 2-SUBSYSTEMS, MULTIPLE AREAS

- ▶ Each subsystem is composed of several areas for balancing power.
- ▶ These areas might be connected by other interchanges internal to the subsystems. The interchanges can be in AC or via HVDC.
- ▶ Each subsystem also defines interfaces which might coincide with the interchanges or contain several



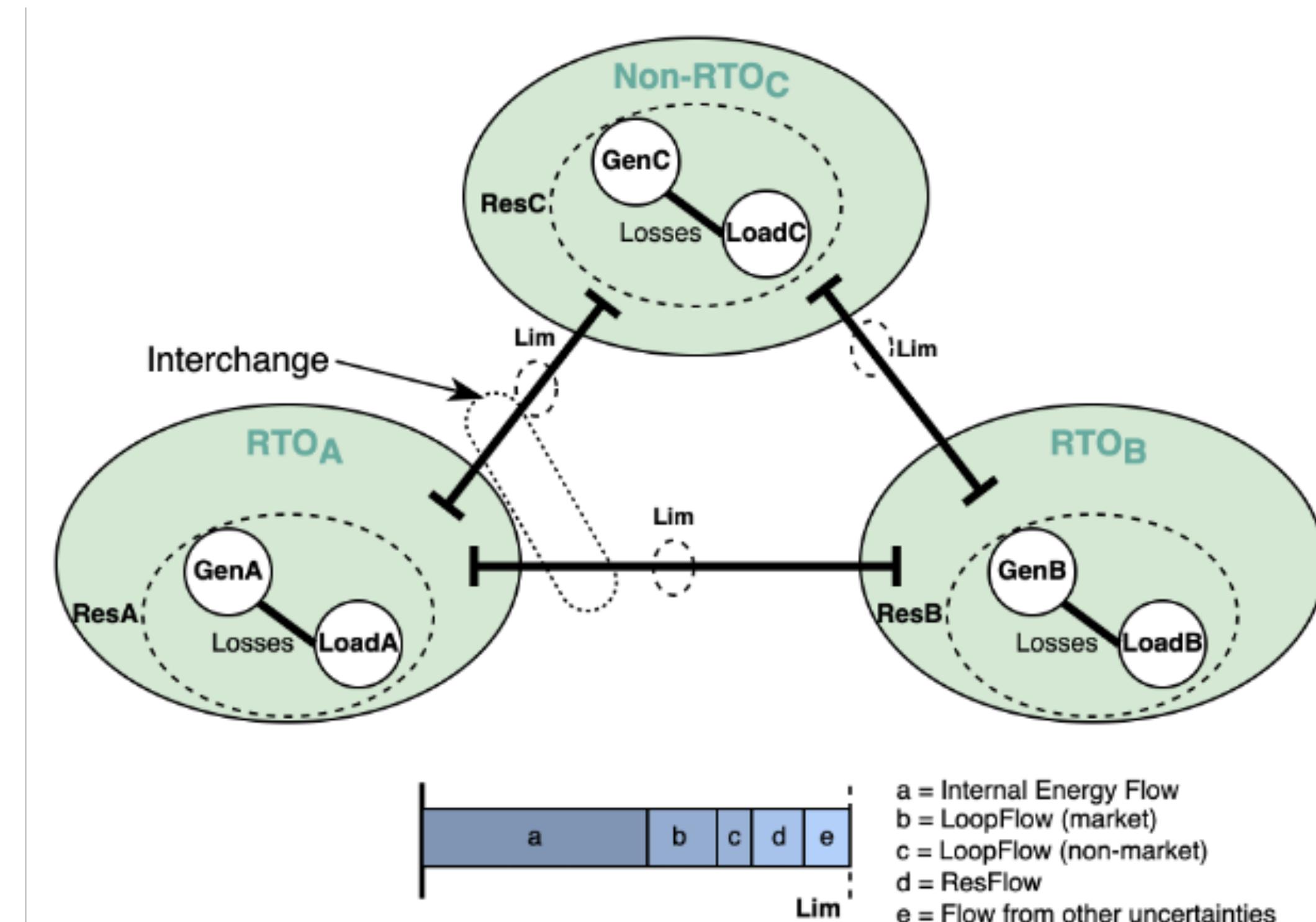
## 2-SUBSYSTEMS, MULTIPLE AREAS, MULTIPLE SYNCHRONOUS REGIONS

- ▶ The areas are split across synchronous regions connected via HVDC.
- ▶ Modeling the synchronous regions adequately matters such that the PTDF assumptions are correct and the line flows are estimated correctly.
- ▶ The combination of balancing areas, regions and systems makes the problem complex to build and simulate



# COORDINATION PROBLEMS

- ▶ Coordinated Transaction / Interchange Optimization
  - ▶ Congestion management
  - ▶ Settlement cost reductions
- ▶ Market to market coordination (M2M) under Joint operating agreements (JOAs)
  - ▶ NERC Transmission Line Loading Relief (TLR)
  - ▶ Reserve sharing group
  - ▶ Coordination mostly happens in real time, and with significant opportunities for improvement
  - ▶ Limited coordination in operational forward processes
    - ▶ Values and needs for coordination in operational forward processes
    - ▶ Intra- and inter-regional HVDC optimization
    - ▶ Intra- and inter-regional reserve deliverability



More coordination

Less coordination



System wide constraints	Co-optimized	Individual clearing with coordination	Individual clearing without coordination
Power balance	$\text{GenA} + \text{GenB} = \text{LoadA} + \text{LoadB}$	$\text{GenA} + \text{NSIA} = \text{LoadA}$ $\text{GenB} + \text{NSIB} = \text{LoadB}$ <b>Interchange optimization</b>	$\text{GenA} + \text{NSIA} = \text{LoadA}$ $\text{GenB} + \text{NSIB} = \text{LoadB}$
Transmission constraint (energy flow)	$\text{EnergyFlowA} + \text{EnergyFlowB} \leq \text{Limit}$	$\text{EnergyFlowA} + \text{loopflowA} \leq \text{Limit}$ $\text{EnergyFlowB} + \text{loopflowB} \leq \text{Limit}$ <b>M2M congestion management energy flow</b>	$\text{EnergyFlowA} + \text{loopflow} \leq \text{Limit}$ <b>On monitoring RTO</b>
Reserve requirement	$\text{ResA} + \text{ResB} \geq \text{ResRequirement}$	$\text{ResA} \geq \text{ResRequirementA}$ $\text{ResB} \geq \text{ResRequirementB}$ <b>Reserve sharing group for contingency reserve</b>	$\text{ResA} \geq \text{ResRequirementA}$ $\text{ResB} \geq \text{ResRequirementB}$
Transmission constraint (energy+reserve flow)	$\text{EnergyFlowA} + \text{EnergyFlowB} + \text{ResFlowA} + \text{ResFlowB} \leq \text{Limit}$	$\text{EnergyFlowA} + \text{ResFlowA} + \text{loopflowA} \leq \text{Limit}$ $\text{EnergyFlowB} + \text{ResFlowB} + \text{loopflowB} \leq \text{Limit}$ <b>M2M congestion management with reserve deliverability</b>	$\text{EnergyFlowA} + \text{ResFlowA} + \text{loopflow} \leq \text{Limit}$ <b>On monitoring RTO</b>

Two RTOs A and B assuming lossless

Red: variables

Black: parameters

Blue: components with coordination mechanism

## MODEL FORMULATION – SETS

$\mathcal{B}$	System Buses
$\mathcal{R}$	Synchronous Regions
$\mathcal{A}$	Balancing Areas
$\mathcal{L}$	AC Lines
$\mathcal{H}$	Two Terminal HVDC Lines
$\mathcal{E} := \{e \in \mathbf{C}(\mathcal{A}, 2)\}$	Inter-area exchanges
$\mathcal{I}$	Transmission interfaces
$\mathcal{G}$	Generators
$\mathcal{X}$	Feasibility Set
$\mathcal{T} := \{1, \dots, T\}$	Time steps

## MODEL FORMULATION - INDEXING

$b_r$	bus in synchronous region $r \in \mathcal{R}$
$b_a$	bus in area $a \in \mathcal{A}$
$\mathcal{G}_r$	Subset of generators in region $r \in \mathcal{R}$
$\mathcal{G}_a$	Subset of generators in area $a \in \mathcal{A}$
$\mathcal{B}_r$	Subset of buses in region $r \in \mathcal{R}$
$\mathcal{B}_a$	Subset of buses in area $a \in \mathcal{A}$
$\mathcal{H}_i$	Subset of two Terminal HVDC assigned to interface $i \in \mathcal{I}$
$\mathcal{L}_i$	Subset of AC Line assigned to interface $i \in \mathcal{I}$
$h_{b\rightarrow}$	From bus Two Terminal HVDC Line $h \in \mathcal{H}$
$h_{b\leftarrow}$	To bus Two Terminal HVDC Line $h \in \mathcal{H}$
$h_{r\rightarrow}$	From region Two Terminal HVDC Line $h \in \mathcal{H}$
$h_{r\leftarrow}$	To region Two Terminal HVDC Line $h \in \mathcal{H}$
$h_{a\rightarrow}$	From area Two Terminal HVDC Line $h \in \mathcal{H}$
$h_{a\leftarrow}$	To area Two Terminal HVDC Line $h \in \mathcal{H}$
$l_{b\rightarrow}$	From bus Line $l \in \mathcal{L}$
$l_{b\leftarrow}$	To bus Line $l \in \mathcal{L}$
$l_{a\rightarrow}$	From area Line $l \in \mathcal{L}$
$l_{a\leftarrow}$	To area Line $l \in \mathcal{L}$
$e_{a\rightarrow}$	From area Inter-area exchange $e \in \mathcal{E}$
$e_{a\leftarrow}$	To area Inter-area exchange $e \in \mathcal{E}$

## MODEL FORMULATION – PARAMETERS

$\text{PTDF}^r$

PTDF subnetwork  $n \in \mathcal{R}$

$D_{b,t}$

Net demand at bus  $b$  time  $t$

$P_g^{max}$

Generator Max Power Output

$F_l^{max}$

AC line max rating normal operation

$F_l^{max}$

Two-terminal HVDC max flow normal operation

$F_i^{max}$

Max Flow Transmission Interface

$F_i^{min}$

Min Flow Transmission Interface

$F_e^{max,\leftarrow}$

Max Flow from-to Inter-area exchange

$F_e^{max,\rightarrow}$

Max Flow to-from Inter-area exchange

## MODEL FORMULATION – VARIABLES & EXPRESSIONS

$$p_{g,t} \in [0, P_g^{max}] \quad \text{Generator Power Output}$$

$$f_{h,t} \in [-F_h^{max}, F_h^{max}] \quad \text{HVDC Line flow}$$

$$f_{e,t} \in [-F_e^{max,\rightarrow}, F_e^{max,\leftarrow}] \quad \text{Inter-area exchange flow}$$

$$i_{b,t} := D_{b,t} - \sum_{g \in \mathcal{G}_b} p_{g,t} + \sum_{\{h \in \mathcal{H} | h_{b\leftarrow} = b\}} f_{h,t} - \sum_{\{h \in \mathcal{H} | h_{b\rightarrow} = b\}} f_{h,t} \quad \text{Net Injection at bus } b \text{ at time } t$$

$$f_{l,t} := \sum_{l \in \mathcal{L}_r, b \in \mathcal{B}_r} \mathbf{PTDF}_{l,b}^r i_{b,t} \quad \text{Power flow over branch } l \text{ in region } r \text{ at time } t$$

## MODEL FORMULATION - CONSTRAINTS

$$\min_{\mathbf{p}, \mathbf{f}_h, \mathbf{f}_e} \sum_{t \in \mathcal{T}, g \in \mathcal{G}} \mathcal{O}_g(p_{g,t})$$

s.t.

$$\begin{aligned} p_{g,t} &\in \mathcal{X}_g & \forall g \in \mathcal{G}, \forall t \in \mathcal{T} \\ f_{l,t} &\in \mathcal{X}_l & \forall l \in \mathcal{L}, \forall t \in \mathcal{T} \\ f_{h,t} &\in \mathcal{X}_h & \forall h \in \mathcal{H}, \forall t \in \mathcal{T} \\ f_{e,t} &\in \mathcal{X}_e & \forall e \in \mathcal{E}, \forall t \in \mathcal{T} \end{aligned}$$

$$\sum_{g \in \mathcal{G}_r} p_{g,t} + \sum_{\{h \in \mathcal{H} | h_b \leftarrow r\}} f_{h,t} - \sum_{\{h \in \mathcal{H} | h_b \rightarrow \mathcal{B}_r\}} f_{h,t} = \sum_{b \in \mathcal{B}_r} D_b \quad \forall r \in \mathcal{R}, \forall t \in \mathcal{T}$$

$$\sum_{g \in \mathcal{G}_a} p_{g,t} + \sum_{\{E \in \mathcal{E} | e_a \leftarrow a\}} f_{e,t} - \sum_{\{e \in \mathcal{E} | e_a \rightarrow a\}} f_{e,t} = \sum_{b \in \mathcal{B}_a} D_b \quad \forall a \in \mathcal{A}, \forall t \in \mathcal{T}$$

$$\sum_{\{l \in \mathcal{L} | l_a \rightarrow = e_a \rightarrow \wedge l_a \leftarrow = e_a \leftarrow\}} f_{l,t} - \sum_{\{l \in \mathcal{L} | l_a \rightarrow = e_a \leftarrow \wedge l_a \rightarrow = e_a \leftarrow\}} f_{l,t} + \sum_{\{h \in \mathcal{H} | h_a \rightarrow = e_a \rightarrow \wedge h_a \leftarrow = e_a \leftarrow\}} f_{h,t} - \sum_{\{h \in \mathcal{H} | h_a \rightarrow = e_a \leftarrow \wedge h_a \rightarrow = e_a \leftarrow\}} f_{h,t} \leq f_{e,t} \quad \forall e \in \mathcal{E}, t \in \mathcal{T}$$

$$\sum_{\{l \in \mathcal{L} | l_a \rightarrow = e_a \rightarrow \wedge l_a \leftarrow = e_a \leftarrow\}} f_{l,t} - \sum_{\{l \in \mathcal{L} | l_a \rightarrow = e_a \leftarrow \wedge l_a \rightarrow = e_a \leftarrow\}} f_{l,t} + \sum_{\{h \in \mathcal{H} | h_a \rightarrow = e_a \rightarrow \wedge h_a \leftarrow = e_a \leftarrow\}} f_{h,t} - \sum_{\{h \in \mathcal{H} | h_a \rightarrow = e_a \leftarrow \wedge h_a \rightarrow = e_a \leftarrow\}} f_{h,t} \geq f_{e,t} \quad \forall e \in \mathcal{E}, t \in \mathcal{T}$$

$$\sum_{l \in \mathcal{L}_i} f_{l,t} + \sum_{h \in \mathcal{H}_i} f_{h,t} \leq F_i^{max} \quad \forall i \in \mathcal{I}, t \in \mathcal{T}$$

$$\sum_{l \in \mathcal{L}_i} f_{l,t} + \sum_{h \in \mathcal{H}_i} f_{h,t} \geq F_i^{min} \quad \forall i \in \mathcal{I}, t \in \mathcal{T}$$

Feasibility sets for the different model components

Synchronous Region Power Balance

Area Power Balance

Area Exchange Upper Bound

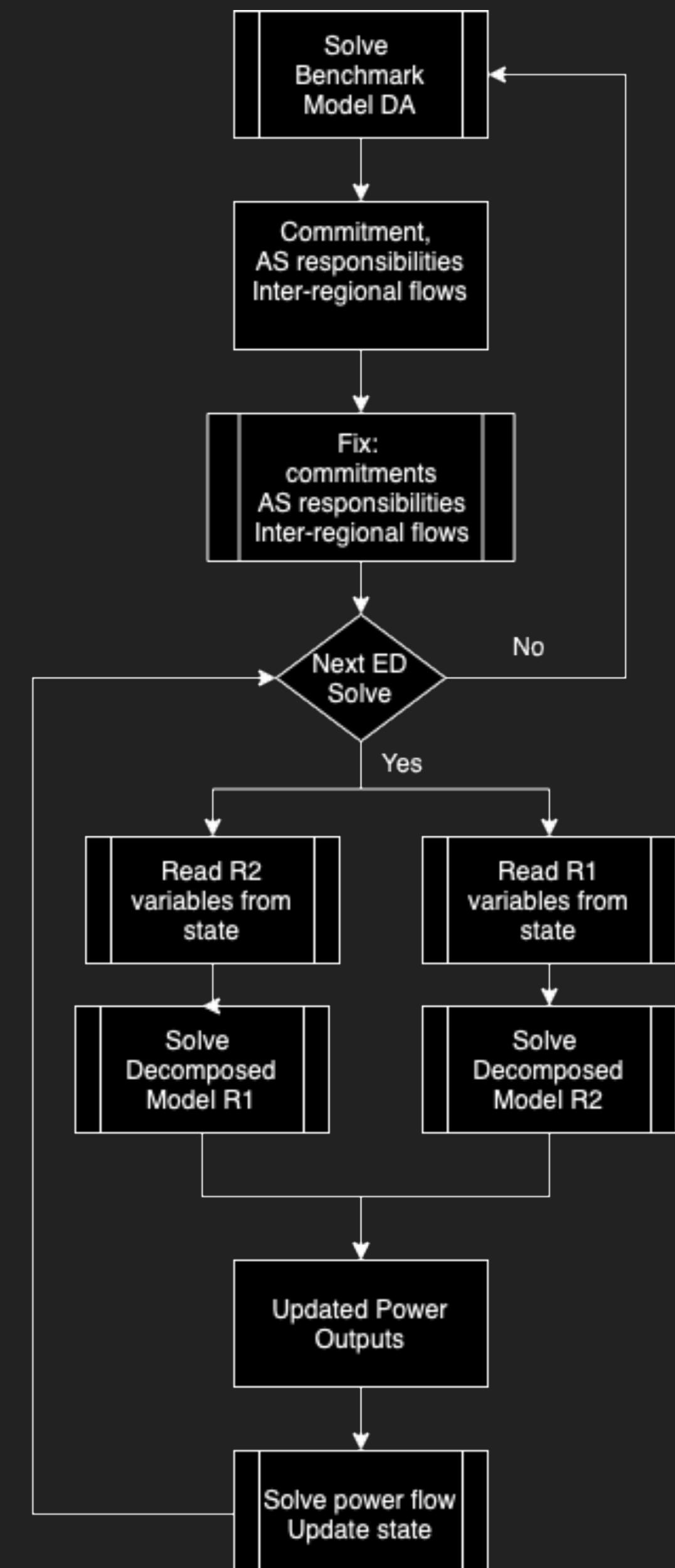
Area Exchange Lower Bound

Interface Upper Bound

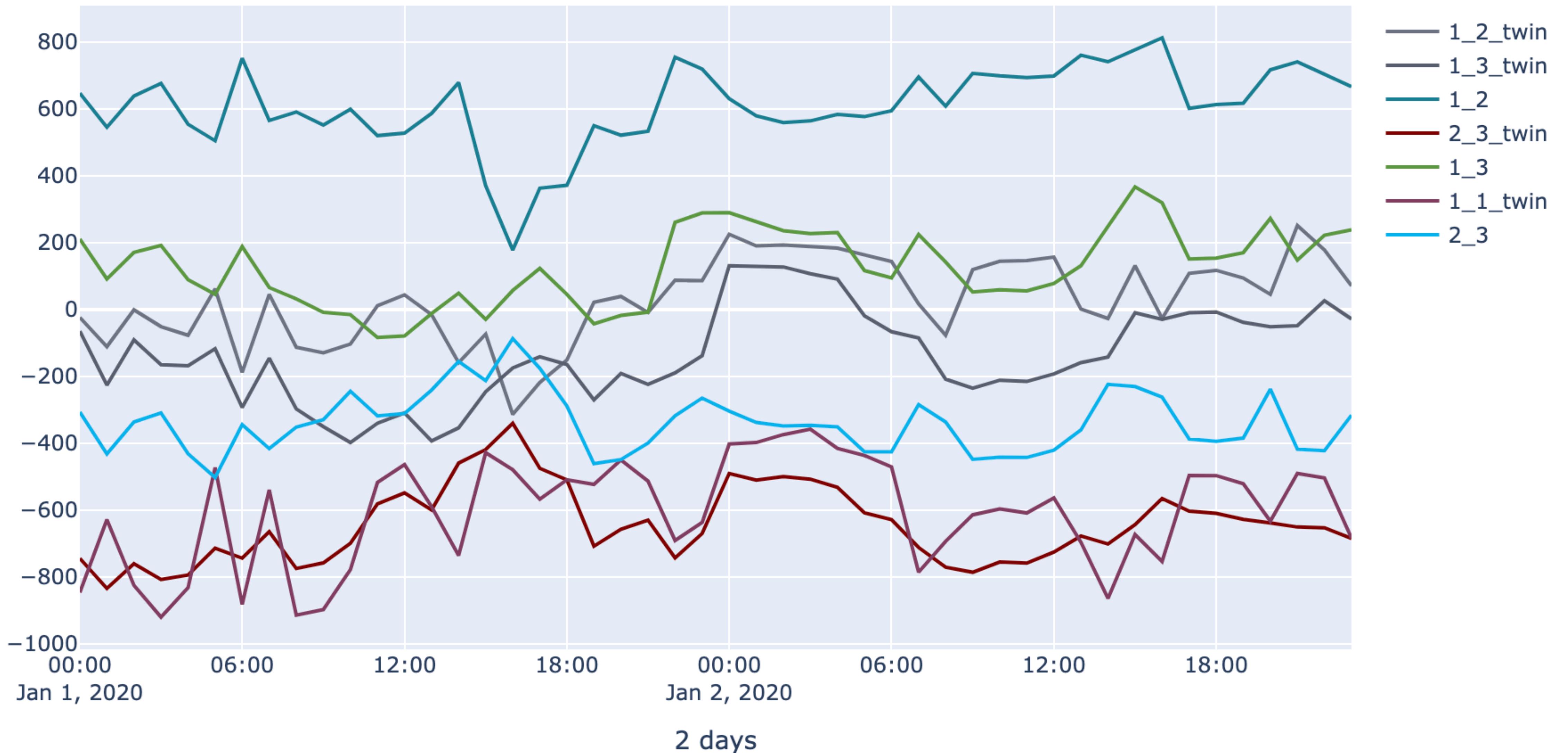
Interface Lower Bound

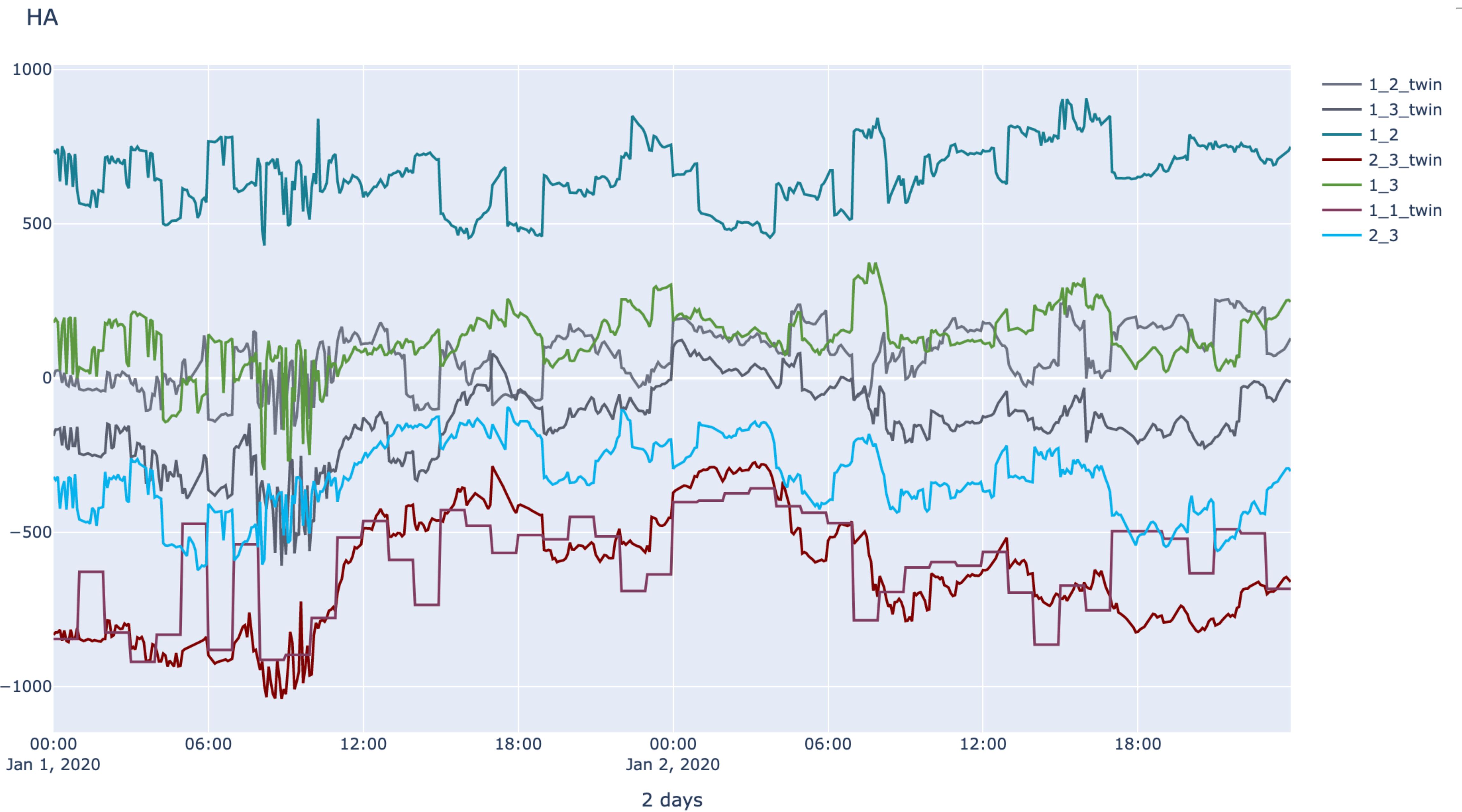
## POWERSIMULATIONSDECOMPOSITION.JL

- ▶ The simulation workflow takes advantage of the emulator concept to implement the equivalent of the state estimator.
- ▶ At each time step in the ED all the variables from the emulator are available to the decomposed model by subsystem. It includes potentially duals from the other subsystem's problem.
- ▶ Solving these problems at scale requires several stability tricks:
  - ▶ Reduce radial branches in the PTDF and sparsity the matrices
  - ▶ Use Ward equivalents to reduce the number of branches from the neighboring region each subproblem needs to solve values for

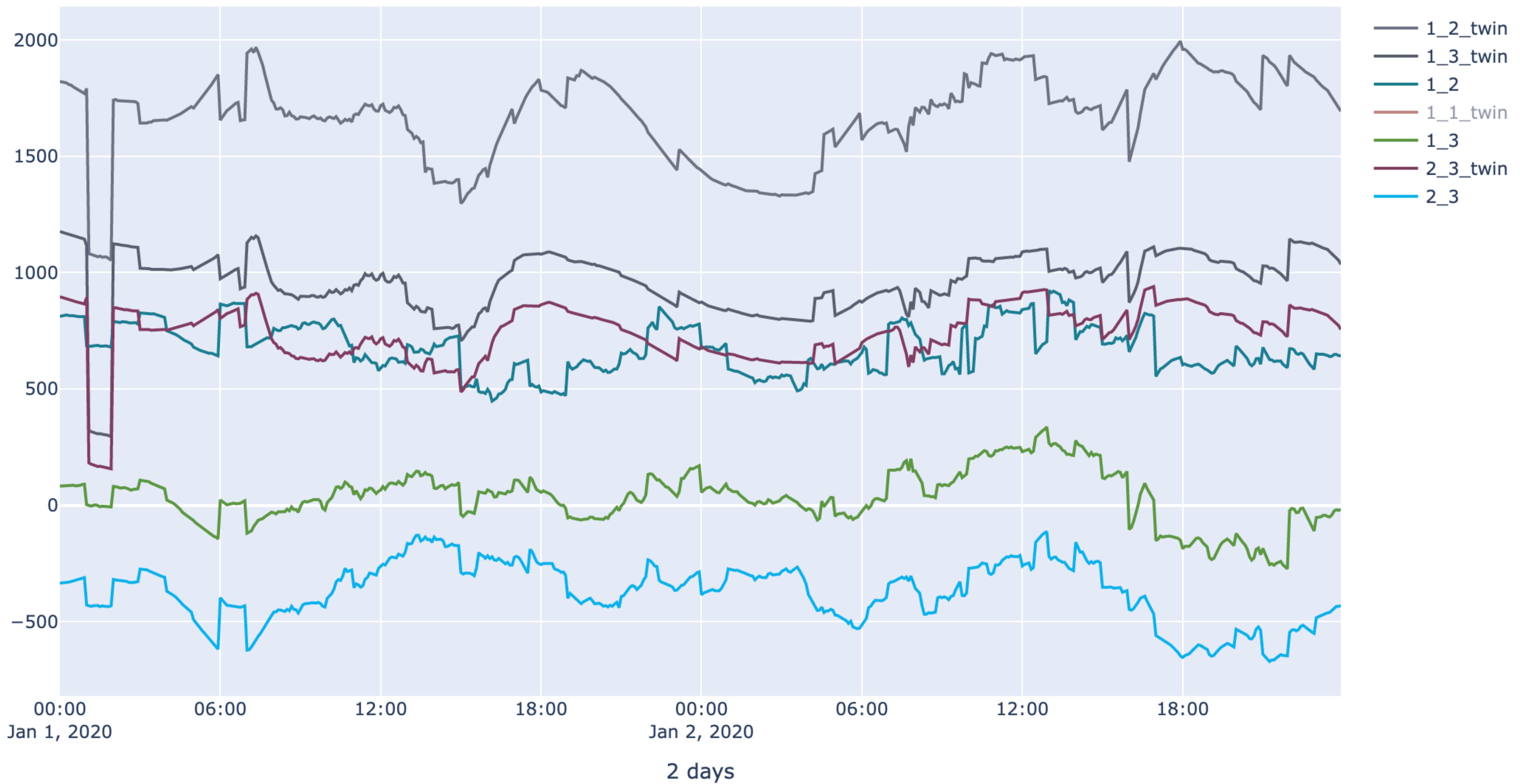


DA



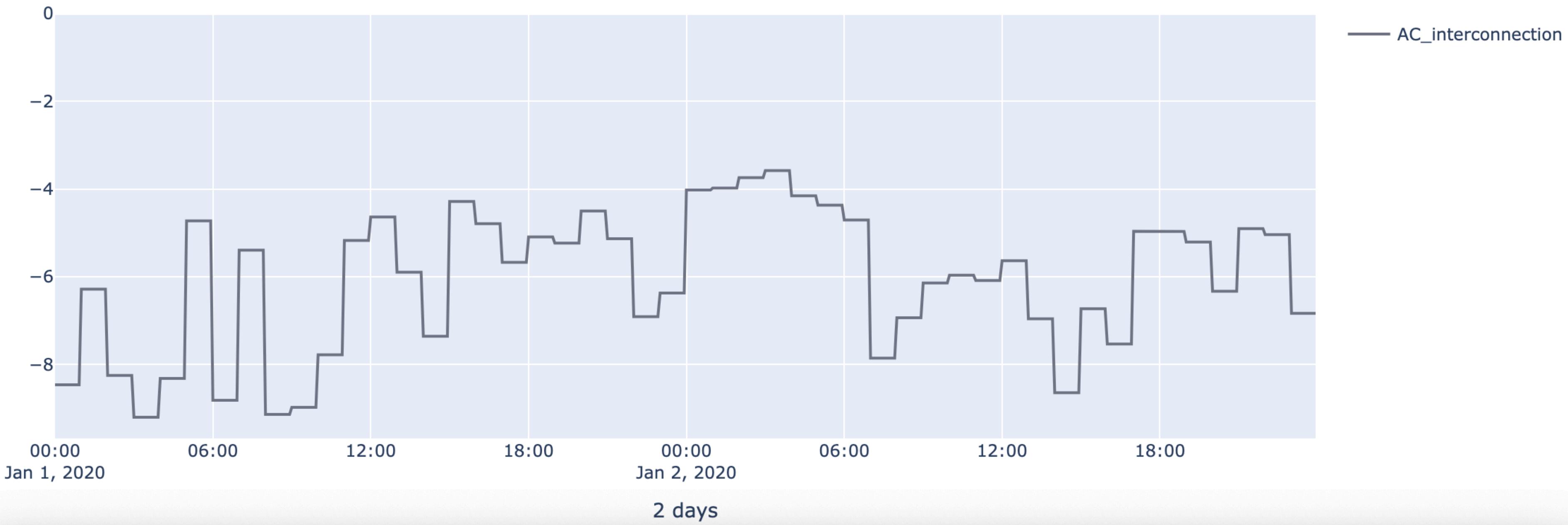


ED

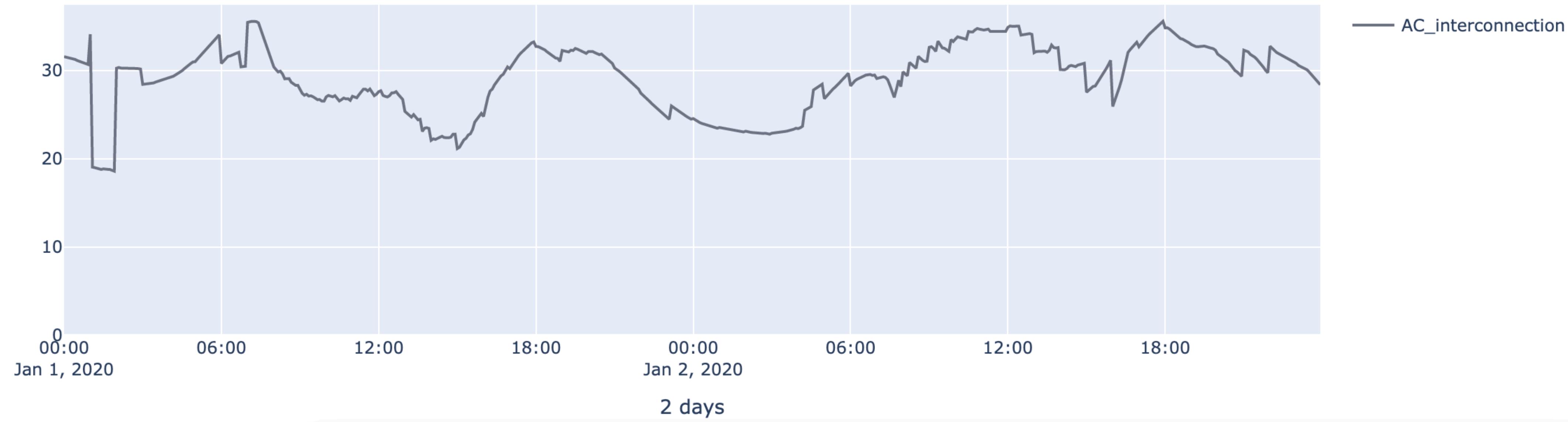


ED\_1

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ED\_2



## NEXT STEPS

- ▶ Testing information sharing approaches (using JuMP parameters) to improve the coordination of the inter-ties and interfaces.
  - ▶ Copperplate dual sharing
  - ▶ Constraint violation supply function implementation.
- ▶ Implement ADMM based iterative approach for geographic decomposition
- ▶ Implement MPI parallel version of the algorithms to run in HPC

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# Thank You!

