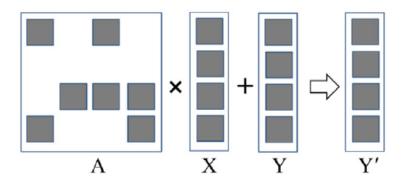
CHAPTER 14

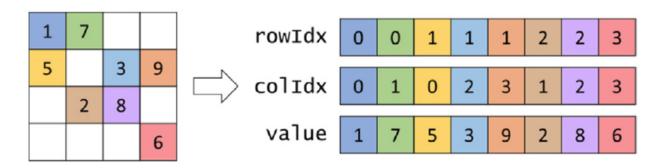
Sparse matrix computation

Row 0	1	7		
Row 1	5		3	9
Row 2		2	8	
Row 3				6

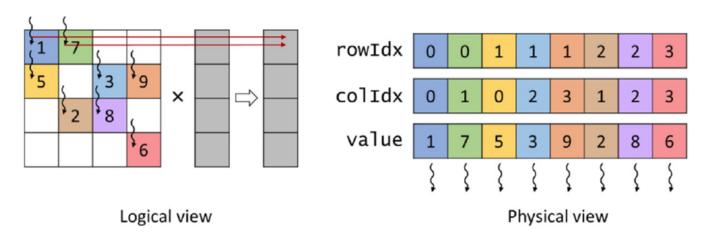
A simple sparse matrix example.



A small example of matrix-vector multiplication and accumulation.



Example of the coordinate list (COO) format.



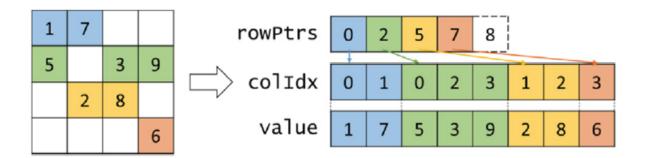
Example of parallelizing SpMV with the COO format.

```
01
               void spmv coo kernel (COOMatrix cooMatrix, float* x, float* y) {
        global
02
          unsigned int i = blockIdx.x*blockDim.x + threadIdx.x;
03
          if(i < cooMatrix.numNonzeros) {</pre>
04
              unsigned int row = cooMatrix.rowIdx[i];
05
              unsigned int col = cooMatrix.colIdx[i];
              float value = cooMatrix.value[i];
06
07
              atomicAdd(&y[row], x[col]*value);
08
09
```

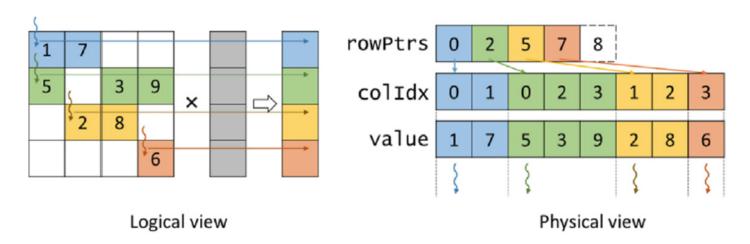
A parallel SpMV/COO kernel.

1	7			rowIdx	1	3	2	2	0	1	1	0
5		3	9	□ colidx	3	3	1	2	0	0	2	1
	2	8		V								_
			6	value	9	6	2	8	1	5	3	7

Reordering coordinate list (COO) format.



Example of compressed sparse row (CSR) format.



Example of parallelizing SpMV with the CSR format.

```
01
      global void spmv csr kernel(CSRMatrix csrMatrix, float* x, float* y) {
02
       unsigned int row = blockIdx.x*blockDim.x + threadIdx.x;
03
       if(row < csrMatrix.numRows) {</pre>
04
         float sum = 0.0f;
05
         for(unsigned int i=csrMatrix.rowPtrs[row]; i<csrMatrix.rowPtrs[row+1];</pre>
06
                                                                             ++i) {
07
            unsigned int col = csrMatrix.colIdx[i];
0.8
            float value = csrMatrix.value[i];
09
            sum += x[col]*value;
10
11
         y[row] += sum;
12
13 }
```

A parallel SpMV/CSR kernel.

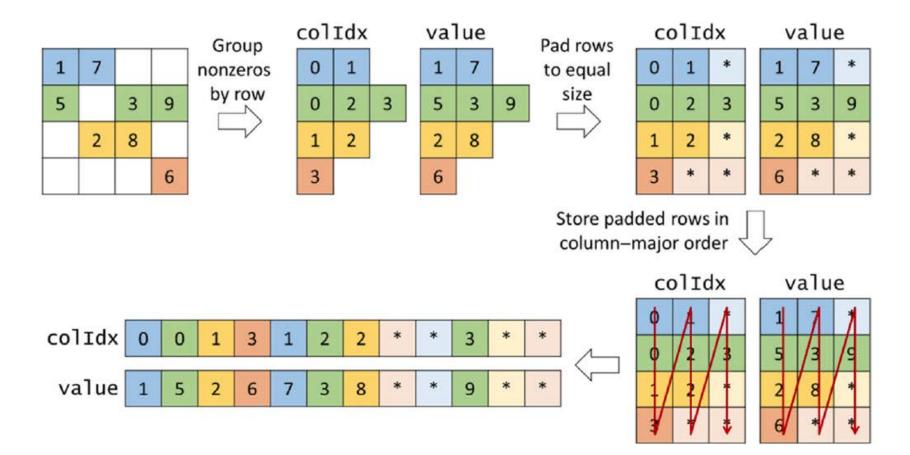
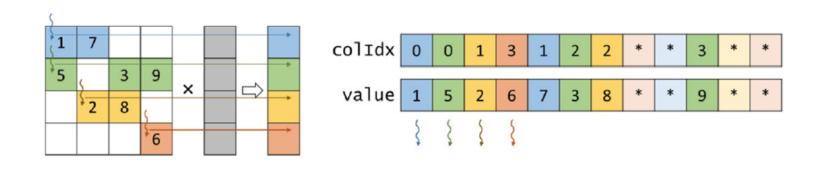


FIGURE 14.10

Example of ELL storage format.



Physical view

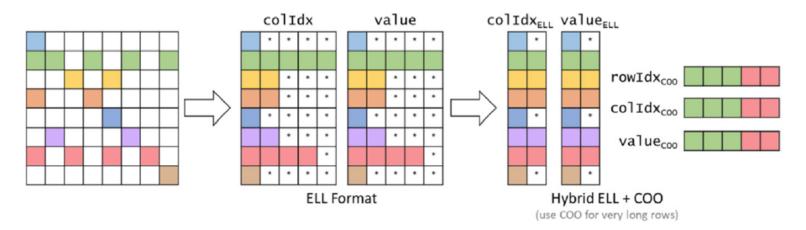
FIGURE 14.11

Example of parallelizing SpMV with the ELL format.

Logical view

```
01
        global void spmv ell kernel (ELLMatrix ellMatrix, float* x, float* y) {
02
          unsigned int row = blockIdx.x*blockDim.x + threadIdx.x;
03
          if(row < ellMatrix.numRows) {</pre>
              float sum = 0.0f;
04
05
              for(unsigned int t = 0; t < ellMatrix.nnzPerRow[row]; ++t) {</pre>
06
                   unsigned int i = t*ellMatrix.numRows + row;
07
                  unsigned int col = ellMatrix.colIdx[i];
                   float value = ellMatrix.value[i];
08
09
                   sum += x[col]*value;
10
11
              y[row] = sum;
12
13
```

A parallel SpMV/ELL kernel.



Hybrid ELL-COO example.

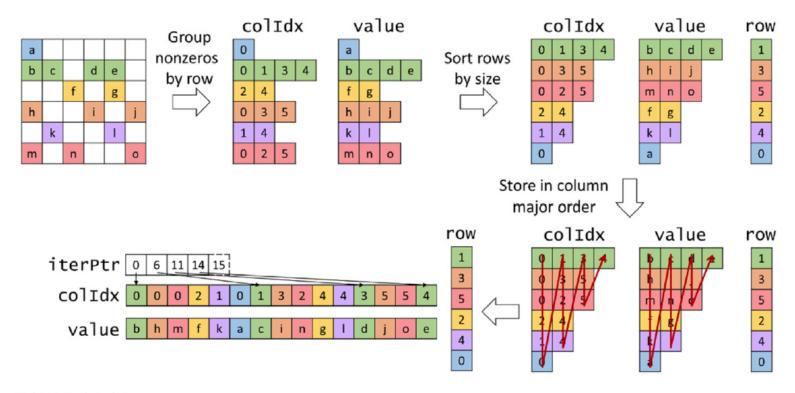
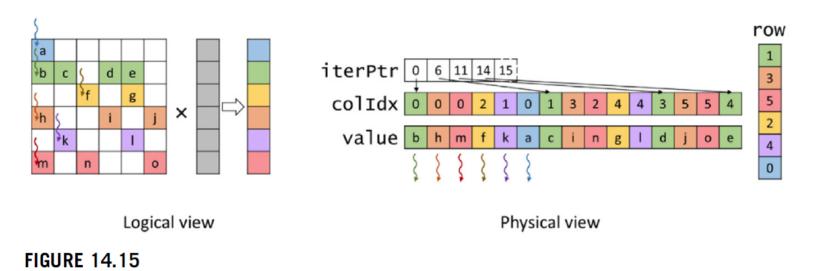


FIGURE 14.14

Example of JDS storage format.



Example of parallelizing SpMV with the JDS format.

i = t*ellMatrix.numRows + row

row = i%ellMatrix.numRows