

# Probability Theory of Random Polygons from the Quaternionic Viewpoint

<https://community.wolfram.com/groups/-/m/t/760148>

```
In[ ]:= ToComplex[{x_, y_}] := x + I y;
      |虚数单位
ToReal[z_] := {Re[z], Im[z]};
      |实部 |虚部
FrameToEdges[frame_] := ToReal[ToComplex[#]^2] & /@ Transpose[frame];
      |转置
FrameToVertices[frame_] := Accumulate[FrameToEdges[frame]];
      |累加

Manipulate[Module[{mat, frame, rotatedframe, verts, com},
|交互式操作 |模块
  mat = RotationMatrix[t, {Cos[θ] Sin[φ], Sin[θ] Sin[φ], Cos[φ]}] /.
      |旋转矩阵 |余弦 |正弦 |正弦 |余弦
    {θ → 3 π / 4, φ → 3 π / 4};
  frame = Transpose[ToReal[Sqrt[#]] & /@ (E^(I #) * 2 / 3 & /@ Range[0, 4 π / 3, 2 π / 3])];
      |转置 |平方根 |... |虚数单位 |范围
  rotatedframe = frame.Transpose[mat];
      |转置
  verts = FrameToVertices[rotatedframe];
  com = Mean[verts];
      |平均值
  verts = RotationMatrix[t].# & /@ (# - com & /@ verts);
      |旋转矩阵
  Graphics[{FaceForm[None],
|图形 |表面样式 |无
    EdgeForm[Directive[RGBColor["#383a40"], Thickness[.009], JoinForm["Round"]]],
      |边的格式 |指令 |RGB颜色 |粗细 |连接形式 |舍入
    Polygon[verts]], PlotRange → .8, ImageSize → 540,
      |多边形 |绘制范围 |图像尺寸
    Background → RGBColor["#F9F9F9"]], {t, 0, 2 π}]
      |背景色 |RGB颜色
```

Out[ ]:=

