

# 一些有趣的极限

In[\*]:= **Sum** $\left[\frac{1}{x^n}, \{n, 1, \text{Infinity}\}\right]$   
|求和 |无穷大

Out[\*]=

$$\frac{1}{-1 + x}$$

In[\*]:= **Manipulate** $\left[\text{Sum}\left[\frac{1}{x^n}, \{n, 1, \text{Infinity}\}\right], \{\{x, 6\}, 1, 10\}\right]$   
|交互式操作 |求和 |无穷大

Out[\*]=



In[\*]:= **1 / 5.5**

Out[\*]=

0.181818

下面两个在取整数时相等

In[\*]:= **Manipulate** $\left[\left\{\text{Sum}\left[x^2, \{x, 1, n\}\right], \frac{1}{6} n (n + 1) (2 n + 1)\right\}, \{\{n, 5\}, 1, 100\}\right]$   
|交互式操作 |求和

Out[\*]=



In[\*]:= **Manipulate** $\left[\left\{\text{Sum}\left[x^3, \{x, 1, n\}\right], \left(\frac{n (n + 1)}{2}\right)^2\right\}, \{\{n, 5\}, 1, 100\}\right]$   
|交互式操作 |求和

Out[\*]=



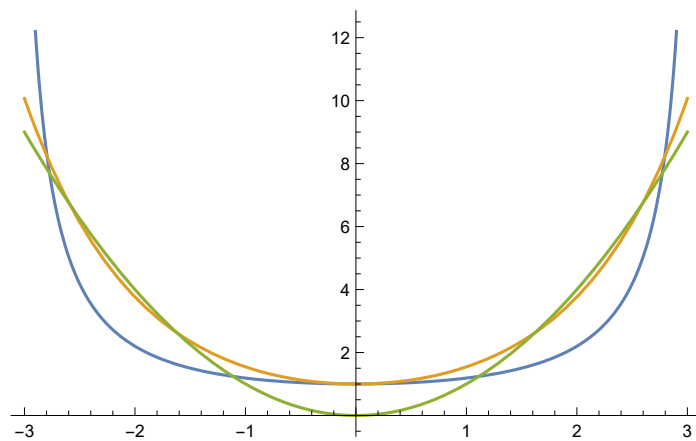
In[\*]:= **Limit** $\left[\frac{x}{\text{Sin}[x]}, x \rightarrow 0\right]$   
 [极限]

Out[\*]=

1

In[\*]:= **Plot** $\left[\left\{\frac{x}{\text{Sin}[x]}, \text{Cosh}[x], x^2\right\}, \{x, -3, 3\}\right]$   
 [绘图] [双曲余弦]

Out[\*]=



In[\*]:= **Limit** $\left[\frac{x}{\text{Log}[x+1]}, x \rightarrow 0\right]$   
 [极限]

Out[\*]=

1

In[\*]:= **Plot** $\left[\frac{x}{\text{Log}[x+1]}, \{x, -3, 3\}\right]$   
 [绘图]

Out[\*]=

