

Set theory

- the fundamental units of math are "sets"
- sets are unsorted & unique.

$$F := \{ \text{Jane, Mary, Susan, Dana} \}$$

denotes
the set, "RHS"

↑ "defines"

$$M := \{ \text{Dana, Bob, Joe, Max} \}$$

- sets can have infinite elements

e.g. $\mathbb{N} := \{ 1, 2, 3, \dots \}$ (natural #s)

$$\mathbb{Z} := \{ \dots, -2, -1, 0, 1, 2, \dots \}$$
 (integers)

Operators on sets

- element operators

Jane \in F "Jane is an element of
element set the set F"

Joe \notin F "Joe is not an element
of the set F"

$\{ \text{Jane, Mary} \} \subseteq F$ "the set $\{ \text{Jane, Mary} \}$
subset is a subset of set F"

- subset: all elements of the set on LHS are in the set on the RHS.

$\{ \text{Joe, Mary} \} \not\subseteq F$ "there exists at least one
element on the LHS that is not on
the RHS."

let $F' := \{Jane, Mary, Susan, Dana\}$

$$F = F'$$

→ set equality: $F \subseteq F' \neq F' \subseteq F$

$\{Jane, Mary\} \neq F$ * F isn't a subset of $\{Jane, Mary\}$

$\{Jane, Mary\} \subset F$ * not equal
proper subset

→ proper subset: LHS is a subset of RHS,
but RHS isn't a subset of LHS

ex. ① $\{Jane\} \subset F$ (true)

② $\{Jane\} \in F$ (false)

↑
the SET $\{Jane\}$ isn't in the set F , only
the ELEMENT Jane.

③ $Jane \in F$ (true)

④ $Jane \subset F$ (false)

↑
not defined

$\in, \notin, =, \neq, \subset, \subseteq$ - predicate functions
that return T/F.

ex. $\in(Jane, F) = \text{true}$.

Set Functions * return sets:

$F \cup M = \{Jane, Mary, Susan, Dana, Bob, Joe, Max\}$
Union

* doesn't include duplicates.

ex. ① $\{Dana\} \cup \{Dana\} = \{Dana\}$

② $Dana \in M \cup F$ (true)

③ $\mathbb{N}_0 := \mathbb{N} \cup \{0\} = \{0, 1, 2, 3, \dots\}$

$$F \cap M = \{Dana\}$$

Intersection

* elements that appear in both sets.

ex. ① $F \cap \{Bob, Joe\} = \emptyset$

$\emptyset := \{\}$, null set

② A, B both have ∞ elements.

can $A \cap B = \emptyset$?

yes, if $A = \text{even \#s}$ & $B = \text{odd \#s}$.

③ $\emptyset \subseteq F$ (true) * all sets contain empty set

④ $\emptyset \in F$ (false) * in this case, \emptyset not added as an element of F.