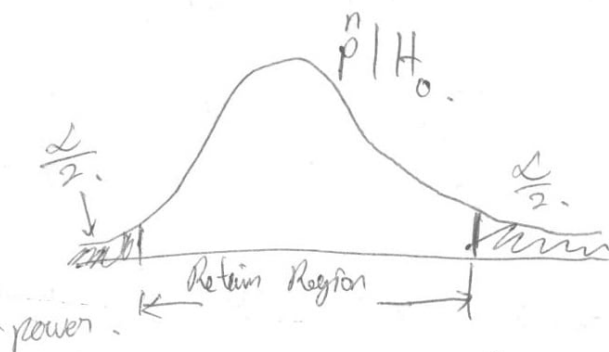


#23. Decision.

	Retain H_0	Reject H_0
H_0 true.	✓	Type I error Prob = α
H_0 false.	Type II error. Prob = β	✓



Consider $\alpha \downarrow \Rightarrow \beta \uparrow$ $n \uparrow = \beta \downarrow$ $n \uparrow \text{ or } \downarrow \Rightarrow \text{no change in } \alpha$
 $\alpha \uparrow \Rightarrow \beta \downarrow$ $n \downarrow = \beta \uparrow$

Clinical Trial for a drug

H_0 : Drug doesn't work, H_a : Drug Works.

Type I error: Selling the drug that doesn't work.

Type II error: Not selling the drug that does work.

Fire alarm system.

H_0 : No fire, H_a : Fire.

Type I error: False Alarm.

Type II error: Alarm doesn't go off when there is fire.

$\Rightarrow \alpha$ should be big: Minimal cost.

American Court system.

H_0 : Innocent, until he is proven guilty.

H_a : guilty.

Type I error: Innocent but go to jail.

Type II error: Guilty but not go to jail.

Scientific Theory.

H_0 : old theory.

H_a : New theory.

$\alpha = 1\%$ or 5% .

Human sex $p = 50\%$ (male).

$\hat{p} | p=0.5$.

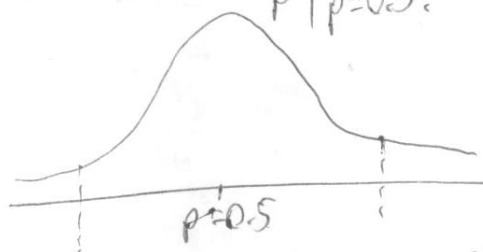
$H_0: p = 50\%$.

$H_a: p \neq 50\%$.

$\alpha = 5\%$.

2008 all American Births

$n = 4,247,000$.



old experiment $n = 345$.

Retain Region = $[0.446, 0.554]$

$$\text{Retain Region} \left[0.5 \pm 2 \sqrt{\frac{0.5(0.5)}{4247000}} \right] = [0.449, 0.505]$$

male = 2173000.

$$\hat{p} = \frac{2173000}{4247000} = 0.512 \notin \text{Retain Region}.$$

\therefore Reject $H_0 \Rightarrow$ sex isn't even.

$$CI_{p, 1-\alpha} := \left[\hat{p} \pm \frac{z_{\alpha/2}}{2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \right]$$

$$\text{Retain Region} := \left[p_0 \pm \frac{z_{\alpha/2}}{2} \sqrt{\frac{p_0(1-p_0)}{n}} \right]$$



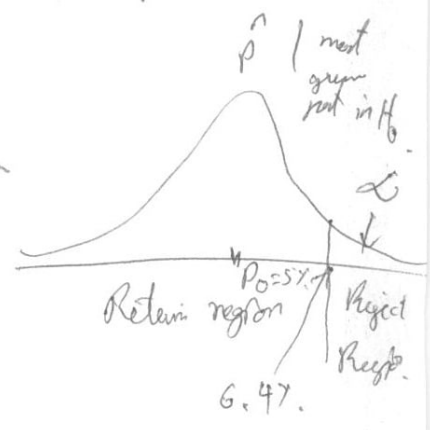
H_0 : Don't exist. Aliens.
 H_a : Exist.

α low. (ppl can't accept ^{even} with proof.)
 α - high (ppl can accept with prove)

I sided ^{prob} not be in the exam.

19. When fired bad drivers. If the driver has more than 5% ^{bad} rating which are bad, they are fired.

20. H_0 : Good driver. $p \leq P_0 = 5\%$.
 H_a : Bad driver. $p > P_0 = 5\%$.



$$\text{Ret: } \text{Reject}(-\infty, P_0 \pm z_{\alpha} \sqrt{\frac{P_0(1-P_0)}{n}})$$

$n=1000$, Ret Region $(-\infty, 0.064)$