Lec 8 9/26/17 Mars 241 Mork Hill Demo (if true) Know 11 $P(A | CD) = \frac{1}{13}$ $P(A) = \frac{4}{52} = \frac{1}{13}$ P(AID) Since this docks charge... dol the informany of O moster is the prob ale? P(IBM Stock 7) Vaits in Brenos Ares) = PIBM Stock 7) Def: A, D are indepute across P(A B) = P(A) =) (AB) = P()(Bb) (Molt. Rule, P(010) = P(0)

let
$$A_1, A_2, \dots$$
 be indepler evers

$$P(A_1, A_2, \dots) = P\left(\bigcap_{i=1}^{\infty} A_i\right) = \frac{1}{|A_i|} P(A_i)$$

Flip our coin.

$$P(H_1, H_2) = P(H_1) = 0.5$$

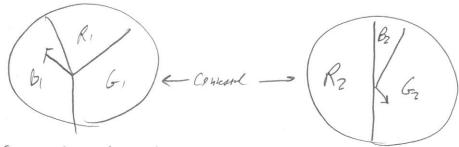
$$P(H_1, H_2, H_3, H_4, H_5) = \frac{1}{2^5} = |\Omega^5|$$

Clarifier de Pare

$$\begin{array}{rcl}
M(n+6-6) &= 1 - P(6,6) \\
&= 1 - P(6)^{2} \\
&= 1 - (\frac{1}{6})^{3} \\
&= \frac{25}{36}
\end{array}$$

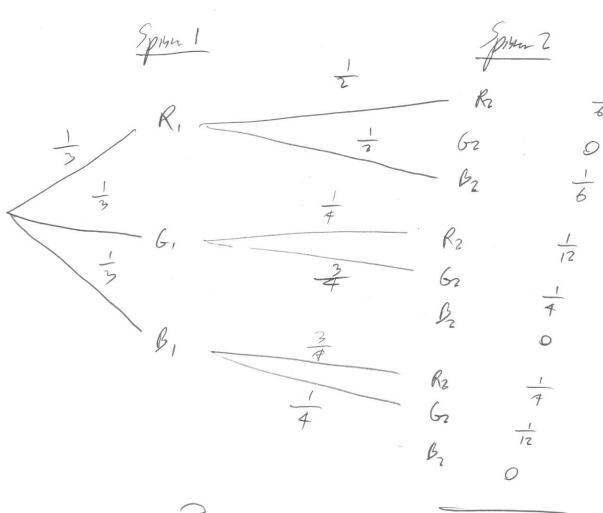
If P(B/A) \neq P(B) or P(A/O) \neq P(A) or P(A) \neq P(A =) A, B are not ideplan (depaler) P(Q64 /nx) ARBA Ine Stonston PQ64 love / no truffice) P(Q64 Ine) P(ly com Snoke) Rlyg comm Assm A,B = P = indepelar ? Tess is ewas al non rein prob. $P(0|B) \stackrel{?}{=} P(A) | O = P(1/T) \neq P(A) = \frac{1}{2}$ Consider de Repeder Coin (H) (H) Anysa Con Rayula Con P(HH) = 1/2 2 T T P(TT)=1

Dressus Paggeles doesn't ren Paggelar 14 a physial sense



$$P(R_1) = P(G_1) = P(G_1) = \frac{1}{3}$$

$$P(R_2) = \frac{1}{2}, P(G_2) = \frac{1}{3}, P(B_2) = \frac{1}{6}$$



R, Re Folepulero?

$$P(R, R_2) \stackrel{?}{=} P(R) P(R_2) \Rightarrow \frac{1}{6} = \frac{1}{3} \cdot \frac{1}{8} = \frac{1}{6}$$

Ac R, & 62 Appeles?

 $P(R, G_2) \stackrel{?}{=} P(R) P(G_2)$ $Q \not= \frac{1}{3} \frac{1}{3} = \frac{1}{9}$

No. ty one depoter. Only R, & R, on "Magelor"
or intropolog included

Birthay Problem Plas leus p. of you show he some boy = P(De pair sen bod) +P(2 pairs Sm bod) +P(3 pairs sm bods) due in Easier may ?? Pars she boy = | - P (AL) = | - P(no de stres same body) Assure bours eggly likely =) P(B)=1- = 19,4%

Hns Problem
n people walk me a room and por ster hors on the solle.
n people walk into a room and por their hors on he on the. The hors are then randonly gon ont so common p: (con people go hor)
() (at leurs or peus yess ho) = P (1 p gers ha) + Rep gers ha) + + A a profes
Looks HARD
h > >
A B C
$\begin{cases} \frac{1}{2} & A & \frac{1}{2} & A & - C \\ \frac{1}{2} & \frac{1}{2} $
But iffiner 95 hgos up!
los A: clan is which it's person area
OR In
$= P\left(\bigcup_{i=1}^{n} A_{i}\right)$
$= \mathcal{E} P(A_i) - \mathcal{E} P(A_i \cap A_j) + \mathcal{E} (PA_i \cap A_j \cap A_p) - + - + \dots (-1)^{n+1} P(A_i)$ $= \mathcal{E} P(A_i) - \mathcal{E} P(A_i \cap A_j) + \mathcal{E} (PA_i \cap A_j \cap A_p) - + - + \dots (-1)^{n+1} P(A_i)$
gland rule. prom w) Adretion
$P(A_1) = \frac{1}{h!} = \frac{(A_1)^2}{h!} = \frac{1}{h!}$
$P(A_1) = \frac{n-1}{2} = \frac{1}{5}$
$\Rightarrow \mathcal{E} P(A_i) = 1$

$$P(A, Az) = \frac{1 \cdot 1 \cdot 2 \cdot 4 \cdot 3}{4!} = \frac{(4-2)!}{4!}$$

$$P(A, Az) = \frac{1 \cdot 4 \cdot 2 \cdot 4 \cdot 3}{4!} = \frac{(4-2)!}{4!}$$

Hon nay?

$$= \sum_{i \neq j} P(A_i(A_j)) = {\binom{3}{2}} {\binom{6-2}{1}!} = \frac{1}{2!(6-2)!} \frac{5-25!}{5!} = \frac{1}{2!}$$

Hommy?

$$= \sum_{\substack{i+j+k}} P(A_i \cap A_i \cap A_n) = \binom{h}{3} \frac{(6-3)!}{h!} = \frac{h!}{(6-3)!3!} \frac{(6-3)!}{h!} = \frac{h!}{(6-3)!3!} \frac{(6-3)!}{h!} = \frac{1}{3!}$$

Desom $f(x) = \sum_{i=0}^{\infty} \frac{f(i)(c)}{i!} (x-c)^{i} \quad \forall c \in \mathbb{R} \quad \text{(Taylor Server)}$

(14 mly if fin mo fa) when x2 > fa) 2 fa) + f'(7) (x-7) + f''(1) (x-7)2

Stop at 2 terms

$$e^{x} = e^{0} + \frac{e^{0}}{1!} \times \frac{e^{0}}{2!} \times \frac{1}{2!} + \frac{x^{2}}{2!} + \dots$$

$$\Rightarrow |-e^{-1}| = |-\frac{1}{2!} + \frac{1}{3!} - \frac{1}{4!} + \cdots - \frac{1}{4!} +$$

$$\Rightarrow 1-p=1-e^{-1} \Rightarrow p=e^{-1} \approx 0.368 \approx \frac{1}{3}$$