

1 cup with 6 coins in it. 2 of the coins are marked.

- shake the cup then quarry 1 coin, is it Marked? - NO

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record the number of shakes, repeat the entire process again

- shake the cup then quarry 1 coin, is it Marked? - Yes \rightarrow STOP record the number of flips. We repeat the experiment

The cup can be viewed as a single entity capable to deliver a marked coin with the probability of 1/3. It is as if we

had a single 'unfair coin' with probability of Heads = 1/3.

We keep flipping this 'unfair coin' until we get Heads. We

Thus a single trial means that we keep conducting iid

Bernoulli experiments over and over until we get the first

success which is the 'stopping time' for each trial.

 $X \sim Bernoulli (1/3) := \begin{cases} 1 & wp \ 1/3 \end{cases}$ (Heads = marked coin) wp 2/3

Custom r.v.s? Ever wondered how to build custom r.v.s?

	Custom r.v.s Ever wondered how to build custom r.v.s?	
Rademacher	Bet on Black. Payout is 1:1 (bet \$1 win \$1) Roulette in U.S. total of 38 pockets: 18 black 18 red 2 green 0,	
	what is the expectation ?	
	$E[X] = \sum_{x \in Supp[X]} x p(x) = \$1 \cdot p(\$1) + (-\$1) \cdot p(-\$1)$ $= \$1 \cdot 18/_{38} + (-\$1) \cdot 20/_{38}$ the more you play the more you loose in a long run you loose in a long run you loose everything - you can you are loosing ≈ 5.3 cents (per play)	$pu'll X_1 \;,\; X_2 \;, \ldots \;,\; X_n \overset{iid}{\sim} \; \left\{ \begin{array}{c} x_1 \;\; x_1 \;\; x_2 \;\; x_3 \;\; x_4 \;\; x_4 \;\; x_5 \;\; x_6 \;\; x_6$
	Bet on 'lucky' # 7. Payout is 35:1 (bet \$1 win \$35) Roulette in U.S. total of 38 pockets: 18 black 18 red 2 green 0 $\frac{1}{38}$	means very little when you have only few rand variables.
	what is the expectation? $E[X] = \sum_{x \in Supp[X]} x p(x) = \$35 \cdot p(\$35) + (-\$1) \cdot p(-\$1)$ $= \$35 \cdot 1/_{38} + (-\$1) \cdot 37/_{38}$ $= -\$0.053$	hint: - play video draw poker duces wild
	Bet on 'dozen' # 112 Payout is 2:1 (bet \$1 win \$2) Roulette in U.S. total of 38 pockets: 18 black 18 red 2 green 0 $\frac{12}{38}$	
	what is the expectation? $E[X] = \sum_{x \in Supp[X]} x p(x) = \$2 \cdot p(\$2) + (-\$1) \cdot p(-\$1)$ $= \$2 \cdot 12/_{38} + (-\$1) \cdot 26/_{38}$ $= -\$0.053$	
	Bet on 'dozen' # 112 Payout is 2:1 (bet \$1 win \$2) Roulette in European Street St	rope
	what is the expectation? in a long run you will loose half the money playing the European $= \frac{\sum_{x \in Supp[X]} x}{\sum_{x \in Supp[X]} p(x)} = \frac{2 \cdot p(\$2) + (-\$1) \cdot p(-\$1)}{\sum_{x \in Supp[X]} p(x)} = \frac{2 \cdot 12}{37} + (-\$1) \cdot \frac{25}{37}$ $= -\$0.027$ in a long run you will loose half the money playing the European Roulette over the US version.	
	if X models a payout of a game, "Fair Game" is if E[X] = 0	
	Basic r.v. transportation – Uber example	
	P(traffic on route A) = 0.3 If there is traffic on route A, take route - route A is 7min	≥ B.

- route B is 12min

– on average in all my trips the time spend in the taxi is ≈8.5 min

- this exact value pertains to an infinite amount of trips

7min w.p. 0.7

12min w.p. 0.3 not a Bernoulli b/c Supp[X] # {0,1}

= 8.5 min

 $E[W] = \sum x p(x) = 7\min \cdot p(7\min) + 12\min \cdot p(12\min)$

 $= 7\min \cdot 0.7 + 12\min \cdot 0.3$