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*Model Predictive Control:  
From Design to Implementation*

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# Overview

1. Introduction to design vs. implementation
2. Four tank process as illustrative example
3. Brief overview of OPC
4. Testing before commissioning using a process emulator
5. Implementation of MPC on four tank process

# Design vs. Implementation

- ▶ MPC may be designed using simulation models
  - ▶ Sensors and actuators are ideal and local
  - ▶ System states are known
  - ▶ Computation time is not an issue

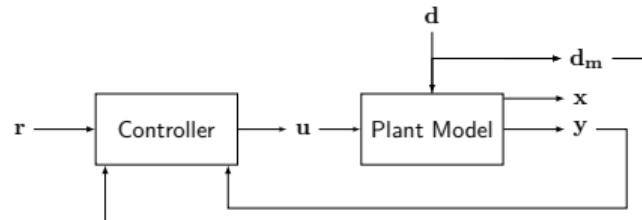


Figure: System considered in the design phase.

- ▶ This is seldom the case when implementing

# Design vs. Implementation

- ▶ An advanced controller interfaces with equipment through an interoperability layer
  - ▶ Sensors and actuators are *not* ideal
  - ▶ System states are *not* known
  - ▶ Computation time *may* be an issue

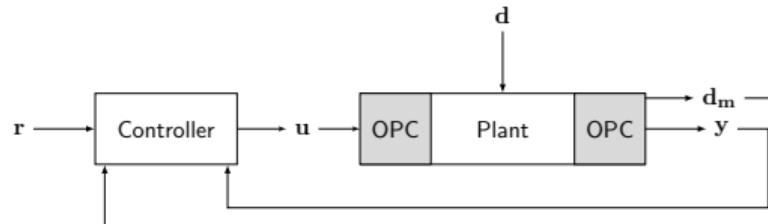


Figure: System considered in the implementation phase.

# Four Tank Process



Figure: Four tank process.

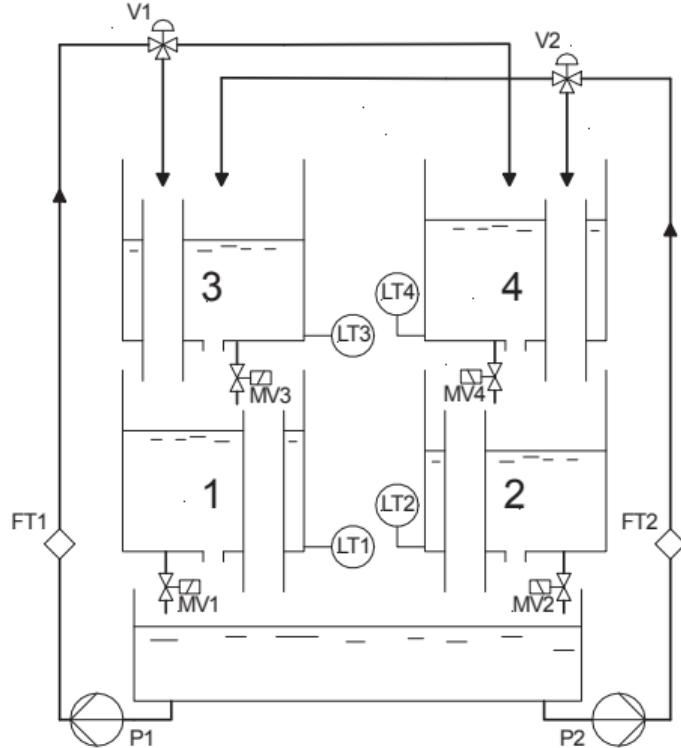


Figure: Four tank process P&ID.

# Four Tank Process

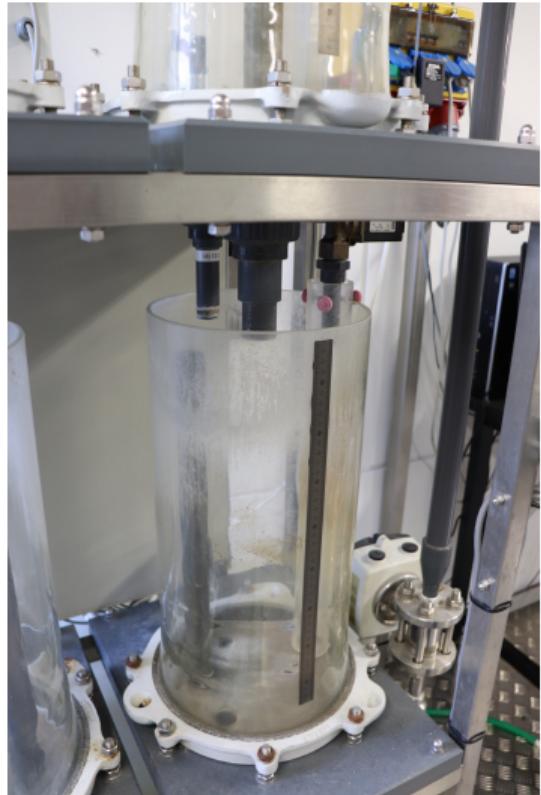


Figure: Four tank process.

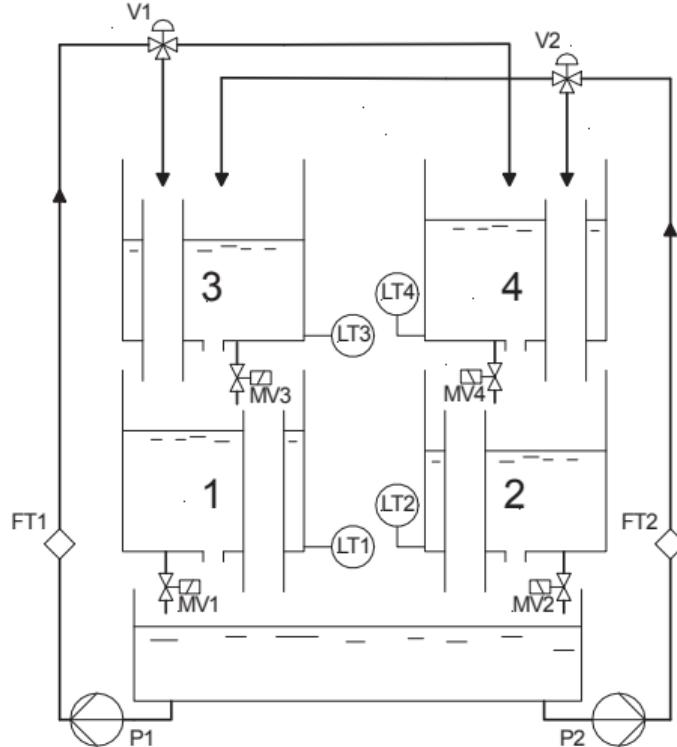


Figure: Four tank process P&ID.

# Model Predictive Control of Four Tank Process

- Constrained MPC using discretized linearization of first-principles ODE model

$$\dot{m}_1 = \rho (q_{1,\text{in}} + q_{3,\text{out}} - q_{1,\text{out}})$$

$$\dot{m}_2 = \rho (q_{2,\text{in}} + q_{4,\text{out}} - q_{3,\text{out}})$$

$$\dot{m}_3 = \rho (q_{3,\text{in}} - q_{3,\text{out}})$$

$$\dot{m}_4 = \rho (q_{4,\text{in}} - q_{4,\text{out}})$$

$$q_{i,\text{out}} = a \sqrt{\frac{2g}{\rho A}} m_i, \quad q_{1,\text{in}} = F_1 \gamma_1, \quad q_{2,\text{in}} = F_2 \gamma_2$$

$$q_{3,\text{in}} = F_2 (1 - \gamma_2), \quad q_{4,\text{in}} = F_1 (1 - \gamma_1),$$

$$A = 380 \text{ cm}^2, \quad a = 1.22 \text{ cm}^2, \quad \gamma_1 = 0.38, \quad \gamma_2 = 0.24$$

- Variable classification:

$u$ : P1, P2

$y$ : LT1, LT2, LT3, LT4

$z$ : LT1, LT2

$d$ : MV1, MV2, MV3, MV4

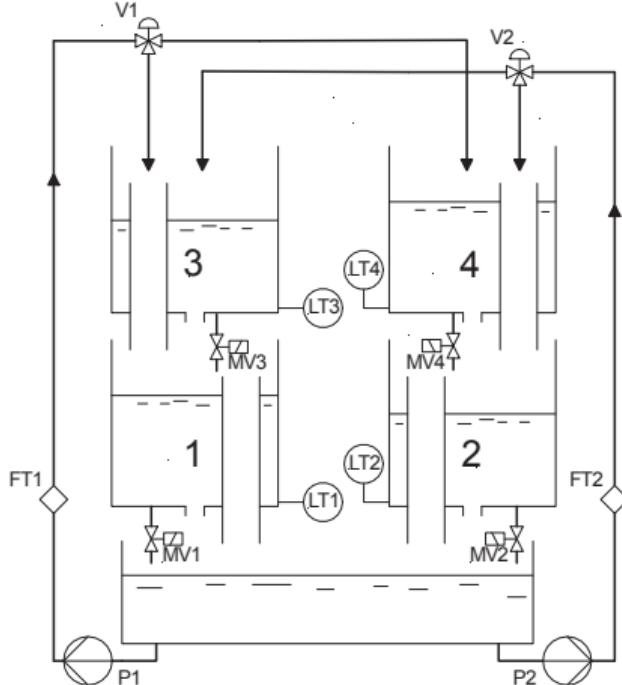


Figure: Four tank process P&ID.

# Regulator

- ▶ Model is augmented with integrating states to enable offset-free control
- ▶ Linear time-invariant measurement-update time-update Kalman filter
- ▶ Linear MPC:

$$\min_{\mathbf{u}} \quad \frac{1}{2} \sum_{k=1}^{N_{\text{mpc}}} \|\mathbf{z}_k - \mathbf{r}_k\|_{\mathbf{Q}_z}^2 + \|\mathbf{u}_{k-1} - \mathbf{u}_{k-2}\|_{\mathbf{Q}_{\Delta u}}^2$$

subject to

$$\mathbf{x}_{k+1} = \mathbf{A}_d + \mathbf{B}_d \mathbf{u}_k + \mathbf{E}_d \mathbf{d}_k, \quad k = 0, 1, 2, \dots, N_{\text{MPC}} - 1$$

$$\mathbf{z}_k = \mathbf{C}_{d,z} \mathbf{x}_k, \quad k = 1, 2, 3, \dots, N_{\text{MPC}}$$

$$\mathbf{u}_{\min, k} \leq \mathbf{u}_k \leq \mathbf{u}_{\max, k}, \quad k = 0, 1, 2, \dots, N_{\text{MPC}} - 1$$

$$\Delta \mathbf{u}_{\min, k} \leq \mathbf{u}_{k+1} - \mathbf{u}_k \leq \Delta \mathbf{u}_{\max, k}, \quad k = 0, 1, 2, \dots, N_{\text{MPC}} - 1$$

- ▶  $\mathbf{Q}_z = 5 \cdot 10^5 \mathbf{I}$ ,  $\mathbf{Q}_{\Delta u} = \mathbf{I}$ ,  $|\Delta u| \leq 100 \text{ cm}^3 \text{ s}^{-1}$  and  $170 \text{ cm}^3 \text{ s}^{-1} \leq u \leq 500 \text{ cm}^3 \text{ s}^{-1}$
- ▶ Prediction horizon: 200, control horizon: 190,  $T_s = 5 \text{ s}$

# Instrumentation

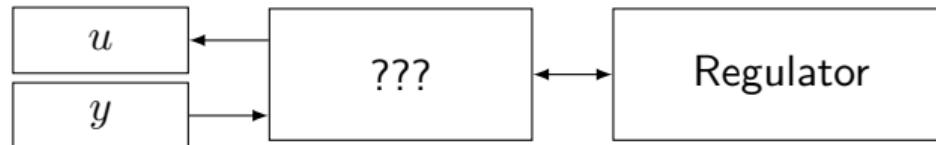
**Table:** Process equipment.

P&ID Id	Brand	Model	IO
V1, V2	Samson	3226, I/P positioner 3760	4 – 20 mA
MV1–MV4	Bürkert	6213	0 or 10 V
LT1–LT4	Siemens SITRANS	7MF1563-3AA-00	4 – 20 mA
FT1, FT2	Danfoss MAG	1100/5000	4 – 20 mA
P1, P2	Grundfos MAGNA	25-60 N 180 1x230-240V PN6/10	0 – 10 V

- ▶ Sensors and actuators are calibrated
- ▶ Regulator is implemented in Python

*Libraries: OpenOPC, freeopcua, cvxopt, scipy, matplotlib*

# The Problem



**Figure:** Communications between process equipment and regulator.

# The OPC Foundation

*OPC technologies were created to allow information to be easily and securely exchanged between diverse platforms from multiple vendors and to allow seamless integration of those platforms without costly, time-consuming software development.*

– OPC Foundation

- ▶ Acronym for Microsoft Object Linking & Embedding for **Process Control**
- ▶ Original OPC standard (now referred to as OPC Classic) was published in 1996
- ▶ Most recent OPC standard called OPC Unified Architecture was published in 2006
- ▶ 512 members representing industry including ABB, Siemens, Rockwell, Schneider Electric and Omron

## OPC Classic

OPC Classic comprises the following components:

- ▶ **OPC Data Access (OPC DA)**

The OPC DA specification defines the exchange of data including values, time and quality information.

- ▶ **OPC Alarms & Events (OPC AE)**

The OPC A&E specification defines the exchange of alarm and event type message information, as well as variable states and state management.

- ▶ **OPC Historical Data Access (OPC HDA)**

The OPC HDA specification defines query methods and analytics that may be applied to historical, time-stamped data.

### Drawbacks:

- ▶ Only implemented on Windows
- ▶ Low-level data structures
- ▶ Difficult to handle securely on a network

### Advantages:

- ▶ Widely adopted by industry

# OPC Unified Architecture

OPC-UA is the key to IoT and Industry 4.0

- ▶ All COM OPC Classic specifications are mapped to UA ensuring compatibility
- ▶ Platform independent
- ▶ Encrypted communications
- ▶ Supports complex data structures
- ▶ A single interoperability standard

A major drawback to OPC-UA is that the lifetime of industrial equipment is typically longer than the period since OPC-UA was published. A lot of equipment currently in place was only designed for OPC Classic.

# OPC in General

- ▶ Client-server model
  - ▶ Process is the server
  - ▶ Regulator is the client
- ▶ An OPC server may be thought of as a database
- ▶ An OPC client can retrieve data (measure) and save data (actuate) on the server

## Matlab and Python Minimal Client Examples

```
1 % Connect to OPC-UA server
2 ua = opcua('opc.tcp://kt-pr-4tank:4840/four_tank_process/');
3 connect(ua);
4 % Browse namespace to find IW04 (FT1) and QW04 (P1)
5 % The ua.browseNamespace function opens a GUI where the
6 % namespace may be browsed.
7 S7200 = findNodeByName(ua.Namespace,'S7200.OPCServer');
8 Microwin = findNodeByName(S7200,'Microwin');
9 CPU224 = findNodeByName(Microwin,'CPU224');
10 IW04 = findNodeByName(CPU224,'IW04');
11 QW04 = findNodeByName(CPU224,'QW04');
12 % Read value of IW04
13 readValue(IW04)
14 % Write value to QW04
15 writeValue(QW04,0);
16 % Disconnect
17 disconnect(ua);
```

```
1 from opcua import Client
2 # Connect to OPC-UA server
3 ua = Client('opc.tcp://kt-pr-4tank:4840/four_tank_process/')
4 ua.connect()
5 # Browse namespace to find IW04 (FT1) and QW04 (P1)
6 # You may browse the namespace in a
7 # GUI using the opcua-client software.
8 objects = ua.get_root_node().get_child('0:Objects')
9 S7200 = objects.get_child('2:S7200.OPCServer')
10 Microwin = S7200.get_child('2:Microwin')
11 CPU224 = Microwin.get_child('2:CPU224')
12 IW04 = CPU224.get_child('2:IW04')
13 QW04 = CPU224.get_child('2:QW04')
14 # Read value of IW04
15 print(IW04.get_value())
16 # Write value to QW04
17 QW04.set_value(0)
18 # Disconnect
19 ua.disconnect();
```

# Testing Before Commissioning Using Process Emulator

You can make your own OPC server

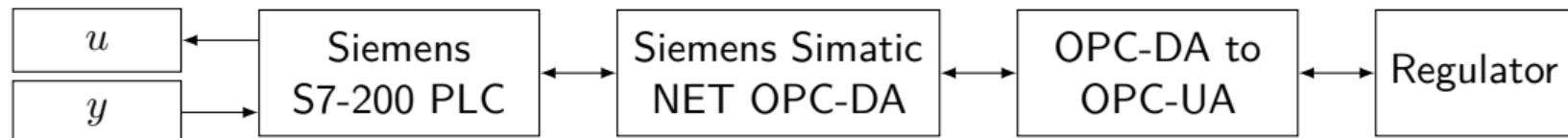
- ▶ Wrap process simulator in OPC-UA server with structure identical to the actual plant
- ▶ Implement functionality such as PID loops, sensor/actuator calibration and dynamics in the OPC server

The emulator allows risk-free testing of regulators which communicate using OPC-UA before commissioning

If a regulator works as expected when applied on the test OPC-UA server then there is a good chance that it will also work when implemented on the actual process

# Implementation of MPC on Four Tank Process

- ▶ The four tank process offers data access at three layers:
  1. PLC
  2. OPC Classic Server
  3. OPC-UA Server (proxy to OPC Classic Server)
- ▶ Regulator may be implemented using open source software



**Figure:** Communications between process equipment and regulator.

A simulation OPC-UA server which emulates the actual four tank process is implemented in Python to aid the development of regulators communicating using the OPC-UA standard

# Implementation of MPC on Four Tank Process

Demonstration

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