

HUMBOLDT UNIVERSITY OF BERLIN

PROJEKTPRAKTIKUM

# Documentation of qr.py

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The following is the documentation for the module `qr.py`.

## 1 `qr(A)`

This function computes the QR-decomposition.

### Arguments

A (ndarray): Two dimensional ndarray.

### Returns

(ndarray): Two dimensional ndarray of the QR-decomposition, Q.

(ndarray): Two dimensional ndarray of the QR-decomposition, R.

## 2 `full_rank(A)`

A boolean-function to check if the matrix has full column rank.

### Arguments

A (ndarray): Two dimensional ndarray.

### Returns

(boolean): True if A has full column rank and False otherwise.

## 3 `solve_QR(A, b)`

Solves the equation  $Ax = b$  for x with the QR-decomposition.

### Arguments

A (ndarray): Two dimensional ndarray. Should have full column rank.

b (ndarray): One dimensional ndarray.

### Returns

(ndarray): One dimensional ndarray for x.

## 4 `norm(A, b)`

Computes the normed error induced by solving the linear equation with the function above.

### Arguments

A (ndarray): Two dimensional ndarray. Should have full column rank.

b (ndarray): One dimensional ndarray.

### Returns

(float): The normed difference between  $Ax$  and  $b$ .

## 5 **condition(A)**

Calculates the condition of  $A$  and  $A^T A$ .

### **Arguments**

A (ndarray): Two dimensional ndarray.

### **Returns**

(float, float): The condition of  $A$  and  $A^T A$ .

## 6 **input\_data(file\_name, indices=None)**

Takes a properly formatted text file and builds a two dimensional ndarray. Additionally, a list of indices can be passed to return specific entries.

### **Arguments**

file\_name (String): The path and the name of the text file.

indices (list): List of indices.

### **Returns**

(ndarray): The entries of the matrix with the passed indices. If the argument indices were left out, this returns the entire matrix.

## 7 **draw(data)**

Draws the plot of the linear regression according to the data passed.

### **Arguments**

data (ndarray): Two dimensional ndarray.

## 8 **norm\_residuals(data)**

Computes the residuals for the solution with and without  $p_2$ .

### **Arguments**

data (ndarray): Two dimensional ndarray.

### **Returns**

(float, float): The residuals for  $Ax = b$  without taking  $p_2$  into consideration and with.

## 9 **main()**

The main-function to demonstrate the capabilities of the module.