

# An assessment of racial disparities in pretrial decision-making using misclassification models

**Kimberly A. H. Webb**, Sarah A. Riley, and Martin T. Wells

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# Problem setting



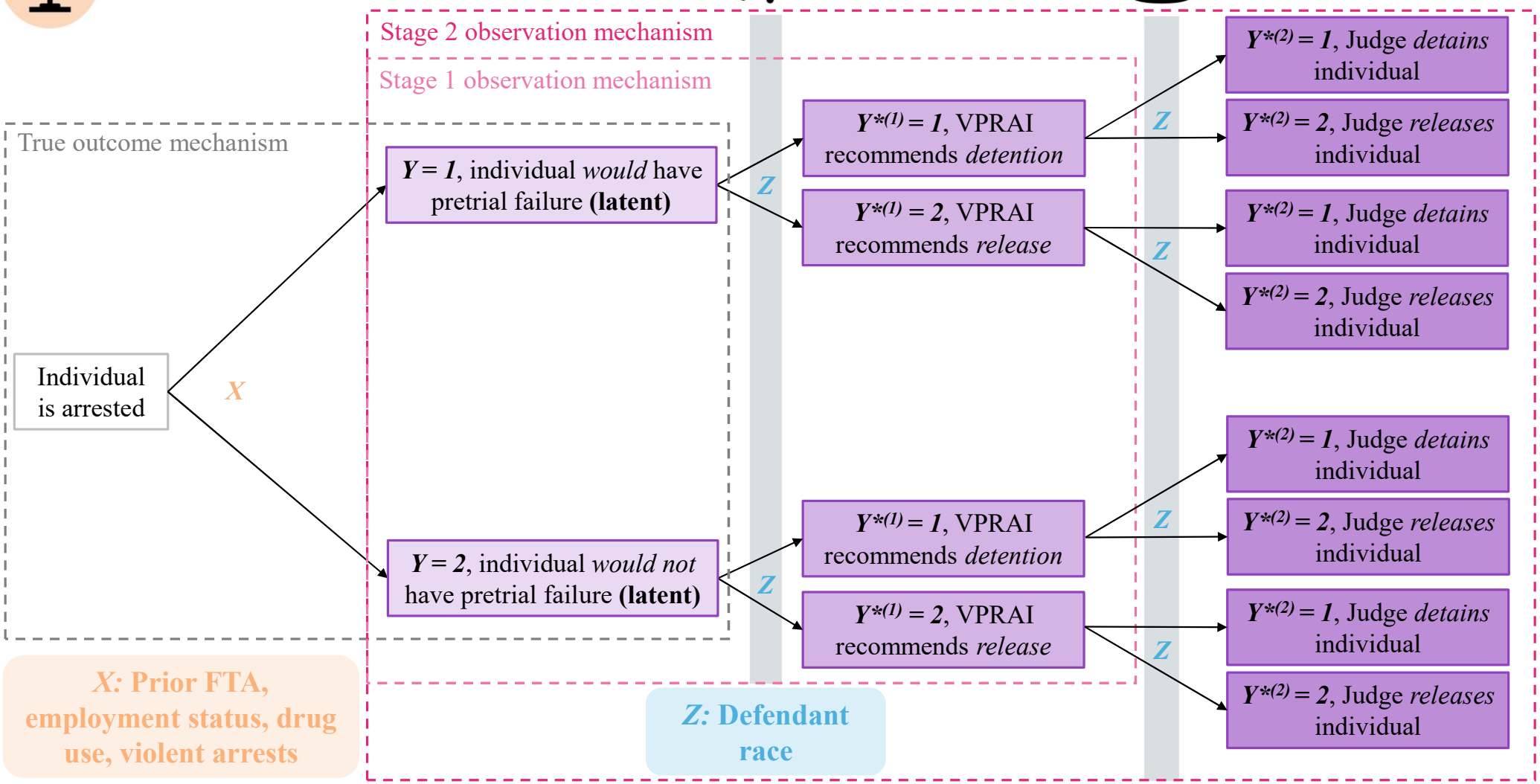
- **Goal:** Study **algorithmic bias** in **pretrial risk assessment**.

***Pretrial failure:***  
Reoffending before trial or failing to appear for trial

- **Pretrial risk assessment algorithms** provide an evaluation of the likelihood of “**pretrial failure**”.
- Used by judges at arraignment to determine whether to release or detain defendants pending trial.
- What are **risk factors** for pretrial failure? Are judges and risk assessments **accurate**? Are they **biased**?

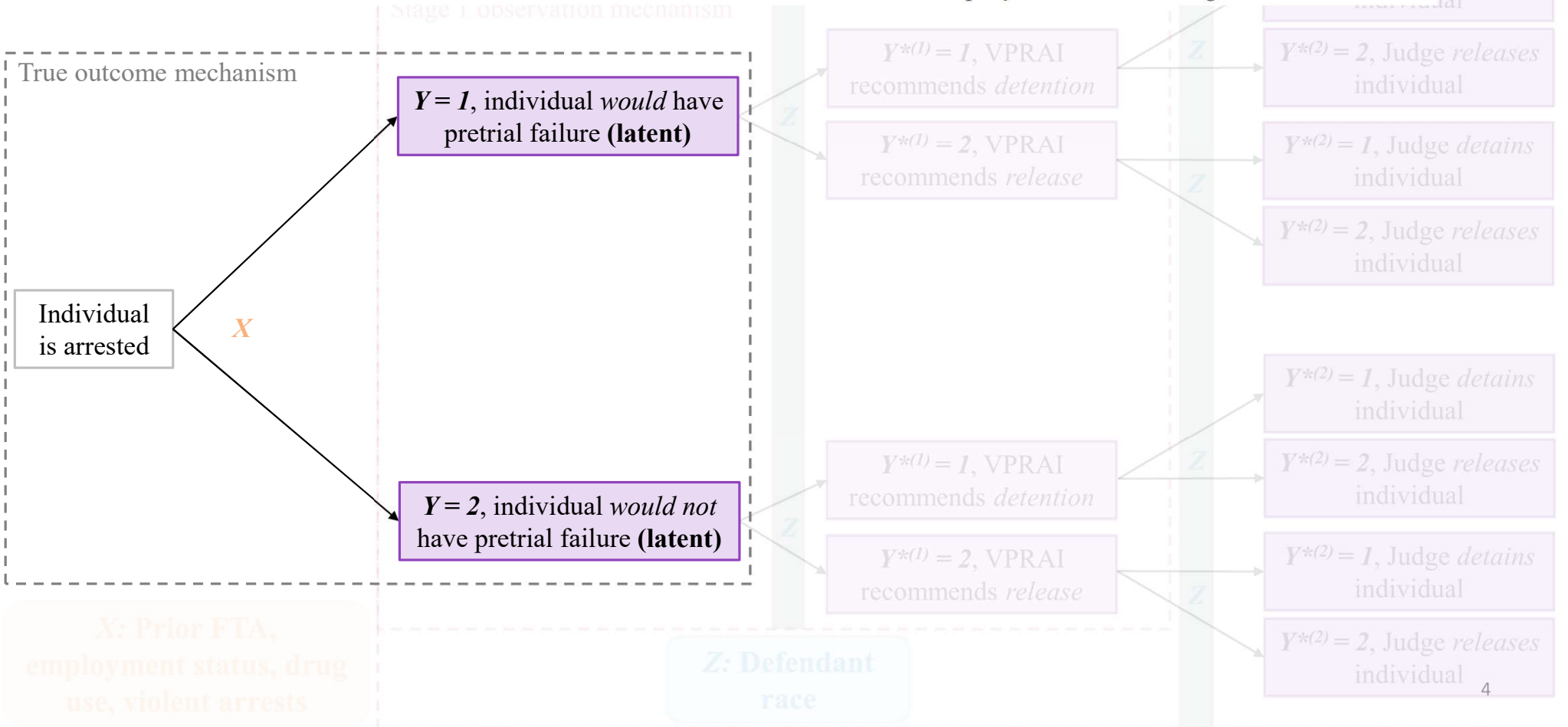


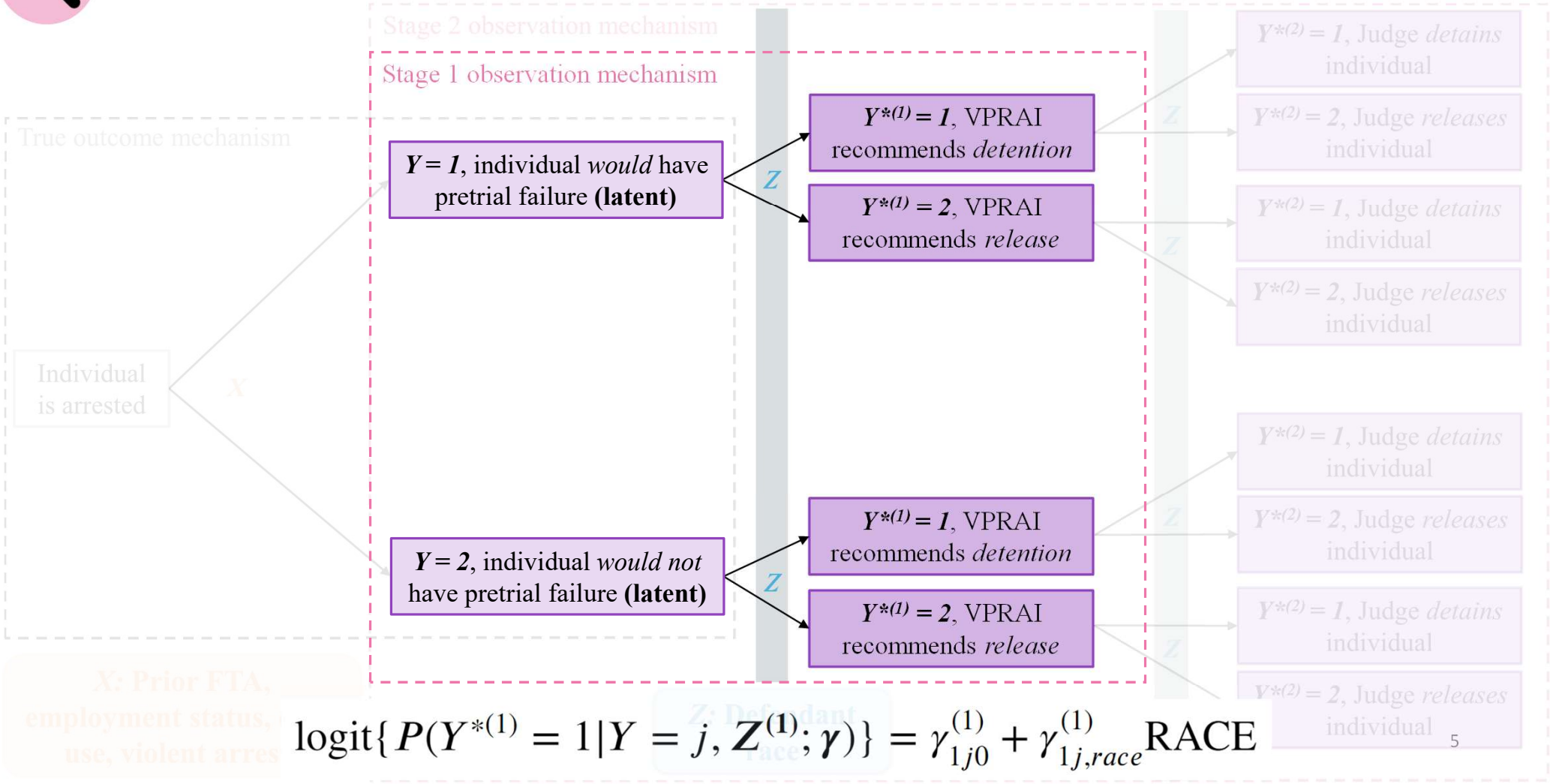
- **Method:** Develop misclassification modeling approach, incorporating the “two stage” nature of this system.





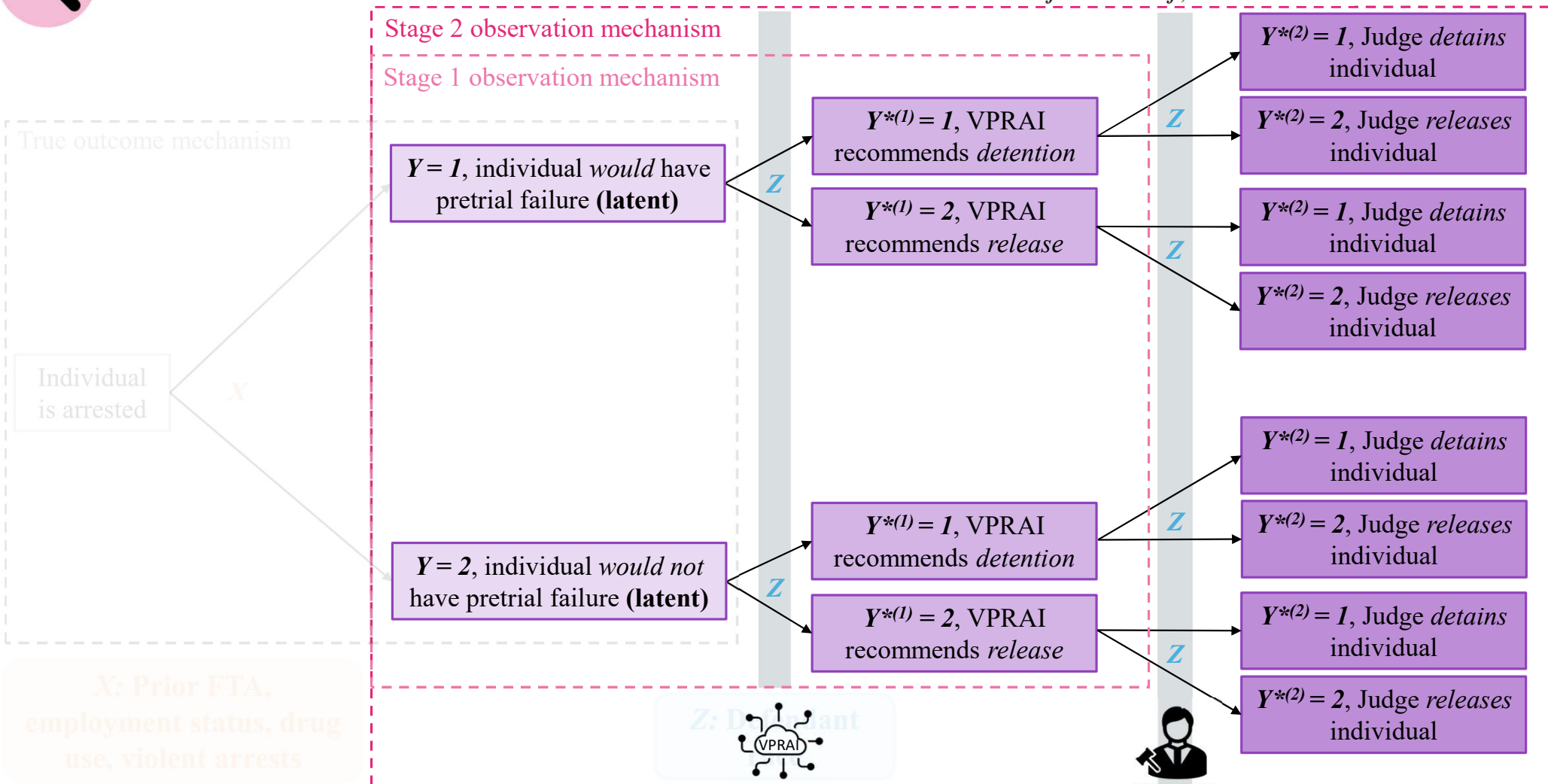
$$\text{logit}\{P(Y = 1|X; \beta)\} = \beta_0 + \beta_{FTA} FTA + \beta_{unemployed} E + \beta_{drug} D + \beta_{violent} V$$







$$\text{logit}\{P(Y^{*(2)} = 1 | Y^{*(1)} = k, Y = j, \mathbf{Z}^{(2)}; \boldsymbol{\gamma})\} = \gamma_{1kj0}^{(2)} + \gamma_{1kj, \text{race}}^{(2)} \text{RACE}$$





**Primary interest: Estimating  $\beta$**

**Secondary interest: Estimating  $\gamma$**

True outcome mechanism:

$$\text{logit}\{P(Y = 1|X; \beta)\} = \beta_0 + \beta_{FTA} FTA + \beta_{unemployed} E + \beta_{drug} D + \beta_{violent} V$$

Stage 1 (VPRAI) observation mechanism:

$$\text{logit}\{P(Y^{*(1)} = 1|Y = j, Z^{(1)}; \gamma)\} = \gamma_{1j0}^{(1)} + \gamma_{1j,race}^{(1)} \text{RACE}$$

Stage 2 (Judge) observation mechanism:

$$\text{logit}\{P(Y^{*(2)} = 1|Y^{*(1)} = k, Y = j, Z^{(2)}; \gamma)\} = \gamma_{1kj0}^{(2)} + \gamma_{1kj,race}^{(2)} \text{RACE}$$



Primary interest: Estimating  $\beta$

Secondary interest: Estimating  $\gamma$

Estimation methods

- Proposed **EM algorithm**
- Bayesian methods (**MCMC**)





# Complete data log-likelihood

- **Y (true pretrial failure status)** is a latent variable, but let's pretend we know it:

$$\begin{aligned}
 \ell_{complete}(\boldsymbol{\beta}, \boldsymbol{\gamma}; \mathbf{X}, \mathbf{Z}^{(1)}, \mathbf{Z}^{(2)}) = & \sum_{i=1}^N \left[ \sum_{j=1}^2 y_{ij} \log\{P(Y_i = j | \mathbf{X}_i)\} \right. && \text{True outcome mechanism} \\
 & + \sum_{j=1}^2 \sum_{k=1}^2 y_{ij} y_{ik}^{*(1)} \log\{P(Y_i^{*(1)} = k | Y_i = j, \mathbf{Z}^{(1)})\} && \text{Stage 1 (VPRAI) observation mechanism} \\
 & + \sum_{j=1}^2 \sum_{k=1}^2 \sum_{\ell=1}^2 y_{ij} y_{ik}^{*(1)} y_{i\ell}^{*(2)} \log\{P(Y_i^{*(2)} = \ell | P(Y_i^{*(1)} = k, Y_i = j, \mathbf{Z}^{(1)})\} \} && \text{Stage 2 (Judge) observation mechanism} \\
 & \left. \right]
 \end{aligned}$$



# Estimation: EM algorithm

## Expectation Step

$$w_{ij} = P(Y_i = j | Y_i^{*(2)}, Y_i^{*(1)}, \mathbf{X}, Z^{(1)}, Z^{(2)})$$

**“Fill in” the latent outcome:**  
Given the parameters and other data,  
compute the probability of **pretrial failure** for each subject.

## Maximization Step

$$\begin{aligned} Q = & \sum_{i=1}^N \left[ \sum_{j=1}^2 w_{ij} \log \{ P(Y_i = j | \mathbf{X}_i) \} \right. \\ & + \sum_{j=1}^2 \sum_{k=1}^2 w_{ij} y_{ik}^{*(1)} \log \{ P(Y_i^{*(1)} = k | Y_i = j, Z^{(1)}) \} \\ & \left. + \sum_{j=1}^2 \sum_{k=1}^2 \sum_{\ell=2}^2 w_{ij} y_{ik}^{*(1)} y_{i\ell}^{*(2)} \log \{ P(Y_i^{*(2)} = \ell | Y_i^{*(1)} = k, Y_i = j, Z^{(1)}) \} \right] \end{aligned}$$

**Update estimates:**  
Replace the **y terms** in the likelihood  
with the E-step weights and then  
**maximize**.



# Estimation: EM algorithm

**Expectation Step**

$$w_{ij} = P(Y_i = j | Y_i^{*(2)}, Y_i^{*(1)}, \mathbf{X}, Z^{(1)}, Z^{(2)})$$

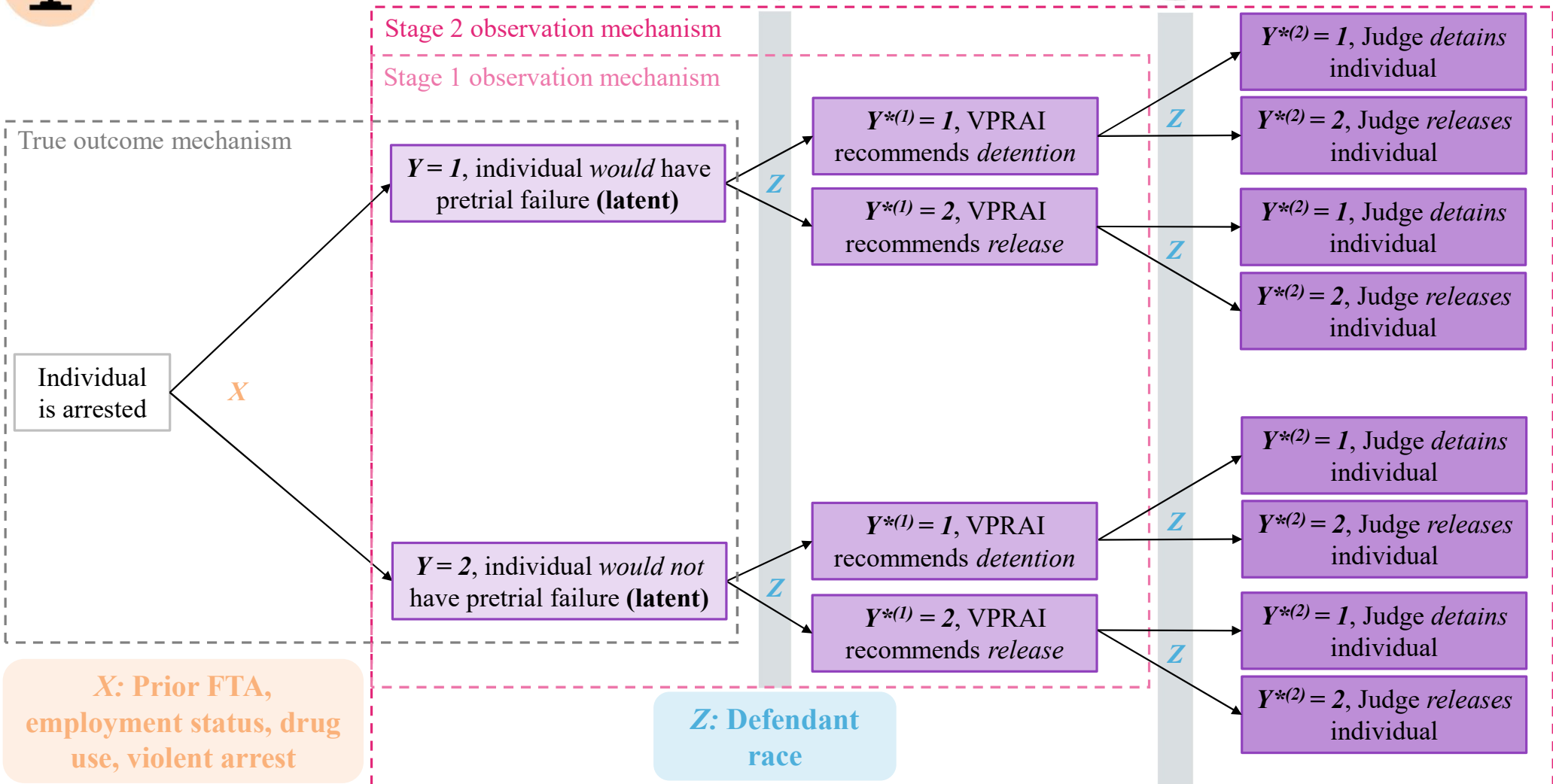
**Maximization Step**

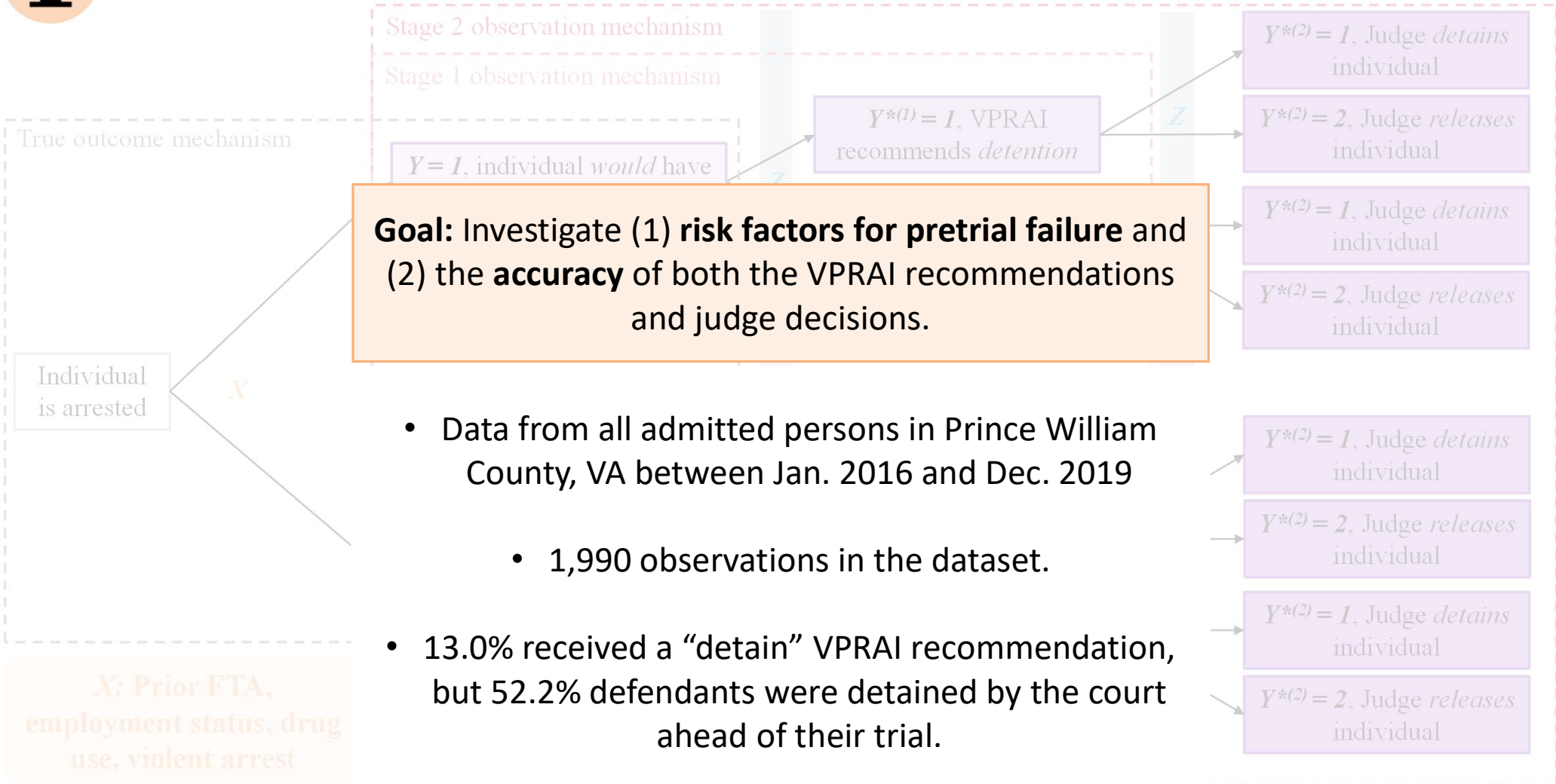
$$\begin{aligned} Q = \sum_{i=1}^N & \left[ \sum_{j=1}^2 w_{ij} \log \{ P(Y_i = j | \mathbf{X}_i) \} \right. \\ & + \sum_{j=1}^2 \sum_{k=1}^2 w_{ij} y_{ik}^{*(1)} \log \{ P(Y_i^{*(1)} = k | Y_i = j, Z^{(1)}) \} \\ & \left. + \sum_{j=1}^2 \sum_{k=1}^2 \sum_{\ell=2}^2 w_{ij} y_{ik}^{*(1)} y_{i\ell}^{*(2)} \log \{ P(Y_i^{*(2)} = \ell | Y_i^{*(1)} = k, Y_i = j, Z^{(1)}) \} \right] \end{aligned}$$

Apply the label switching correction

**Estimates of  $\beta$**

**Estimates of  $\gamma$**







True outcome mechanism:

$$\text{logit}\{P(Y = 1|X; \beta)\} = \beta_0 + \beta_{FTA}FTA + \beta_{unemployed}E + \beta_{drug}D + \beta_{violent}V$$

	EM Algorithm		Naïve Analysis	
	Est.	SE	Est.	SE
$\beta_{FTA}$	1.22	0.22	1.02	0.13
$\beta_{unemployed}$	0.73	0.06	0.67	0.15
$\beta_{drug}$	1.97	0.13	1.74	0.17
$\beta_{violent}$	0.28	0.02	0.26	0.03

Association between risk factors and pretrial failure is generally attenuated when misclassification in the VPRAI and judge decisions is *not* accounted for.



Stage 1 (VPRAI) observation mechanism:

$$\text{logit}\{P(Y^{*(1)} = 1|Y = j, \mathbf{Z}^{(1)}; \boldsymbol{\gamma})\} = \gamma_{1j0}^{(1)} + \gamma_{1j,race}^{(1)} \text{RACE}$$

	<b>Estimated VPRAI Specificity</b> P( Release   <i>Would not</i> have pretrial failure )	<b>Estimated VPRAI Sensitivity</b> P( Detain   <i>Would</i> have pretrial failure )
White defendant	100%	49.3%
Black defendant	99.3%	86.0%



Stage 2 (Judge) observation mechanism:

$$\text{logit}\{P(Y^{*(2)} = 1 | Y^{*(1)} = k, Y = j, Z^{(2)}; \gamma)\} = \gamma_{1kj0}^{(2)} + \gamma_{1kj,race}^{(2)} \text{RACE}$$

	<b>Estimated Judge Specificity</b> P( Release   <i>Would not</i> have pretrial failure )	<b>Estimated Judge Sensitivity</b> P( Detain   <i>Would</i> have pretrial failure )
White defendant	60.3%	76.8%
Black defendant	48.6%	88.8%



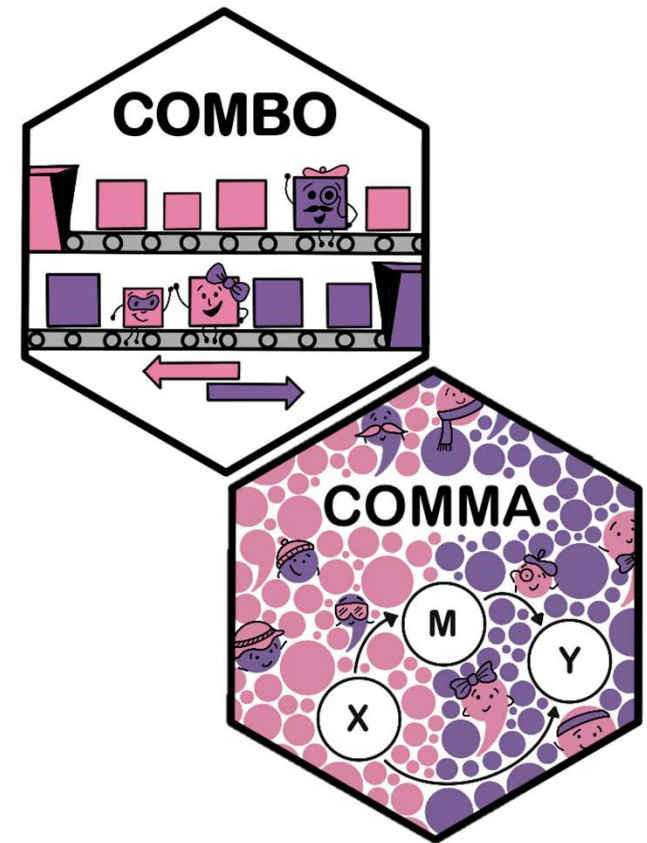


## Key takeaways

- Developed new methods for handling misclassified sequential and dependent binary outcome variables.
- Used these methods to estimate misclassification rates when algorithms and judges predict pretrial failure risk.

# Software

- Estimation methods for **misclassified outcomes** are available in the *COMBO* R Package on CRAN.
  - **C**orrecting **M**isclassified **B**inary **O**utcomes
- Estimation methods for **misclassified mediators** are in the *COMMA* R Package on CRAN.
  - **C**orrecting **M**isclassified **M**ediation **A**nalysis



# Thank you!

Kimberly A. H. Webb

[kah343@cornell.edu](mailto:kah343@cornell.edu)

[kimhwebb.com](http://kimhwebb.com) → My “webb-site” 😊



Cornell Bowers CIS  
**Statistics and Data Science**



University of  
**Pittsburgh**

arXiv paper:

[arxiv.org/abs/2309.08599](https://arxiv.org/abs/2309.08599)

