




1 记号

- 用 `const` 标识 `const`.
- 用 \hookleftarrow 标识 函数返回值.
- 模板类参数首字母大写. 如: `T`, `Key`, `Compare`. 用于 `template` 定义.
- 有时省略 `class`, `typename`.
- 模板类参数省略, 如 `C` 有时用来替代 `C(T)`.
- “示例” 如 , 输出如  .

2 容器

2.1 对

```
#include <utility>
```

```
template<class T1, class T2>
struct pair {
    T1 first; T2 second;
    pair() {}
    pair(const T1& a, const T2& b):
        first(a), second(b) {} };
```

2.1.1 类型

```
pair::first_type
pair::second_type
```

2.1.2 函数 & 操作符

参见 2.2.3.

```
pair(T1,T2)
make_pair(const T1&, const T2&);
```

2.2 容器 — 公用

这里 `X` 表示下列类之一
`{vector, deque, list,`
`set, multiset, map, multimap}`

2.2.1 类型

```
X::value_type
X::reference
X::const_reference
X::iterator
X::const_iterator
X::reverse_iterator
X::const_reverse_iterator
X::difference_type
X::size_type
```

迭代器引用 `value_type` (见 6).

2.2.2 成员函数 & 操作符

```
X::X();
X::X(const X&);
X::~X();
X& X::operator=(const X&);
X::iterator X::begin();
X::const_iterator X::begin() const;
X::iterator X::end();
X::const_iterator X::end() const;
X::reverse_iterator X::rbegin();
X::const_reverse_iterator X::rbegin() const;
X::reverse_iterator X::rend();
X::const_reverse_iterator X::rend() const;
```

```
X::size_type X::size() const;
X::size_type X::max_size() const;
bool X::empty() const;
void X::swap(X& x);
```

```
void X::clear();
```

2.2.3 比较操作符

令, `X v, w`. `X` 可以是 `pair` (2.1).

```
v == w    v != w
v < w    v > w
v <= w   v >= w
```

按字典序且 \hookleftarrow `bool`.

2.3 顺序容器

`S` 是以下类之一 `{vector, deque, list}`

2.3.1 构造器

```
S::S(S::size_type n,
    const S::value_type& t);
S::S(S::const_iterator first,
    S::const_iterator last); 7.2, 7.3
```

2.3.2 方法

```
S::iterator // 插入复制
S::insert(S::iterator before,
    const S::value_type& val);
```

```
S::iterator // 插入复制
S::insert(S::iterator before,
    S::size_type nVal,
    const S::value_type& val);
```

```
S::iterator // 插入复制
S::insert(S::iterator before,
    S::const_iterator first,
    S::const_iterator last);
```

```
S::iterator S::erase(S::iterator position);
```

```
S::iterator S::erase(S::const_iterator first,
    S::const_iterator last);
```

\hookleftarrow 最后移除的 `S::const_iterator last`);

```
void S::push_back(const S::value_type& x);
```

```
void S::pop_back();
```

```
S::reference S::front();
```

```
S::const_reference S::front() const;
```

```
S::reference S::back();
```

```
S::const_reference S::back() const;
```

2.4 向量

```
#include <vector>
```

```
template<class T,
    class A lloc=allocator>
class vector;
```

参见 2.2 和 2.3.

```
size_type vector::capacity() const;
```

```
void vector::reserve(size_type n);
```

```
vector::reference
vector::operator[](size_type i);
```

```
vector::const_reference
vector::operator[](size_type i) const;
```

 7.1.

2.5 双向队列

```
#include <deque>
```

```
template<class T,
    class A lloc=allocator>
class deque;
```

包含 `vector` 所有方法 (见 2.4).

```
void deque::push_front(const T& x);
```

```
void deque::pop_front();
```

2.6 链表

```
#include <list>
```

```
template<class T,
    class A lloc=allocator>
class list;
```

参见 2.2 和 2.3.

```
void list::pop_front();
```

```
void list::push_front(const T& x);
```

```
void // 移动 pos 前的所有 x (&x != this)
list::splice(iterator pos, list(T)& x); 7.2
```

```
void // 移动 pos 前 x 的 xElemPos
list::splice(iterator pos,
    list(T)& x,
    iterator xElemPos); 7.2
```

```
void // 移动 pos 前 x 的 [xFirst,xLast)
list::splice(iterator pos,
    list(T)& x,
    iterator xFirst,
    iterator xLast); 7.2
```

```
void list::remove(const T& value);
```

```
void list::remove_if(Predicate pred);
```

// 调用后: \forall *this* 迭代器 *p*, $*p \neq *(p+1)$

```
void list::unique(); // 移除重复
```

```
void // 同上, 但  $\neg binPred(*p, *(p+1))$ 
```

```
list::unique(BinaryPredicate binPred);
```

// 假定 *this* 和 *x* 有序

```
void list::merge(list(T)& x);
```

// 合并且假设以 *cmp* 排序

```
void list::merge(list(T)& x, Compare cmp);
```

```
void list::reverse();
```

```
void list::sort();
```

```
void list::sort(Compare cmp);
```

2.7 有序集合

这里 `A` 是以下类之一

`{set, multiset, map, multimap}`.

2.7.1 类型

对 `A=[multi]set` 都有

```
A::key_type A::value_type
A::key_compare A::value_compare
```

2.7.2 构造器

```
A::A(Compare c=Compare())
```

```
A::A(A::const_iterator first,
    A::const_iterator last,
    Compare c=Compare());
```

2.7.3 成员函数

```
A::key_compare A::key_comp() const;
A::value_compare A::value_comp() const;
```

```
A::iterator
A::insert(A::iterator hint,
    const A::value_type& val);
```

```
void A::insert(A::iterator first,
    A::iterator last);
```

```
A::size_type // # 移除的
```

```
A::erase(const A::key_type& k);
```

```
void A::erase(A::iterator p);
```

```
void A::erase(A::iterator first,
    A::iterator last);
```

```
A::size_type
A::count(const A::key_type& k) const;
```

```
A::iterator A::find(const A::key_type& k) const;
```

```
A::iterator
A::lower_bound(const A::key_type& k) const;
A::iterator
A::upper_bound(const A::key_type& k) const;
pair(A::iterator, A::iterator) // 见 4.3.1
A::equal_range(const A::key_type& k) const;
```

2.8 集合

```
#include <set>
```

```
template(class Key,
         class Compare=less<Key>,
         class Alloc=allocator)
class set;
```

参见 2.2 和 2.7.

```
set::set(const Compare& cmp=Compare());
pair(set::iterator, bool) // bool = 是否为新
set::insert(const set::value_type& x);
```

2.9 多重集合

```
#include <set>
```

```
template(class Key,
         class Compare=less<Key>,
         class Alloc=allocator)
class multiset;
```

参见 2.2 和 2.7.

```
multiset::multiset(
    const Compare& cmp=Compare());
multiset::multiset(
    InputIterator first,
    InputIterator last,
    const Compare& cmp=Compare());
multiset::iterator // 插入复制
multiset::insert(const multiset::value_type& x);
```

2.10 映射

```
#include <map>
```

```
template(class Key, class T,
         class Compare=less<Key>,
         class Alloc=allocator)
class map;
```

参见 2.2 和 2.7.

2.10.1 类型

```
map::value_type // pair<const Key, T>
```

2.10.2 成员函数

```
map::map(
    const Compare& cmp=Compare());
pair(map::iterator, bool) // bool = 是否为新
map::insert(const map::value_type& x);
T& map::operator[] (const map::key_type&);
map::const_iterator
map::lower_bound(
    const map::key_type& k) const;
map::const_iterator
map::upper_bound(
    const map::key_type& k) const;
pair(map::const_iterator, map::const_iterator)
map::equal_range
```

```
const map::key_type& k) const;
```

例

```
1 typedef map<string, int> MSI;
2 MSI nam2num;
3 nam2num.insert(MSI::value_type("one", 1));
4 nam2num.insert(MSI::value_type("two", 2));
5 nam2num.insert(MSI::value_type("three", 3));
6 int n3 = nam2num["one"] + nam2num["two"];
7 cout << n3 << " called ";
8 for (MSI::const_iterator i = nam2num.begin();
9      i != nam2num.end(); ++i)
10     if ((*i).second == n3) {
11         cout << (*i).first << endl;
12     }
```

④ 

3 called three

2.11 多重映射

```
#include <map>
```

```
template(class Key, class T,
         class Compare=less<Key>,
         class Alloc=allocator)
class multimap;
```

参见 2.2 和 2.7.

2.11.1 类型

```
multimap::value_type // pair<const Key, T>
```

2.11.2 成员函数

```
multimap::multimap(
    const Compare& cmp=Compare());
multimap::multimap(
    InputIterator first,
    InputIterator last,
    const Compare& cmp=Compare());
```

```
multimap::const_iterator
multimap::lower_bound(
    const multimap::key_type& k) const;
multimap::const_iterator
multimap::upper_bound(
    const multimap::key_type& k) const;
pair(multimap::const_iterator,
     multimap::const_iterator)
multimap::equal_range(
    const multimap::key_type& k) const;
```

3 容器适配器

3.1 栈

```
#include <stack>
```

```
template(class T,
         class Container=deque<T>)
class stack;
```

默认构造器。Container 要有 back(), push_back(), pop_back(). 所以 vector, list 和 deque 可用。

```
bool stack::empty() const;
```

```
Container::size_type stack::size() const;
```

```
void
stack::push(const Container::value_type& x);
void stack::pop();
```

```
const Container::value_type&
stack::top() const;
```

```
Container::value_type& stack::top();
```

比较操作符

```
bool operator==(const stack& s0,
                const stack& s1);
```

```
bool operator<(const stack& s0,
               const stack& s1);
```

3.2 队列

```
#include <queue>
```

```
template(class T,
         class Container=deque<T>)
class queue;
```

默认构造器。Container 要有 empty(), size(), back(), front(), push_back() 和 pop_front(). 所以 list 和 deque 可用。

```
bool queue::empty() const;
```

```
Container::size_type queue::size() const;
```

```
void
queue::push(const Container::value_type& x);
void queue::pop();
```

```
const Container::value_type&
queue::front() const;
Container::value_type& queue::front();
const Container::value_type&
queue::back() const;
Container::value_type& queue::back();
```

比较操作符

```
bool operator==(const queue& q0,
                const queue& q1);
```

```
bool operator<(const queue& q0,
               const queue& q1);
```

3.3 优先队列

```
#include <queue>
```

```
template(class T,
         class Container=vector<T>,
         class Compare=less<T>)
class priority_queue;
```

Container 必须提供随机访问迭代器且有 empty(), size(), front(), push_back() 和 pop_back(). 所以 vector 和 deque 可用。

多以 堆实现。

3.3.1 构造器

```
explicit priority_queue::priority_queue(
    const Compare& comp=Compare());
priority_queue::priority_queue(
    InputIterator first,
    InputIterator last,
    const Compare& comp=Compare());
```

3.3.2 成员函数

```
bool priority_queue::empty() const;
```

```
Container::size_type
priority_queue::size() const;
```

```
const Container::value_type&
priority_queue::top() const;
```

```
Container::value_type& priority_queue::top();
```

```
void priority_queue::push(
    const Container::value_type& x);
```

```
void priority_queue::pop();
```

无比较操作符。

4 算法

```
#include <algorithm>
```

STL 算法使用迭代器类型参数。名适应类 (见 6.1)。

声明 `template <class Foo, ...>` 省略, 用首字母
大写表示 `template`.

注意: 以下两个序列: $S_1 = [first_1, last_1)$ 和
 $S_2 = [first_2, ?)$ 或 $S_2 = [?, last_2)$ — 表示调用函数不
会超过 S_2 .

4.1 查询算法

```
Function // f 不改变 [first, last)
for_each(InputIterator first,
         InputIterator last,
         Function f); 7.4

InputIterator // 首个 i 满足 i==last 或 *i==val
find(InputIterator first,
     InputIterator last,
     const T val); 7.2

InputIterator // 首个 i 满足 i==last 或 pred(i)
find_if(InputIterator first,
        InputIterator last,
        Predicate pred); 7.7

ForwardIterator // 首个重复
adjacent_find(ForwardIterator first,
              ForwardIterator last);

ForwardIterator // 首个 binPred-定义重复
adjacent_find(ForwardIterator first,
              ForwardIterator last,
              BinaryPredicate binPred);

void // n = # 等于 val
count(ForwardIterator first,
      ForwardIterator last,
      const T val,
      Size& n);

void // n = # 满足 pred
count_if(ForwardIterator first,
         ForwardIterator last,
         Predicate pred,
         Size& n);

// 首个 != 值对
pair(InputIterator1, InputIterator2)
mismatch(InputIterator1 first1,
         InputIterator1 last1,
         InputIterator2 first2);

// 首个 binPred-定义不匹配值对
pair(InputIterator1, InputIterator2)
mismatch(InputIterator1 first1,
         InputIterator1 last1,
         InputIterator2 first2,
         BinaryPredicate binPred);
```

```
bool
equal(InputIterator1 first1,
      InputIterator1 last1,
      InputIterator2 first2);

bool
equal(InputIterator1 first1,
      InputIterator1 last1,
      InputIterator2 first2,
      BinaryPredicate binPred);

// [first2, last2)  $\subseteq$  [first1, last1)
ForwardIterator
search(ForwardIterator1 first1,
       ForwardIterator1 last1,
       ForwardIterator2 first2,
       ForwardIterator2 last2);

// [first2, last2)  $\subseteq$  binPred [first1, last1)
ForwardIterator
search(ForwardIterator1 first1,
       ForwardIterator1 last1,
       ForwardIterator2 first2,
       ForwardIterator2 last2,
       BinaryPredicate binPred);
```

4.2 修改算法

```
OutputIterator //  $\hookrightarrow first_2 + (last_1 - first_1)$ 
copy(InputIterator first1,
     InputIterator last1,
     OutputIterator first2);

//  $\hookrightarrow last_2 - (last_1 - first_1)$ 
BidirectionalIterator
copy_backward(BidirectionalIterator1 first1,
             BidirectionalIterator1 last1,
             BidirectionalIterator2 last2);

void swap(T& x, T& y);

ForwardIterator2 //  $\hookrightarrow first_2 + \#[first_1, last_1)$ 
swap_ranges(ForwardIterator1 first1,
            ForwardIterator1 last1,
            ForwardIterator2 first2);

OutputIterator //  $\hookrightarrow result + (last_1 - first_1)$ 
transform(InputIterator first,
          InputIterator last,
          OutputIterator result,
          UnaryOperation op); 7.6

OutputIterator //  $\forall s_i^k \in S_k \ r_i = bop(s_i^1, s_i^2)$ 
transform(InputIterator1 first1,
          InputIterator1 last1,
          InputIterator2 first2,
          OutputIterator result,
          BinaryOperation bop);
```

```
void replace(ForwardIterator first,
             ForwardIterator last,
             const T& oldVal,
             const T& newVal);

void
replace_if(ForwardIterator first,
           ForwardIterator last,
           Predicate& pred,
           const T& newVal);

OutputIterator //  $\hookrightarrow result_2 + \#[first, last)$ 
replace_copy(InputIterator first,
            InputIterator last,
            OutputIterator result,
            const T& oldVal,
            const T& newVal);

OutputIterator // 同上但用 pred
replace_copy_if(InputIterator first,
               InputIterator last,
               OutputIterator result,
               Predicate& pred,
               const T& newVal);

void fill(ForwardIterator first,
         ForwardIterator last,
         const T& value);

void fill_n(ForwardIterator first,
            Size n,
            const T& value);

void // 区间调用 gen()
generate(ForwardIterator first,
        ForwardIterator last,
        Generator gen);

void // n 次调用 gen()
generate_n(ForwardIterator first,
           Size n,
           Generator gen);

所有 remove 和 unique 的变体返回指向新的末端  
或上次复制的迭代器。

ForwardIterator // [first, last) is all value
remove(ForwardIterator first,
      ForwardIterator last,
      const T& value);

ForwardIterator // 同上但用 pred
remove_if(ForwardIterator first,
          ForwardIterator last,
          Predicate pred);

OutputIterator // 同上复制
remove_copy(InputIterator first,
           InputIterator last,
           OutputIterator result,
           const T& value);
```

```
OutputIterator // 同上但用 pred
remove_copy_if(InputIterator first,
              InputIterator last,
              OutputIterator result,
              Predicate pred);

所以 unique 模板函数的变体移除连续 (binPred-)
重复. 排序后很有用 (见 4.3).

ForwardIterator // [first, last) 得重复
unique(ForwardIterator first,
      ForwardIterator last);

ForwardIterator // 同上但用 binPred
unique(ForwardIterator first,
      ForwardIterator last,
      BinaryPredicate binPred);

OutputIterator // 上次复制
unique_copy(InputIterator first,
           InputIterator last,
           OutputIterator result);

OutputIterator // 同上但用 binPred
unique_copy(ForwardIterator first,
           InputIterator last,
           OutputIterator result,
           BinaryPredicate binPred);

void
reverse(BidirectionalIterator first,
        BidirectionalIterator last);

OutputIterator // 上次复制
reverse_copy(BidirectionalIterator first,
            BidirectionalIterator last,
            OutputIterator result);

void // 将 first 移动到 middle
rotate(ForwardIterator first,
       ForwardIterator middle,
       ForwardIterator last);

OutputIterator // first 到 middle 位置
rotate_copy(ForwardIterator first,
            ForwardIterator middle,
            ForwardIterator last,
            OutputIterator result);

void
random_shuffle(
    RandomAccessIterator first,
    RandomAccessIterator last);

void // rand() 返回 [0,1) 间的 double
random_shuffle(
    RandomAccessIterator first,
    RandomAccessIterator last,
    RandomGenerator rand);
```

```
BidirectionalIterator // 以 true 开始
partition(BidirectionalIterator first,
          BidirectionalIterator last,
          Predicate pred);
```

```
BidirectionalIterator // 以 true 开始
stable_partition(
    BidirectionalIterator first,
    BidirectionalIterator last,
    Predicate pred);
```

4.3 排序和应用

```
void sort(RandomAccessIterator first,
          RandomAccessIterator last);
```

```
void sort(RandomAccessIterator first,
          RandomAccessIterator last,
          Compare comp);
```

```
void
stable_sort(RandomAccessIterator first,
            RandomAccessIterator last);
```

```
void
stable_sort(RandomAccessIterator first,
            RandomAccessIterator last,
            Compare comp);
```

```
void // [first,middle) 有序,
partial_sort( // [middle,last) 大于等于
    RandomAccessIterator first,
    RandomAccessIterator middle,
    RandomAccessIterator last);
```

```
void // 同上但用 comp(ei, ej)
partial_sort(
    RandomAccessIterator first,
    RandomAccessIterator middle,
    RandomAccessIterator last,
    Compare comp);
```

```
RandomAccessIterator // 上次排序
partial_sort_copy(
    InputIterator first,
    InputIterator last,
    RandomAccessIterator resultFirst,
    RandomAccessIterator resultLast);
```

```
RandomAccessIterator
partial_sort_copy(
    InputIterator first,
    InputIterator last,
    RandomAccessIterator resultFirst,
    RandomAccessIterator resultLast,
    Compare comp);
```

令 $n = \text{position} - \text{first}$, `nth_element` 划分 $[first, last)$ 到: $L = [first, position)$, e_n ,

$R = [\text{position} + 1, last)$ 使得
 $\forall l \in L, \forall r \in R \quad l \not> e_n \leq r$.

```
void
nth_element(
    RandomAccessIterator first,
    RandomAccessIterator position,
    RandomAccessIterator last);
```

```
void // 同上但用 comp(ei, ej)
nth_element(
    RandomAccessIterator first,
    RandomAccessIterator position,
    RandomAccessIterator last,
    Compare comp);
```

4.3.1 二分查找

```
bool
binary_search(ForwardIterator first,
              ForwardIterator last,
              const T& value);
```

```
bool
binary_search(ForwardIterator first,
              ForwardIterator last,
              const T& value,
              Compare comp);
```

```
ForwardIterator
lower_bound(ForwardIterator first,
            ForwardIterator last,
            const T& value);
```

```
ForwardIterator
lower_bound(ForwardIterator first,
            ForwardIterator last,
            const T& value,
            Compare comp);
```

```
ForwardIterator
upper_bound(ForwardIterator first,
            ForwardIterator last,
            const T& value);
```

```
ForwardIterator
upper_bound(ForwardIterator first,
            ForwardIterator last,
            const T& value,
            Compare comp);
```

`equal_range` 返回 `lower_bound` 和 `upper_bound` 返回的迭代器对。

```
pair(ForwardIterator, ForwardIterator)
equal_range(ForwardIterator first,
            ForwardIterator last,
            const T& value);
```

```
pair(ForwardIterator, ForwardIterator)
equal_range(ForwardIterator first,
            ForwardIterator last,
            const T& value,
            Compare comp);
```

7.5

4.3.2 合并

假设 $S_1 = [first_1, last_1)$ 和 $S_2 = [first_2, last_2)$ 有序, 稳定合并入 $[result, result + N)$ 其中 $N = |S_1| + |S_2|$.

```
OutputIterator
merge(InputIterator1 first1,
      InputIterator1 last1,
      InputIterator2 first2,
      InputIterator2 last2,
      OutputIterator result);
```

```
OutputIterator
merge(InputIterator1 first1,
      InputIterator1 last1,
      InputIterator2 first2,
      InputIterator2 last2,
      OutputIterator result,
      Compare comp);
```

```
void // 区间 [first,middle) [middle,last)
inplace_merge( // 到 [first,last)
    BidirectionalIterator first,
    BidirectionalIterator middle,
    BidirectionalIterator last);
```

```
void // 同上但用 comp
inplace_merge(
    BidirectionalIterator first,
    BidirectionalIterator middle,
    BidirectionalIterator last,
    Compare comp);
```

4.3.3 函数和集合

用于操作有序集合容器 (见 2.7). 对于 `multiset` 的操作 — `union`, `intersection` 和 `difference` 取决于: `maximum`, `minimum` 和 `subtraction` 的行为.

令 $S_i = [first_i, last_i)$ 对于 $i = 1, 2$.

```
bool //  $S_1 \supseteq S_2$ 
includes(InputIterator1 first1,
         InputIterator1 last1,
         InputIterator2 first2,
         InputIterator2 last2);
```

```
bool // 同上但用 comp
includes(InputIterator1 first1,
         InputIterator1 last1,
         InputIterator2 first2,
         InputIterator2 last2,
         Compare comp);
```

```
OutputIterator //  $S_1 \cup S_2$ ,  $\hookrightarrow$  上次结尾
set_union(InputIterator1 first1,
          InputIterator1 last1,
          InputIterator2 first2,
          InputIterator2 last2,
          OutputIterator result);
```

```
OutputIterator // 同上但用 comp
set_union(InputIterator1 first1,
          InputIterator1 last1,
          InputIterator2 first2,
          InputIterator2 last2,
          OutputIterator result,
          Compare comp);
```

```
OutputIterator //  $S_1 \cap S_2$ ,  $\hookrightarrow$  上次结尾
set_intersection(InputIterator1 first1,
                 InputIterator1 last1,
                 InputIterator2 first2,
                 InputIterator2 last2,
                 OutputIterator result);
```

```
OutputIterator // 同上但用 comp
set_intersection(InputIterator1 first1,
                 InputIterator1 last1,
                 InputIterator2 first2,
                 InputIterator2 last2,
                 OutputIterator result,
                 Compare comp);
```

```
OutputIterator //  $S_1 \setminus S_2$ ,  $\hookrightarrow$  上次结尾
set_difference(InputIterator1 first1,
               InputIterator1 last1,
               InputIterator2 first2,
               InputIterator2 last2,
               OutputIterator result);
```

```
OutputIterator // 同上但用 comp
set_difference(InputIterator1 first1,
               InputIterator1 last1,
               InputIterator2 first2,
               InputIterator2 last2,
               OutputIterator result,
               Compare comp);
```

```
OutputIterator //  $S_1 \Delta S_2$ ,  $\hookrightarrow$  上次结尾
set_symmetric_difference(
    InputIterator1 first1,
    InputIterator1 last1,
    InputIterator2 first2,
    InputIterator2 last2,
    OutputIterator result);
```

```
OutputIterator // 同上但用 comp
set_symmetric_difference(
    InputIterator1 first1,
    InputIterator1 last1,
    InputIterator2 first2,
    InputIterator2 last2,
    OutputIterator result,
    Compare comp);
```

4.3.4 堆

```
void // (last - 1) 压入
push_heap(RandomAccessIterator first,
           RandomAccessIterator last);

void // 同上但用 comp
push_heap(RandomAccessIterator first,
           RandomAccessIterator last,
           Compare comp);

void // first 弹出
pop_heap(RandomAccessIterator first,
          RandomAccessIterator last);

void // 同上但用 comp
pop_heap(RandomAccessIterator first,
          RandomAccessIterator last,
          Compare comp);

void // [first,last) 乱序
make_heap(RandomAccessIterator first,
           RandomAccessIterator last);

void // 同上但用 comp
make_heap(RandomAccessIterator first,
           RandomAccessIterator last,
           Compare comp);

void // 排序 [first,last) 堆
sort_heap(RandomAccessIterator first,
           RandomAccessIterator last);

void // 同上但用 comp
sort_heap(RandomAccessIterator first,
           RandomAccessIterator last,
           Compare comp);
```

4.3.5 最大和最小

```
const T& min(const T& x0, const T& x1);

const T& min(const T& x0,
             const T& x1,
             Compare comp);

const T& max(const T& x0, const T& x1);

const T& max(const T& x0,
             const T& x1,
             Compare comp);
```

```
ForwardIterator
min_element(ForwardIterator first,
             ForwardIterator last);

ForwardIterator
min_element(ForwardIterator first,
             ForwardIterator last,
             Compare comp);

ForwardIterator
max_element(ForwardIterator first,
             ForwardIterator last);

ForwardIterator
max_element(ForwardIterator first,
             ForwardIterator last,
             Compare comp);
```

4.3.6 排列

所有排列, 开始于递增, 结束于递减.

```
bool //  $\curvearrowright$  当且仅当可用
next_permutation(
    BidirectionalIterator first,
    BidirectionalIterator last);

bool // 同上但用 comp
next_permutation(
    BidirectionalIterator first,
    BidirectionalIterator last,
    Compare comp);

bool //  $\curvearrowright$  当且仅当可用
prev_permutation(
    BidirectionalIterator first,
    BidirectionalIterator last);

bool // 同上但用 comp
prev_permutation(
    BidirectionalIterator first,
    BidirectionalIterator last,
    Compare comp);
```

4.3.7 字典序

```
bool lexicographical_compare(
    InputIterator1 first1,
    InputIterator1 last1,
    InputIterator2 first2,
    InputIterator2 last2);

bool lexicographical_compare(
    InputIterator1 first1,
    InputIterator1 last1,
    InputIterator2 first2,
    InputIterator2 last2,
    Compare comp);
```

4.4 计算

```
#include <numeric>

T //  $\sum_{i=first, last}$  7.6
accumulate(InputIterator first,
            InputIterator last,
            T initVal);

T // 同上但用 binop
accumulate(InputIterator first,
            InputIterator last,
            T initVal,
            BinaryOperation binop);

T //  $\sum_i e_i^1 \times e_i^2$  其中  $e_i^k \in S_k, (k = 1, 2)$ 
inner_product(InputIterator1 first1,
              InputIterator1 last1,
              InputIterator2 first2,
              T initVal);

T // 类似地, 使用  $\sum^{(sum)}$  和  $\times^{(mult)}$ 
inner_product(InputIterator1 first1,
              InputIterator1 last1,
              InputIterator2 first2,
              T initVal,
              BinaryOperation sum,
              BinaryOperation mult);

OutputIterator //  $r_k = \sum_{i=first}^{first+k} e_i$ 
partial_sum(InputIterator first,
            InputIterator last,
            OutputIterator result);
```

```
OutputIterator // 同上但用 binop
partial_sum(
    InputIterator first,
    InputIterator last,
    OutputIterator result,
    BinaryOperation binop);

OutputIterator //  $r_k = s_k - s_{k-1}$  其中  $k > 0$ 
adjacent_difference( //  $r_0 = s_0$ 
    InputIterator first,
    InputIterator last,
    OutputIterator result);
```

```
OutputIterator // 同上但用 binop
adjacent_difference(
    InputIterator first,
    InputIterator last,
    OutputIterator result,
    BinaryOperation binop);
```

5 函数对象

```
#include <functional>
```

```
template<class Arg, class Result>
struct unary_function {
    typedef Arg argument_type;
    typedef Result result_type;};
```

预定义的一元对象:

```
struct negate<T>;
struct logical_not<T>;
```

7.6

```
template<class Arg1, class Arg2,
         class Result>
struct binary_function {
    typedef Arg1 first_argument_type;
    typedef Arg2 second_argument_type;
    typedef Result result_type;};
```

以下预定义模板对象接受两个操作数. 结果如其名.

```
struct plus<T>;
struct minus<T>;
struct multiplies<T>;
struct divides<T>;
struct modulus<T>;
struct equal_to<T>;
struct not_equal_to<T>;
struct greater<T>;
struct less<T>;
struct greater_equal<T>;
struct less_equal<T>;
struct logical_and<T>;
struct logical_or<T>;
```

5.1 函数适配器

5.1.1 取反

```
template<class Predicate>
class unary_negate : public
    unary_function<Predicate::argument_type,
                  bool>;
```

```
unary_negate::unary_negate(
    Predicate pred);

bool // negate pred
unary_negate::operator()(
    Predicate::argument_type x);

unary_negate<Predicate>
not1(const Predicate pred);
```

```
template<class Predicate>
class binary_negate : public
    binary_function<
        Predicate::first_argument_type,
        Predicate::second_argument_type>;
bool);
```

```
binary_negate::binary_negate(
    Predicate pred);
bool // 取反 pred
binary_negate::operator()(
    Predicate::first_argument_type x
    Predicate::second_argument_type y);

binary_negate(Predicate)
not2(const Predicate pred);
```

5.1.2 绑定

```
template<class Operation>
class binder1st: public
    unary_function<
        Operation::second_argument_type,
        Operation::result_type>;
```

```
binder1st::binder1st(
    const Operation& op,
    const Operation::first_argument_type y);
// argument_type 来自 unary_function
Operation::result_type
binder1st::operator()(
    const binder1st::argument_type x);

binder1st(Operation)
bind1st(const Operation& op, const T& x);
```

```
template<class Operation>
class binder2nd: public
    unary_function<
        Operation::first_argument_type,
        Operation::result_type>;
```

```
binder2nd::binder2nd(
    const Operation& op,
    const Operation::second_argument_type y);
// argument_type 来自 unary_function
Operation::result_type
binder2nd::operator()(
    const binder2nd::argument_type x);

binder2nd(Operation)
bind2nd(const Operation& op, const T& x);
7.7.
```

5.1.3 函数指针

```
template<class Arg, class Result>
class pointer_to_unary_function :
    public unary_function<Arg, Result>;
```

```
pointer_to_unary_function<Arg, Result>
ptr_fun(Result (*)(Arg));
```

```
template<class Arg1, class Arg2,
        class Result>
class pointer_to_binary_function :
    public binary_function<Arg1, Arg2,
        Result>;
```

```
pointer_to_binary_function<Arg1, Arg2,
    Result>
ptr_fun(Result (*)(Arg1, Arg2));
```

6 迭代器

#include <iterator>

6.1 迭代器分类

这里我们用:

- X 迭代器类型.
- a, b 迭代器值.
- r 迭代器引用 (X& r).
- t 一个 T 类型的值.

用空的 struct 标签.

6.1.1 输入、输出、前引用

```
struct input_iterator_tag {} 7.8
struct output_iterator_tag {}
struct forward_iterator_tag {}
```

下表显示 Input, Output 和 Forward 迭代器.

表达式	条件	I	O	F
X()	可单用			•
X u				•
X(a)	$\Rightarrow X(a) == a$ $*a=t \Leftrightarrow *X(a)=t$	•	•	
X u(a)	$\Rightarrow u == a$	•	•	
X u=a	u copy of a		•	
a==b	equivalence relation	•	•	
a!=b	$\Leftrightarrow !(a==b)$	•	•	
r = a	$\Rightarrow r == a$		•	•
*a	convertible to T. $a==b \Leftrightarrow *a==*b$	•	•	
*a=t	(for forward, if X mutable)		•	•
++r	result is dereferenceable or past-the-end. $\&r == \&++r$ convertible to const X& convertible to X& $r==s \Leftrightarrow ++r==++s$	•	•	•
r++	convertible to X& $\Leftrightarrow \{X x=r; ++r; return x;\}$	•	•	•
++r	convertible to T	•	•	•

7.7.

6.1.2 Bidirectional Iterators

```
struct bidirectional_iterator_tag {}
The forward requirements and:
```

```
--r Convertible to const X&. If  $\exists r=++s$  then --r  
refers same as s.  $\&r==\&--r$ .  $--(++r)==r$ .  
(--r == --s  $\Rightarrow$  r==s.  
r--  $\Leftrightarrow \{X x=r; --r; return x;\}$ .
```

6.1.3 Random Access Iterator

```
struct random_access_iterator_tag {}
The bidirectional requirements and  
(m,n iterator's distance (integral) value):
```

```
r+n  $\Leftrightarrow \{for (m=n; m-->0; ++r);$   
for (m=n; m++<0; --r);  
return r;\} //but time = O(1).  
a+n  $\Leftrightarrow n+a \Leftrightarrow \{X x=a; return a+=n\}$   
r-n  $\Leftrightarrow r += -n$ .  
a-n  $\Leftrightarrow a+(-n)$ .  
b-a Returns iterator's distance value n, such  
that a+n == b.  
a[n]  $\Leftrightarrow *(a+n)$ .  
a<b Convertible to bool, < total ordering.  
a<b Convertible to bool, > opposite to <.  
a<=b  $\Leftrightarrow !(a>b)$ .  
a>b  $\Leftrightarrow !(a<b)$ .
```

6.2 Stream Iterators

```
template<class T,
        class Distance=ptrdiff_t>
class istream_iterator :
    public iterator<input_iterator_tag, T, Distance>;
```

```
// end of stream 7.4
istream_iterator::istream_iterator();
istream_iterator::istream_iterator(
    istream& s); 7.4
istream_iterator::istream_iterator(
    const istream_iterator(T, Distance)&);
istream_iterator::~istream_iterator();
const T& istream_iterator::operator*() const;

istream_iterator& // Read and store T value
istream_iterator::operator++() const;

bool // all end-of-streams are equal
operator==(const istream_iterator,
    const istream_iterator);
```

```
template<class T>
class ostream_iterator :
    public iterator<output_iterator_tag, void, ...>;
```

```
// If delim  $\neq$  0 add after each write
ostream_iterator::ostream_iterator(
    ostream& s,
    const char* delim=0);

ostream_iterator::ostream_iterator(
    const ostream_iterator s);

ostream_iterator& // Assign & write (*o=t)
ostream_iterator::operator*() const;

ostream_iterator&
ostream_iterator::operator=(
    const ostream_iterator s);

ostream_iterator& // No-op
ostream_iterator::operator++();

ostream_iterator& // No-op
ostream_iterator::operator++(int);
7.4.
```

6.3 类型定义 & 适配器

```
template<Category, T,
        Distance=ptrdiff_t,
        Pointer=T*, Reference= T&>
class iterator {
    Category iterator_category;
    T value_type;
    Distance difference_type;
    Pointer pointer;
    Reference reference;};
```

6.3.1 Traits

```
template<I>
class iterator_traits {
    I::iterator_category
        iterator_category;

    I::value_type
        value_type;
    I::difference_type
        difference_type;
    I::pointer
        pointer;
    I::reference
        reference;}
```

Pointer specilaizations: 7.8

```
template<T>
class iterator_traits<T*> {
    random_access_iterator_tag
        iterator_category ;
    T value_type;
    ptrdiff_t difference_type;
    T* pointer;
    T& reference;}
```

```
template<T>
class iterator_traits<const T*> {
    random_access_iterator_tag
        iterator_category;
    T
        value_type;
    ptrdiff_t
        difference_type;
    const T*
        pointer;
    const T&
        reference;};
```

6.3.2 Reverse Iterator

Transform $[i \nearrow j] \mapsto [j - 1, \searrow i - 1)$.

```
template<Iter>
class reverse_iterator : public iterator<
    iterator_traits<Iter>::iterator_category,
    iterator_traits<Iter>::value_type,
    iterator_traits<Iter>::difference_type,
    iterator_traits<Iter>::pointer,
    iterator_traits<Iter>::reference>;
```

Denote
RI = **reverse_iterator**
AI = **RandomAccessIterator**.

Abbreviate:
typedef RI<AI, T,
Reference, Distance> self;

// Default constructor \Rightarrow singular value
self::RI();

explicit // Adaptor Constructor
self::RI(AI i);

AI self::base(); // adpatee's position

// so that: $\&*(RI(i)) == \&*(i-1)$ Reference
self::operator*();

self // position to & return base()-1
RI::operator++();

self& // return old position and move
RI::operator++(int); // to base()-1

self // position to & return base()+1
RI::operator--();

self& // return old position and move
RI::operator--(int); // to base()+1

bool // $\Leftrightarrow s0.base() == s1.base()$
operator==(const self& s0, const self& s1);

reverse_iterator Specific

self // returned value positioned at base()-n
reverse_iterator::operator+(
Distance n) const;

self& // change & return position to base()-n
reverse_iterator::operator+=(Distance n);

self // returned value positioned at base()+n
reverse_iterator::operator-(
Distance n) const;

self& // change & return position to base()+n
reverse_iterator::operator=(Distance n);
Reference // $*(this + n)$
reverse_iterator::operator[](Distance n);
Distance // $r0.base() - r1.base()$
operator-(const self& r0, const self& r1);
self // $n + r.base()$
operator-(Distance n, const self& r);
bool // $r0.base() < r1.base()$
operator<(const self& r0, const self& r1);

6.3.3 Insert Iterators

```
template<class Container>
class back_insert_iterator :
    public output_iterator;
```

```
template<class Container>
class front_insert_iterator :
    public output_iterator;
```

```
template<class Container>
class insert_iterator :
    public output_iterator;
```

Here T will denote the Container::value_type.

Constructors

explicit // \exists Container::push_back(const T&)
back_insert_iterator::back_insert_iterator(
Container& x);

explicit // \exists Container::push_front(const T&)
front_insert_iterator::front_insert_iterator(
Container& x);

// \exists Container::insert(const T&)
insert_iterator::insert_iterator(
Container x,
Container::iterator i);

Denote

InsIter = **back_insert_iterator**
insFunc = **push_back**
iterMaker = **back_inserter** 7.4

or

InsIter = **front_insert_iterator**
insFunc = **push_front**
iterMaker = **front_inserter**

or

InsIter = **insert_iterator**
insFunc = **insert**

Member Functions & Operators

InsIter& // calls x.insFunc(val)
InsIter::operator=(const T& val);

InsIter& // return *this
InsIter::operator*();
InsIter& // no-op, just return *this
InsIter::operator++();
InsIter& // no-op, just return *this
InsIter::operator++(int);
Template Function
InsIter // return InsIter(Container)(x)
iterMaker(Container& x);
// return insert_iterator(Container)(x, i)
insert_iterator(Container)
inserter(Container& x, Iter i);

7 示例

7.1 向量

```
1 // safe get
2 int vi(const vector<unsigned>& v, int i) {
3     return (i < (int)v.size() ? (int)v[i] : -1);
4 }
5
6 // safe set
7 void vin(vector<int>& v, unsigned i, int n) {
8     int nAdd = i - v.size() + 1;
9     if (nAdd > 0) v.insert(v.end(), nAdd, n);
10    else v[i] = n;
11 }
```

7.2 链表分割

```
1 void lShow(ostream& os, const list<int>& l) {
2     ostream_iterator<int> ois(os, " ");
3     copy(l.begin(), l.end(), ois); os << endl;
4 }
5
6 void lmShow(ostream& os, const char* msg,
7     const list<int>& l,
8     const list<int>& m) {
9     os << msg << (m.size() ? ":\n" : ": ");
10    lShow(os, l);
11    if (m.size()) lShow(os, m);
12 } // lmShow
13
14 list<int>::iterator p(list<int>& l, int val) {
15     return find(l.begin(), l.end(), val);
16 }
17
18 static int prim[] = { 2, 3, 5, 7 };
19 static int perf[] = { 6, 28, 496 };
20 const list<int> lPrimes(prim + 0, prim + 4);
21 const list<int> lPerfects(perf + 0, perf + 3);
22 list<int> l(lPrimes), m(lPerfects);
23 lmShow(cout, "primes & perfects", l, m);
24 l.splice(l.begin(), m);
25 lmShow(cout, "splice(l.beg, m)", l, m);
26 l = lPrimes; m = lPerfects;
27 l.splice(l.begin(), m, p(m, 28));
```

```
1 lmShow(cout, "splice(l.beg, m, ^28)", l, m);
2 m.erase(m.begin(), m.end()); // <=> m.clear()
3 l = lPrimes;
4 l.splice(p(l, 3), l, p(l, 5));
5 lmShow(cout, "5 before 3", l, m);
6 l = lPrimes;
7 l.splice(l.begin(), l, p(l, 7), l.end());
8 lmShow(cout, "tail to head", l, m);
9 l = lPrimes;
10 l.splice(l.end(), l, l.begin(), p(l, 3));
11 lmShow(cout, "head to tail", l, m);
```



```
primes & perfects:
2 3 5 7
6 28 496
splice(l.beg, m): 6 28 496 2 3 5 7
splice(l.beg, m, ^28):
28 2 3 5 7
6 496
5 before 3: 2 5 3 7
tail to head: 7 2 3 5
head to tail: 3 5 7 2
```

7.3 比较对象排序

```
1 class ModN {
2 public:
3     ModN(unsigned m) : _m(m) {}
4     bool operator()(const unsigned& u0,
5         const unsigned& u1) {
6         return ((u0 % _m) < (u1 % _m));
7     }
8 private: unsigned _m;
9 }; // ModN
```

```
1 ostream_iterator<unsigned> ois(cout, " ");
2 unsigned q[6];
3 for (int n = 6, i = n - 1; i >= 0; n = i--)
4     q[i] = n*n*n*n;
5 cout << "four-powers: ";
6 copy(q + 0, q + 6, ois);
7 for (unsigned b = 10; b <= 1000; b *= 10) {
8     vector<unsigned> sq(q + 0, q + 6);
9     sort(sq.begin(), sq.end(), ModN(b));
10    cout << endl << "sort mod " << setw(4) << b << ":
11    copy(sq.begin(), sq.end(), ois);
12 } cout << endl;
```



```
four-powers: 1 16 81 256 625 1296
sort mod 10: 1 81 625 16 256 1296
sort mod 100: 1 16 625 256 81 1296
sort mod 1000: 1 16 81 256 1296 625
```

7.4 流迭代器

```

1 void unitRoots(int n) {
2     cout << "unit " << n << "-roots:" << endl;
3     vector<complex<float>> roots;
4     float arg = 2.*M_PI / (float)n;
5     complex<float> r, r1 = polar((float)1., arg);
6     for (r = r1; --n; r *= r1)
7         roots.push_back(r);
8     copy(roots.begin(), roots.end(),
9         ostream_iterator<complex<float>>(cout,
10         "\n"));
11 } // unitRoots

```



```

1 {ofstream o("primes.txt"); o << "2 3 5"; }
2 ifstream pream("primes.txt");
3 vector<int> p;
4 istream_iterator<int> priter(pream);
5 istream_iterator<int> eos;
6 copy(riter, eos, back_inserter(p));
7 for_each(p.begin(), p.end(), unitRoots);

```

7.5 二分查找

```

1 // first 5 Fibonacci
2 static int fb5[] = { 1, 1, 2, 3, 5 };
3 for (int n = 0; n <= 6; ++n) {
4     pair<int*, int*> p =
5         equal_range(fb5, fb5 + 5, n);
6     cout << n << ":[" << p.first - fb5 << ", "
7         << p.second - fb5 << "] ";
8     if (n == 3 || n == 6) cout << endl;
9 }

```



```

0:[0,0] 1:[0,2] 2:[2,3] 3:[3,4]
4:[4,4] 5:[4,5] 6:[5,5]

```

7.6 转换 & 计算

```

1 template <class T>
2 class AbsPwr : public unary_function < T, T > {
3 public:
4     AbsPwr(T p) : _p(p) {}
5     T operator()(const T& x) const {
6         return pow(fabs(x), _p);
7     }
8 private: T _p;
9 }; // AbsPwr
10
11 template<typename InpIter> float
12 normNP(InpIter xb, InpIter xe, float p) {
13     vector<float> vf;
14     transform(xb, xe, back_inserter(vf),
15         AbsPwr<float>(p > 0. ? p : 1.));
16     return((p > 0.)
17         ? pow(accumulate(vf.begin(), vf.end(), 0.,
18             1. / p)
19             : *(max_element(vf.begin(), vf.end())));
20 } // normNP
21
22 float distNP(const float* x, const float* y,
23     unsigned n, float p) {
24     vector<float> diff;
25     transform(x, x + n, y, back_inserter(diff),
26         minus<float>());
27     return normNP(diff.begin(), diff.end(), p);
28 } // distNP

```



```

1 d_{1}=19
2 d_{2}=13
3 d_{3.14159}=12.1676
4 d_{0}=12

```

7.7 迭代和绑定

```

1 // self-referring int
2 class Iterator : public
3     iterator < input_iterator_tag, int, size_t,
4     int _n;
5 public:
6     Iterator(int n = 0) : _n(n) {}
7     int operator*() const { return _n; }
8     Iterator& operator++() {

```

```

9         ++_n; return *this;
10     }
11     Iterator operator++(int) {
12         Iterator t(*this);
13         ++_n; return t;
14     }
15     // Iterator
16     bool operator==(const Iterator& i0,
17         const Iterator& i1) {
18         return (*i0 == *i1);
19     }
20     bool operator!=(const Iterator& i0,
21         const Iterator& i1) {
22         return !(i0 == i1);
23     }
24
25 struct Fermat : public
26     binary_function < int, int, bool > {
27     Fermat(int p = 2) : n(p) {}
28     int n;
29     int nPower(int t) const
30     { // t^n
31         int i = n, tn = 1;
32         while (i-->0) tn *= t;
33         return tn;
34     } // nPower
35     int nRoot(int t) const {
36         return (int)pow(t + .1, 1. / n);
37     }
38     int xNyN(int x, int y) const {
39         return(nPower(x) + nPower(y));
40     }
41     bool operator()(int x, int y) const {
42         int zn = xNyN(x, y), z = nRoot(zn);
43         return(zn == nPower(z));
44     }
45 }; // Fermat

```

```

1 for (int n = 2; n <= Mp; ++n) {
2     Fermat f(n);
3     for (int x = 1; x < Mx; ++x) {
4         binder1st<Fermat>
5             fx = bind1st(f, x);
6         Iterator iy(x), iyEnd(My);
7         while ((iy = find_if(++iy, iyEnd, fx))
8             != iyEnd) {
9             int y = *iy,
10                 z = f.nRoot(f.xNyN(x, y));
11             cout << x << '^' << n << " = "
12                 << y << '^' << n << " = "
13                 << z << '^' << n << endl;
14             if (n > 2)
15                 cout << "Fermat is wrong!" << endl;
16         }
17     }
18 }

```



```

3^2 + 4^2 = 5^2
5^2 + 12^2 = 13^2
6^2 + 8^2 = 10^2
7^2 + 24^2 = 25^2

```

7.8 特征迭代

```

1 template <class Itr>
2 typename iterator_traits<Itr>::value_type
3 mid(Itr b, Itr e, input_iterator_tag) {
4     cout << "mid(general):\n";
5     Itr bm(b); bool next = false;
6     for (; b != e; ++b, next = !next) {
7         if (next) { ++bm; }
8     }
9     return *bm;
10 } // mid<input>
11
12 template <class Itr>
13 typename iterator_traits<Itr>::value_type
14 mid(Itr b, Itr e,
15     random_access_iterator_tag) {
16     cout << "mid(random):\n";
17     Itr bm = b + (e - b) / 2;
18     return *bm;
19 } // mid<random>
20
21 template <class Itr>
22 typename iterator_traits<Itr>::value_type
23 mid(Itr b, Itr e) {
24     typename
25         iterator_traits<Itr>::iterator_category t;
26     mid(b, e, t);
27 } // mid
28
29 template <class Ctr>
30 void fillmid(Ctr& ctr) {
31     static int perfects[5] =
32         { 6, 14, 496, 8128, 33550336 },
33         *pb = &perfects[0];
34     ctr.insert(ctr.end(), pb, pb + 5);
35     int m = mid(ctr.begin(), ctr.end());
36     cout << "mid=" << m << "\n";
37 } // fillmid

```



```

1 list<int> l; vector<int> v;
2 fillmid(l); fillmid(v);

```