

Problem 1:

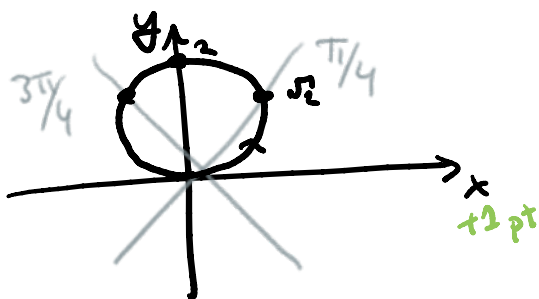
$$\underbrace{x^2 + y^2}_{=r^2} = 2 \underbrace{y}_{=r \sin \theta}$$

+2pts

10pts

$$r = 2 \sin \theta$$

+2pts



θ	r
0	0
$\pi/4$	$\sqrt{2}$
$\pi/2$	2
$3\pi/4$	$\sqrt{2}$
π	0

+5pts

10pts

Problem 2:

$$\frac{\sin(2\theta)}{\cos \theta} + \sin^2 \theta = -1$$

+4pts

$$\frac{2 \cancel{\cos \theta} \sin \theta}{\cancel{\cos \theta}} + \sin^2 \theta = -1$$

17pts

$$\sin^2 \theta + 2 \sin \theta + 1 = 0$$

$$(\sin \theta + 1)^2 = 0$$

$$\sin \theta = -1$$

+2pts

$$\theta = \frac{3\pi}{2} + 2k\pi$$

+1pt

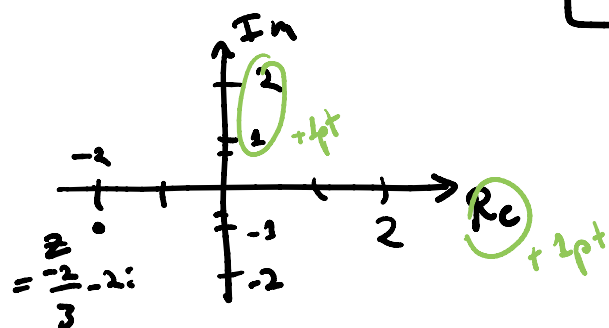
+2pts

Problem 3.

$$z = \frac{6-2i}{3i}$$

$$\frac{6-2i}{3i} \cdot \frac{i}{i} = \frac{6i+2}{-3}$$

$$z = \boxed{-\frac{2}{3} - 2i}$$



$$|z| = \sqrt{\left(\frac{2}{3}\right)^2 + (2)^2}$$

$$= \sqrt{\frac{4}{9} + 4}$$

$$= 2\sqrt{\frac{10}{9}}$$

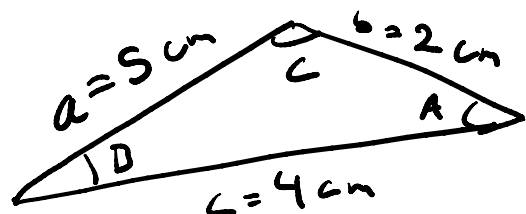
$$\boxed{|z| = \frac{2}{3}\sqrt{10}}$$

argument: $\theta = \tan^{-1}\left(\frac{2}{-2/3}\right)$

$$\boxed{\theta = \tan^{-1}(3)}$$

$$z = \frac{2}{3}\sqrt{10} \left(\cos(\tan^{-1}(3)) + i \sin(\tan^{-1}(3)) \right)$$

Problem 4.



Law of Cos:

$$+4 \text{ pts } a^2 = b^2 + c^2 - 2bc \cos(A)$$

$$25 = 4 + 16 - 2 \cdot 4 \cdot 16 \cos A$$

$$\frac{5}{2 \cdot 4 \cdot 16} = \cos A$$

$$A = \cos^{-1}\left(\frac{5}{8 \cdot 16}\right)$$

Law of Sines:

$$\frac{\sin A}{a} = \frac{\sin B}{b} + 3 \text{ pts}$$

$$\frac{\sin(\cos^{-1}(\frac{5}{8 \cdot 16}))}{5} = \frac{\sin B}{2} + 2 \text{ pts}$$

$$\frac{2}{5} \left(\sqrt{1 - \left(\frac{5}{8 \cdot 16}\right)^2} \right) = \sin B$$

$$B = \sin^{-1} \left(\frac{2}{5} \sqrt{1 - \left(\frac{5}{8 \cdot 16}\right)^2} \right)$$

$$A + B + C = 180^\circ$$

$$\underline{A + B + C = 190^\circ}$$

$$\boxed{C = 190^\circ - \sin^{-1}\left(\frac{2}{5}\sqrt{1 - \left(\frac{5}{9 \cdot 16}\right)^2}\right) - \cos^{-1}\left(\frac{5}{9 \cdot 16}\right)}$$

+ 6 pts

Problem 5.

$$\vec{u} = \langle -1, 1 \rangle$$

$$\vec{v} = \langle 2, -2 \rangle$$

$$\frac{\vec{u}}{|\vec{u}|} = \frac{\langle -1, 1 \rangle}{\sqrt{1^2 + 1^2}}$$

$$= \boxed{\left\langle \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}} \right\rangle}$$

$$\frac{\vec{v}}{|\vec{v}|} = \frac{\langle 2, -2 \rangle}{\sqrt{4 + 4}}$$

$$= \boxed{\left\langle \frac{1}{\sqrt{2}}, \frac{-1}{\sqrt{2}} \right\rangle}$$

$$\vec{u} \cdot \vec{v} = |\vec{u}| |\vec{v}| \cos \theta$$

+ 5 pts

+ 10 pts

+ 5 pts

$$\begin{array}{lcl}
 \nearrow & \langle -1, 1 \rangle \cdot \langle 2, -2 \rangle = \sqrt{2} \cdot \sqrt{8} \cos \theta & \\
 +5 \text{ pts} & -2 - 2 = 4 \cos \theta & \\
 & -1 = \cos \theta & \left. \begin{array}{l} \\ +4 \text{ pts} \end{array} \right\} \\
 & \boxed{\theta = \pi} & +4 \text{ pts} \left. \vphantom{\begin{array}{l} \\ +4 \text{ pts} \end{array}} \right\} +10 \text{ pts}
 \end{array}$$