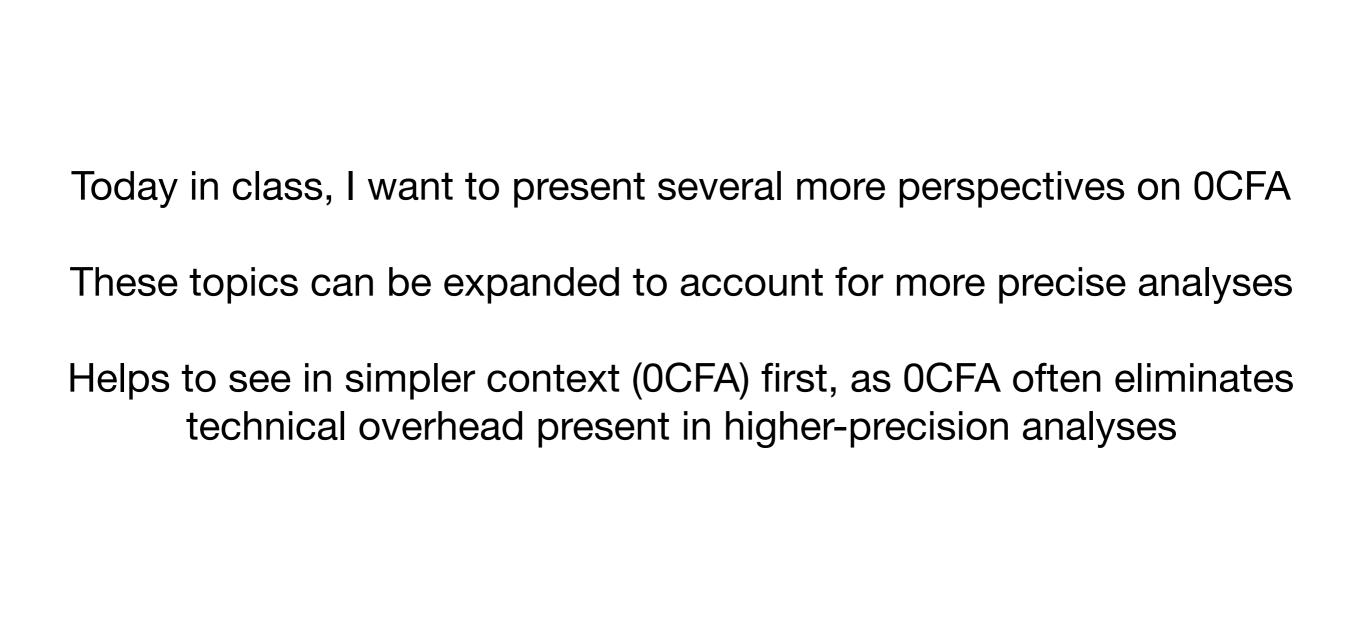
Constraint-based and Declarative Analyses

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$$\{\mathbf{fn} \ \mathbf{x} => [\mathbf{x}]^1\} \subseteq \widehat{\mathsf{C}}(2)$$
$$\{\mathbf{fn} \ \mathbf{y} => [\mathbf{y}]^3\} \subseteq \widehat{\mathsf{C}}(4)$$



Last class we saw 0CFA

$$\begin{array}{c} \text{Base} \\ \left(\lambda(x) \ e\right) \Rightarrow \left(\lambda(x) \ e\right) \\ \text{Salls} \\ \left(\lambda(x) \ e'\right) \Rightarrow e_0 \ v \Rightarrow e_1 \ (e_0 \ e_1) \\ \hline v \Rightarrow x \end{array}$$

$$\frac{\left(\lambda(x) \ e\right) \Rightarrow e_0 \ v \Rightarrow e}{\left(\lambda(x) \ e\right) \Rightarrow \left(e_0 \ e_1\right)}$$

$$v \Rightarrow \left(e_0 \ e_1\right)$$

$$(\lambda(x) e) \Rightarrow (\lambda(x) e)$$

$$(\lambda(x) e') \Rightarrow e_0 v \Rightarrow e_1$$

$$v \Rightarrow x$$

$$\frac{(\lambda(x) \ e) \Rightarrow e_0 \ v \Rightarrow e}{v \Rightarrow (e_0 \ e_1)}$$

We run these "flow implications" until we can't run them anymore

$$\left((\lambda(x^1) \ x^2)^3 \ (\lambda(y^4) \ y^5)^6 \right)^7$$

$$(\lambda(x) e) \Rightarrow (\lambda(x) e)$$

$$(\lambda(x) e') \Rightarrow e_0 \quad v \Rightarrow e_1$$

$$v \Rightarrow x$$

$$\frac{(\lambda(x) \ e) \Rightarrow e_0 \ v \Rightarrow e}{v \Rightarrow (e_0 \ e_1)}$$

We run these "flow implications" until we can't run them anymore

$$\left((\lambda(x^1) \ x^2)^3 \left(\lambda(y^4) \ y^5)^6\right)^7$$

$$(\lambda(x^{1}) (x^{2} x^{3}))^{4} \Rightarrow (\lambda(x^{1}) (x^{2} x^{3}))^{4} (\lambda(y^{5}) (y^{6} y^{7}))^{8} \Rightarrow (\lambda(y^{5}) (y^{6} y^{7}))^{8}$$

$$\left(\left(\lambda(x^1) \, (x^2 \, x^3) \right)^4 \, \left(\lambda(y^5) \, (y^6 \, y^7) \right)^8 \right)^9$$

$$\left(\lambda(x^1) \ (x^2 \ x^3)\right)^4 \Rightarrow \left(\lambda(x^1) \ (x^2 \ x^3)\right)^4$$

$$\left(\lambda(y^5) \ (y^6 \ y^7)\right)^8 \Rightarrow \left(\lambda(y^5) \ (y^6 \ y^7)\right)^8$$

$$\left(\lambda(y^5) \ (y^6 \ y^7)\right)^8 \Rightarrow x$$

$$\left(\left(\lambda(x^1) \, \left(x^2 \, x^3 \right) \right)^4 \, \left(\lambda(y^5) \, \left(y^6 \, y^7 \right) \right)^8 \right)^9$$

$$(\lambda(x^{1}) (x^{2} x^{3}))^{4} \Rightarrow (\lambda(x^{1}) (x^{2} x^{3}))^{4}$$

$$(\lambda(y^{5}) (y^{6} y^{7}))^{8} \Rightarrow (\lambda(y^{5}) (y^{6} y^{7}))^{8}$$

$$(\lambda(y^{5}) (y^{6} y^{7}))^{8} \Rightarrow x$$

$$(\lambda(y^{5}) (y^{6} y^{7}))^{8} \Rightarrow y$$

$$((\lambda(x^{1}) (x^{2} x^{3}))^{4} (\lambda(y^{5}) (y^{6} y^{7}))^{8})^{9}$$

How do we actually "solve" these flow equations

$$(\lambda(x) e) \Rightarrow (\lambda(x) e)$$

Observe: can read them as a collection of constraints over sets

$$\frac{\left(\lambda(x) \ e'\right) \Rightarrow e_0 \ v \Rightarrow e_1}{v \Rightarrow x}$$

$$\frac{\left(\lambda(x) \ e\right) \Rightarrow e_0 \ v \Rightarrow e}{v \Rightarrow (e_0 \ e_1)}$$

For each subexpression in the program, we define R(e), called the **flow set** associated w/ that point

$$(\lambda(x) e) \Rightarrow (\lambda(x) e) \qquad (\lambda(x) e) \in R(\lambda(x) e)$$

$$(\lambda(x) e') \Rightarrow e_0 \quad v \Rightarrow e_1 \quad (\lambda(x) e') \in R(e_0) \quad v \in R(e_1)$$

$$v \Rightarrow x \qquad v \in R(x)$$

$$(\lambda(x) e) \Rightarrow e_0 \quad v \Rightarrow e \quad (\lambda(x) e) \in R(e_0) \quad v \in R(e)$$

 $v \Rightarrow (e_0 \ e_1)$

 $v \in R((e_0 e_1))$

So we have the following schema for constraints for 0CFA

$$(\lambda(x) \ e) \in R(\lambda(x) \ e)$$
$$(\lambda(x) \ e') \in R(e_0) \quad v \in R(e_1) \longrightarrow v \in R(x)$$
$$(\lambda(x) \ e) \in R(e_0) \quad v \in R(e) \longrightarrow v \in R((e_0 \ e_1))$$

```
(define (constraint? constraint)
  (match constraint
    [`(⊆ ,s0 ,s1) #t]
    \Gamma`(\in ,element ,st) #t]
    [`(\leftarrow (\subseteq ,s0 ,s1) ,(? constraint? bodies) ...) #t]
    [`(\leftarrow (\in ,e ,s) ,(? constraint? bodies) ...) #t]
    [Felse #f]))
(define (expr? e)
  (match e
    \lceil (? \text{ symbol? } x) \#t \rceil
    [`(,(? expr? e0) ,(? expr? e1)) #t]
    [`(lambda (,(? symbol? x)) ,(? expr? e-body)) \#t]
     [Felse #f]))
```

A tiny constraint solver ...

```
(define (solve-constraints constraints)
  (define (body-true body h)
    (match body
      [`(⊆ ,s0 ,s1) (subset? (hash-ref h s0 (set)) (hash-ref h s1 (set)))]
      \lceil (\in ,e ,st) \text{ (set-member? (hash-ref h st (set)) e)} \rceil \rangle
  (define (iter h)
    (let ([next
            (foldl
             (lambda (constraint h)
               (match constraint
                 \lceil (\in ,e ,s) \pmod{hash-set}  (set-add (hash-ref h s (set)) e))
                 \lceil (\subseteq, s0, s1) \pmod{hash-set}  (set-union (hash-ref h s0 (set)) (hash-ref h s1 (set)))]
                 [`(\leftarrow (\subseteq ,s0 ,s1) ,(? constraint? bodies) ...)
                  (if (andmap (lambda (body) (body-true body h)) bodies)
                       (hash-set h s1 (set-union (hash-ref h s0 (set)) (hash-ref h s1 (set))))
                       h)]
                 [`(\leftarrow (\in ,e ,s),(? constraint? bodies) ...)]
                  (if (andmap (lambda (body) (body-true body h)) bodies)
                       (hash-set h s (set-add (hash-ref h s (set)) e))
                       h)]))
             (set->list constraints))])
      (if (equal? next h) h (iter next))))
  (iter (hash)))
```

((lambda (x) x) (lambda (y) y))

```
(pretty-print
 (solve-constraints
  (set \in (lambda(x) x) (flow-set(lambda(x) x))
       `(∈ (lambda (y) y) (flow-set (lambda (y) y)))
       (\leftarrow (\in (lambda (x) x) (flow-set x))
            (\in (lambda (x) x) (flow-set (lambda (x) x)))
            (\in (lambda (x) x) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (y) y) (flow-set x))
            (\in (lambda (x) x) (flow-set (lambda (x) x)))
            (\in (lambda (y) y) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (x) x) (flow-set y))
            (\in (lambda (y) y) (flow-set (lambda (x) x)))
            (\in (lambda (x) x) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (y) y) (flow-set y))
            (\in (lambda (y) y) (flow-set (lambda (x) x)))
            (\in (lambda (y) y) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (x) x) (flow-set ((lambda (x) x) (lambda (y) y))))
            (\in (lambda (x) x) (flow-set (lambda (x) x)))
            (\in (lambda (x) x) (flow-set x)))
       (\leftarrow (\in (lambda (y) y) (flow-set ((lambda (x) x) (lambda (y) y))))
            (\in (lambda (x) x) (flow-set (lambda (x) x)))
            (\in (lambda (y) y) (flow-set x)))))
```

Treat rule as schema...

$$(\lambda(x) e) \in R(e_0) \quad v \in R(e) \longrightarrow v \in R((e_0 e_1))$$

Generate a separate constraint for each syntactic lambda and application in the program.

```
(pretty-print
 (solve-constraints
  (set \in (lambda(x) x)(flow-set(lambda(x) x))
       `(∈ (lambda (y) y) (flow-set (lambda (y) y)))
       (\leftarrow (\in (lambda (x) x) (flow-set x))
            (\in (lambda (x) x) (flow-set (lambda (x) x)))
            (\in (lambda (x) x) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (y) y) (flow-set x))
            (\in (lambda (x) x) (flow-set (lambda (x) x)))
            (\in (lambda (y) y) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (x) x) (flow-set y))
            (\in (lambda (y) y) (flow-set (lambda (x) x)))
            (\in (lambda (x) x) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (y) y) (flow-set y))
            (\in (lambda (y) y) (flow-set (lambda (x) x)))
            (\in (lambda (y) y) (flow-set (lambda (y) y))))
       (\leftarrow (\in (lambda (x) x) (flow-set ((lambda (x) x) (lambda (y) y))))
```

Treat rule as schema...

$$(\lambda(x) e) \in R(e_0) \quad v \in R(e) \longrightarrow v \in R((e_0 e_1))$$

Generate a separate constraint for each syntactic lambda and application in the program.

```
(sel Cantaido, this better if we use a
```

```
`(∈ (lambda (y) y) (flow-set (lambda (y) y)))
`(← (∈ (lambda (x) x) (flow-set (lambda (x) X)))
    (∈ (lambda (x) x) (flow-set (lambda (y) y))))
(\leftarrow (\in (lambda (y) y) (flow-set x))
    (\in (lambda (x) x) (flow-set (lambda (x) x)))
    (∈ (lambda (y) y) (flow-set (lambda (y) y))))
(\leftarrow (\in (lambda (x) x) (flow-set y))
    (\in (lambda (y) y) (flow-set (lambda (x) x)))
    (\in (lambda (x) x) (flow-set (lambda (y) y))))
(\leftarrow (\in (lambda (y) y) (flow-set y))
    (\in (lambda (y) y) (flow-set (lambda (x) x)))
    (∈ (lambda (y) y) (flow-set (lambda (y) y))))
(\leftarrow (\in (lambda (x) x) (flow-set ((lambda (x) x) (lambda (y) y))))
```

Datalog

Datalog is a logic programming language that enables chain-forward logical inference via rules

```
edge(0,1).

edge(1,2).

path(x,y) :- edge(x,y).

path(x,z) :- path(x,y), path(y,z).
```

Datalog

Equally correct is...

```
edge(0,1).

edge(1,2).

path(x,y) :- edge(x,y).

path(x,z) :- edge(x,y), path(y,z).
```

Transitive closure implemented via Datalog

Facts are atomically "true" statements

```
edge(0,1).

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path(x,y) :- edge(x,y).

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```

Transitive closure implemented via Datalog

Rules are inductively defined relations

Facts are atomically "true" statements

```
edge(0,1).

edge(1,2).

path(x,y) :- edge(x,y).

path(x,z) :- path(x,y), path(y,z).
```

Edge		
Column 0	Column 1	
0	1	
1	2	

Path		
Column 0	Column 1	

edge(0,1).

edge(1,2).

To start the process, facts are loaded into tables

path(x,y) := edge(x,y).

path(x,z) :- path(x,y), path(y,z).

Edge		
Column 0	Column 1	
0	1	
1	2	

Path		
Column 0	Column 1	

```
edge(0,1). Computation evolves according to rules edge(1,2).
```

```
path(x,y) := edge(x,y).
```

$$path(x,z) :- path(x,y), path(y,z).$$

Ec	lge	Pa	ath
Column 0	Column 1	Column 0	Column 1
0	1	0	1
1	2	1	2

edge(0,1). Computation evolves according to rules edge(1,2). path(x,y) :- edge(x,y).

path(x,z) :- path(x,y), path(y,z).

Edge		
Column 0	Column 1	
0	1	
1	2	

Path		
Column 0	Column 1	
0	1	
1	2	
0	2	

```
edge(0,1).

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path(x,y) :- edge(x,y).

path(x,z) :- path(x,y), path(y,z).
```

```
edge(0,1).

edge(1,2).

path(x,y) :- edge(x,y).

path(x,z) :- path(x,y), path(y,z).
```

These rules can be compiled to relational algebra

Relational algebra:

- Projections (take columns x,y, and z from relation R)
- Renamings (rename column x to column y)
- Joins (matches tuples)

Let's take this rule...

$$path(x,z) :- path(x,y), path(y,z).$$

Compiling to relational algebra:

- Need to join "path" on itself
 - Want pairs of tuples (x,y), (y,z) such that the y matches
 - This can be implemented as a combo rename+join
 - Then putting the result into the path relation

In general, Datalog engines compile to relational algebra, and use optimizations to cull redundant rules / inline appropriately

Crucially, Datalog is extremely fast

Fastest program analyses in world currently implemented using Datalog (Smaragdakis et al.)

Relational algebra can be implemented efficiently on GPUs, MPI, and (recently!) supercomputers!



Souffle is an:

Implementation of Datalog

path(x, y) :- edge(x, y).

Super-fast single-node implementation of Datalog

path(x, y) := path(x, z), edge(z, y).

Let's think back to our rules...

$$(\lambda(x) \ e) \in R(\lambda(x) \ e)$$
$$(\lambda(x) \ e') \in R(e_0) \quad v \in R(e_1) \longrightarrow v \in R(x)$$
$$(\lambda(x) \ e) \in R(e_0) \quad v \in R(e) \longrightarrow v \in R((e_0 \ e_1))$$

How can we represent this in Datalog?

First attempt...

Reaches $(\lambda(x) e), (\lambda(x) e)$

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Unfortunately, this doesn't work: plain Datalog requires tuples contain atoms (e.g., numbers)

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Reaches
$$(\lambda(x) e), (\lambda(x) e)$$

Unfortunately, this doesn't work: plain Datalog requires tuples contain atoms (e.g., numbers)

Idea: number each subexpression

$$((\lambda(x^1) x^2)^3 (\lambda(y^4) y^5)^6)^7$$

Decompose AST into facts

```
.decl sourceLambda(exprId:number, varName:number, bodyId:number)
.decl sourceVarRef(exprId:number, varName:number)
.decl sourceApplication(exprId:number, fnId:number, argId:number)
// ((lambda (x^10) x^2)^3 (lambda (y^11) y^5)^6)^7
// Assume that variable x is named 10 and y is named 11
sourceLambda(3,10,2).
sourceLambda(6,11,5).
sourceVarRef(2,10).
sourceVarRef(5,11).
sourceApplication(7,3,6).
```

$$((\lambda(x^1) \ x^2)^3 \ (\lambda(y^4) \ y^5)^6)^7$$

```
.decl sourceLambda(exprId:number, varName:number, bodyId:number)
.decl sourceVarRef(exprId:number, varName:number)
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// ((lambda (x^10) x^2)^3 (lambda (y^11) y^5)^6)^7

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.decl sourceApplication(exprId:number, fnId:number, argId:number)

// ((lambda (x^10) x^2)^3 (lambda (y^11) y^5)^6)^7

// Assume that variable x is named 10 and y is named 11
sourceLambda(3,10,2).
sourceLambda(6,11,5).
sourceVarRef(2,10).
sourceVarRef(5,11).
sourceVarRef(5,11).
sourceVarRef(5,11).
reference to variable varName
```

$$((\lambda(x^1) \ x^2)^3 \ (\lambda(y^4) \ y^5)^6)^7$$

```
.decl sourceLambda(exprId:number, varName:number, bodyId:number)
.decl sourceVarRef(exprId:number, varName:number)
.decl sourceApplication(exprId:number, fnId:number, argId:number)
// ((lambda (x^10) x^2)^3 (lambda (y^11) y^5)^6)^7
// Assume that variable x is named 10 and y is named 11
sourceLambda(3,10,2).
sourceLambda(6,11,5).
sourceVarRef(2,10).
sourceVarRef(5,11).
sourceApplication(7,3,6).
```

sourceLambda(id, varName, bodyId) says "the subexpression numbered id is a lambda w/variable varName and whose body is identified by bodyld"

$$((\lambda(x^1) \ x^2)^3 \ (\lambda(y^4) \ y^5)^6)^7$$

Decompose AST into facts

```
.decl sourceLambda(exprId:number, varName:number, bodyId:number)
.decl sourceVarRef(exprId:number, varName:number)
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// ((lambda (x^10) x^2)^3 (lambda (y^11) y^5)^6)^7

// Assume that variable x is named 10 and y is named 11
sourceLambda(3,10,2).
sourceLambda(6,11,5). sourceVarRef(2,10). sourceVarRef(2,10). sourceVarRef(5,11). sourceVarRef(5,11). sourceApplication(7,3,6).
sourceApplication(7,3,6).
```

$$((\lambda(x^1) \ x^2)^3 \ (\lambda(y^4) \ y^5)^6)^7$$

```
.decl sourceLambda(exprId:number, varName:number, bodyId:number)
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// ((lambda (x^10) x^2)^3 (lambda (y^11) y^5)^6)^7

// Assume that variable x is named 10 and y is named 11
sourceLambda(3,10,2).
sourceLambda(6,11,5).
sourceVarRef(2,10).
sourceVarRef(5,11).
sourceApplication(7,3,6).
```

In general, we will assume that the fact tables have been created for us.

As a preprocessing pass, we can generate these rules.

```
;; Populate tables for a term
(define (make-tables expr)
 (match expr
   [(? symbol? x)
    (let ([id (newid)])
      (hash-set! source-var-ref id `(,id ,(lookup-or-new x)))
      id)
   [`(,e0 ,e1)
    (let* ([id (newid)]
           [fnid (make-tables e0)]
           [argid (make-tables e1)])
      (hash-set! source-application id `(,id ,fnid ,argid))
      id)
   (let* ([id (newid)]
           [varid (lookup-or-new x)]
           [body-id (make-tables e-body)])
      (hash-set! source-lambda id `(,id ,varid ,body-id))
      id)]))
```

```
;; Tables
(define source-lambda (make-hash))
(define source-var-ref (make-hash))
(define source-application (make-hash))
;; Ids
(define var->id (make-hash))
(define/contract (lookup-or-new var)
 (any/c . -> . number?)
 (if (hash-has-key? var->id var)
      (car (hash-ref var->id var))
      (let ([id (newid)])
        (hash-set! var->id var `(,id ,var))
        id)))
(define x 0)
(define (newid) (let ([id x]) (set! x (add1 x)) id))
(define (expr? e)
 (match e
    [(? symbol? x) #t]
    [`(,(? expr? e0) ,(? expr? e1)) #t]
    [`(lambda (,x),(? expr? e-body)) \#t]))
```

```
(define (dump-table table name)
  (for ([tuple (hash-values table)])
    (displayln
      (format "\sima(\sima)."
              name
              (string-join (map number->string tuple) ","))))
; (make-tables `((lambda (x) x) (lambda (y) y)))
(make-tables `((lambda (x) (x x)) (lambda (y) (y y))))
(dump-table source-lambda "sourceLambda")
(dump-table source-var-ref "sourceVarRef")
(dump-table source-application "sourceApplication")
```

```
// The flowsTo relation
.decl valueFlowsTo(value:number, expr:number)
.output valueFlowsTo
```

We can now build valueFlowsTo(v,e)

In the abstract world, valueFlowsTo relates an abstract value (a lambda, for 0CFA) and an expression.

Here, values will be represented by numbers that identify lambdas in the source program.

Expressions will be represented by numbers that identify subexpressions in the source program.

```
// The flowsTo relation
.decl valueFlowsTo(value:number, expr:number)
.output valueFlowsTo
```

Upshot: valueFlowsTo is a relation between numbers

We can now build valueFlowsTo(v,e)

In the abstract world, valueFlowsTo relates an abstract value (a lambda, for 0CFA) and an expression.

Here, values will be represented by numbers that identify lambdas in the source program.

Expressions will be represented by numbers that identify subexpressions in the source program.

Now we must translate each of our rules...

$$(\lambda(x) \ e) \in R(\lambda(x) \ e)$$
$$(\lambda(x) \ e') \in R(e_0) \quad v \in R(e_1) \longrightarrow v \in R(x)$$

$$(\lambda(x) e) \in R(e_0) \quad v \in R(e) \longrightarrow v \in R((e_0 e_1))$$

$$(\lambda(x) e) \in R(\lambda(x) e)$$

 $valueFlowsTo(lambdaId, lambdaId) :- sourceLambda(lambdaId,_,_).$

$$(\lambda(x) e') \in R(e_0) \quad v \in R(e_1) \longrightarrow v \in R(x)$$

$$(\lambda(x) e) \in R(e_0) \quad v \in R(e) \longrightarrow v \in R((e_0 e_1))$$

valueFlowsTo(v,bodyId).

```
.decl sourceLambda(exprId:number, varName:number, bodyId:number)
.decl sourceVarRef(exprId:number, varName:number)
.decl sourceApplication(exprId:number, fnId:number, argId:number)
// The flowsTo relation
 .decl valueFlowsTo(value:number, expr:number)
 .output valueFlowsTo
valueFlowsTo(lambdaId,lambdaId) :- sourceLambda(lambdaId,_{-},_{-}).
valueFlowsTo(argVal,x) := sourceApplication(\_,fnId,argId),
                           valueFlowsTo(_,argId),
                           sourceLambda(fnId,x,_),
                           valueFlowsTo(argVal,argId).
valueFlowsTo(v,exprId) :- sourceVarRef(exprId,var),
                           valueFlowsTo(v,var).
valueFlowsTo(v,exprId) :- sourceApplication(exprId,fnId,_),
                           valueFlowsTo(lambdaId,fnId),
                           sourceLambda(lambdaId,_,bodyId),
                           valueFlowsTo(v,bodyId).
```

```
.decl sourceLambda(exprId:number, varName:number, bodyId:number)
.decl sourceVarRef(exprId:number, varName:number)
.decl sourceApplication(exprId:number, fnId:number, argId:number)
// Here's the omega combinator
sourceLambda(6,7,8).
sourceLambda(1,2,3).
sourceVarRef(5,2).
sourceVarRef(4,2).
sourceVarRef(10,7).
sourceVarRef(9,7).
sourceApplication(8,9,10).
sourceApplication(0,1,6).
sourceApplication(3,4,5).
 // The flowsTo relation
 .decl valueFlowsTo(value:number, expr:number)
 .output valueFlowsTo
 valueFlowsTo(lambdaId, lambdaId) :- sourceLambda(lambdaId,_,_).
 valueFlowsTo(argVal,x) := sourceApplication(_,fnId,argId),
                            valueFlowsTo(_,argId),
                            sourceLambda(fnId,x,_),
```

souffle Ocfa-flow.dl

Which generates valueFlowsTo.csv!

valueFlowsTo	
1	1
6	2
6	4
6	5
6	6