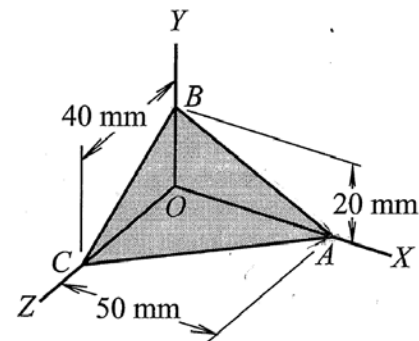


**ME EN 534**  
**Homework #1**

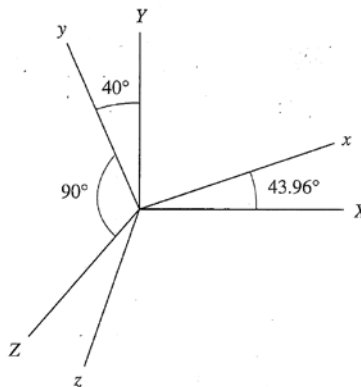
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1. Complete Problem 2.20 from the text.
2. At a certain instant an inertial measurement unit (IMU) on an aircraft report that it is heading  $40^\circ$  west of north, climbing at  $20^\circ$  and that its wings are banked at an angle of  $10^\circ$  clockwise as viewed looking forward. At this instant, the aircraft's accelerometers indicate that the center of mass has acceleration components of  $2g$  directed out of the belly of the aircraft and  $0.5g$  directed out of the nose. What are the acceleration components in terms of a north-south, east-west, and vertical frame?

3. The corners of triangular plate  $ABC$  are situated along the axes of coordinate system  $XYZ$  as shown. Another coordinate system,  $xyz$ , whose origin is at corner  $A$ , is defined such that its  $x$  axis is aligned along  $AB$ , pointing from  $A$  to  $B$ , and its  $z$  axis is perpendicular to plane  $ABC$  with a positive component in the direction of  $Y$ . Determine the coordinate transformation matrix from  $XYZ$  to  $xyz$ . Then determine the coordinates of the origin  $O$  relative to  $xyz$  and expressed in  $xyz$ . Hint: Define a coordinate system parallel to  $XYZ$  with its origin at  $A$ , and then carry out the necessary rotations to align it with the plate as described above.



4. Two coordinate systems  $XYZ$  and  $xyz$  are related to each other as shown in the figure. Find the rotation matrix  $[R]$ , where  $\{x \ y \ z\}^T = [R]\{X \ Y \ Z\}^T$ .



5. The rectangular box in Figure 2.39a of the text is rotated counterclockwise by  $45^\circ$  about a line passing through points  $A$  and  $B$  (viewed from  $B$ ). Find the coordinates of point  $C$  (relative to and in terms of  $XYZ$ ) after this rotation sequence. Hint: Create a new coordinate frame with its origin at point  $A$ , and then perform the rotations.