

Arrays

Q14 Merge overlapping sub-intervals

i/p $\rightarrow [1, 3], [2, 6], [8, 10], [15, 18]$

o/p $\rightarrow [1, 6], [8, 10], [15, 18]$

The first step would be to sort the intervals on the basis of starting point.

Now simply take a pair & linearly traverse the input & if we found they are merging, then simply merge them if not merging then simply push that to the ans vector of vector.

Merging step

① $[1, 3]$
 $[2, 6]$ \rightarrow max. of 3 and 6
 $3 \leq 6$ & hence merge $\Rightarrow [1, 6]$

② $[1, 4]$
 $[2, 3]$ \rightarrow max. of 4 & 3
 $4 \geq 3$ and hence merge $\Rightarrow [1, 4]$

Dry run

$\{1, 3\}, \{2, 6\}, \{8, 10\}, \{15, 18\}$

1) Simply sort it on the basis of starting number.

$\{1, 3\}, \{2, 6\}, \{8, 10\}, \{15, 18\}$

2) Considering the pair $\{1, 3\}$

- (i) $\{1, 3\}$ is merging with $\{1, 3\}$ and hence we get $\{1, 3\}$
- (ii) $\{1, 3\}$ is merging with $\{2, 6\}$ & hence we merged to get $\{1, 6\}$
- (iii) Now $\{1, 6\}$ is not merging with $\{8, 10\}$ & hence push $\{1, 6\}$ in the ans vector.

3) Considering the pair $\{8, 10\}$

- (i) $\{8, 10\}$ is merging with $\{8, 10\}$ and hence we get $\{8, 10\}$
- (ii) $\{8, 10\}$ is not merging with $\{15, 18\}$ & hence push $\{8, 10\}$ in the answer vector.

4) Considering the pair $\{15, 18\}$

- (i) $\{15, 18\}$ is merging with $\{15, 18\}$ & hence we get $\{15, 18\}$. Push this in ans vector. {left}
Now the i/p vector array has finished & we got ans vector as

$\{1, 6\}, \{8, 10\}, \{15, 18\}$

Why the above algorithm work?

This is because of sorting & if overlapping intervals exist they would be consecutive only.

Code

```
vector <vector <int>> merge Intervals (  
vector <vector <int>> & intervals) {
```

```
    // Creation of ans
```

```
    vector <vector <int>> ans;
```

```
    // Edge case  $\rightarrow$  no interval
```

```
    if (intervals.size() == 0) {
```

```
        return ans;
```

```
    }
```

```
    // Temp vector to be created
```

```
    vector <int> temp = intervals[0];
```

```
    // Linear traversal
```

```
    for (auto i : intervals) {
```

```
        // Merging condition
```

```
        if (i[0] <= temp[1]) {
```

```
starting  $\leftarrow$ 
```

```
 $\leftarrow$  ending
```

```
        temp[1] = max(temp[1], i[1]);
```

```
    }
```

```
    // Not merging case
```

```
    else {
```

```
        // Push the pair
```

```
        ans.push_back(temp);
```

```
        // Update or Consider new pair
```

```
        temp = i;
```

```
    }
```

```
}
```

```
    // Push left interval
```

```
    ans.push_back(temp);
```

```
    // return
```

```
    return ans;
```

\nearrow Sorting

3 Time complexity = $O(n \log n)$ Space = $O(n)$