

however we can use for loop.

Number system

Method to represent numeric values or quantities using different digits.

There are digits from 0-9.

10

1st digit = 1 2nd digit = 0

Digits are arranged & we get a quantity.

Like 1 & 0 digits are used to make 10 which is a number/quantity

Decimal system

This system has base 10. It uses digits from 0 to 9.

Base can be defined as no. of symbols / digits a number system uses.

Binary system

This system has base 2. This uses only 2 symbols namely 0 and 1. We can represent any quantity with these 2 symbols. These symbols are also known as bits.

CPU does calculations, storage in memory all are done in binary system.

0	1	1	0	1	0
---	---	---	---	---	---

This have 6 grids & hence it is known as 6 bit CPU.

→ 0V

0 → nothing . Power is 0 (No power)
1 → something is there. Voltage is 5V (Power is there)

int a = 5 ;

integer occupy 4 bytes of space or 32 bits . At the backend everything is stored or calculated in the form of bits.

Counting in binary system

0 - 0

1 - 1

2 - 10

3 - 11

4 - 100

5 - 101

6 - 110

7 - 111

⋮

Any integer can be written in the binary form.

Decimal to binary conversion

(i) This is done by the division method.

- 1) Divide number by 2.
- 2) Store remainder.
- 3) Repeat the above steps until quotient is less than 2.
- 4) Reverse the bits so obtained.

Ex → Convert 10 into binary form

Division

$$10/2 \rightarrow 5$$

$$5/2 \rightarrow 2$$

$$2/2 \rightarrow 1$$

$$1/2 \rightarrow 0$$

Remainder

0

1

0

1

Read
like this

10 is stored as 1010 in the binary form.

Code

```
int decToBinary (int n) {
    int binaryNumber = 0;
    int i = 0;
    while (n > 0) {
        int bit = n % 2;
        // Number from digits question
        binaryNumber = bit * pow(10, i)
            + binaryNumber;
        n = n / 2;
        i++;
    }
    return binaryNumber;
}
```

Note → To use pow function, we need to include cmath header file.

(ii) This can also be done via bitwise method

1) Obtain bit with bitwise AND operation
i.e $n \& 1$.

- 2) Right shift n by 1. $n = n \gg 1$
- 3) Repeat above steps till $n > 0$
- 4) Reverse bits so obtained.

Ex → Convert 10 in the decimal form.

$$N = 10 \rightarrow 1010$$

$$* \quad 1010 \& 0001 = 0000 \rightarrow 0$$

$$* \quad 1010 \gg 1 \rightarrow 101$$

$$\text{Now } 101 \& 1 \rightarrow 101$$

$$001$$

$$001 \rightarrow 1$$

$$* \quad 101 \gg 1 \rightarrow 10$$

$$\text{Now } 10 \& 1 \rightarrow 10$$

$$01$$

$$00 \rightarrow 0$$

$$* \quad 10 \gg 1 \rightarrow 1$$

$$\text{Now } 1 \& 1 \rightarrow 1$$

$$1$$

$$1 \rightarrow 1$$

Now same logic will be applied on making a number from digits or bits.

Code

```
int decToBin (int n) {
```

```
    int binaryNumber = 0;
```

```
    int i = 0;
```

```
    while (n > 0) {
```

```
        int bit = n & 1;
```

binaryNumber = bit * pow(10, i) +
binaryNumber;

n = n >> 1;

i++;

}

return binaryNumber;

}

Note → It is better to use the bitwise method as it is faster operation.

Binary to decimal conversion

1) Multiply each digit with its place value

$$\begin{array}{ccc} 1 & 2 & 3 \rightarrow 3 \times 10^0 \\ 1 \times 10^2 \leftarrow & & \downarrow 2 \times 10^1 \end{array}$$

These are the place values in case of decimals.
Place values in case of binary numbers.

$$\begin{array}{ccc} \dots 8 \leftarrow & & \uparrow 2 \\ 1 & 0 & 1 & 0 \\ \downarrow 4 & & \downarrow 1 \end{array}$$

2) Add up all the place values.

3) Sum is decimal number.

Place value = Digit * (Base)ⁱ

$$\begin{array}{cccc} 1 & 0 & 1 & 0 \\ 1 \times 2^3 & + & 0 \times 2^2 & + & 1 \times 2^1 & + & 0 \times 2^0 \end{array}$$

$$8 + 0 + 2 + 0 = 10 \text{ } \} \text{ Decimal number}$$

Code

```
int binToDecimal (int bin) {
    int ans = 0;
    int i = 0;
    while (bin > 0) {
        int bit = bin % 10;
        ans = ans + bit * pow(2, i);
        i++;
        bin = bin / 10;
    }
    return ans;
}
```

Note → Also we can extract the bit in above question by using bitwise AND.

```
int bit = bin & 1;
```