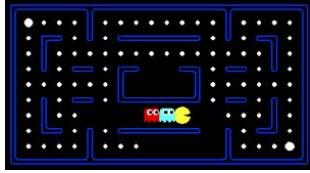




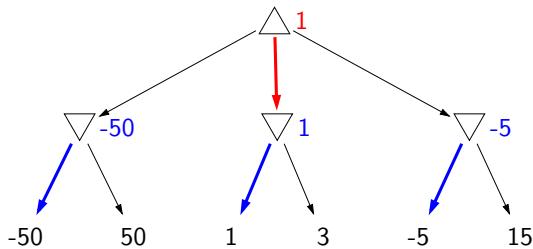
Lecture 10: Games II



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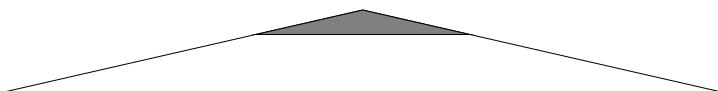
Review: minimax

agent (max) versus opponent (min)



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Review: depth-limited search



$$V_{\text{minmax}}(s, d) = \begin{cases} \text{Utility}(s) & \text{IsEnd}(s) \\ \text{Eval}(s) & d = 0 \\ \max_{a \in \text{Actions}(s)} V_{\text{minmax}}(\text{Succ}(s, a), d) & \text{Player}(s) = \text{agent} \\ \min_{a \in \text{Actions}(s)} V_{\text{minmax}}(\text{Succ}(s, a), d - 1) & \text{Player}(s) = \text{opp} \end{cases}$$

Use: at state s , choose action resulting in $V_{\text{minmax}}(s, d_{\text{max}})$



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Question

For a simultaneous two-player zero-sum game (like rock-paper-scissors), can you still be optimal if you reveal your strategy?

yes
no

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1

- Recall that the central object of study is the game tree. Game play starts at the root (starting state) and descends to a leaf (end state), where at each node s (state), the player whose turn it is ($\text{Player}(s)$) chooses an action $a \in \text{Actions}(s)$, which leads to one of the children $\text{Succ}(s, a)$.
- The **minimax principle** provides one way for the agent (your computer program) to compute a pair of minimax policies for both the agent and the opponent ($\pi_{\text{agent}}^*, \pi_{\text{opp}}^*$).
- For each node s , we have the minimax value of the game $V_{\text{minmax}}(s)$, representing the expected utility if both the agent and the opponent play optimally. Each node where it's the agent's turn is a max node (right-side up triangle), and its value is the maximum over the children's values. Each node where it's the opponent's turn is a min node (upside-down triangle), and its value is the minimum over the children's values.
- Important properties of the minimax policies: The agent can only decrease the game value (do worse) by changing his/her strategy, and the opponent can only increase the game value (do worse) by changing his/her strategy.

2

- In order to approximately compute the minimax value, we used a **depth-limited search**, where we compute $V_{\text{minmax}}(s, d_{\text{max}})$, the approximate value of s if we are only allowed to search to at most depth d_{max} .
- Each time we hit $d = 0$, we invoke an evaluation function $\text{Eval}(s)$, which provides a fast reflex way to assess the value of the game at state s .

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Evaluation function

Old: hand-crafted

Example: chess

$$\text{Eval}(s) = \text{material} + \text{mobility} + \text{king-safety} + \text{center-control}$$

$$\text{material} = 10^{100}(K - K') + 9(Q - Q') + 5(R - R') + 3(B - B' + N - N') + 1(P - P')$$

$$\text{mobility} = 0.1(\text{num-legal-moves} - \text{num-legal-moves}')$$

$$\dots$$

New: learn from data

$$\text{Eval}(s) = V(s; \mathbf{w})$$

Roadmap

TD learning

Simultaneous games

Non-zero-sum games

State-of-the-art



- When we looked at Q-learning, we considered linear evaluation functions (remember, linear in the weights \mathbf{w}). This is the simplest case, but it might not be suitable in some cases.
- But the evaluation function can really be any parametrized function. For example, the original TD-Gammon program used a neural network, which allows us to represent more expressive functions that capture the non-linear interactions between different features.
- Any model that you could use for regression in supervised learning you could also use here.

- Having a good evaluation function is one of the most important components of game playing. So far we've shown how one can manually specify the evaluation function by hand. However, this can be quite tedious, and moreover, how does one figure out to weigh the different factors? In this lecture, we will consider a method for learning this evaluation function automatically from data.
- The three ingredients in any machine learning approach are to determine the (i) model family (in this case, what is $V(s; \mathbf{w})$?), (ii) where the data comes from, and (iii) the actual learning algorithm. We will go through each of these in turn.

Model for evaluation functions

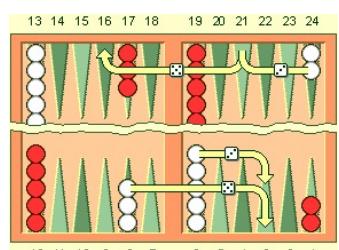
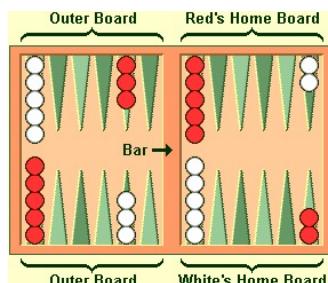
Linear:

$$V(s; \mathbf{w}) = \mathbf{w} \cdot \phi(s)$$

Neural network:

$$V(s; \mathbf{w}, \mathbf{v}_{1:k}) = \sum_{j=1}^k w_j \sigma(\mathbf{v}_j \cdot \phi(s))$$

Example: Backgammon



- As an example, let's consider the classic game of backgammon. Backgammon is a two-player game of strategy and chance in which the objective is to be the first to remove all your pieces from the board.
- The simplified version is that on your turn, you roll two dice, and choose two of your pieces to move forward that many positions.
- You cannot land on a position containing more than one opponent piece. If you land on exactly one opponent piece, then that piece goes on the bar and has start over from the beginning. (See the Wikipedia article for the full rules.)

Features for Backgammon

state s	Features $\phi(s)$:
2	$(\#\text{ o in column } 0) = 1]$: 1
3	$(\#\text{ o on bar})$: 1
	$(\text{fraction o removed})$: $\frac{1}{2}$
x	$(\#\text{ x in column } 1) = 1]$: 1
x	$(\#\text{ x in column } 3) = 3]$: 1
o	(is it o's turn) : 1
o	
1	
0	

- As an example, we can define the following features for Backgammon, which are inspired by the ones used by TD-Gammon.
- Note that the features are pretty generic; there is no explicit modeling of strategies such as trying to avoid having singleton pieces (because it could get clobbered) or preferences for how the pieces are distributed across the board.
- On the other hand, the features are mostly **indicator** features, which is a common trick to allow for more expressive functions using the machinery of linear regression. For example, instead of having one feature whose value is the number of pieces in a particular column, we can have multiple features for indicating whether the number of pieces is over some threshold.

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Generating data

Generate using policies based on current $V(s; \mathbf{w})$:

$$\pi_{\text{agent}}(s; \mathbf{w}) = \arg \max_{a \in \text{Actions}(s)} V(\text{Succ}(s, a); \mathbf{w})$$

$$\pi_{\text{opp}}(s; \mathbf{w}) = \arg \min_{a \in \text{Actions}(s)} V(\text{Succ}(s, a); \mathbf{w})$$

Note: don't need to randomize (ϵ -greedy) because game is already stochastic (backgammon has dice) and there's function approximation

Generate episode:

$$s_0; a_1, r_1, s_1; a_2, r_2, s_2; a_3, r_3, s_3; \dots; a_n, r_n, s_n$$

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Learning algorithm

Episode:

$$s_0; a_1, r_1, s_1; a_2, r_2, s_2; a_3, r_3, s_3; \dots, a_n, r_n, s_n$$

A small piece of experience:

$$(s, a, r, s')$$

Prediction:

$$V(s; \mathbf{w})$$

Target:

$$r + \gamma V(s'; \mathbf{w})$$

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- With a model family $V(s; \mathbf{w})$ and data $s_0, a_1, r_1, s_1, \dots$ in hand, let's turn to the learning algorithm.
- A general principle in learning is to figure out the **prediction** and the **target**. The prediction is just the value of the current function at the current state s , and the target uses the data by looking at the immediate reward r plus the value of the function applied to the successor state s' (discounted by γ). This is analogous to the SARSA update for Q-values, where our target actually depends on a one-step lookahead prediction.

General framework

Objective function:

$$\frac{1}{2} (\text{prediction}(\mathbf{w}) - \text{target})^2$$

Gradient:

$$(\text{prediction}(\mathbf{w}) - \text{target}) \nabla_{\mathbf{w}} \text{prediction}(\mathbf{w})$$

Update:

$$\mathbf{w} \leftarrow \mathbf{w} - \eta \underbrace{(\text{prediction}(\mathbf{w}) - \text{target}) \nabla_{\mathbf{w}} \text{prediction}(\mathbf{w})}_{\text{gradient}}$$

- Having identified a prediction and target, the next step is to figure out how to update the weights. The general strategy is to set up an objective function that encourages the prediction and target to be close (by penalizing their squared distance).
- Then we just take the gradient with respect to the weights \mathbf{w} .
- Note that even though technically the target also depends on the weights \mathbf{w} , we treat this as constant for this derivation. The resulting learning algorithm by no means finds the global minimum of this objective function. We are simply using the objective function to motivate the update rule.

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Temporal difference (TD) learning

Algorithm: TD learning

On each (s, a, r, s') :
 $\mathbf{w} \leftarrow \mathbf{w} - \eta [\underbrace{\text{prediction}}_{\text{prediction}} - \underbrace{(r + \gamma V(s'; \mathbf{w}))}_{\text{target}}] \nabla_{\mathbf{w}} V(s; \mathbf{w})$

For linear functions:

$$V(s; \mathbf{w}) = \mathbf{w} \cdot \phi(s)$$

$$\nabla_{\mathbf{w}} V(s; \mathbf{w}) = \phi(s)$$

- Plugging in the prediction and the target in our setting yields the TD learning algorithm. For linear functions, recall that the gradient is just the feature vector.

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Comparison

Algorithm: TD learning

On each (s, a, r, s') :
 $\mathbf{w} \leftarrow \mathbf{w} - \eta [\underbrace{\hat{V}_{\pi}(s; \mathbf{w})}_{\text{prediction}} - \underbrace{(r + \gamma \hat{V}_{\pi}(s'; \mathbf{w}))}_{\text{target}}] \nabla_{\mathbf{w}} \hat{V}_{\pi}(s; \mathbf{w})$

Algorithm: Q-learning

On each (s, a, r, s') :
 $\mathbf{w} \leftarrow \mathbf{w} - \eta [\underbrace{\hat{Q}_{\text{opt}}(s, a; \mathbf{w})}_{\text{prediction}} - \underbrace{(r + \gamma \max_{a' \in \text{Actions}(s)} \hat{Q}_{\text{opt}}(s', a'; \mathbf{w}))}_{\text{target}}] \nabla_{\mathbf{w}} \hat{Q}_{\text{opt}}(s, a; \mathbf{w})$

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Comparison

Q-learning:

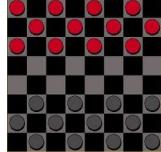
- Operate on $\hat{Q}_{\text{opt}}(s, a; \mathbf{w})$
- Off-policy: value is based on estimate of optimal policy
- To use, don't need to know MDP transitions $T(s, a, s')$

TD learning:

- Operate on $\hat{V}_\pi(s; \mathbf{w})$
- On-policy: value is based on exploration policy (usually based on \hat{V}_π)
- To use, need to know rules of the game $\text{Succ}(s, a)$

- TD learning is very similar to Q-learning. Both algorithms learn from the same data and are based on gradient-based weight updates.
- The main difference is that Q-learning learns the Q-value, which measures how good an action is to take in a state, whereas TD learning learns the value function, which measures how good it is to be in a state.
- Q-learning is an off-policy algorithm, which means that it tries to compute Q_{opt} , associated with the optimal policy (not Q_π), whereas TD learning is on-policy, which means that it tries to compute V_π , the value associated with a fixed policy π . Note that the action a does not show up in the TD updates because a is given by the fixed policy π . Of course, we usually are trying to optimize the policy, so we would set π to be the current guess of optimal policy $\pi(s) = \arg \max_{a \in \text{Actions}(s)} V(\text{Succ}(s, a); \mathbf{w})$.
- When we don't know the transition probabilities and in particular the successors, the value function isn't enough, because we don't know what effect our actions will have. However, in the game playing setting, we do know the transitions (the rules of the game), so using the value function is sufficient.

Learning to play checkers

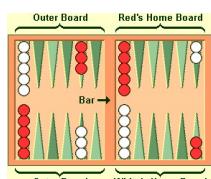


Arthur Samuel's checkers program [1959]:

- Learned by playing itself repeatedly (self-play)
- Smart features, linear evaluation function, use intermediate rewards
- Used alpha-beta pruning + search heuristics
- Reach human amateur level of play
- IBM 701: 9K of memory!

- The idea of using machine learning for game playing goes as far back as Arthur Samuel's checkers program. Many of the ideas (using features, alpha-beta pruning) were employed, resulting in a program that reached a human amateur level of play. Not bad for 1959!

Learning to play Backgammon

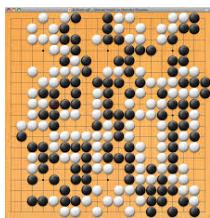


- Tesauro refined some of the ideas from Samuel with his famous TD-Gammon program provided the next advance, using a variant of TD learning called TD(λ). It had dumber features, but a more expressive evaluation function (neural network), and was able to reach an expert level of play.

Gerald Tesauro's TD-Gammon [1992]:

- Learned weights by playing itself repeatedly (1 million times)
- Dumb features, neural network, no intermediate rewards
- Reached human expert level of play, provided new insights into opening

Learning to play Go



- Very recently, self-play reinforcement learning has been applied to the game of Go. AlphaGo Zero uses a single neural network to predict winning probability and actions to be taken, using raw board positions as inputs. Starting from random weights, the network is trained to gradually improve its predictions and match the results of an approximate (Monte Carlo) tree search algorithm.

AlphaGo Zero [2017]:

- Learned by self play (4.9 million games)
- Dumb features (stone positions), neural network, no intermediate rewards, Monte Carlo Tree Search
- Beat AlphaGo, which beat Le Sedol in 2016
- Provided new insights into the game

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Summary so far

- Parametrize evaluation functions using features
- TD learning: learn an evaluation function

$$(\text{prediction}(\mathbf{w}) - \text{target})^2$$

Up next:



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Roadmap

TD learning

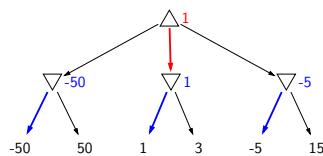
Simultaneous games

Non-zero-sum games

State-of-the-art



Turn-based games:



- Game trees were our primary tool to model turn-based games. However, in simultaneous games, there is no ordering on the player's moves, so we need to develop new tools to model these games. Later, we will see that game trees will still be valuable in understanding simultaneous games.

Simultaneous games:



?

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Two-finger Morra



Example: two-finger Morra

Players A and B each show 1 or 2 fingers.
If both show 1, B gives A 2 dollars.
If both show 2, B gives A 4 dollars.
Otherwise, A gives B 3 dollars.

[play with a partner]



Question

What was the outcome?

- player A chose 1, player B chose 1
- player A chose 1, player B chose 2
- player A chose 2, player B chose 1
- player A chose 2, player B chose 2

Payoff matrix



Definition: single-move simultaneous game

Players = {A, B}
Actions: possible actions
 $V(a, b)$: A's utility if A chooses action a , B chooses b
(let V be payoff matrix)

Example: two-finger Morra payoff matrix

A \ B	1 finger	2 fingers
1 finger	2	-3
2 fingers	-3	4

- In this lecture, we will consider only single move games. There are two players, A and B who both select from one of the available actions. The value or utility of the game is captured by a payoff matrix V whose dimensionality is $|Actions| \times |Actions|$. We will be analyzing everything from A's perspective, so entry $V(a, b)$ is the utility that A gets if he/she chooses action a and player B chooses b .

Strategies (policies)

Definition: pure strategy

A pure strategy is a single action:
 $a \in \text{Actions}$

Definition: mixed strategy

A mixed strategy is a probability distribution
 $0 \leq \pi(a) \leq 1$ for $a \in \text{Actions}$

Example: two-finger Morra strategies

Always 1: $\pi = [1, 0]$
Always 2: $\pi = [0, 1]$
Uniformly random: $\pi = [\frac{1}{2}, \frac{1}{2}]$

- Each player has a **strategy** (or a policy). A pure strategy (deterministic policy) is just a single action. Note that there's no notion of state since we are only considering single-move games.
- More generally, we will consider **mixed strategies** (randomized policy), which is a probability distribution over actions. We will represent a mixed strategy π by the vector of probabilities.

Game evaluation



Definition: game evaluation

The **value** of the game if player A follows π_A and player B follows π_B is

$$V(\pi_A, \pi_B) = \sum_{a,b} \pi_A(a)\pi_B(b)V(a,b)$$



Example: two-finger Morra

Player A always chooses 1: $\pi_A = [1, 0]$

Player B picks randomly: $\pi_B = [\frac{1}{2}, \frac{1}{2}]$

Value:
$$\begin{bmatrix} -\frac{1}{2} \\ 2 \end{bmatrix}$$

[whiteboard: matrix]

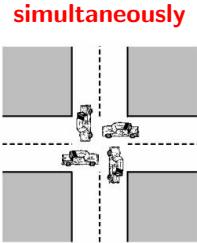
- Given a game (payoff matrix) and the strategies for the two players, we can define the value of the game.
- For pure strategies, the value of the game by definition is just reading out the appropriate entry from the payoff matrix.
- For mixed strategies, the value of the game (that is, the expected utility for player A) is gotten by summing over the possible actions that the players choose: $V(\pi_A, \pi_B) = \sum_{a \in \text{Actions}} \sum_{b \in \text{Actions}} \pi_A(a)\pi_B(b)V(a,b)$. We can also write this expression concisely using matrix-vector multiplications: $\pi_A^\top V \pi_B$.

How to optimize?

Game value:

$$V(\pi_A, \pi_B)$$

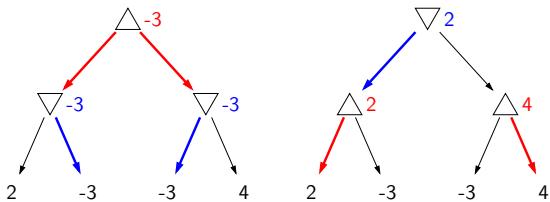
Challenge: player A wants to maximize, player B wants to minimize...



- Having established the values of fixed policies, let's try to optimize the policies themselves. Here, we run into a predicament: player A wants to maximize V but player B wants to minimize V **simultaneously**.
- Unlike turn-based games, we can't just consider one at a time. But let's consider the turn-based variant anyway to see where it leads us.

Pure strategies: who goes first?

Player A goes first:



Player B goes first:

- Let us first consider pure strategies, where each player just chooses one action. The game can be modeled by using the standard minimax game trees that we're used to.
- The main point is that if player A goes first, he gets -3 , but if he goes second, he gets 2 . In general, it's at least as good to go second, and often it is strictly better. This is intuitive, because seeing what the first player does gives more information.



Proposition: going second is no worse

$$\max_a \min_b V(a,b) \leq \min_b \max_a V(a,b)$$

General theorem

Theorem: minimax theorem [von Neumann, 1928]

For every simultaneous two-player zero-sum game with a finite number of actions:

$$\max_{\pi_A} \min_{\pi_B} V(\pi_A, \pi_B) = \min_{\pi_B} \max_{\pi_A} V(\pi_A, \pi_B),$$

where π_A, π_B range over **mixed strategies**.

- It turns out that having no gap is not a coincidence, and is actually one of the most celebrated mathematical results: the von Neumann minimax theorem. The theorem states that for any simultaneous two-player zero-sum game with a finite set of actions (like the ones we've been considering), we can just swap the min and the max: it doesn't matter which player reveals his/her strategy first, as long as their strategy is optimal. This is significant because we were stressing out about how to analyze the game when two players play simultaneously, but now we find that both orderings of the players yield the same answer. It is important to remember that this statement is true only for mixed strategies, not for pure strategies.
- This theorem can be proved using linear programming duality, and policies can be computed also using linear programming. The sketch of the idea is as follows: recall that the optimal strategy for the second player is always deterministic, which means that the $\max_{\pi_A} \min_{\pi_B} \dots$ turns into $\max_{\pi_A} \min_{\pi_B} \dots$. The min is now over n actions, and can be rewritten as n linear constraints, yielding a linear program.
- As an aside, recall that we also had a minimax result for turn-based games, where the max and the min were over agent and opponent policies, which map states to actions. In that case, optimal policies were always deterministic because at each state, there is only one player choosing.

Upshot: revealing your optimal mixed strategy doesn't hurt you!

Proof: linear programming duality

Algorithm: compute policies using linear programming

Summary

- Challenge: deal with simultaneous min/max moves
- Pure strategies: going second is better
- Mixed strategies: doesn't matter (von Neumann's minimax theorem)

Utility functions

Competitive games: minimax (linear programming)



Collaborative games: pure maximization (plain search)



Real life: ?



Roadmap

TD learning

Simultaneous games

Non-zero-sum games

State-of-the-art

- So far, we have focused on competitive games, where the utility of one player is the exact opposite of the utility of the other. The minimax principle is the appropriate tool for modeling these scenarios.
- On the other extreme, we have collaborative games, where the two players have the same utility function. This case is less interesting, because we are just doing pure maximization (e.g., finding the largest element in the payoff matrix or performing search).
- In many practical real life scenarios, games are somewhere in between pure competition and pure collaboration. This is where things get interesting...

Prisoner's dilemma

Example: Prisoner's dilemma

Prosecutor asks A and B individually if each will testify against the other.
If both testify, then both are sentenced to 5 years in jail.
If both refuse, then both are sentenced to 1 year in jail.
If only one testifies, then he/she gets out for free; the other gets a 10-year sentence.

[play with a partner]



Question

What was the outcome?

- player A testified, player B testified
- player A refused, player B testified
- player A testified, player B refused
- player A refused, player B refused

Prisoner's dilemma



Example: payoff matrix

	testify	refuse
testify	$A = -5, B = -5$	$A = -10, B = 0$
refuse	$A = 0, B = -10$	$A = -1, B = -1$



Definition: payoff matrix

Let $V_p(\pi_A, \pi_B)$ be the utility for player p .

Nash equilibrium

Can't apply von Neumann's minimax theorem (not zero-sum), but get something weaker:



Definition: Nash equilibrium

A **Nash equilibrium** is (π_A^*, π_B^*) such that no player has an incentive to change his/her strategy:

$$V_A(\pi_A^*, \pi_B^*) \geq V_A(\pi_A, \pi_B^*) \text{ for all } \pi_A$$

$$V_B(\pi_A^*, \pi_B^*) \geq V_B(\pi_A^*, \pi_B) \text{ for all } \pi_B$$

- Since we no longer have a zero-sum game, we cannot apply the minimax theorem, but we can still get a weaker result.
- A Nash equilibrium is kind of a state point, where no player has an incentive to change his/her policy unilaterally. Another major result in game theory is Nash's existence theorem, which states that any game with a finite number of players (importantly, not necessarily zero-sum) has at least one Nash equilibrium (a stable point). It turns out that finding one is hard, but we can be sure that one exists.



Theorem: Nash's existence theorem [1950]

In any finite-player game with finite number of actions, there exists **at least one** Nash equilibrium.

Examples of Nash equilibria



Example: Two-finger Morra

Nash equilibrium: A and B both play $\pi = [\frac{7}{12}, \frac{5}{12}]$.



Example: Collaborative two-finger Morra

Two Nash equilibria:

- A and B both play 1 (value is 2).
- A and B both play 2 (value is 4).



Example: Prisoner's dilemma

Nash equilibrium: A and B both testify.

- Here are three examples of Nash equilibria. The minimax strategies for zero-sum are also equilibria (and they are global optima).
- For purely collaborative games, the equilibria are simply the entries of the payoff matrix for which no other entry in the row or column are larger. There are often multiple local optima here.
- In the Prisoner's dilemma, the Nash equilibrium is when both players testify. This is of course not the highest possible reward, but it is stable in the sense that neither player would want to change his/her strategy. If both players had refused, then one of the players could testify to improve his/her payoff (from -1 to 0).



Summary so far

Simultaneous zero-sum games:

- von Neumann's minimax theorem
- Multiple minimax strategies, single game value

Simultaneous non-zero-sum games:

- Nash's existence theorem
- Multiple Nash equilibria, multiple game values

Huge literature in game theory / economics

- For simultaneous zero-sum games, all minimax strategies have the same game value (and thus it makes sense to talk about the value of a game). For non-zero-sum games, different Nash equilibria could have different game values (for example, consider the collaborative version of two-finger Morra).



Roadmap

TD learning

Simultaneous games

Non-zero-sum games

State-of-the-art



State-of-the-art: chess

1997: IBM's Deep Blue defeated world champion Gary Kasparov

Fast computers:

- Alpha-beta search over 30 billion positions, depth 14
- Singular extensions up to depth 20

Domain knowledge:

- Evaluation function: 8000 features
- 4000 "opening book" moves, all endgames with 5 pieces
- 700,000 grandmaster games
- Null move heuristic: opponent gets to move twice



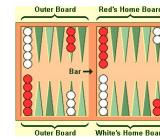
State-of-the-art: checkers

1990: Jonathan Schaeffer's **Chinook** defeated human champion; ran on standard PC

Closure:

- 2007: Checkers solved in the minimax sense (outcome is draw), but doesn't mean you can't win
- Alpha-beta search + 39 trillion endgame positions

Alpha-beta search isn't enough...



Challenge: large branching factor

- Backgammon: randomness from dice (can't prune!)
- Go: large board size (361 positions)

Solution: learning

- For games such as checkers and chess with a manageable branching factor, one can rely heavily on minimax search along with alpha-beta pruning and a lot of computation power. A good amount of domain knowledge can be employed as to attain or surpass human-level performance.
- However, games such as Backgammon and Go require more due to the large branching factor. Backgammon does not intrinsically have a larger branching factor, but much of this branching is due to the randomness from the dice, which cannot be pruned (it doesn't make sense to talk about the most promising dice move).
- As a result, programs for these games have relied a lot on TD learning to produce good evaluation functions without searching the entire space.

AlphaGo



- Supervised learning: on human games
- Reinforcement learning: on self-play games
- Evaluation function: convolutional neural network (value network)
- Policy: convolutional neural network (policy network)
- Monte Carlo Tree Search: search / lookahead

Section: AlphaGo Zero

- The most recent visible advance in game playing was March 2016, when Google DeepMind's AlphaGo program defeated Le Sedol, one of the best professional Go players 4-1.
- AlphaGo took the best ideas from game playing and machine learning. DeepMind executed these ideas well with lots of computational resources, but these ideas should already be familiar to you.
- The learning algorithm consisted of two phases: a supervised learning phase, where a policy was trained on games played by humans (30 million positions) from the KGS Go server; and a reinforcement learning phase, where the algorithm played itself in attempt to improve, similar to what we say with Backgammon.
- The model consists of two pieces: a value network, which is used to evaluate board positions (the evaluation function); and a policy network, which predicts which move to make from any given board position (the policy). Both are based on convolutional neural networks, which we'll discuss later in the class.
- Finally, the policy network is not used directly to select a move, but rather to guide the search over possible moves in an algorithm similar to Monte Carlo Tree Search.

Other games

Security games: allocate limited resources to protect a valuable target. Used by TSA security, Coast Guard, protect wildlife against poachers, etc.



- The techniques that we've developed for game playing go far beyond recreational uses. Whenever there are multiple parties involved with conflicting interests, game theory can be employed to model the situation.
- For example, in a security game a defender needs to protect a valuable target from a malicious attacker. Game theory can be used to model these scenarios and devise optimal (randomized) strategies. Some of these techniques are used by TSA security at airports, to schedule patrol routes by the Coast Guard, and even to protect wildlife from poachers.

Other games

Resource allocation: users share a resource (e.g., network bandwidth); selfish interests leads to volunteer's dilemma



Language: people have speaking and listening strategies, mostly collaborative, applied to dialog systems



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- For example, in resource allocation, we might have n people wanting to access some Internet resource. If all of them access the resource, then all of them suffer because of congestion. Suppose that if $n - 1$ connect, then those people can access the resource and are happy, but the one person left out suffers. Who should volunteer to step out (this is the volunteer's dilemma)?
- Another interesting application is modeling communication. There are two players, the speaker and the listener, and the speaker's actions are to choose what words to use to convey a message. Usually, it's a collaborative game where utility is high when communication is successful and efficient. These game-theoretic techniques have been applied to building dialog systems.

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Summary

- Main challenge:** not just one objective
- Minimax principle:** guard against adversary in turn-based games
- Simultaneous non-zero-sum games:** mixed strategies, Nash equilibria
- Strategy:** search game tree + learned evaluation function

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- Games are an extraordinary rich topic of study, and we have only seen the tip of the iceberg. Beyond simultaneous non-zero-sum games, which are already complex, there are also games involving partial information (e.g., poker).
- But even if we just focus on two-player zero-sum games, things are quite interesting. To build a good game-playing agent involves integrating the two main thrusts of AI: search and learning, which are really symbiotic. We can't possibly search an exponentially large number of possible futures, which means we fall back to an evaluation function. But in order to learn an evaluation function, we need to search over enough possible futures to build an accurate model of the likely outcome of the game.