数论

筛选法素数打表

```
void isPrime()
{
    for (int i = 2; i < N; i++)
        if (!a[i])
        for (int j = i + i; j < N; j += i)
        a[j] = 1;
}</pre>
```

组合数

```
//扩展欧几里得求组合数
LL fac[N];
void init()
{
   LL i;
   fac[0]=1;
   for (LL i = 1; i < N; i++)
   fac[i] = fac[i - 1] * i % MOD;
}
LL exgcd(LL a, LL b, LL &x, LL &y) {
   if (!b) \{x = 1; y = 0; return a;\}
   LL d = exgcd(b, a \% b, y, x);
   y -= a / b * x;
   return d;
}
LL inv(LL a, LL n) {
   LL x, y;
   exgcd(a, n, x, y);
   return (x + n) \% n;
```

```
LL C(LL n, LL m) {
    return fac[n] * inv(fac[m] * fac[n - m] % MOD, MOD) % MOD;
}

//递推求 O(n^2)
int comb[N][N];//comb[n][m]就是 C(n,m)

void init() {
    for(int i = 0; i < N; i ++) {
        comb[i][0] = comb[i][i] = 1;
        for(int j = 1; j < i; j ++) {
            comb[i][j] = comb[i-1][j] + comb[i-1][j-1];
            comb[i][j] %= MOD;
        }
    }
}
</pre>
```

线性基

```
const int MN=60;
ll a[61],tmp[61];
bool flag;
void ins(ll x){
   for(reg int i=MN;~i;i--)
       if(x&(1ll<<i))
           if(!a[i]){a[i]=x;return;}
           else x^=a[i];
   flag=true;
}
bool check(ll x){
   for(reg int i=MN;~i;i--)
       if(x&(1ll<<i))
           if(!a[i])return false;
           else x^=a[i];
   return true;
}
```

```
11 qmax(11 res=0){
    for(reg int i=MN;~i;i--)
        res=max(res,res^a[i]);
    return res;
}
11 qmin(){
    if(flag)return 0;
    for(reg int i=0;i<=MN;i++)</pre>
        if(a[i])return a[i];
}
11 query(11 k){
    reg ll res=0;reg int cnt=0;
    k-=flag;if(!k)return 0;
    for(reg int i=0;i<=MN;i++){</pre>
        for(int j=i-1;~j;j--)
            if(a[i]&(1ll<<j))a[i]^=a[j];
        if(a[i])tmp[cnt++]=a[i];
    }
    if(k>=(111<<cnt))return -1;</pre>
    for(reg int i=0;i<cnt;i++)</pre>
        if(k&(1ll<<i))res^=tmp[i];</pre>
    return res;
}
```

冬

链式前向星

```
//存储结构
struct Edge {
    int to; //边的终点
    int w; //边的权值
    int next; //起点相同的下一条边
} edge[M]; //M 为边数, N 为顶点数
int head[N]; //head[i]是以 i 为起点的第一条边的编号
int cnt; //记录边数
```

```
//初始化
cnt = 0;
memset(head, -1, sizeof(head));
//建图
void addEdge(int u, int v, int w)
   edge[cnt].to = v;
   edge[cnt].w = w;
   edge[cnt].next = head[u];
   head[u] = cnt++;
}
//遍历以 u 为起点的邻接边
for (int i = head[u]; i != -1; i = edge[i].next) {
   int to = edge[i].to; //终点
   int w = edge[i].w; //权值
}
Dinic 算法
const int maxn=300;
const int INF=0x3f3f3f3f3f;
struct Edge{
   int to,next,cap;
}edge[maxn*maxn];
int head[maxn],tot;
int dep[maxn], cur[maxn];
void init(){
   tot=0;
   memset(head,-1,sizeof(head));
}
void addEdge(int u,int v,int c){
   edge[tot].to=v;edge[tot].cap=c;
   edge[tot].next=head[u];head[u]=tot++;
   edge[tot].to=u;edge[tot].cap=0;
   edge[tot].next=head[v];head[v]=tot++;
}
```

```
bool bfs(int s,int t){
   memset(dep,-1,sizeof(dep));
   for(int i=1;i<=n;i++)cur[i]=head[i];</pre>
   queue<int> que;
   dep[s]=0;
   que.push(s);
   while(que.size()){
       int u=que.front();que.pop();
       for(int i=head[u];i!=-1;i=edge[i].next){
           int v=edge[i].to;
           if(edge[i].cap>0&&dep[v]==-1){
               dep[v]=dep[u]+1;
               que.push(v);
           }
       }
   }
   if(dep[t]!=-1)return true;
   return false;
}
int dfs(int now,int t,int limit){
   if(!limit||now==t)return limit;
   int flow=0,f;
   for(int i=cur[now];i!=-1;i=edge[i].next){
       cur[now]=i;
       int v=edge[i].to;
       if(dep[v]==dep[now]+1&&(f=dfs(v,t,min(limit,edge[i].cap)))){
           flow+=f;
           limit-=f;
           edge[i].cap-=f;
           edge[i^1].cap+=f;
           if(!limit)break;
       }
   }
   return flow;
}
```

```
int dinic(int s,int t){
   int maxflow=0;
   while(bfs(s,t)){
      maxflow+=dfs(s,t,INF);
   }
   return maxflow;
}
```

数据结构

Treap

```
const int maxn=1e5+5;
const int INF=2e9+7;
struct Treap {
   int ch[maxn][2];//结点左右儿子
   int val[maxn],dat[maxn];//基本值和优先级
   int size[maxn], cnt[maxn];//子树大小,结点副本数
   int tot,root;
   int New(int v) {
      val[++tot]=v;
      dat[tot]=rand();//随机优先级
      size[tot]=1;
      cnt[tot]=1;
      return tot;
   }
   void pushup(int id) {
      size[id]=size[ch[id][0]]+size[ch[id][1]]+cnt[id];
   }
   void build() {
      root=New(-INF),ch[root][1]=New(INF);
      pushup(root);
   }
   void rotate(int& id,int d) { //id 是引用传递,d(irection)为旋转方向,0
```

```
为左旋,1为右旋
       int temp=ch[id][d^1];
       ch[id][d^1]=ch[temp][d];
       ch[temp][d]=id;
       id=temp;
       pushup(ch[id][d]),pushup(id);
   }
   void insert(int& id,int v) {
       if(!id) {
           id=New(v);
           return;
       }
       if(v==val[id])cnt[id]++;
       else {
           int d=v<val[id]?0:1;</pre>
           insert(ch[id][d],v);
           if(dat[id]<dat[ch[id][d]])rotate(id,d^1);</pre>
       }
       pushup(id);
   }
   void remove(int&id,int v) {
       if(!id)return;
       if(v==val[id]) {
           if(cnt[id]>1) {
               cnt[id]--,pushup(id);
               return;
           }
           if(ch[id][0]||ch[id][1]) {
               if(!ch[id][1]||dat[ch[id][0]]>dat[ch[id][1]]) {
                   rotate(id,1),remove(ch[id][1],v);
               } else {
                   rotate(id,0),remove(ch[id][0],v);
               }
               pushup(id);
           } else id=0;
           return;
       v<val[id]?remove(ch[id][0],v):remove(ch[id][1],v);</pre>
```

```
pushup(id);
   }
   int getRank(int id,int v) {
       if(!id)return 0;
       if(v==val[id])return size[ch[id][0]]+1;
       else if(v<val[id])return getRank(ch[id][0],v);</pre>
       else return size[ch[id][0]]+cnt[id]+getRank(ch[id][1],v);
   }
   int getVal(int id,int rank) {
       if(!id)return INF;
       if(rank<=size[ch[id][0]])return getVal(ch[id][0],rank);</pre>
       else if(rank<=size[ch[id][0]]+cnt[id])return val[id];</pre>
       else return getVal(ch[id][1],rank-size[ch[id][0]]-cnt[id]);
   }
   int getPre(int v) {
       int id=root,pre;
       while(id) {
           if(val[id]<v)pre=val[id],id=ch[id][1];</pre>
           else id=ch[id][0];
       }
       return pre;
   }
   int getNext(int v) {
       int id = root,next;
       while(id) {
           if(val[id] > v)next = val[id],id = ch[id][0];
           else id = ch[id][1];
       }
       return next;
   }
} trp;
int main() {
   trp.build();
   int n;
   scanf("%d",&n);
   while(n--) {
       int opt,x;
```

```
scanf("%d%d",&opt,&x);
int ans=-INF;
int& r=trp.root;
trp.insert(r,x);
trp.remove(r,x);
ans= trp.getRank(r,x)-1;
ans=trp.getVal(r,x+1);
ans=trp.getPre(x);
ans=trp.getNext(x);
}
```

字符串

字典树 trie

```
struct Trie{
   int ch[M][27];
   int val[M];
   int sz;
   Trie(){sz=1;memset(ch[0],0,sizeof(ch[0]));}
   int idx(char c){return c-'a';}
   void insert(char s[],int v) {
       int u=0,n=strlen(s);
       for(int i=0;i<n;i++){</pre>
           int c=idx(s[i]);
           if(!ch[u][c]){
               memset(ch[sz],0,sizeof(ch[sz]));
               val[sz]=0;
               ch[u][c]=sz++;
           }
           u=ch[u][c];
       }
       val[u]=v;
   }
}tr;
```

AC 自动机

```
queue<int> q;
struct ACauto{
   int ch[N][26],val[N],fail[N],cnt;
   void ins(char* s){
       int len=strlen(s),u=0;
       for(int i=0;i<len;i++){</pre>
           int v=s[i]-'a';
           if(!ch[u][v])ch[u][v]=++cnt;
           u=ch[u][v];
       }
       val[u]++;
   }
   void getFail(){
       for(int i=0;i<26;i++){if(ch[0][i]){
           fail[ch[0][i]]=0;
           q.push(ch[0][i]);
       }}
       while(!q.empty()){
           int u=q.front();q.pop();
           for(int i=0;i<26;i++){
              if(ch[u][i])fail[ch[u][i]]=ch[fail[u]][i],q.push(ch[u][i]);
               else ch[u][i]=ch[fail[u]][i];
           }
       }
   }
   int query(char* s) {
       int len=strlen(s);int u=0,ans=0;
       for(int i=0;i<len;i++){</pre>
           u=ch[u][s[i]-'a'];
           for(int t=u;t&&~val[t];t=fail[t]){
               ans+=val[t],val[t]=-1;
           }
       }
       return ans;
   }
}AC;
```

其他

输入输出挂

```
//适用于正负整数
template <class T>
inline bool scan_d(T &ret) {
   char c;
   int sgn;
   if(c=getchar(),c==EOF) return 0; //EOF
   while(c!='-'&&(c<'0'||c>'9')) c=getchar();
   sgn=(c=='-')?-1:1;
   ret=(c=='-')?0:(c-'0');
   while(c=getchar(),c>='0'&&c<='9') ret=ret*10+(c-'0');
   ret*=sgn;
   return 1;
}
inline void out(int x) {
   if(x>9) out(x/10);
   putchar(x%10+'0');
}
```