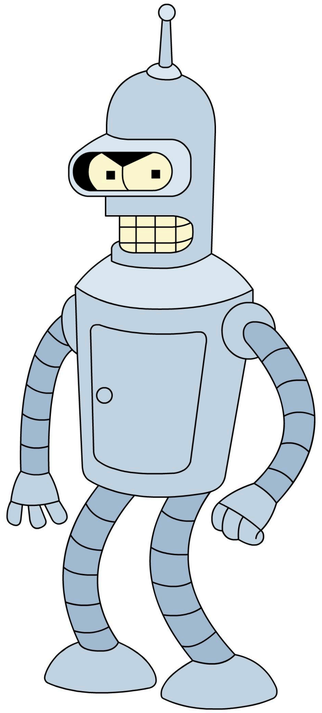
Reinforcement Learning

HSE, autumn - winter 2022

Lecture 1



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Home assignments and grading
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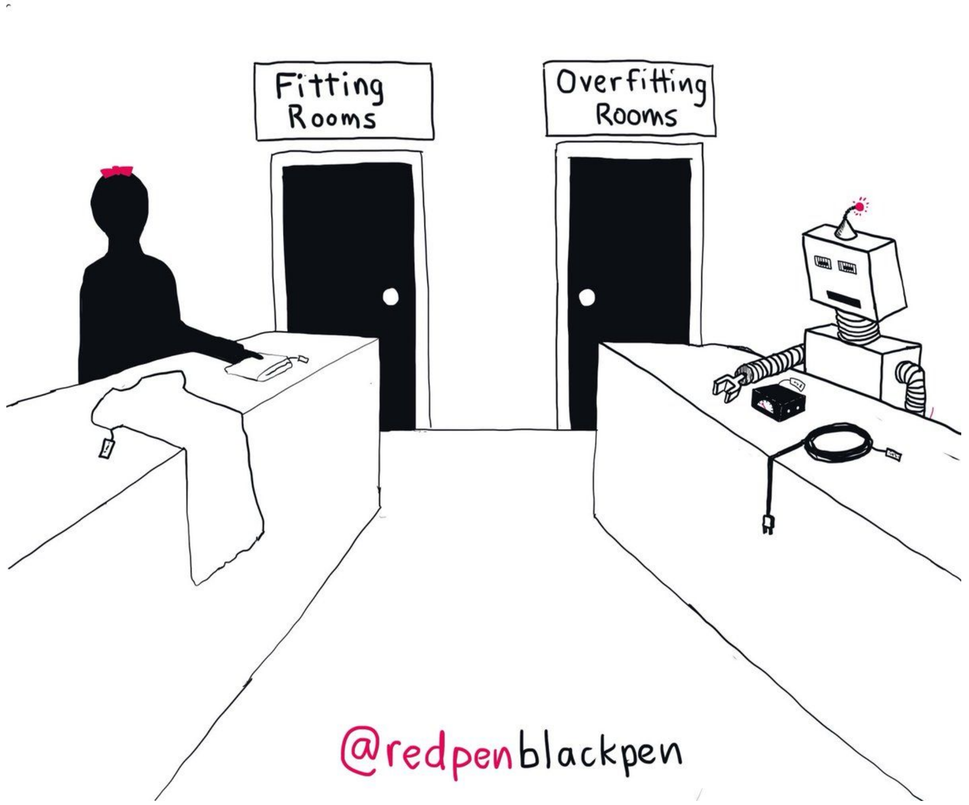

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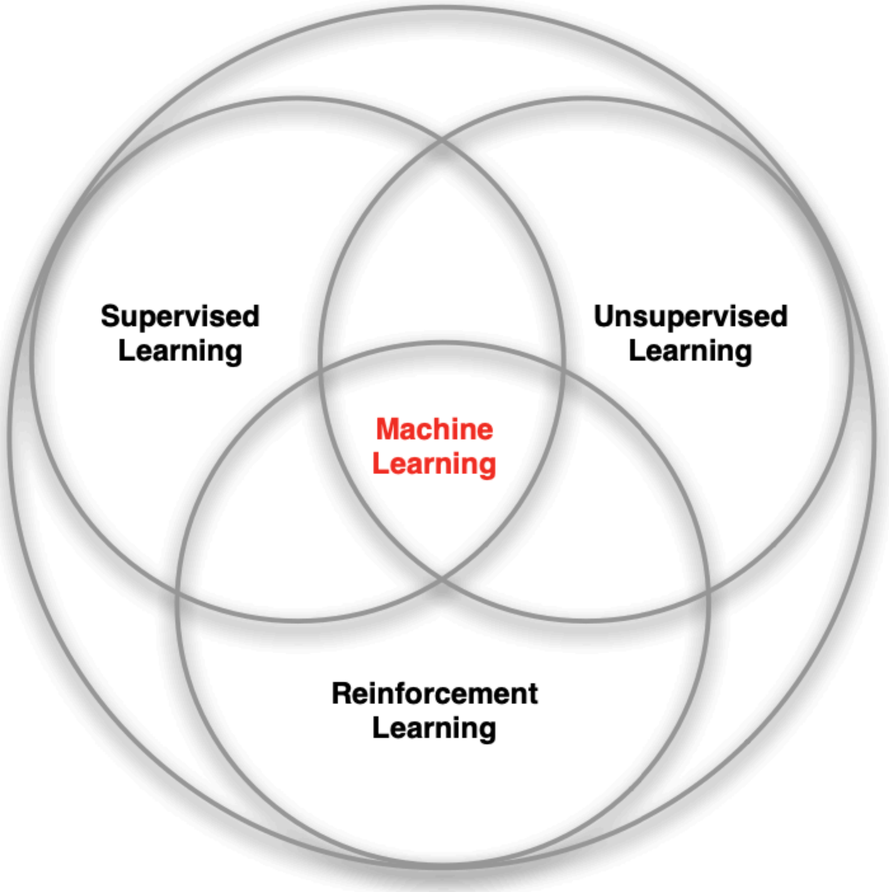
Course Plan

1. 01.11.2022: RL problem statement. Cross-entropy method. (HW1)
2. 08.11.2022: Bellman equations and Dynamic programming. (HW2)
3. 15.11.2022: Model free algorithms. Tabular methods.
4. 22.11.2022: Introduction to deep RL. DQN (HW3)
5. 29.11.2022: Policy based methods. REINFORCE
6. 06.12.2022: Actor-critic algorithms (HW4)
7. 13.12.2022: Bandits
8. 20.12.2022: TBA

Useful Links

1. http://incompleteideas.net/book/the-book-2nd.html
2. http://rail.eecs.berkeley.edu/deeprlcourse/
3. https://github.com/yandexdataschool/Practical_RL
4. https://www.deepmind.com/learning-resources/reinforcement-learning-lecture-series-2021
5. https://web.stanford.edu/class/cme241/
6. https://github.com/huggingface/deep-rl-class

Recap



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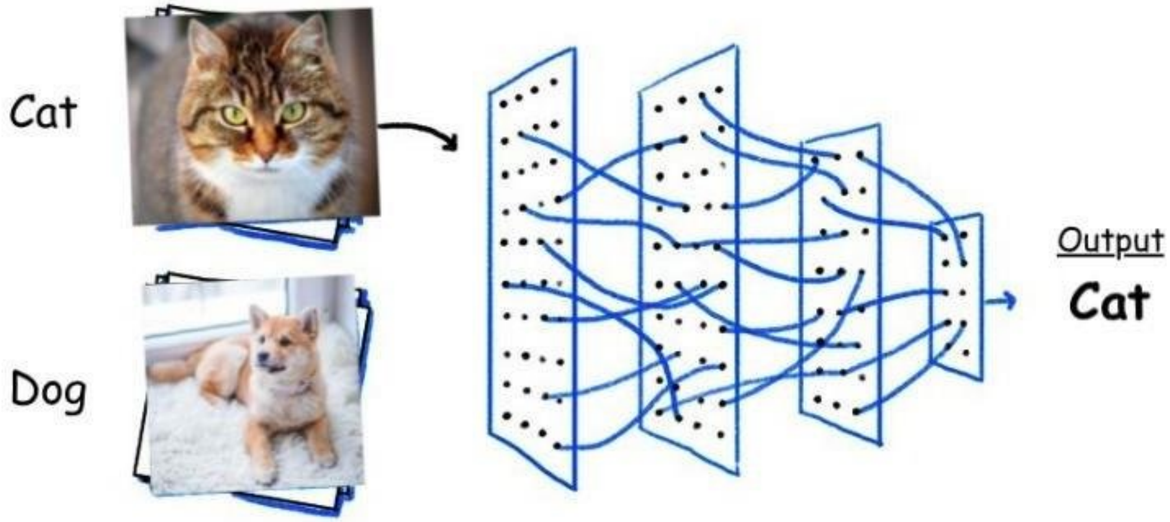
Supervised Learning

Train sample: $(\mathbf{x}_i, y_i) \sim i\,.\,i\,.\,d\,.$

Approximation: $f(\mathbf{x}_i) = \hat{y}_i \approx y_i$

Optimization: $\frac{1}{n}\sum_{i=1}^{n} L(f(\mathbf{x}_i), y_i) \to \min_{f \in \mathcal{F}}$



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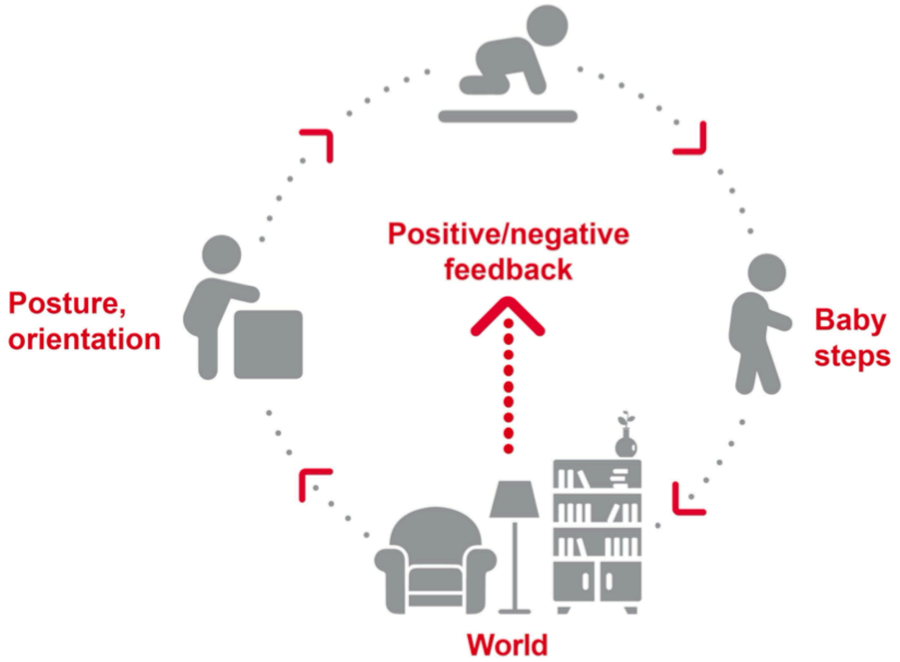
Decision Making Process

Baby learning



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Self-driving car

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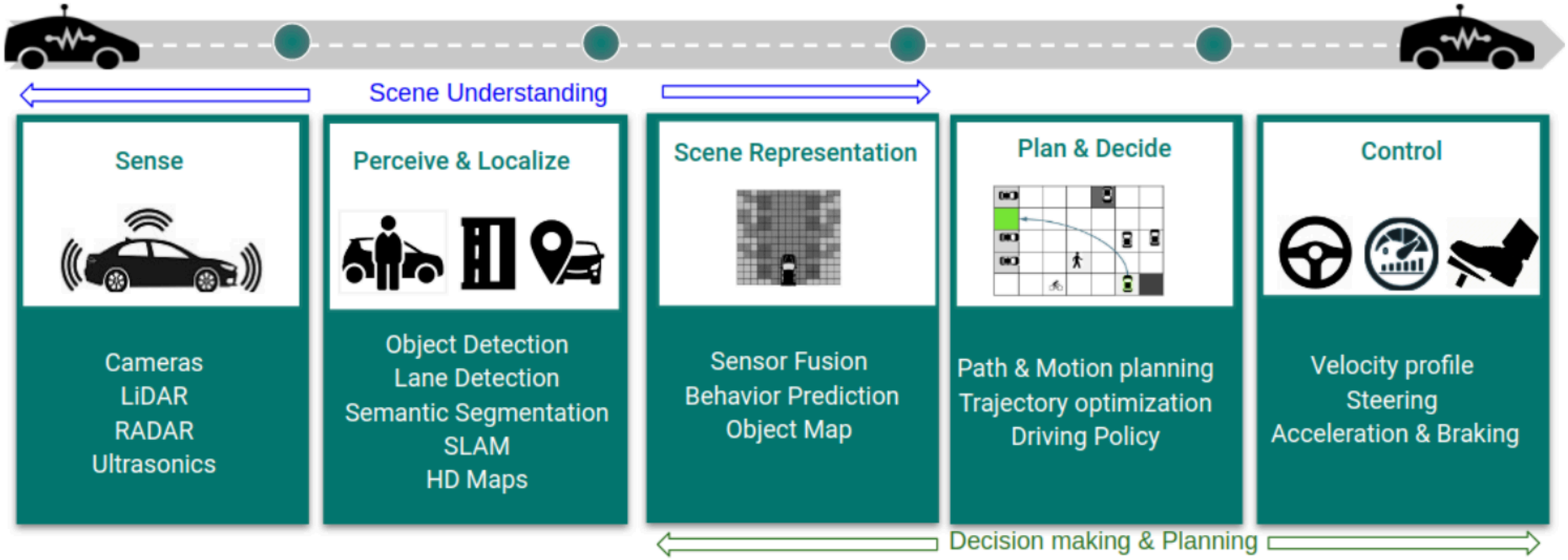
Self-driving Cars



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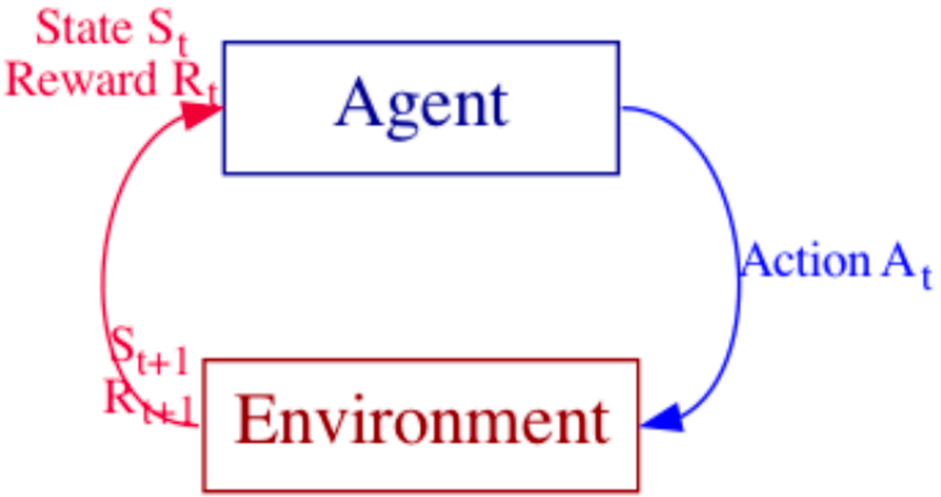
Reinforcement Learning Features

1. Trial-and-error search
2. Delayed rewards
3. Interaction with the environment



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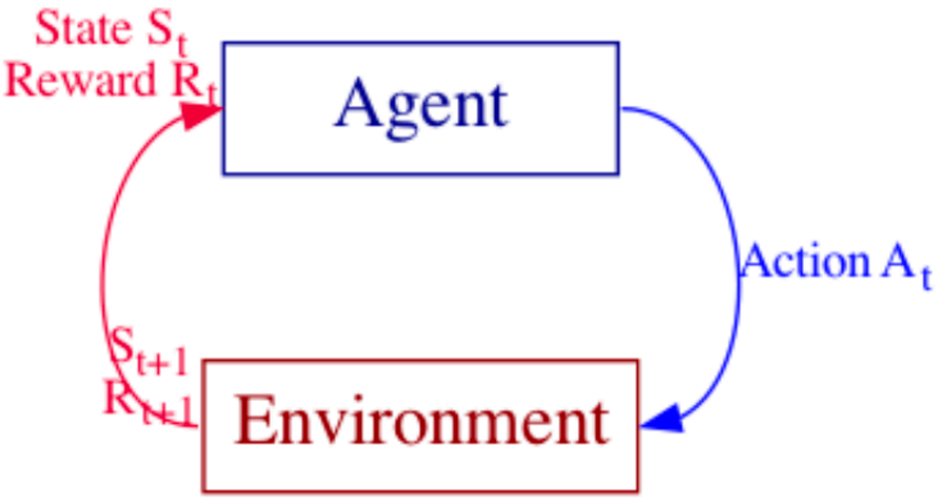
Reward hypothesis:

“That all of what we mean by goals and purposes can be well thought of as maximization of the expected value of the cumulative sum of a received scalar signal (reward).”

Reinforcement Learning Features

The agent chooses the action by using a **policy** π.



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Deterministic policy

$a := \pi(s)$

Stochastic policy

$a \sim \pi(a \mid s)$

Imitation Learning and Behavioural Cloning

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Imitation Learning is useful when it is easier for an expert to demonstrate the desired behaviour rather than to specify a reward function which would generate the same behaviour or to directly learn the policy.

The simplest form of imitation learning is Behavioural Cloning, which focuses on learning the expert's policy using supervised learning.

ALVINN:
AN AUTONOMOUS LAND VEHICLE IN A NEURAL NETWORK

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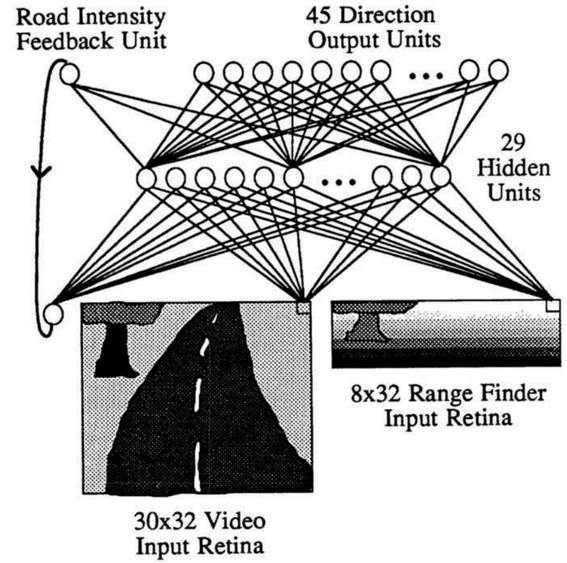

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Behavioral Cloning for Self-driving Cars

1. Collect demonstrations (trajectories τ^*) from expert
2. Treat the demonstrations as i.i.d. state-action pairs: (s_i, a_i)
3. Learn the policy in a supervised mode: $\frac{1}{n}\sum_{i=1}^{n} L(\pi(s_i), a_i) \rightarrow \min_{\pi \in \mathscr{P}}$

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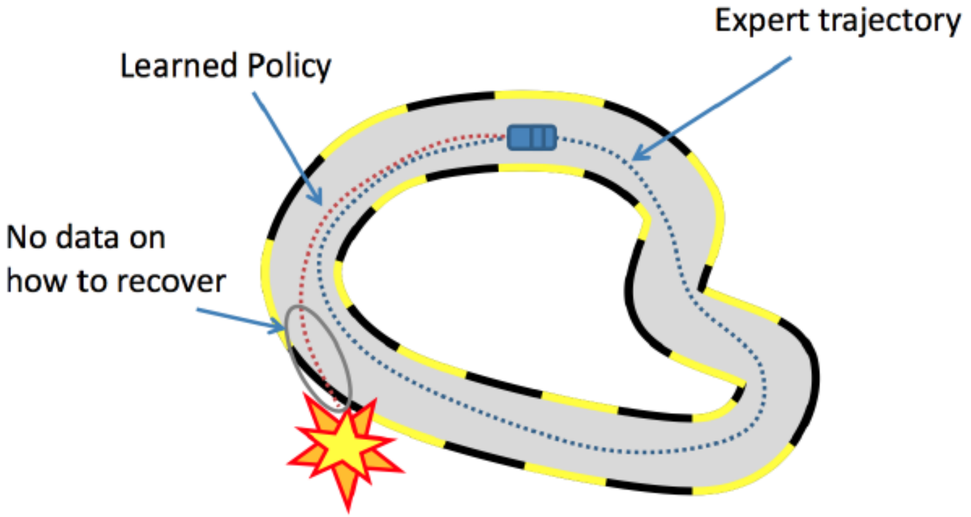
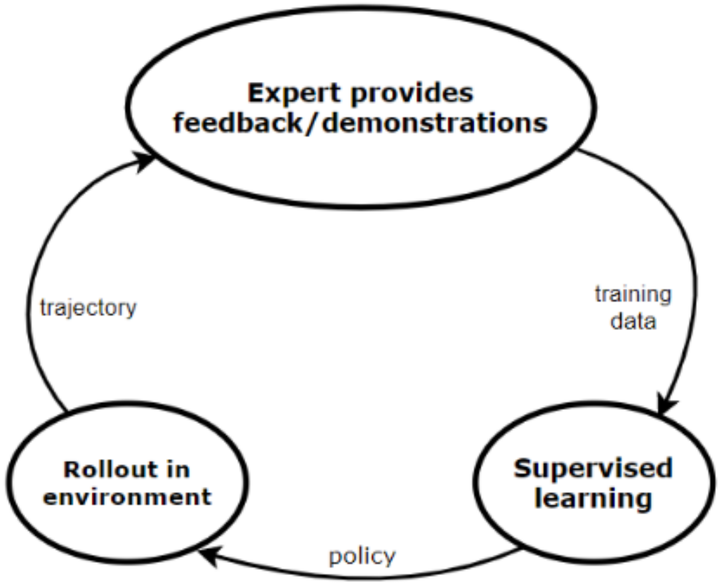


Direct Policy Learning



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Initial predictor: π_0

For $m = 1$:

- Collect trajectories τ by rolling out π_{m-1}
- Estimate state distribution P_m using $s \in \tau$
- Collect interactive feedback $\{\pi^*(s) \mid s \in \tau\}$
- Data Aggregation (e.g. Dagger)
  - Train π_m on $P_1 \cup \ldots \cup P_m$
- Policy Aggregation (e.g. SEARN & SMILe)
  - Train π'_m on P_m
  - $\pi_m = \beta\pi'_m + (1-\beta)\pi_{m-1}$

Source

Demonstration

More Examples

Robotics

- Optimal control

Chess, Go

- AlphaGo
- AlphaZero

Quantitative Finance:

- Market making
- Optimal execution
- Portfolio management

- Healthcare
- Insdustry automation
- Engineering

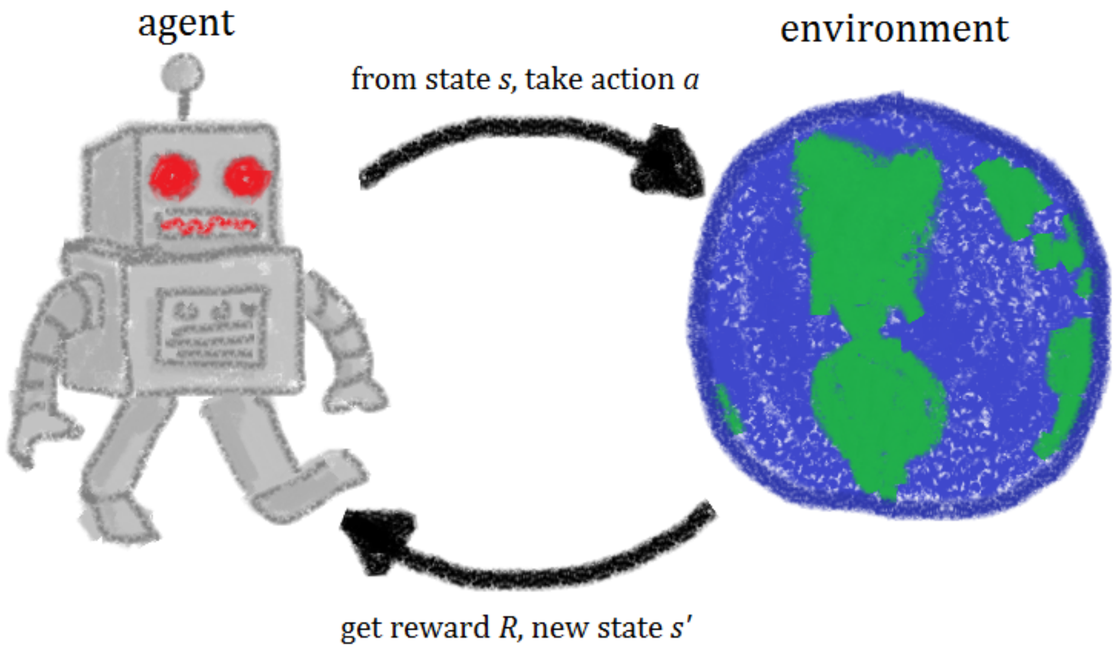
Reinforcement Learning Framework

At each step t the agent:

1. Receives state (observation) s_t (o_t) and reward r_t
2. Executes action a_t

The environment:

1. Receives action a_t
2. Emits state (observation) s_{t+1} (o_{t+1}) and reward r_{t+1}



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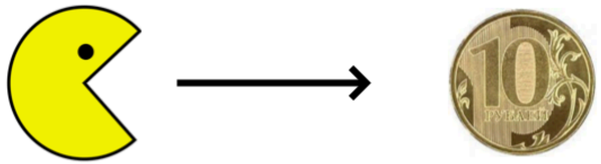
$$\mathbb{E}_{p(\tau|\pi)}\left(\sum_{t=0}^{T} r_t\right) \rightarrow \max_{\pi}$$

Reward Design

… is a tricky task

Discount Factor



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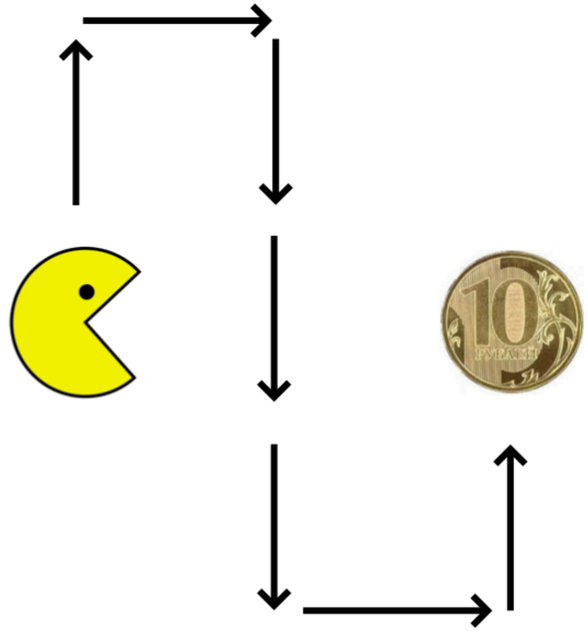

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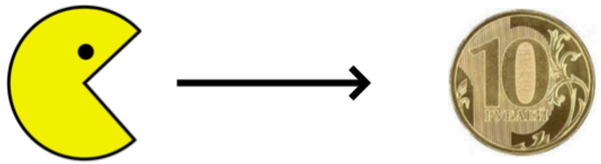
Discount Factor



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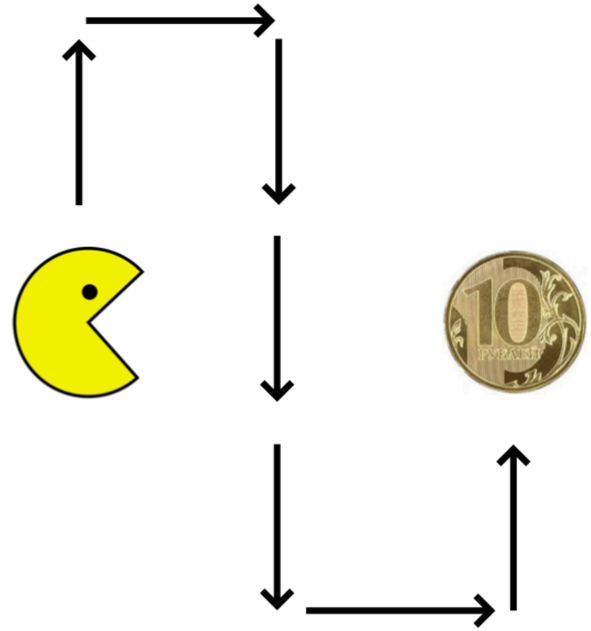

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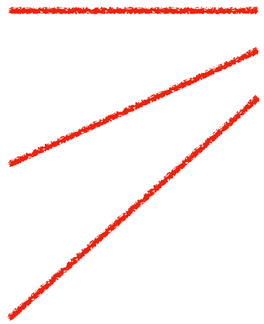
For $\gamma \in [0,1]$ consider $\mathbb{E}_\pi(\sum_{t=0}^{T} \gamma^t r_t) \to \max_\pi$

Reinforcement Learning Formalism

1. $a \in \mathcal{A}$ - action space
2. $s \in \mathcal{S}$ - state space

2*. $o \in \mathcal{O}$ - observation space for partial observable environment

3. $r(s, a) : \mathcal{A} \times \mathcal{S} \to \mathcal{P}(\mathcal{R})$ - reward function
4. $p(r_t, s_{t+1} \mid s_t, a_t)$ - environment dynamics
5. $p(s_0)$ - initial state distribution
6. $\pi(a \mid s) : \mathcal{S} \to \mathcal{P}(\mathcal{A})$ - policy function



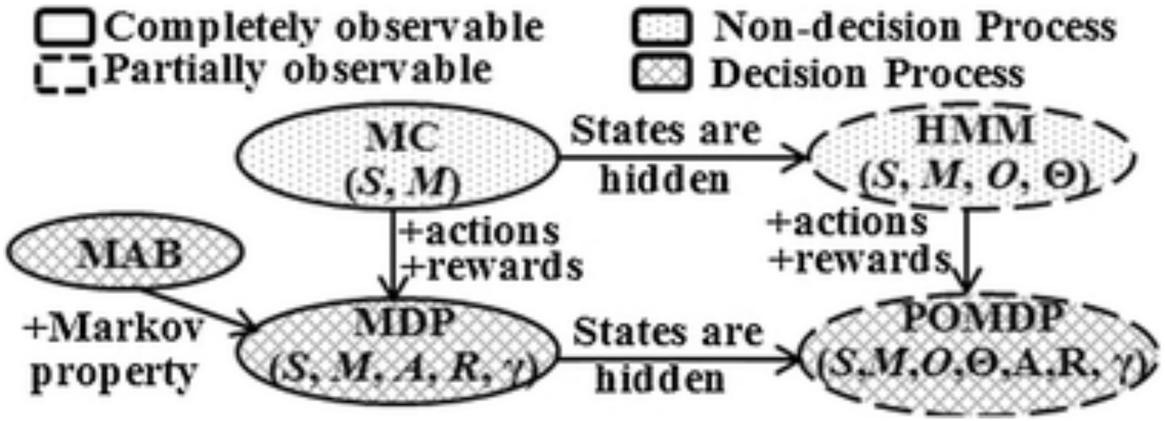
In general, unknown

Would like to find optimal

Markov Decision Process

Markov property:

$$p(r_t, s_{t+1} \mid s_t, a_t, r_{t-1}, s_{t-1}, a_{t-1}, \ldots) = p(r_t, s_{t+1} \mid s_t, a_t)$$



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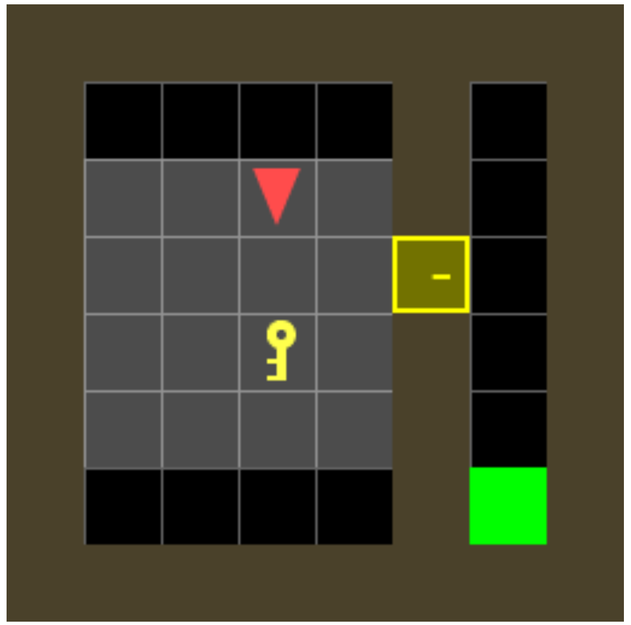
Markov Decision Process

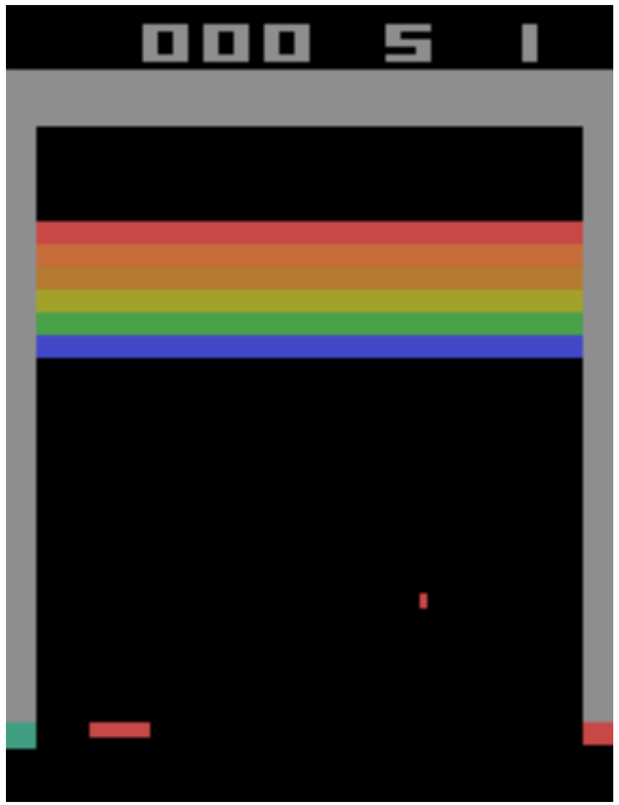
Possible states:

1. Full history
2. Coordinates
3. Coordinates + does the agent have a key
4. Image



Non Markovian Environment

Can you observe ball's direction if only this observation is available?



Reinforcement Learning Problem

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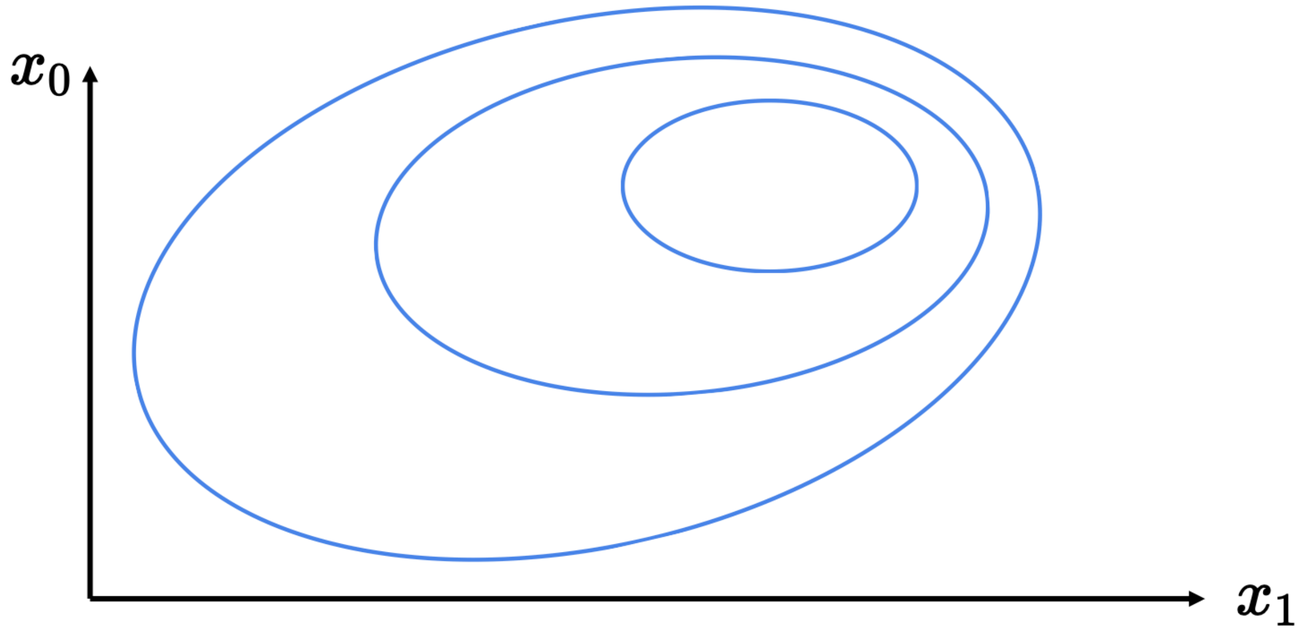
4. $p(r_t, s_{t+1} \mid s_t, a_t)$ - environment dynamics
5. $p(s_0)$ - initial state distribution
6. $\pi(a \mid s) : \mathcal{S} \to \mathcal{P}(\mathcal{A})$ - policy function
7. $\gamma \in [0,1]$ - discount factor
8. T - time horizon, can be infinite

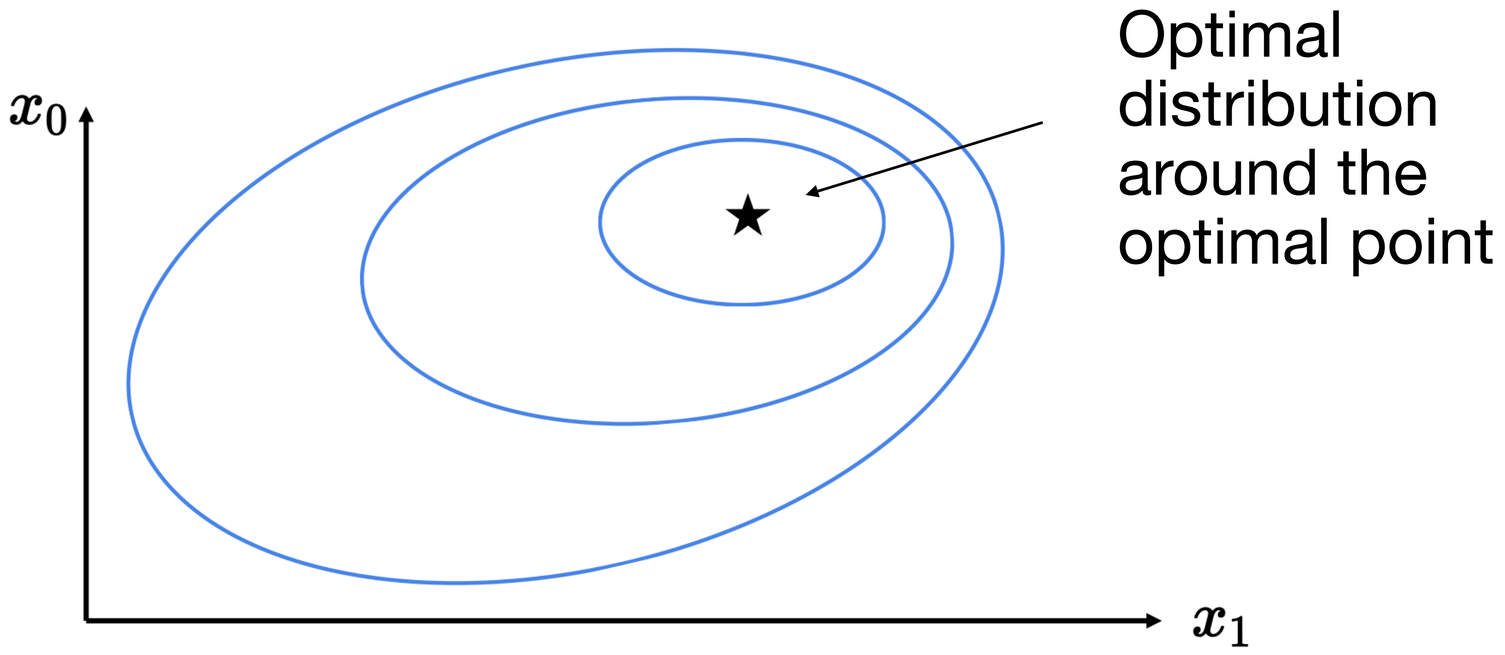
$$J(\pi) = \mathbb{E}_{p(\tau|\pi)}\left(\sum_{t=0}^{T} \gamma^t r_t\right) = \mathbb{E}_{s_0 \sim p(s_0)} \dots \mathbb{E}_{a_t \sim \pi(a|s_t)} \mathbb{E}_{r_T, s_{T+1} \sim p(r, s'|s_t, a_t)}\left(\sum_{t=0}^{T} \gamma^t r_t\right) \to \max_{\pi}$$

Cross-entropy Method

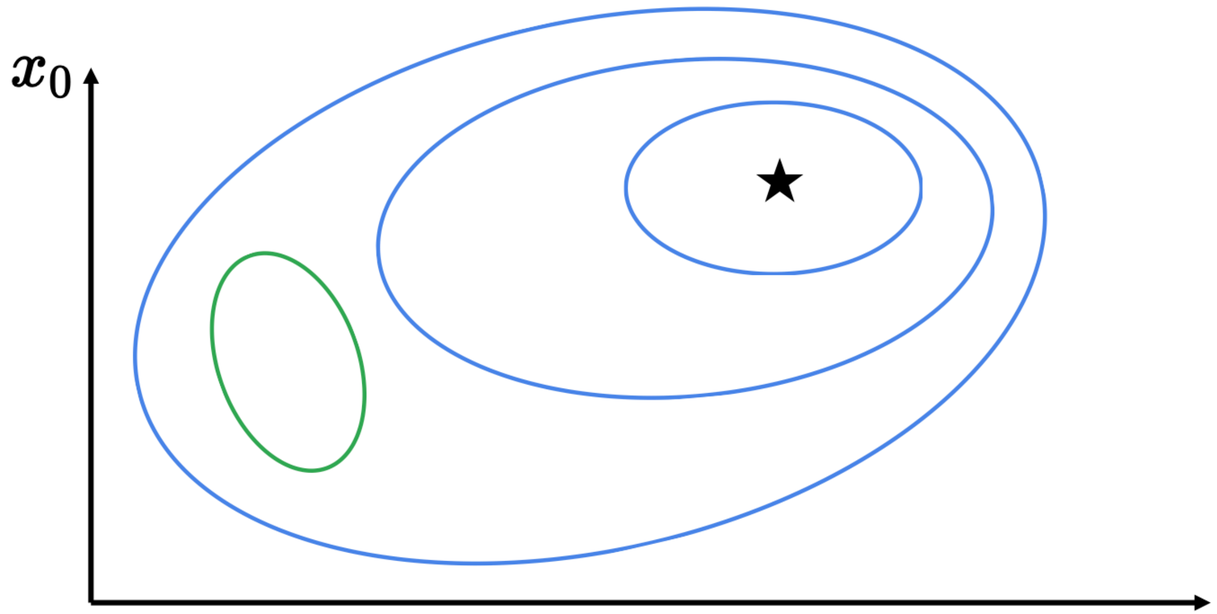
1. Zero-order optimization method
2. Try to find distribution around the optimal point (instead of point itself)



Cross-entropy Method

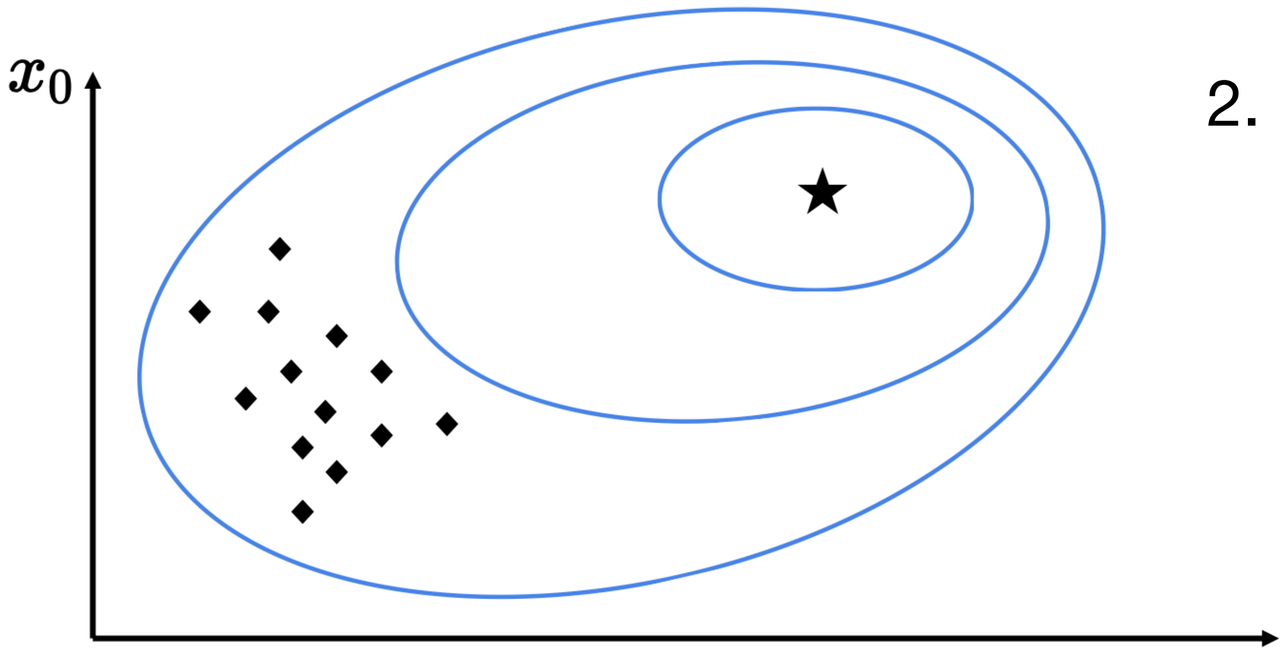


Cross-entropy Method



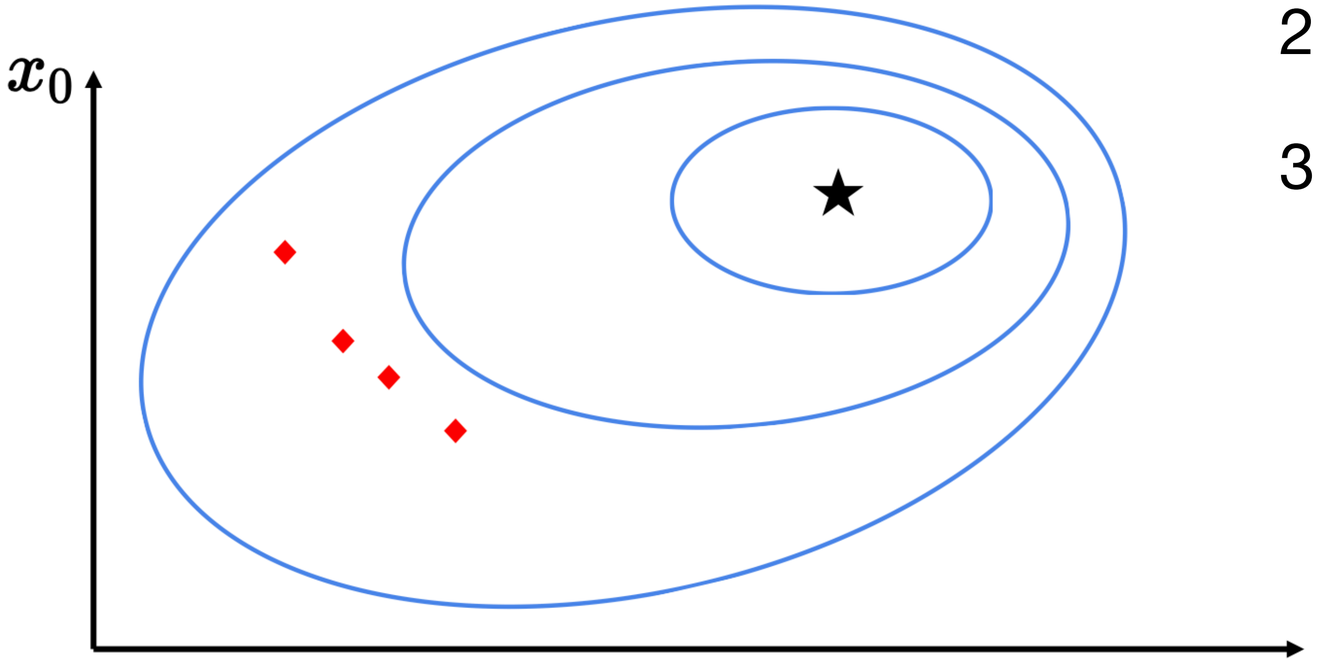
1. Initialise points distribution q_0

Cross-entropy Method



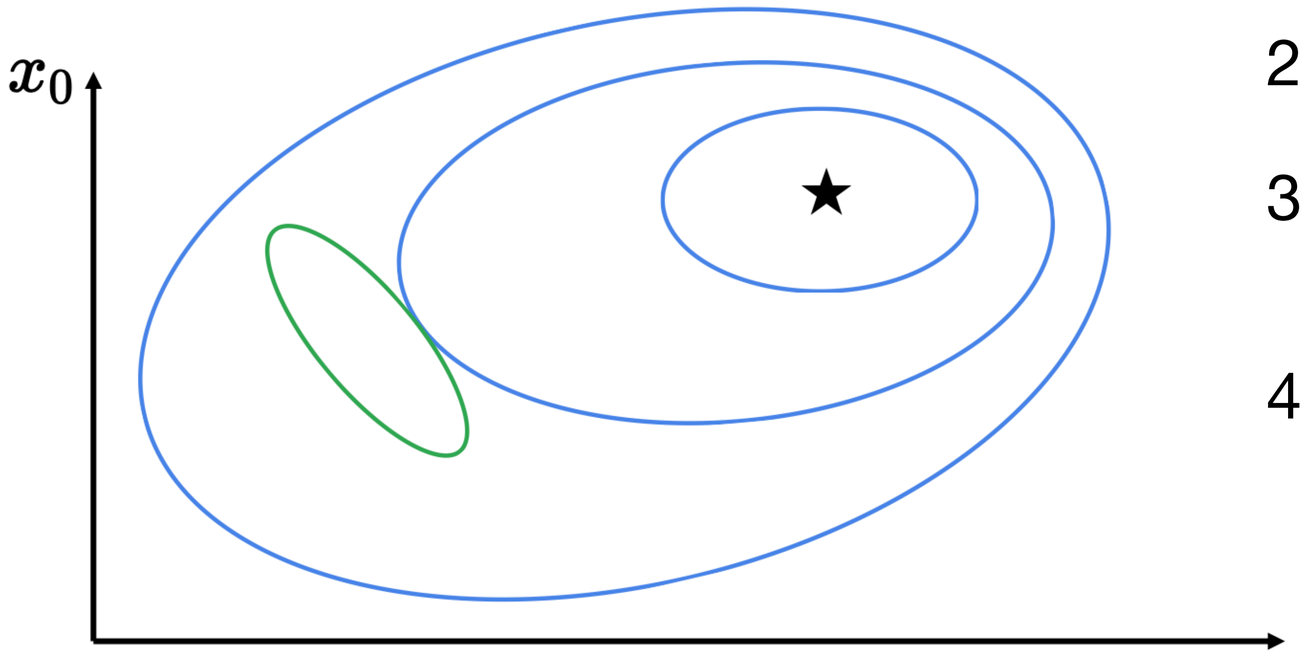
1. Initialise points distribution q_0
2. Sample from $x_i \sim q_0$

Cross-entropy Method



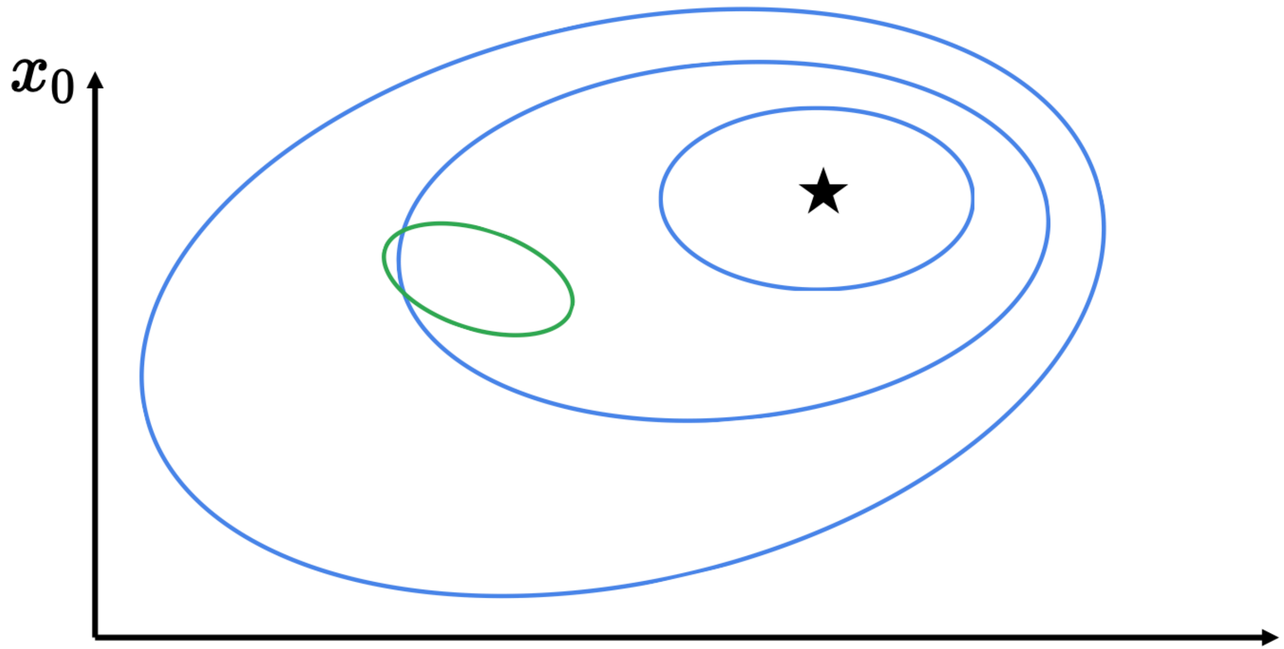
1. Initialise points distribution q_0
2. Sample from $x_i \sim q_0$
3. Select M elite point based on criteria

Cross-entropy Method



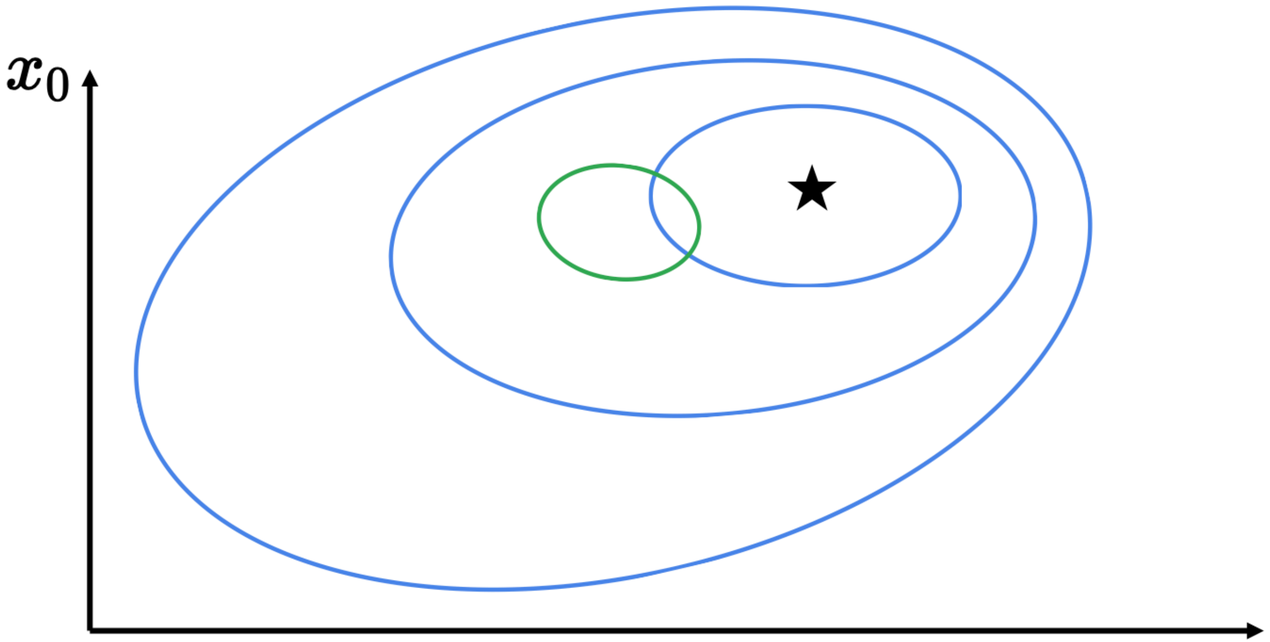
1. Initialise points distribution q_0
2. Sample from $x_i \sim q_0$
3. Select M elite point based on criteria
4. Update to get new distribution q_1

Cross-entropy Method



1. Initialise points distribution q_0
2. Sample from $x_i \sim q_0$
3. Select M elite point based on criteria
4. Update to get new distribution q_1
5. Repeat 2-4 until convergence

Cross-entropy Method



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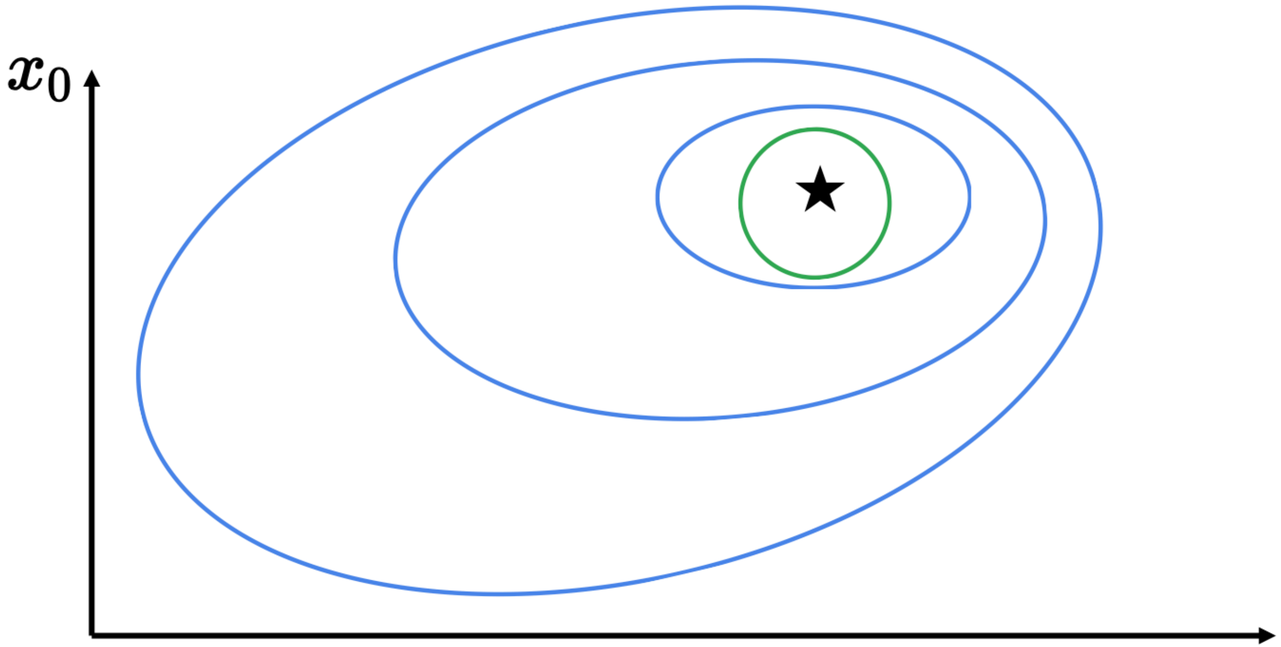
Cross-entropy Method



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Cross-entropy Method

Distribution update:

$$KL(p_{\text{data}}||q) = \mathbb{E}_{p_{\text{data}}} \log(\frac{p_{\text{data}}}{q}) = -\mathbb{E}_{x\sim p_{\text{data}}} \log q(x) \to \min_q$$

Distribution update: $q^{k+1} = \text{argmin}_q[-\frac{1}{|\mathscr{M}^k|}\sum_{x\in\mathscr{M}^k} \log q(x)]$,

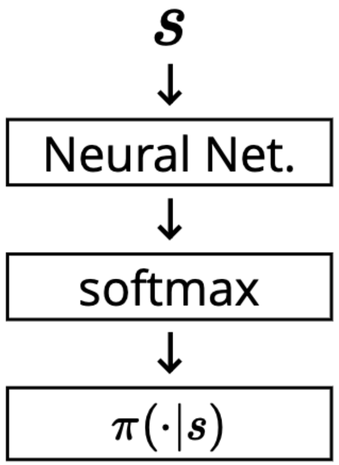
where $\mathscr{M}^k$ is a set of elites points from the k-th iteration

Deep CME for RL

$$J(\pi) = \mathbb{E}_{p(\tau|\pi)}\left(\sum_{t=0}^{T} \gamma^t r_t\right) \to \max_{\pi}$$

Let $\pi = \pi_\theta$ is a neural network

Discrete actions



Continuous actions

Deep CME for RL

$$J(\pi) = \mathbb{E}_{p(\tau|\pi)}\left(\sum_{t=0}^{T} \gamma^t r_t\right) \to \max_{\pi}$$

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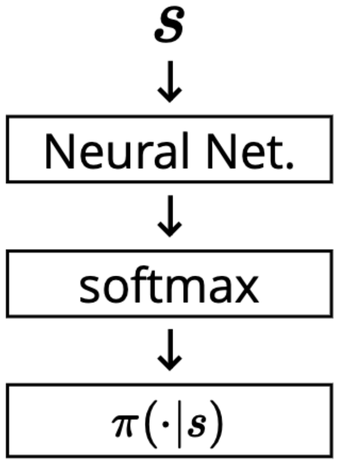
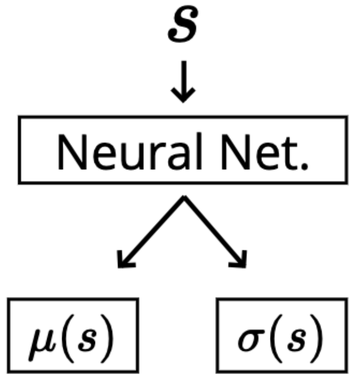
Discrete actions



Continuous actions



Deep CME for RL

1. Input: elite percentile α
2. Initialize $\pi = \pi_\theta$ as a neural network
3. Repeat until convergence:
    1. Run agent π_θ to collect trajectories $\mathcal{T} = \{\tau_i\}$
    2. $\delta =$ percentile$(\mathcal{T}, p = \alpha)$
    3. $\mathcal{M} =$ select_elites$(\mathcal{T}, \delta)$
    4. Partial fit π_θ to predict a_i from s_i, $(a_i, s_i) \in \mathcal{M}$

Bonus

Evolution Strategies as a Scalable Alternative to Reinforcement Learning

Thank you for your attention!