



Description

Evaluation

Предсказание рейтинга фильмов

Вам необходимо реализовать алгоритм implicit ALS для обучения факторизационной машины и применить его для предсказания рейтинга фильмов.

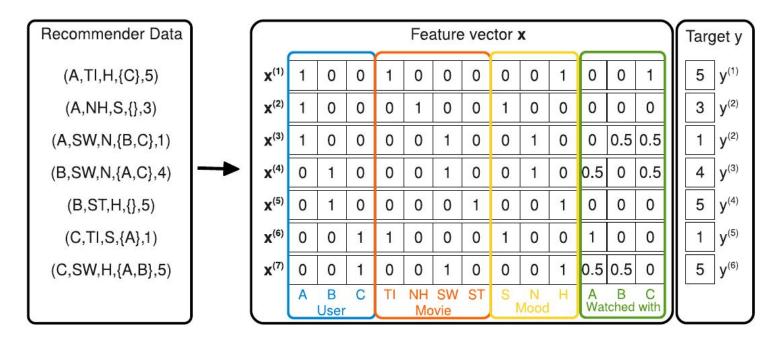


Figure 2: Context-aware recommendation data (left side) is transformed into a prediction problem from real-valued features (right side) by encoding the categorical and set categorical variables (left side) with indicator variables (right side). Here in the feature vector x, the first three values indicate the user, the next four ones the movie, the next three ones the mood and the last three ones the other users a movie has been watched with.

\bigcap	Feature vector x															Tar	get y					
X ⁽¹⁾	1	0	0		1	0	0	0		0.3	0.3	0.3	0		13	0	0	0	0		5	y ⁽¹⁾
X ⁽²⁾	1	0	0		0	1	0	0	200	0.3	0.3	0.3	0		14	1	0	0	0		3	y ⁽²⁾
X ⁽³⁾	1	0	0	3443	0	0	1	0		0.3	0.3	0.3	0		16	0	1	0	0		1	y ⁽²⁾
x ⁽⁴⁾	0	1	0		0	0	1	0		0	0	0.5	0.5		5	0	0	0	0		4	y ⁽³⁾
X ⁽⁵⁾	0	1	0		0	0	0	1		0	0	0.5	0.5		8	0	0	1	0		5	y ⁽⁴⁾
X ⁽⁶⁾	0	0	1	:	1	0	0	0		0.5	0	0.5	0		9	0	0	0	0	3.636	1	y ⁽⁵⁾
X ⁽⁷⁾	0	0	1		0	0	1	0		0.5	0	0.5	0		12	1	0	0	0	, 	5	y ⁽⁶⁾
	A	B Us	C		П	NH	SW Movie	ST		Ott	NH ner M	SW lovie	ST s rate	ed	Time		NH ast	SW Movie	ST e rate	 ed		

Factorization Machines

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Описание модели

Steffen Rendle, Zeno Gantner, Christoph Freudenthaler, and Lars Schmidt-Thieme. 2011. Fast context-aware recommendations with factorization machines.

1) Model Equation: The model equation for a factorization machine of degree d=2 is defined as:

$$\hat{y}(\mathbf{x}) := w_0 + \sum_{i=1}^n w_i \, x_i + \sum_{i=1}^n \sum_{j=i+1}^n \langle \mathbf{v}_i, \mathbf{v}_j \rangle \, x_i \, x_j \quad (1)$$

where the model parameters that have to be estimated are:

$$w_0 \in \mathbb{R}, \quad \mathbf{w} \in \mathbb{R}^n, \quad \mathbf{V} \in \mathbb{R}^{n \times k}$$
 (2)

And $\langle \cdot, \cdot \rangle$ is the dot product of two vectors of size k:

$$\langle \mathbf{v}_i, \mathbf{v}_j \rangle := \sum_{f=1}^k v_{i,f} \cdot v_{j,f}$$
 (3)

A row \mathbf{v}_i within \mathbf{V} describes the *i*-th variable with k factors. $k \in \mathbb{N}_0^+$ is a hyperparameter that defines the dimensionality of the factorization.

A 2-way FM (degree d=2) captures all single and pairwise interactions between variables:

- w_0 is the global bias.
- w_i models the strength of the i-th variable.
- $\hat{w}_{i,j} := \langle \mathbf{v}_i, \mathbf{v}_j \rangle$ models the interaction between the i-th and j-th variable. Instead of using an own model parameter $w_{i,j} \in \mathbb{R}$ for each interaction, the FM models the interaction by factorizing it. We will see later on, that this is the key point which allows high quality parameter estimates of higher-order interactions $(d \geq 2)$ under sparsity.

ALS алгоритм

Steffen Rendle, Zeno Gantner, Christoph Freudenthaler, and Lars Schmidt-Thieme. 2011. Fast context-aware recommendations with factorization machines.

$$h_{(v_{l,f})}(\mathbf{x}) = x_l \sum_{i=1}^n v_{i,f} x_i - x_l^2 v_{l,f}$$

$$= x_l q(\mathbf{x}, f|\Theta) - x_l^2 v_{l,f}$$
(14)
(15)

with

$$q(\mathbf{x}, f|\Theta) := \sum_{i=1}^{n} v_{i,f} x_i \tag{16}$$

$$e(x, y|\Theta^*) = e(x, y|\Theta) + (\theta^* - \theta) h_{(\theta)}(\mathbf{x})$$
 (13)

```
    procedure LearnALS(S)

             w_0 \leftarrow 0
                                                  ▷ Initialize the model parameters
             \mathbf{w} \leftarrow (0, \dots, 0)
             \mathbf{V} \sim \mathcal{N}(0, \sigma)
             for (\mathbf{x}, y) \in S do
                                                                       \triangleright Precompute e and q
                    e(\mathbf{x}, y|\Theta) \leftarrow \hat{y}(\mathbf{x}, y) - y
                    for f \in \{1, ..., k\} do
                           q(\mathbf{x}, f|\Theta) \leftarrow \sum_{i=1}^{n} v_{i,f} x_i
 9:
              end for
10:
11:
                                                                 ▶ Main optimization loop
              repeat
                    w_0^* \leftarrow -\frac{\sum_{(\mathbf{x},y)\in S}(e(\mathbf{x},y|\Theta)-w_0)}{|S|+\lambda_{\ell,\dots,\ell}}
12:
                                                                                         ▷ global bias
                    e(\mathbf{x}, y|\Theta^*) \leftarrow e(\mathbf{x}, y|\Theta) + (w_0^* - w_0)
13:
14:
                    w_0 \leftarrow w_0^*
                    for l \in \{1, ..., n\} do \triangleright 1-way interactions
15:
                          w_l \leftarrow -\frac{\sum_{(\mathbf{x},y) \in S} (e(\mathbf{x},y|\Theta) - w_l x_l) x_l}{\sum_{(\mathbf{x},y) \in S} x_l^2 + \lambda_{(w_l)}}
16:
                           e(\mathbf{x}, y|\Theta^*) \leftarrow e(\mathbf{x}, y|\Theta) + (w_l^* - w_l) x_l
17:
18:
                           w_l \leftarrow w_l^*
                    end for
19:
                    for f \in \{1, \ldots, k\} do
20:

▷ 2-way interactions

21:
                           for l \in \{1, ..., n\} do
                                 v_{l,f}^* \leftarrow -\frac{\sum_{(\mathbf{x},y)\in S} \left(e(\mathbf{x},y|\Theta) - v_{l,f} h_{(v_{l,f})}(\mathbf{x})\right) h_{(v_{l,f})}(\mathbf{x})}{\sum_{(\mathbf{x},y)\in S} h_{(v_{l,f})}^2(\mathbf{x}) + \lambda_{(v_{l,f})}}
22:
                                 e(\mathbf{x}, y|\Theta^*) \leftarrow e(\mathbf{x}, y|\Theta) + (v_{l,f}^* - v_{l,f}) x_l
24:
                                 q(\mathbf{x}, f|\Theta^*) \leftarrow q(\mathbf{x}, f|\Theta) + (v_{l,f}^* - v_{l,f}) x_l
25:
                                  v_{l,f} \leftarrow v_{l,f}^*
26:
                           end for
27:
                    end for
28:
              until stopping criterion is met
              return w_0, \mathbf{w}, \mathbf{V}
30: end procedure
```

Figure 3: Alternating least algorithm that optimizes the model parameters w_0 , w and V for least-square in $O(|S|\overline{m}_{|S|}|k)$ time (see section 4.3.3) where |S| are the number of training examples and $\overline{m}_{|S|}$ the average number of non-zero elements in an input vector x.

Параметры обучения

n_iter 16

latent dimension 5

lambda w 4

lambda v 7

Инициализация весов

w₀- средняя оценка фильма по всей базе

v₀ - [средняя оценка пользователя, средняя оценка фильма,

средняя оценка пользователя, средняя оценка фильма]

V - Xavier Glorot initialization

$$W \sim U \left[-\frac{\sqrt{6}}{\sqrt{n_i + n_{i+1}}}, \frac{\sqrt{6}}{\sqrt{n_i + n_{i+1}}} \right]$$
 (16)

