### SUPPLEMENTARY MATERIAL

### **APPENDICES**

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### Appendix A. Description of agents' state variables

Individuals are described by state variables, presented in Table S1. The first state variable is the 4 total mass (in kilograms) of the individual, divided in two compartments, lean mass and fat mass. Lean mass increases with the growth of the individual while fat mass describes his energy 7 reserves. Two other attributes describe if individuals are alive and how they allocate their energy to growth (depending on the resources they get). Each individual is also characterized by the timing of key life events: cycling, conception, birth, weaning, sexual maturity, death (Fig. 1). These timings are expressed in days, and 0 corresponds to the first day of the simulation. A lifespan is also assigned to each individual and represents their maximal life duration. It can equate the longevity of the species or be lower to account for extrinsic mortality (e.g. predation, disease, infanticide). For foetuses, this attribute represents the gestation duration, either equal to the usual gestation length or lower to account for miscarriages. Individuals can also die before this lifespan is reached if they fail to find enough energy supplies 16 at any point of the simulation. Energetically speaking, we compute the energy balance of each 17 individual who has reached nutritional independence (juvenile or female) by comparing its needs to the available energy. Energy needs represent the amount of energy needed for maintenance, growth and (in adults only) reproduction while available energy is the sum of the energy intake (extracted from the environment) and the energy that can be released from storage. In addition, each female follows a given phenology strategy that remains constant throughout the simulation and which sets the starting point and length of a time window during which she can cycle and conceive. For each reproductive cycle, females are attributed a cycling duration (which can vary) before they conceive. Females are also characterized by their current

- 25 reproductive status: anoestrus, oestrus, gestation or lactation (Fig. 1) which is associated with
- 26 the list of their offspring at each life stage (foetus, infant and juvenile).

### 27 Appendix B. Submodels

#### 28 **1. Death**

- 29 An individual dies if he reaches his assigned lifespan (external mortality causes or natural death)
- or if his lean mass falls beyond a critical threshold (starvation). If a female dies, her current
- 31 foetus or infant dies as well, but juveniles survive because they are independent from their
- 32 mother.

#### 33 1.1 External mortality:

- To account for external mortality causes or natural deaths in females, we used data of observed
- breeding female lifespans in the Amboseli population of yellow baboons (McLean *et al.*, 2019)
- 36 to assign randomly a realistic lifespan value to each adult female at the beginning of each
- simulation (96 values ranging from 2234 days or 6.1 years to 9457 days or 25.9 years). We used
- 38 the same process to account for external mortality (or miscarriage) in the other life stages:
- 39 foetuses, infants and juveniles.
- In the wild, 13.9% of pregnancies result in foetal losses (Beehner et al., 2006). A part of
- 41 those miscarriages, due to bad nutritional conditions, was already taken into account by the
- 42 model (see submodel "Energy allocation"), but we needed to add an external probability of
- 43 miscarriage to account for other causes of miscarriages. Because the actual value is unknown,
- 44 we tried several proportions and chose the one that made the overall miscarriage rate in the
- 45 model fit best the 13.9% observed in the wild. This was obtained for an external proportion of
- 46 miscarriage of 7%. As a result, in the model, 7% of foetus created after a successful conception
- 47 were assigned a lifespan between 1 and 178 days (the average gestation length), meaning that
- 48 they died before being born.

The proportion of infants dying from external causes before weaning was fixed at 54% of the overall mortality, corresponding to the proportion of infants deaths suspected or confirmed to be violent deaths (Alberts, 2019). The overall mortality between birth and weaning in a natural population being of 21.5% (McLean *et al.*, 2019), we estimated the proportion of infants dead from external causes at 11.6%. Consequently, 11.6% of infants were assigned, at birth, a lifespan randomly picked from all infants' lifespans observed in the Amboseli population which were inferior to the average weaning age (116 values ranging from 1 to 319 days). The other infants were assigned a lifespan fixed at yellow baboon longevity (27 years or 9862 days, (Bronikowski *et al.*, 2002)).

Because there were no data on the causes of death for juveniles, we used the same external mortality rate as for infant, assuming that the low infanticide rate in Amboseli, responsible for external deaths of infants but not juveniles, was insufficient to justify a diminishing of the external mortality for juveniles, especially considering that the overall mortality for juveniles (from weaning to sexual maturity) is slightly higher than for infants (McLean *et al.*, 2019). 11.6% of juveniles were therefore also assigned, at weaning, a lifespan randomly picked from all juveniles' lifespans observed in the Amboseli population which corresponded to death after weaning and before sexual maturity (128 values ranging from 329 to 1731 days).

### 1.2 Starvation:

Individuals die from starvation when they take too much energy from their lean mass, after having already used all the available energy in the environment and in their fat reserves. We estimated the critical threshold for lean mass from two different studies. The first one calculates the energy requirement for growth and estimates that healthy tissue is composed at 84% of lean mass (Payne & Waterlow, 1971). The second one is a study on women with anorexia (Scalfi *et al.*, 2002) whose lean mass when malnourished represented 86 % of their lean mass after

- 73 complete recovery. Thus, we estimated in the model that when lean mass falls below 85% of
- 74 its regular value, the individual would die.

### 2. Change of reproductive status

- 76 The female reproductive cycle consists in four successive phases: Oestrus, Gestation, Lactation
- and Anoestrus, each occurring after defined life events: cycling, conception, birth and weaning
- 78 (Fig.1).

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- 79 *2.1 Cycling:*
- 80 There are two conditions for a female to switch from the "anoestrus" to the "oestrus" status.
- First, the current time t must be within the time window defined by the female phenology
- strategy. Second, as showed in Gesquiere et al., 2018, the female needs to have a positive energy
- balance, with an increase in body fat for at least one month. If the female is still cycling when
- the end of the reproductive window is reached, she goes back to "anoestrus".
- 85 2.2 Conception:
- 86 To enter the "gestation" phase, a female has to conceive. Gesquiere et al., 2018 showed that
- duration of cycling until conception is highly variable ( $138 \pm 82$  days, cv = 60%) but insensitive
- 88 to environmental variation. We thus chose in the model to randomly pick this duration from
- observed data in Amboseli (Gesquiere et al., 2018) at the beginning of each oestrus period.
- Once gestation starts, a foetus is created (Table S4) and added to the female "list of foetuses"
- 91 attribute. There is always a single foetus produced (Altmann, 1983).
- 92 *2.3 Birth:*
- 93 Birth occurs after a constant gestation length of 178 days (Gesquiere et al., 2018). The female's
- 94 reproductive status changes then to "lactation", an infant is created using the foetus attributes
- 95 (Table S4) and added to the female "list of infants" attribute.
- 96 *2.4 Weaning:*

Weaning is a continuous process whose beginning and end are difficult to quantify. Cessation of suckling and complete feeding independence is reached at approximately 595 days (85 weeks) of age in yellow baboons (Altmann, 1998). Nevertheless, the observed lactational anoestrus is much shorter, around 322 days (Gesquiere et al., 2018) with resumption of cycling that corresponds to a drop in suckling time (Lee et al., 1991). Moreover, it has been observed in yellow baboons that independence from the mother for nourishment and transportation was almost reached by 365 days of age (Rhine et al., 1985), even if occasional suckling often continues throughout gestation (Lee et al., 1991). To simplify the model, we chose to assume a complete weaning around the age of 46 weeks (322 days), corresponding to the mean postpartum amenorrhea duration in Amboseli (Gesquiere et al., 2018). Nevertheless, it has been shown that weaning is better explained by a threshold mass than a threshold age (Lee, 1996). Because total mass can vary between same-age individuals, this condition allows us to introduce variability in the postpartum amenorrhea duration, as observed in wild population (Gesquiere et al., 2018). We thus calculated the weaning threshold total mass at 2.32 kg (birthMass + ppaDuration x growthRate). After weaning, the infant becomes a juvenile (Table S4) and the mother goes back to the anoestrus status. During gestation or lactation, if the foetus or the infant dies, the female goes back to anoestrus.

### 3. Energy intake

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Females and juveniles feed every day. Food availability is approximated by NDVI, and we assume that saturation occurs for high NDVI values, while for low NDVI values, alternative sources of food, called "fallback foods", (Altmann, 1998; Brockman & van Schaik, 2005) are used. Therefore, we chose to describe energy intake as a saturating function of NDVI (Figure S1) as follows:

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$$E(m,t) = E_{max}(m) \times \left(1 - exp^{-\frac{NDVI(t)}{\tau}}\right) \text{ (Equation 1)}$$

Where  $E_{max}$  is the maximum value of energy intake for a baboon of mass m, when food is non-limiting and  $\tau$  represents the speed at which this value is reached, and therefore the efficiency of fallback foods. The parameter  $\tau$  being unknown, we used it to calibrate our model. Technically, we tried various values until obtaining realistic life history traits in the model outputs (Table 1, main text) and found the value of  $\tau = 0.117$ .

We used a study calculating energy intake for non-reproductive adult female baboons (*Papio cynocephalus* and *Papio anubis*) fed at libitum to estimate  $E_{max}$  at 4891.1 kJ/day (Roberts *et al.*, 1985) for adult females of 11.9 kg (Altmann *et al.*, 1993). Because energy needs increase allometrically (Kleiber, 1932), we chose to reproduce this variation for energy needs, with  $E_{max}$  being a function of mass to the power 0.75 (see submodel "energy needs" for details):

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$$E_{max}(m) = 4891.1 \times \frac{m}{m_{adult}}^{0.75}$$
 (Equation 2)

Similarly, a female's energy needs increase during reproduction, and so does her energy intake. For gestating females, this increase in energy intake is considered through an increase in total mass (Equation 2). For lactating females, Roberts *et al.*, 1985 reported that energy intake increased by 11% at the beginning of lactation with a maximum of 27% at the beginning of weaning. We translated this increase in energy intake through a multiplying coefficient c, varying linearly with infant mass  $m_i$  and therefore with lactation progress (Fig S2). In a first phase, when the infant is completely dependent, c increases from 1.11 at birth to a maximum of 1.27 at beginning of weaning:

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$$c_1\left(m_i\right) = 1.11 + \left(1.27 - 1.11\right) \times \frac{m_i - birthMass}{massAtBeginningOfWeaning - birthMass}$$
(Equation 3)

In a second phase, when the infant starts to become independent, *c* decreases back from 1.27 to a final value of 1 when the infant is completely weaned and lactation stops:

$$c_2 \ (m_i) = 1.27 + (1-1.27) \times \frac{infantMass-massAtBeginningOfWeaning}{weaningMass-massAtBeginningOfWeaning} \ (\text{Equation 4})$$

Moreover, it is reasonable to think that energy extraction efficiency changes with age, increasing rapidly at first and reaching an asymptote at last. We used again the same saturating

function type and obtained a final equation for energy intake, depending on the time t, the mass of the female m, her age a, and the mass of her dependant infant  $m_i$ :

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$$E_{intake}(t, m, a, m_i) = c(m_i) * 4891 \times \left(\frac{m}{m_{adult}}\right)^{0.75} \times \left(1 - exp^{-\frac{NDVI(t)}{\tau}}\right) \times \left(1 - exp^{-\frac{a}{\tau_{age}}}\right)$$

- 149 (Equation 5)
- We chose  $\tau_{age}$  in order to model a realistic offspring survival (Table 1, main text) and fixed it to  $\tau_{age} = 193$  days, giving a foraging efficiency of 81% for a juvenile just weaned (322 days).
- With this final equation, we obtain, for the average NDVI in Amboseli (0.228), a daily energy intake for an adult female at the beginning of lactation of about 4670 kJ. This value is consistent with the average observed value in Amboseli for mixed groups of pregnant females, lactating females and males (4620 kJ/day for a 12kg baboon (Stacey, 1986)).

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### 4. Energy needs

- Energy needs in the model consist in two main components: (i) energy for maintenance and travel ( $E_m$ ), and (ii) energy for growth maintenance ( $E_g$ ). The energy for reproduction can be seen as extra energy for maintenance, travel and growth of the offspring.
- *4.1 Energy for maintenance and travel:* 
  - Altmann & Samuels, 1992 estimated that a 11kg-female baboon alone, in Amboseli, would expend 3493.7 kJ/day for her own maintenance and travel. This value is the result of the sum of the cost of basal metabolism and energy spent for locomotion. The first one follows an allometric relationship to the power 0.75 of body mass (Kleiber, 1932) and the second one to the power 0.684 (Altmann, 1998). To simplify and because these two exponents are close, we chose to use 0.75 as the allometric exponent, which gives the following allometric relationship:

$$E_m(m) = A \times m^{0.75}$$
 (Equation 6)

Based on the 3493.7 kJ/day spent by a 11kg female, we find that  $A = \frac{3493.7}{11^{0.75}} = 578.41$ , and we can re-write equation 6 as follow:

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$$E_m(m) = 578.41 \times m^{0.75}$$
 (Equation 7)

- Where m is the body mass of a female, juvenile or infant. If the female is pregnant, m
- 173 represents her total body mass (including foetus and placenta).
- 174 4.2 Energy for growth:

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Growth in young baboons can be considered as linear with an average growth rate of 5g/day, 176 177 indistinctly for males and females (Altmann & Alberts, 1987). We also assumed a linear growth 178 during gestation, with a growth rate taking into account both foetus and placenta. We estimated the weight of the placenta to be 0.25 times the weight of the foetus (Farley et al., 2009), which 179 gives a growth rate during gestation of  $\frac{1.25 \times birthMass}{gestationLength} = 0.005$  kg/day. This simple calculation 180 shows that growth rate is maintained between gestation and infancy. By simplicity we also kept 181 this growth rate for juveniles (males or females) and adult females even though growth rate 182 starts to increase and differ by sex after 4 years of age (Altmann & Alberts, 1987). 183

With a growth cost of 20.92 kJ/g (Payne & Waterlow, 1971), we can estimate energy needs for growth at all stages of life as:

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$$E_q = 20.92 \times growthRate$$
 (Equation 8)

We give to the individuals the possibility to slow or even pause their growth according to the resources they have, using their "growthAllocation" (gA) attribute, which equals 1 if growth is normal, 0 if growth is stopped and is between 0 and 1 if growth is slowed (see section Energy balance for detail). However, foetuses growth cannot be slowed, because pregnancy length varies very little (Gesquiere  $et\ al.$ , 2018). Except for gestation growth, equation 8 becomes:

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$$E_q(gA) = gA \times 20.92 \times growthRate$$
 (Equation 9)

4.3 Total energy needs:

For juveniles or non-reproductive adult females, total energy needs are the sum of energy needed for maintenance and travel and energy needed for growth:

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$$E_N(m, gA) = E_m(m) + E_g(gA)$$
(Equation 10)

But during gestation and lactation, female energy needs are increased with additional needs for her foetus or infant. During gestation, the female covers all the energy needs of her foetus, and we neglect the costs associated to the energy transfer. Therefore, the total energy needs for a pregnant female, depending on her total mass (including foetus mass) and her growth allocation, are:

$$E_N^{pregnant}(m, gA) = E_m^{pregnant}(m) + E_g^{fem}(gA) + E_g^{foetus}$$
 (Equation 11)

During lactation however, the energy transfer has a cost, due to the production of milk by the mother, and the assimilation of milk by the offspring, which translates into a lactation efficiency of 0.8 (Dewey, 1997). In other words, if the infant needs 1 kJ of energy, the mother would have to give  $\frac{1}{0.8} = 1.25$  kJ to cover such needs. Moreover, weaning being a continuous process, maternal lactation does not cover the full energy needs of an infant during lactation, but a decreasing fraction of it. We consider such decrease to be linear from when the infant reaches 0.99 kg (eighth week of life), that is, when he starts to significantly feed on plant food (Rhine *et al.*, 1985), and until complete weaning at 2.32 kg. Therefore, the total energy needs for a female during lactation are:

$$212 \qquad E_N^{lactating} \left( m, m_i, gA^f, gA^i \right) = E_m(m) + E_g^{fem}(gA^f) + \frac{1}{0.8} \times \alpha \times \left( E_m^{inf}(m_i) + E_g^{inf}(gA^i) \right)$$

213 (Equation 12)

215 where 
$$\alpha = 1$$
 if  $m_i \le 0.99$  and  $\alpha = 1 - \frac{m_i - 0.99}{2.32 - 0.99}$  if  $m_i > 0.99$ 

It should be noted that an infant with a mass over 0.99 kg has to cover a part of his own energy needs. Nevertheless, to simplify the model, we assume, without calculating it, that the infant

succeeds at covering his remaining energetic needs, proportionally to the amount of energy its mother is able to give him (see submodel "Energy allocation" for detail).

### 5. Energy allocation

A flowchart of energy allocation is presented in Figure S3. The first step is to compute the energy balance for the female. Energy balance is the difference between available energy and total energy needs. Energy needs represent the amount of energy needed for maintenance, growth and reproduction (see submodel "Energy needs") while available energy is the sum of the energy intake (extracted from the environment, see submodel "Energy intake") and the energy released from storage. On the one hand, if the energy balance is positive, the female can store the available energy in fat mass. One gram of fat mass contains 39.5 kJ (Livesey & Elia, 1988), but energy storage in the form of fat mass has an efficiency of 0.9 (Rothwell & Stock, 1982). If the female is lactating, she gives half of surplus energy to her infant. Because all ingested energy is not necessarily metabolized, we fixed a maximal daily amount of fat storage equals to the approximate amount of daily fat gain during growth. Baboons gain on average 5g per day of new tissue and have about 2% of fat in their body (Altmann & Alberts, 1987), which gives a maximal daily fat storage of 100 mg. Each day of the simulation, the extra energy that is not stored due to the storage limit is lost.

On the other hand, if the energy balance is negative, the female can reduce or even pause her growth for the day, depending on the amount of energy missing. If still necessary, she can reduce or pause her infant's growth. This decision will reduce the amount of energy needed and could reverse the energy balance. If her energy balance is still negative after these savings steps, the female can try to use the available energy in her fat mass to cover her energetic costs. If after having burnt all her fat mass, her energetic needs are still uncovered, the female has no further choice than to abort if gestating, or abandon the infant if lactating. In both cases, the offspring dies and the female goes back to anoestrus. Finally, the last possibility for the female

if her energy balance is still negative is to burn her lean mass, with 1g of lean mass releasing 20.92 kJ (Payne & Waterlow, 1971). If lean mass falls below a threshold of 85% of its initial value (before the female starts to burn lean mass), the female dies (see "death" submodel for details).

#### 6. Growth

- Once energy is allocated, the female and her potential infant or foetus can grow according to their "growth allocation" attribute. The "growth allocation" attribute can fall below 1 if growth is slowed, or even be null if there is not enough energy for growth, or if the female has reached her final adult size. The total daily body mass increase is therefore:
- $m_{increase} = growthAllocation \times growthRate (kg)$  (Equation 13)
- 253 This daily increase is distributed between lean and fat mass according to the proportions 254 observed in wild baboons (Altmann & Alberts, 1987) and an additional increase in fat mass can 255 exist if the daily energy balance is positive (see submodel "Energy allocation").
- We consider a fully grown female to be 11.9 kg (Altmann *et al.*, 1993), corresponding to a threshold lean mass of 11.6739 kg (adultMass x leanProportion). Yet, if an adult female has lost some of her lean mass because of a dearth of energy, she can grow again to rebuild these tissues. Because juveniles are independent from their mother, we estimate their growth by calculating their own energy balance (energy intake minus energy needs), with the same procedure as for a non-reproductive female.

### Appendix C. Model validation

### 1. Simulated values for key life history traits

We conducted an internal validation by tracking every state variable throughout a simulation in search for any unrealistic value. We then checked the value of some key life history traits calculated from 2000 simulations and compared them to empirical values from the Amboseli wild population. In order to obtain relevant comparisons between simulated and observed

values for each trait, we computed the simulated traits with the calculation methods described in each associated empirical study. Notably, and only in this part of our study, the calculation of the fitness  $\lambda_{ind}$ , was done following methods from McLean *et al.* (2019) and took into account all offspring born, regardless of their subsequent survival (whereas in the rest of our study, we only took into account offspring reaching sexual maturity). Because yellow baboons reproduce year-round in the wild (Campos *et al.*, 2017), we ran this internal validation with females following a non-seasonal phenology strategy.

The values simulated for major key life history traits (mass, fitness, mortality and interbirth interval) were very close to the values observed in the wild (Table S5), which tends to confirm our model's validity. However, the simulated values of body fat and post-partum amenorrhea (PPA) length were not as variable as in the natural population. This could partly be explained by the absence of a social hierarchy in the model, which is known to generate variation in many life history traits. Shorter maternal investment periods have indeed been reported for high-ranking females in several baboon species (Johnson, 2003; Alberts, 2019; Schneider-Crease *et al.*, 2022) and body mass was correlated with dominance rank in female chimpanzees (Pusey *et al.*, 2005). It is also possible that our model does not account precisely enough for the plasticity in offspring growth.

### 2. Comparison of simulated and observed birth seasonality

We evaluated, under realistic conditions, all 133 phenology strategies and subsequently selected the optimal ones by conducting a Student's t-test on their mean fitness distributions. We found a set of 10 best strategies that returned mean fitness values that were not significantly different from the top one (p-value<0.05; Fig. S5). These optimal phenology strategies were only slightly seasonal – as is typically the case of yellow baboons in the wild – with a minimal reproductive time window of 243 days (8 months) and included the non-seasonal phenology strategy.

We then computed the birth seasonality associated with the optimal phenology strategies by calculating the length of the mean vector resulting from all the births from these strategies and compared it to the value observed in the wild (Campos  $et\,al.$ , 2017). Simulated and observed birth distributions are presented in Figure S6. We found that simulated births resulting from pooling all optimal phenology strategies had a seasonality that ranged a little higher (r=0.26) than the one observed in the wild (r=0.15). The mean birth date observed in the wild (10th Nov) occurred 3 months before the one computed from pooled optimal strategies (10th Feb). This slight increase in reproductive seasonality and delay in mean birth date could be due to some structural limitations of the model. For example, NDVI may not reflect exactly the real variation of food abundance experienced by an omnivorous species such as yellow baboons (Altmann, 1998) while the absence of social effects may also contribute to this discrepancy, as reproductive competition can lead to reduced birth seasonality in wild chacma baboons (Dezeure  $et\,al.$ , in press).

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383	

# 384 TABLES

385

# Table S1: Description of the main attributes for each class

Attribute Description			Ow	vner(s)	
	Mass	Foetus	Infant	Juvenile	Female
Total Mass (g)	Total mass of the individual	~	<b>✓</b>	✓	<b>~</b>
Lean Mass (g)	Lean mass of the individual		<b>✓</b>	~	<b>✓</b>
Fat Mass (g)	Fat mass of the individual		~	<b>✓</b>	<b>✓</b>
	Condition	Foetus	Infant	Juvenile	Female
A 1:	False if the individual is dead, true			. 🌶	. 4
Alive	otherwise		•	•	•
	1 if growth is normal, 0 if growth is				
Growth Allocation	stopped and between 0 and 1 if growth		<b>✓</b>	<b>✓</b>	<b>✓</b>
	is slowed.				
	Timings	Foetus	Infant	Juvenile	Female
Cools Time (1)	Day when the first cycle leading to the				
Cycle Time (d)	individual's conception begins		•	•	•
Conception Time	Day when the individual is conceived		<b>✓</b>	•	•
(d)	Bay when the marvidual is conceived	_	•	•	•
Birth Time (d)	Day of birth of the individual		<b>✓</b>	<b>✓</b>	<b>✓</b>
Wassing Time (4)	Day when the individual is fully				<b>~</b>
Weaning Time (d)	weaned			•	•
Sexual Maturity	Day when the individual reaches sexual				
Time (d)	maturity			•	•

Death Time (d)	Death Time (d) Day of death of the individual		<b>~</b>	<b>~</b>	<b>✓</b>
	Life (or gestation) duration of an				
Lifespan (d)	individual (or a foetus) before potential	•	<b>√</b>	•	•
Lifespair (d)	death (or miscarriage) from external	_	•	•	•
	causes				
	Energy	Foetus	Infant	Juvenile	Female
	Energy needed to ensure maintenance,				
Energy needs (kJ)	growth and potential reproduction of			<b>✓</b>	~
	the individual				
Energy intake (kJ)	Energy extracted from the environment			<b>✓</b>	<b>✓</b>
Energy released (kJ)	Energy released from storage (fat mass			.,	•
Lifergy released (R3)	or lean mass)			•	Ť
	Difference between available energy				
Energy balance (kJ)	(energy intake and energy			<b>✓</b>	<b>✓</b>
	released) and energy needs				
	Reproduction	Foetus	Infant	Juvenile	Female
Phenology strategy					
(beginning and	Time window dyning which				
length of	Time window during which				~
reproductive	reproduction is possible				
window) (d)					
List of Foetuses	Record of all 'class Foetus' individuals				.,
List of I octuses	the female has produced				•
List of Infants	Record of all 'class Infant' individuals				.,
List of Illiants	the female has produced				•

List of Juveniles	Record of all 'class Juvenile'	
List of Juvenines	individuals the female has produced	•
Cycling duration (d)	Duration of the ongoing cycling period	<b>✓</b>
	Reproductive status of the female:	
Reproductive status	"anoestrus", "oestrus", "gestation" or	✓
	"lactation"	

## Table S2: Description and values of the main parameters used in the model

See Appendix A for justification and details about how parameters are used in the model.

Parameter	Description	Numerical	Source or	Studied species
		value	equation	
Adult mass	Mean adult female total	11.9 kg	Altmann et	Papio
	mass		al., 1993	cynocephalus
				(wild - Amboseli)
Age at	Age at first significant	56 days	Rhine et al.,	Papio
beginning	consumption of plant		1985	cynocephalus
of weaning	food			(wild - Mikumi)
Age at	Mean age at sexual	1643 days	Charpentier et	Papio
sexual	maturity (first sex skin	(4.5 years)	al., 2008	cynocephalus
maturity	swellings)			(wild - Amboseli)

Birth mass	Mean birth mass	0,710 kg	Altmann &	Papio
			Alberts, 1987	cynocephalus
				(wild - Amboseli)
Body fat	Average duration of the	30 days (1	Gesquiere et	Papio
increase	period of body fat	month)	al., 2018	cynocephalus
duration	increase before cycling			(wild - Amboseli)
Cycling	Vector of observed	Range: 18 -	Gesquiere et	Papio
durations	cycling durations	590 days	al., 2018	cynocephalus
				(wild - Amboseli)
Energy in	Energy released by 1g of	39500	Livesey &	Homo sapiens
fat mass	fat tissue	kJ/kg	Elia, 1988	
Energy in	Energy released by or	20920	Payne &	Mammals
lean mass	needed to create 1g of	kJ/kg	Waterlow,	
	lean tissue		1971	
Female	Vector of observed	Range:	McLean et al.,	Papio
lifespans	lifespans for breeding	2234 - 9457	2019	cynocephalus
	females	days		(wild - Amboseli)
Gestation	Mean gestation length	178 days	Gesquiere et	Papio
length			al., 2018	cynocephalus
				(wild - Amboseli)

Growth rate	Mean weight gain by day	0.005	Altmann &	Papio
	during growth	kg/day	Alberts, 1987	cynocephalus
				(wild - Amboseli)
Infant	Proportion of infants dead	0.1161	Alberts, 2019;	Papio
proportion	from external causes		McLean et al.,	cynocephalus
of external			2019	(wild - Amboseli)
deaths				
Infant	Vector of observed	Range: 1 -	McLean et al.,	Papio
lifespans	lifespans for infants that	319 days	2019	cynocephalus
	died before weaning			(wild - Amboseli)
Juvenile	Vector of observed	Range: 329	McLean et al.,	Papio
lifespans	lifespans for juvenile that	- 1731 days	2019	cynocephalus
	died between weaning			(wild - Amboseli)
	and sexual maturity			
Lactation	Efficiency of milk	0.8	Dewey, 1997	Homo sapiens
efficiency	synthesis			
Lean	Mean lean mass	0.981	Altmann et	Papio
proportion	proportion (of total mass)		al., 1993	cynocephalus
				(wild - Amboseli)
Longevity	Age of the oldest female	9862 days	Bronikowski	Papio
	reported at Amboseli	(27 years)	et al., 2002	cynocephalus
				(wild - Amboseli)

Mass at	Estimated mass at	0.99 kg	= birthMass +	
beginning	beginning of weaning		growthRate×	
of weaning			ageAtBeginni	
			ngOfWeaning	
N/	A	0.475.1	1' 4134	
Mass at	Approximate mean total	9.475 kg	= birthMass +	
Sexual	mass at sexual maturity		growthRate×	
Maturity			ageAtSexual	
			Maturity	
Maximal	Maximal amount of fat	0.0001 kg	growthRate×	
		0.0001 kg		
daily fat	that can be stored each		(1-	
storage	day		leanProportio	
			n)	
Maximal	Maximal daily energy	4891.1	Roberts et al.,	Papio
energy	intake for a female	kJ/day	1985	cynocephalus and
		K3/ddy	1703	
intake	baboon fed <i>ad libitum</i>			Papio anubis
				(captive)
Maximal	Ratio of minimum lean	0.85	Payne &	Mammals and
reduction of	mass causing death and		Waterlow,	Homo sapiens
lean mass	regular lean mass		1971; Scalfi <i>et</i>	
			al., 2002	
NDVI	Vector of NDVI	Range: 0.13	Didan, 2015	
	(Normalized Difference	- 0.42		

	Vegetation Index) values			
	in Amboseli (2000-2021)			
Placental	Placenta mass expressed	0.25	Farley et al.,	Papio spp.
proportion	as a proportion of foetus		2009	(captive)
	mass			
PPA	Mean postpartum	322 day	Gesquiere et	Papio
duration	amenorrhea duration		al., 2018	cynocephalus
				(wild - Amboseli)
Storage	Efficiency of energy	0.9	Rothwell &	Rattus norvegicus
efficiency	storage as fat mass		Stock, 1982	(Zucker rat -
				captive)
Weaning	Estimated threshold mass	2.32 kg	= birthMass +	
mass	at complete weaning		growthRate×	
			ppaDuration	

390

## Table S3: Initial attributes for the female at the beginning of simulation (t=0)

Unknown timings are given the value -999. Mass at sexual maturity, lean proportion and age at
 sexual maturity are given in Table 2.

Attribute	Initial value Comments
	Mass
Total Mass (g)	massAtSexualMaturity = 8.925 kg

Lean Mass (g)	massAtSexualMaturity×leanProportion = 8.755 kg				
Fat Mass (g)	massAtSexualMaturity×(1-leanProportion) = 0.170 l				
Condition					
Alive	true				
Growth Allocation	1				
Timings					
Cycle Time (d)	-999				
Conception Time (d)	-999				
Birth Time (d)	-1643 = - ageAtSexualMaturity				
Weaning Time (d)	-999				
Sexual Maturity Time (d)	0				
Death Time (d)	-999				
Lifespan (d)	Randomly picked from McLean et al., 2019				
	Energy				
Energy needs (kJ)	0				
Energy intake (kJ)	0				
Energy released (kJ)	0				
Energy balance (kJ)	0				
	Reproduction				
Phenology strategy	Picked from the 133 different phenology strategies				
(beginning and length of	considered (see main text)				
reproductive window) (d)	considered (see main text)				
List of Foetuses	empty list				
List of Infants	empty list				
List of Juveniles	empty list				

Cycling duration (d)	0
Reproductive status	anoestrus

### Table S4: Initial attributes for offspring (foetus, infant and juvenile)

The values given correspond to transitional events (conception, birth and weaning), where new individuals from associated classes (foetus, infant and juvenile) are created. A foetus is created from scratch at conception ( $t=t_c$ ), but each infant is created from a foetus that has reached the end of gestation ( $t=t_b$ ) and each juvenile is created from an infant that has reached the total weaning mass threshold ( $t=t_w$ ). In the case where an individual is created from another one, it can take (inherit) some of its attribute values. Lean proportion is given in Table 2. See details for the "lifespan" attribute in the "death" submodel.

	Initial value					
Attribute	Foetus	Infant	Juvenile			
	(at conception: t=t <sub>c</sub> )	(at birth: t=t <sub>b</sub> )	(at weaning: t=t <sub>w</sub> )			
Mass						
Total Mass (g)	0	Inherited from foetus	Inherited from infant			
Lean Mass (g)		totalMass x leanProportion	Inherited from infant			
Fat Mass (g)		totalMass x (1-leanProportion)	Inherited from infant			
State						
Alive	true	Inherited from foetus	Inherited from infant			
Growth Allocation		1	Inherited from infant			

Timings					
Cycle Time (d)	Female's last beginning of cycle	Inherited from foetus	Inherited from infant		
Conception Time (d)	$t_{\rm c}$	Inherited from foetus	Inherited from infant		
Birth Time (d)		$t_b$	Inherited from infant		
Weaning Time (d)			$t_{\rm w}$		
Menarche Time (d)			-999		
Death Time (d)	-999	Inherited from foetus	Inherited from infant		
Lifespan (d)	179 (gestationLength +1) or randomly picked between 1 and gestation length		Longevity or randomly picked from (McLean et al., 2019)		
Energy					
Energy needs (kJ)			0		
Energy intake (kJ)			0		
Energy released (kJ)			0		
Energy balance (kJ)			0		

Table S5: Comparison between simulated and observed data for key life history traits

Mean value and standard deviation (mean  $\pm$  sd) for simulated life history traits were obtained from 2000 simulations following the non-seasonal phenology strategy (reproduction was not

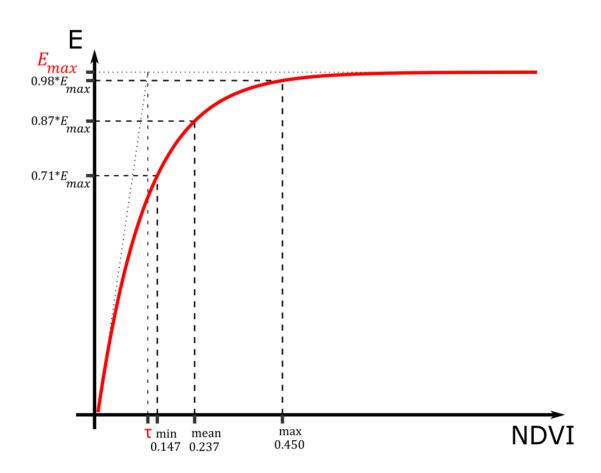
constrained in time). The simulations were run using the NDVI extracted from Amboseli geological coordinates.

Life history trait	Observed data	Simulated data	Source
	$(mean \pm sd)$	(mean ± sd)	
Fitness (λ <sub>ind</sub> )	$1.09 \pm 0.08$	$1.09 \pm 0.09$	McLean et al., 2019
Lifetime reproductive	$5.61 \pm 3.21$ infants	$5.76 \pm 3.16$ infants	McLean et al., 2019
success			
Age at death	$14.75 \pm 5.42$ years	$14.72 \pm 5.42$ years	McLean et al., 2019
Foetus Loss	13.9%	13.2%	Beehner et al., 2006
Infant Loss (before	21.5%	22.0%	Calculated from
weaning)			McLean et al., 2019
Offspring Loss	45.3%	45.0%	Calculated from
(between birth and			McLean et al., 2019
sexual maturity)			
Mean total mass	11.9 ± 1.41 kg	$11.57 \pm 0.32 \text{ kg}$	Altmann et al., 1993
Mean fat percent	$1.9 \pm 4.81$	$2.2 \pm 0.56$	Altmann et al., 1993
Interbirth interval	638 ± 116 days	637 ± 83 days	Gesquiere et al., 2018
duration			
Postpartum	322 ± 87 days	323 ± 17 days	Gesquiere et al., 2018
amenorrhea duration			
Cycling duration	138 ± 82 days	$135 \pm 80 \text{ days}$	Gesquiere et al., 2018
Gestation duration	178 ± 6 days	178 ± 0 days	Gesquiere et al., 2018

## **FIGURES**

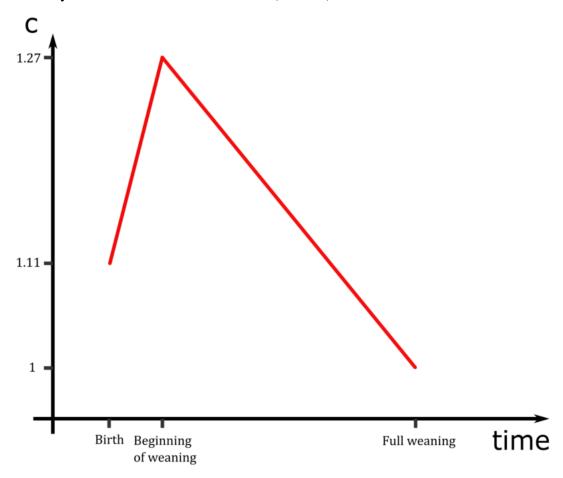
### Figure S1: Variation of energy intake with NDVI

 $E_{max}$  represents the maximum amount of energy an individual can get daily when food is non-limiting. For low values of NDVI, the energy intake associated increases rapidly, simulating the effect of "fallback food". The values of minimal, mean and maximal NDVI are given for the Amboseli national Park, and their associated energy intake are given as proportion of  $E_{max}$ .



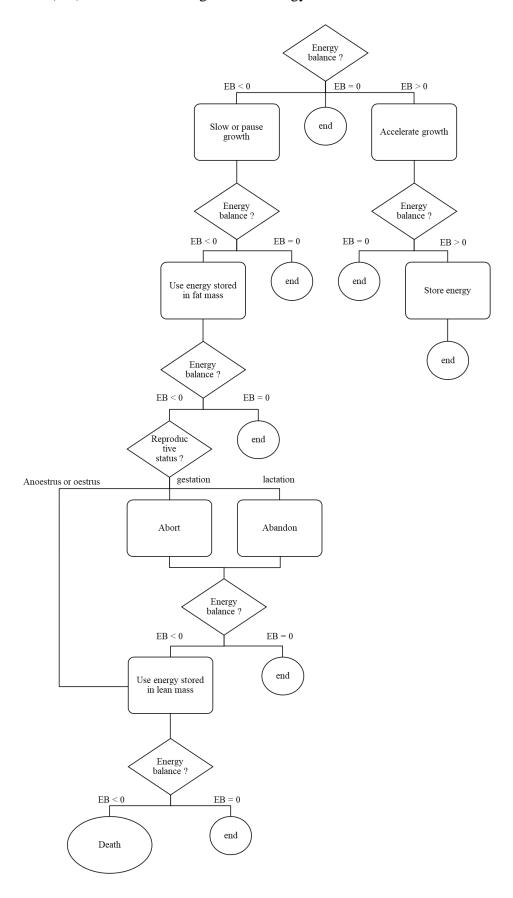
## Figure S2: Multiplying coefficient for energy intake during lactation (C)

During lactation, energy intake is increased by a factor of 1.11 at birth, 1.27 at beginning of weaning and goes back to normal at the end of weaning. Weaning beginning and end are defined by threshold masses for the infant (Table 2).



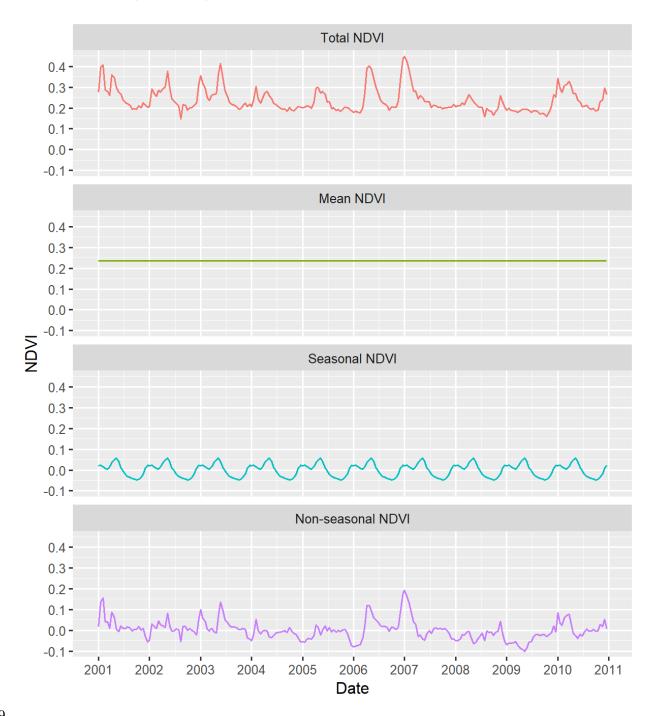
## 421 Figure S3: Flowchart of energy allocation

Energy balance (EB) is evaluated throughout the energy allocation decision tree.



### Figure S4: NDVI time series decomposition

The NDVI values were extracted according to the Amboseli geographical coordinates, and we only show ten years of data, from January 1<sup>st</sup>, 2001 to December 31<sup>st</sup>, 2010 for clarity purposes. Raw NDVI is plotted in the top panel, and is equal to the sum of the values plotted in the other three panels: the mean NDVI (K), the seasonal NDVI (NDVI\_S) and the non-seasonal NDVI (NDVI\_NS).



# Figure S5: Comparison of the fitness distributions associated with different phenology strategies in realistic conditions

Each violin plot represents the distribution of fitness (individual population growth rate) resulting from 2000 simulations of the life cycle of a female following a specific phenology strategy. Environment and life history correspond to the realistic conditions in Amboseli. Phenology strategies are described by a time window with a specific start (day of year) and a specific length (in days) when the female is allowed to conceive. Strategies are ordered by decreasing mean fitness. For clarity reasons, we represented in this figure only nine phenology strategies picked regularly from the best one (associated with the highest mean fitness) to the worst one (associated with the lowest mean fitness). We also added the non-seasonal phenology strategy (i.e. a strategy where the female can conceive all year). We performed a Student's test to compare the mean fitness value between the best strategy and the other ones (NS: non-significant; \*: p-value<0.05; \*\*: p-value<0.01; \*\*\*: p-value<0.001).

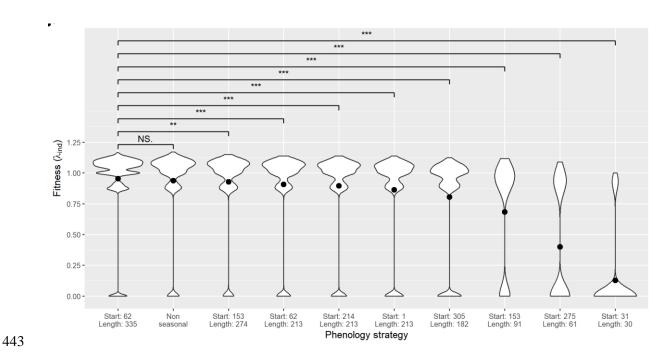


Figure S6: Comparison of birth phenology

Each circular box plot represents the monthly distribution of births and the red segment is the mean vector of births. Its direction,  $\mu$ , gives the mean date of birth while its length, r, quantifies

the seasonality of births (r=0 means that births are equally distributed and r=1 means that all births occur on the same day). The left panel shows the distribution of simulated births resulting from all the optimal phenology strategies (whose mean fitness were not significantly different). The right panel shows the real births distribution observed in the wild in Amboseli (Campos *et al.*, 2017).

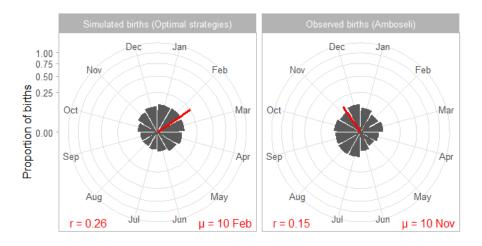
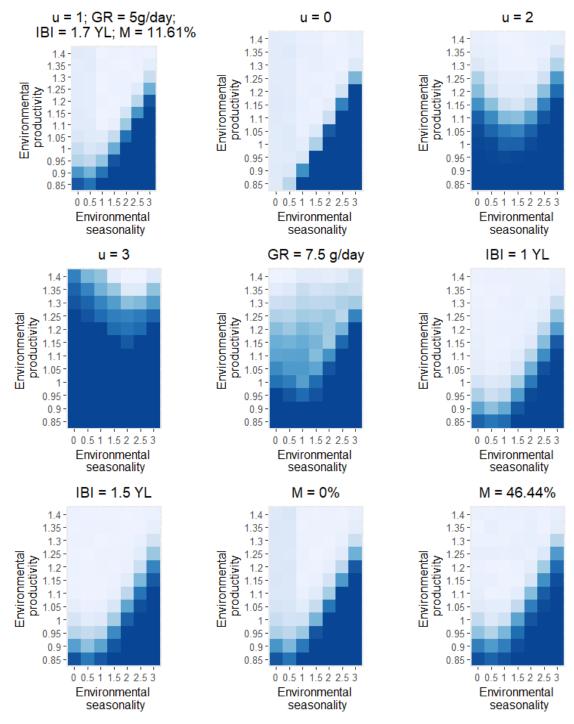


Figure S7: Variation of mean individual fitness

We plotted heatmaps of mean individual fitness ( $\lambda_{ind}$ ) along gradients of environmental productivity and seasonality and with the different values we tested in this study for the four other factors: environmental unpredictability (u), daily energy expenditure (growth rate GR), reproductive cycle length (interbirth interval IBI as a function of year length YL) and infant extrinsic mortality rate (M). The top left panel represents the real conditions for these four factors, as observed in Amboseli.





# Figure S8: Effect of reproductive cycle length and infant mortality on birth seasonality (H5 and H6)

In panel A, we plotted heatmaps of birth seasonality in function of environmental seasonality and productivity in three different conditions of reproductive cycle length: when the interbirth interval (IBI) equals exactly the year length (YL), when its length is 1.5 years, and in normal conditions, when it is 1.7 years long. In panel B, we plotted heatmaps of birth seasonality with varying environmental seasonality and productivity in three different conditions of infant extrinsic mortality: with no infant extrinsic mortality, with a regular infant extrinsic mortality of 11.61% and with a four-time amplified mortality of 46.44%.

