

Priority Queue

- ADT: Abstract data type
- A queue where each object has an associated priority attached
- Operation
 - Insert: with a priority value
 - Remove: max/min
 - Get/Peek: max/min value

Can be implemented using simple sorted array, heap or using balanced BSTs

simple sorted array

- Insert $O(N)$
- Remove $O(1)$
- Peek: Min/max $O(1)$

HEAP

- Insert $O(\log N)$
- Remove $O(\log N)$
- Peek $O(1)$

Balanced BSTs

- Insert $O(\log N)$
- Remove $O(\log N)$
- Peek $O(\log N)$

Practically Heap is the preferred implementation over BST as Heap uses an array which gives better locality of reference (caching) Hence better practical performance even though complexity is same.

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Priority Queue in different languages

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Python

- min heap by default

```
In [10]: 1 import heapq
2 h = [10,4,3,1,7]
3
4 heapq.heapify(h) #  $O(N \log N)$ 
5 print(h)
6
7 print(h[0])
8
9 heapq.heappop(h)
10 print(h)
11
12 heapq.heappush(h, 2)
13
14 print(h)
15
```

[1, 4, 3, 10, 7]

1

[3, 4, 7, 10]

[2, 3, 7, 10, 4]

Strings and heap

```
In [13]: 1
2 h = ["d", "c", "a", "b"]
3 heapq.heapify(h)
4 print(h)
5
6 print(heapq.heappop(h))
7 print(h)
```

['a', 'b', 'd', 'c']

a

['b', 'c', 'd']

```
In [ ]: 1
```

Custom Objects and Heap

```
In [15]: 1 # min heap example using age for priority
2 class Person:
3     def __init__(self, name, age):
4         self.name = name
5         self.age = age
6
7     def __lt__(self, other): # Less than
8         return self.age < other.age
9
10    def __str__(self):
11        return f"({self.name}, {self.age})"
12
13    def __repr__(self):
14        return self.__str__()
15
16 h = [Person("B", 10), Person("P", 13), Person("A", 19), Person("C", 15), Person("D", 11)]
17 heapq.heapify(h)
18
19 print(h)
```

```
[(B, 10), (D, 11), (A, 19), (C, 15), (P, 13)]
```

```
In [ ]: 1
```

Python heap as max heap

```
In [16]: 1 # max heap example using age for priority
2 class Person:
3     def __init__(self, name, age):
4         self.name = name
5         self.age = age
6
7     def __lt__(self, other): # Less than
8         return self.age > other.age
9
10    def __str__(self):
11        return f"({self.name}, {self.age})"
12
13    def __repr__(self):
14        return self.__str__()
15
16 h = [Person("B", 10), Person("P", 13), Person("A", 19), Person("C", 15), Person("D", 11)]
17 heapq.heapify(h)
18
19 print(h)
```

```
[(A, 19), (C, 15), (B, 10), (P, 13), (D, 11)]
```

```
In [17]: 1 # min heap example using name for priority
2 class Person:
3     def __init__(self, name, age):
4         self.name = name
5         self.age = age
6
7     def __lt__(self, other): # Less than
8         return self.name < other.name
9
10    def __str__(self):
11        return f"({self.name}, {self.age})"
12
13    def __repr__(self):
14        return self.__str__()
15
16 h = [Person("B", 10), Person("P", 13), Person("A", 19), Person("C", 15), Person("D", 11)]
17 heapq.heapify(h)
18
19 print(h)
```

```
[(A, 19), (C, 15), (B, 10), (P, 13), (D, 11)]
```

```
In [ ]:
```

```
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```

JAVA

default min heap

```
PriorityQueue<Integer> pq=new PriorityQueue<>();

for(int i=5; i>= 1;i--)
{
    pq.add(i);
}

while(!pq.isEmpty())
{
    System.out.println(pq.poll());
}
```

default min heap

```
int data[]={1,2,3,5,4};

PriorityQueue<Integer> pq=new PriorityQueue<>();

// copy data
for(int i=0;i< data.length;i++)
{
    pq.add(data[i]);
}

while(!pq.isEmpty())
{
    System.out.println(pq.poll());
}
```

max heap using comparator

```
int data[]={1,2,3,5,4};

PriorityQueue<Integer> pq=new PriorityQueue<Integer>((o1,o2)-> o
2-o1);
for(int i=0;i< data.length;i++)
```

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C++

```
#include <iostream>
#include <queue>
using namespace std;

int main()
{
    int arr[]={1,2,3,4,5};

    priority_queue<int> pq(arr, arr+5);
    cout<<"Max priority queue: ";
    while(!pq.empty()){
        cout<<pq.top()<<endl;
        pq.pop();
    }

    priority_queue <int, vector<int>, greater<int> > pq1(arr,arr+5);
    cout<<"Min priority queue: ";
    while(!pq1.empty()){
        cout<<pq1.top()<<endl;
        pq1.pop();
    }

}
```

C#

min heap

```
PriorityQueue<string, int> queue = new PriorityQueue<string, int>();
queue.Enqueue("Item A", 1);
queue.Enqueue("Item B", 2);
queue.Enqueue("Item C", 3);
queue.Enqueue("Item D", 5);
queue.Enqueue("Item E", 4);

while (queue.TryDequeue(out string item, out int priority))
{
    Console.WriteLine($"Popped Item : {item}. Priority Was : {priority}");
}
```

Javascript

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- heapify -> convert a sequence/array to satisfy heap property: $O(N)$
- heappop: assumes data is in heap format/heapified: $O(\log N)$
- heappush: assumes data is in heap format/heapified: $O(\log N)$
- peek: $O(1)$

In []:

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Question: Kth largest/smallest element

<https://leetcode.com/problems/kth-largest-element-in-an-array/>
(<https://leetcode.com/problems/kth-largest-element-in-an-array/>).

Solution-1:

Sort
 Get N-k index element
 TC: $O(n \log n)$
 SC: $O(1)$

Solution-2:

All data in max heap
 Heap pop k times
 TC: $O(N \log N) + O(K \log N)$
 SC: $O(N)$

Solution-3:

Maintain a min heap of k elements: $O(K \log K)$
 Loop over the remaining elements: if `heap.min() < curr` : replace
 $O((N-K) \log K)$
 Get `heap.min()` -> kth largest element $O(1)$
 TC: $O(k \log k) + O((n-k) \log K) + O(1) \Rightarrow O(n \log k)$
 SC: $O(k)$

Solution-4: BST

Put all data in bst
 Reverse Inorder traversal to get Kth element
 TC: $O(n \log n)$
 SC: $O(N)$

Solution-5:

Count: Count frequency of each number [3, 2, 1, 1, 4, 5, 3] ->
 1:2 2:1 3:2 4:1 5:1 [1,1,2,3,3,4,5] -> $O(N)$
 Bucket: 10,11,21,20,45,42,15 : [0-9]:[] [10-19]:[10,11,15] [20-29]:[20,21] [30-39]:[] [40-49]:[42,45]

Solution-6:

Quick sort based solution
 Avg: $O(N)$
 Worst: $O(N^2)$

Java: Heap solution


```

class Solution {
    public int findKthLargest(int[] nums, int k) {
        PriorityQueue<Integer> pq = new PriorityQueue<>();

        for(int i = 0 ; i < nums.length; i++){

class Solution {
public:
    int findKthLargest(vector<int>& nums, int k) {
        priority_queue<int,vector<int>,greater<int>> q(nums.begin(),nu
ms.begin()+k);
        for(int i=k;i<nums.size();i++)
        {
            if(q.top()<nums[i])
            {
                q.pop();
                q.push(nums[i]);
            }
        }
        return q.top();
    }
};

```

```

1  ```Python
2  def findKthLargest(self, nums: List[int], k: int) -> int:
3      return heapq.nlargest(k,nums)[-1]
4  ```

```

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Question: Merge k sorted lists

<https://leetcode.com/problems/merge-k-sorted-lists/> (<https://leetcode.com/problems/merge-k-sorted-lists/>)

K lists.

Each of size N.

k lists of length n

Solution-0:

Join all linked list into 1 list

Sort the single linked list $O(nk \log nk)$

Solution-1: Merge lists sequentially till left with 1 list [k-1 merges]

$O(2n) + O(3n) + \dots O(kn)$

$O(n) (2 + 3 + 4 \dots k)$

$O(n) k(k+1)/2 \Rightarrow O(n) ((k^2)/2 + k/2) \Rightarrow O(n) O(k^2) \Rightarrow O(n * k^2)$

11 12 13 14 15 16 17 18

12 3 4 5 6 7 8

123 4 5 6 7 8

....

12345678

Solution-2: Merge lists pairwise till left with 1 list [k-1 merges]

$O(k*n) * \log k \Rightarrow O(nk \log k)$

1 2 3 4 5 6 7 8

12 34 56 78 $\rightarrow n*k$

1234 5678 $\rightarrow n*k$

12345678

Solution-3: Sorting

Solution-4: Heap

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Sort nearly k sorted array

Given a k-sorted array that is almost sorted such that each of the n elements may be misplaced by no more than k positions from the correct sorted order. Find a space-and-time efficient algorithm to sort the array.

For example,

Input:

arr = [1, 4, 5, 2, 3, 7, 8, 6, 10, 9] k = 2

Output:[1, 2, 3, 4, 5, 6, 7, 8, 9, 10]

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Question Skyline

<https://leetcode.com/problems/the-skyline-problem/> (<https://leetcode.com/problems/the-skyline-problem/>)

In []:

- 1 - Note down the problems
- 2 - SD, DSA, Framework

In []:

- 1 - salary
- 2 - work
- 3 - people, culture
- 4 - work life

In []:

- 1 Upskill:
- 2 - Get someone's experience in your CV
- 3 - Make your own personal project
- 4
- 5 - Tech ?
- 6 - Java
- 7 - Spring
- 8
- 9
- 10 Specific vs Generic
- 11 (Lang, framework etc.)
- 12 - Start a project
- 13 - Deploy on server
- 14

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