

```
In [1]: def recur(n):  
        if n < 0: # base condition  
            return  
  
        print(n)  
        recur(n-1)  
  
recur(10)
```

```
10  
9  
8  
7  
6  
5  
4  
3  
2  
1  
0
```

```
In [3]: def recur(n, i=0):  
        if i > n: # base condition  
            return  
  
        print(i)  
        recur(n, i+1)  
  
recur(10)
```

```
0  
1  
2  
3  
4  
5  
6  
7  
8  
9  
10
```

```
In [6]: def _iter(n):  
        i = 0  
        while i <= n:  
            print(i)  
            i+=1  
  
        _iter(10)
```

```
0  
1  
2  
3  
4  
5  
6  
7  
8  
9  
10
```

```
In [ ]:
```

```
In [ ]: ### Fibonacci series  
0 1 1 2 3 5 8 ....  
1 2 3 4 5 6 7 .... nth
```

```
In [9]: def fib(n):
        if n == 1:
            return 0
        if n == 2:
            return 1

        return fib(n-1) + fib(n-2)

print(fib(4))
print(fib(5))
print(fib(6))
print(fib(7))
print(fib(50))
```

2
3
5
8

KeyboardInterrupt

Traceback (most recent call last)

Cell In[9], line 13
11 print(fib(6))
12 print(fib(7))
----> 13 print(fib(50))

Cell In[9], line 7, in fib(n)
4 if n == 2:
5 return 1
----> 7 return fib(n-1) + fib(n-2)

Cell In[9], line 7, in fib(n)
4 if n == 2:
5 return 1
----> 7 return fib(n-1) + fib(n-2)

[... skipping similar frames: fib at line 7 (30 times)]

Cell In[9], line 7, in fib(n)
4 if n == 2:
5 return 1
----> 7 return fib(n-1) + fib(n-2)

Cell In[9], line 2, in fib(n)
1 def fib(n):
----> 2 if n == 1:
3 return 0
4 if n == 2:

KeyboardInterrupt:

```
In [10]: # top to bottom
cache = {} # unordered_map<int, int>

def fib(n):
    if n == 1:
        return 0
    if n == 2:
        return 1

    if n in cache:
        return cache[n]

    r = fib(n-1) + fib(n-2)
    cache[n] = r
    return r

print(fib(4))
print(fib(5))
print(fib(6))
print(fib(7))
print(fib(50)) # Linear
```

```
2
3
5
8
7778742049
```

```
In [14]: # memoization
cache = {1:0, 2:1} # unordered_map<int, int>
N

cachhe = [n .... -1]
def fib(n):
    if n <= 0:
        raise Exception("n should be >= 1")

    if n in cache:
        return cache[n]

    r = fib(n-1) + fib(n-2) # recurrence relation
    cache[n] = r
    return r

print(fib(4))
print(fib(5))
print(fib(6))
print(fib(7))
print(fib(50)) # Linear
print(fib(0))

# TC: O(n)
# SC: O(n)
```

```
2
3
5
8
7778742049
```

Exception

Traceback (most recent call last)

```
Cell In[14], line 19
    17 print(fib(7))
    18 print(fib(50)) # linear
----> 19 print(fib(0))
```

```
Cell In[14], line 5, in fib(n)
    3 def fib(n):
    4     if n <= 0:
----> 5         raise Exception("n should be >= 1")
    7     if n in cache:
    8         return cache[n]
```

Exception: n should be >= 1

In []:

```
In [19]: # bottom to top
# tabulation
results = [0,1]
def fib(n):
    while len(results) < n:
        curr = results[-1] + results[-2] # results[len(results) - 1] + results
        results.append(curr)

    return results[n-1]

print(fib(1))
print(fib(2))
print(fib(3))
print(fib(4))
print(fib(5))
print(fib(6))

# TC: O(N)
# SC: O(N)
```

0
1
1
2
3
5

```
In [20]: def fib(n):
    a = 0
    b = 0
    c = 1
    while n > 0:
        a = b
        b = c
        c = a + b
        n -= 1

    return a

print(fib(1))
print(fib(2))
print(fib(3))
print(fib(4))
print(fib(5))
print(fib(6))

# TC: O(n)
# SC: O(1)
```

0
1
1
2
3
5

In []:

Question: 1D<https://leetcode.com/problems/climbing-stairs/> (<https://leetcode.com/problems/climbing-stairs/>)

prerna

```
class Solution {
public:
    unordered_map<int,int> mp;
    int climbStairs(int n) {
        if(n==0) return 0;
        if(n==1) return 1;
        if(n==2) return 2;
        if(mp.count(n)>0) return mp[n];
        int r = climbStairs(n-1)+climbStairs(n-2);
        mp[n] = r;
        return r;
    }
};
```

Rajat Kumar

```
public int rec(int n ,Integer dp[]){
    if(n==0) return 1;
    if(n<0) return 0;
    if(dp[n] != null) return dp[n];
    return dp[n] = rec(n-1,dp) + rec(n-2,dp);
}
```

valeti

```
class Solution {  
public:  
    std::map<int,int> cacheMap;  
  
    int climbUtil(int n) {  
  
        if (cacheMap.find(n) != cacheMap.end()) {  
            return cacheMap.at(n);  
        }  
    }  
}
```

```
def climbStairs(n):  
    if n <= 0:  
        return 0  
    elif n == 1:  
        return 1  
    elif n == 2:  
        return 2  
  
    prev_1 = 1  
    prev_2 = 2  
  
    for _ in range(3, n + 1):  
        curr = prev_1 + prev_2  
        prev_1, prev_2 = prev_2, curr  
  
    return prev_2
```



```

class Solution {
    public int climbStairs(int n) {
        int f1,f2,f3=0,i;
        if(n==1)
            return 1;
        else if(n==2)
            return 2;
        else
        {
            f1=1;
            f2=2;
            for(i=2;i<n;i++)
            {
                f3=f2+f1;
                f1=f2;
                f2=f3;
            }

        }
        return f3;
    }
}

```

TC: $O(N)$

SC: $O(1)$

```

class Solution {
public:
    int climbStairs(int n) {
        // 1-> 1
        // 2-> 2
        // n -> n-1 + n-2

        int a = 1;
        int b = 2;
        int curr = 0;
        while (n > 0) {
            curr = a;
            a = b;
            b = curr + a;
            n -= 1;
        }

        return curr;
    }

    // 1->1
    // 2->
};

```

```

Class Solution {
public:
    int climbStairs(int n) {
        if(n==0) return 0;
        if(n==1) return 1;
        if(n==2) return 2;
        int p1= 1;
        int p2= 2;
        for(int i=3;i<n+1;i++)
        {
            int curr = p1 + p2;
            p1=p2;
            p2 = curr;
        }
    }
}

```

In []:

In []:

In []:

Question

<https://leetcode.com/problems/unique-paths/> (<https://leetcode.com/problems/unique-paths/>)

Iterative Optimized

```

class Solution:
    def uniquePaths(self, m: int, n: int) -> int:
        if m == 1 and n == 1:
            return 1

        pathList = [1 for i in range(n)]

        for i in range(1, m):
            for j in range(n):
                if j > 0:
                    pathList[j] = pathList[j] + pathList[j - 1]

        return pathList[-1]

```

TC: $O(m*n)$ SC: $O(n)$

```

class Solution {
public:
    int uniquePaths(int m, int n) {
        vector<vector<int>> nestedVec(m, vector<int>(n,1));
        for (int i=1; i<m; i++) {
            for (int j=1; j<n; j++) {
                nestedVec[i][j] = nestedVec[i][j-1] + nestedVec[i-1]
[j];
            }
        }
        return nestedVec[m-1][n-1];
    }
};
TC: O(m*n)
SC: O(m*n)

```

```

public int uniquePaths(int m, int n) {

    int row[] = new int[n];
    Arrays.fill(row, 1);

    for(int i = 1; i < m; i++){
        for(int j = 1; j < n; j++){
            row[j] = row[j-1] + row[j];
        }
    }
    return row[n - 1];
}

```

In []:

Top Down: Using matrix cache

```

class Solution {
public:
    int uniquePaths(int m, int n) {
        vector<vector<int>> nestedVec(m, vector<int>(n,-1));
        for (int i = 0; i < m; i++) {
            nestedVec[i][0] = 1;
        }
        for (int i = 0; i < n; i++) {
            nestedVec[0][i] = 1;
        }

        return uniquePathsUtil(m,n, cache);
    }
}

```

Top Down: Using hashmap cache. Assuming first cell is 1,1 instead of 0,0

```

typedef unordered_map<pair<int, int>, int> cacheType;
class Solution {
public:
    int uniquePaths(int m, int n) {
        cacheType cache;

        cache[make_pair<int,int>(1,1)] = 1;

        return uniquePathsUtil(m,n, cache);
    }

    int uniquePathsUtil(int m, int n, cacheType& cache) {
        if (m <= 0 || n <= 0) return 0;

        if (cache.count(make_pair<int,int>(m,n)) != 0)
            return cache[make_pair<int,int>(m,n)];

        int res = uniquePathsUtil(m-1, n, cache) + uniquePathsUtil
(m, n-1, cache);
        cache[make_pair<int,int>(m,n)] = res;
        return res;
    }
};

```

```
In [ ]: [a, b ,c , d]
```

```
(ab)  
(ba)
```

```
In [25]:
```

```
def longest_char_seq(s):  
    max_count = 1  
    c = s[0]  
    count = 1  
    for i in range(1, len(s)):  
        if c == s[i]:  
            count += 1  
            max_count = max(max_count, count)  
        else:  
            c = s[i]  
            count = 1  
  
    return max_count  
  
longest_char_seq('abaaaabaaaaaaaaabbbbbbbbbbbbbbb')  
  
['abbbbbbbba', 'aaba', 'aaabba']
```

```
Out[25]: 15
```

https://app.codility.com/programmers/task/concatenating_of_words/
(https://app.codility.com/programmers/task/concatenating_of_words/)