

Sorting

Bubble, Selection, Insertion sort already covered

Assumption till now

- TC: $O(N \log N)$
- SC: $O(1)$

Figure out the TC and SC for your language's sorting implementation

JAVA:

C++

Python

Javascript

C#

In []:

1

comparison based sort

1. Bubble sort
2. selection Sort
3. Insertion Sort
4. Merge sort: Merge 2 sorted arrays **[Divide and Conquer]**
5. Quick sort **[Divide and Conquer]**
6. Heap sort: Heap DS

Non-comparison

- Counting sort
- Radix sort
- Bucket sort

Counting Sort

TC: $\max(O(N), O(\text{range}))$

SC: $O(\text{range})$

2 4 5 1 3 4 2 2: [1,5]

[10,15]

[min, max]

- create a frequency array of size $\text{max} + 1$
- count frequency of each value in the range
- overwrite the data in original array **using** frequency map

Frequency array

[0 1 3 1 2 1]

0 1 2 3 4 5

Sorted result

[1 2 2 2 3 4 4 5]

- | | |
|---|--------------------------|
| 1 | - Stable vs Unstable |
| 2 | - Inplace vs not inplace |

In []:

1

Merge sort

- merging 2 sorted arrays
- assuming an array of size 1 is always sorted

```
1 4 5 2 3 5 7 6
0 1 2 3 4 5 6 7
```

Is an array of size 1 sorted ?
[1]

```
[1] [4] [5] [2] [3] [5] [7] [6]
[1,4] [2,5] [3,5] [6,7]
[1,2,4,5] [3,5,6,7]
[1 2 3 4 5 5 6 7]
```

```
def merge_sort(arr):

    if (len(arr) <= 1):
        return arr;

    a1 = merge_sort(arr[0:len(arr)//2]) # recurse for first half of a
    a2 = merge_sort(arr[len(arr)//2: len(arr)]) # recurse for second
    half of array

    a3 = merge_sorted_arrays(a1, a2)
    return a3

def merge_sorted_arrays(a1, a2):

    i = 0
    j = 0
    a3 = []
    while i < len(a1) and j < len(a2):
        if a1[i] < a2[j]:
            a3.append(a1[i])
            i+=1
        else:
            a3.append(a2[j])
            j+=1

    while i < len(a1):
        .....
    return a3
```

```
[1 4 5 2 3 5 7 6] -> [1 2 3 4 5 5 6 7]
```

N ops

```

    [1 4 5 2]->[1, 2, 4, 5]
6]->[3 5 6 7]
    [1 4]->[1,4]
[3,5]    [7,6]->[6,7]
    [1]->[1] [4]->[4]
[3] [5]->5 [7]->7 [6]->6

```

N ops

[5,2]->[2,5]

N ops

[5]->[5] [2]->[2]

N ops

No. of levels = recursion depth = $\log n$

$N + N + N + \dots$ ($\log N$ times)

TC: $O(n \log n)$

SC: $O(n)$

In []:

1

External Sort : uses merge sort algorithm

RAM: 4G

Data: 32G file.txt

file1.txt (4GB), file2.txt, file3.txt..... file8.txt

f1 f2

file12 file34 file78

file1234 file5678

file12345678

- open -> file pointer
- read from file : read data in chunks and move pointer further.

file1 [10 20 40 50 80] file2 [20 30 60]

^

^

file3 10 20 20 30

out.txt write(1) write(2) write(4) [4 5 6]

[1 2 3 4 5 6]

File O(1)

RAM: random access ? Yes

Disk HDD: random access ? No

Disk SSD: random access ? Yes

```
In [ ]: 1 def merge_files(name1, name2):
2         f1 = open(name1, 'r')
3         f2 = open(name2, 'r')
4
5         f3 = open('temp.txt', 'w')
6
7         while True:
8             d1 = f1.readline()
9             d2 = f2.readline()
10
11             if d1 == '' || d2 == '':
12                 break
13
14             if d1 > d2:
15                 f3.write(d2)
16             else:
17                 f3.write(d1)
18
19             if d1 == '':
20                 while True:
21                     d = f2.readline()
22                     if d == '':
23                         break
24                     f3.write(d)
25
26             if d2 == '':
27                 while True:
28                     d = f1.readline()
29                     if d == '':
30                         break
31                     f3.write(d)
32
```

```
In [ ]: 1
```

quick sort

Properties: inplace, not-stable

- TC
 - AVG = BEST = $O(N \log N)$
 - Worst = $O(N^2)$
- SC
 - AVG = $O(\log N)$
 - WORST = $O(N)$

```

void qsort(array, start, end) {
    if end-start <=1
        return

    p = partition(array, start, end)

    qsort(array, start, p)
    qsort(array, p, end)
}

int partition(array, start, end) {
    // returns the point of partition

    pivot = end-1
    i = start-1
    j = start
    while(j<pivot) {
        if (array[j] < array[pivot]) {
            i+=1
            swap(array[i], array[j])
        }
        j++
    }
}

```

In []:

```

1
2 - numbers
3 - strings

```

In []:

```

1

```

Language Specifics: Comparator Sorting

C++

// Type your code here, or Load an example.

```
# include <vector>
# include <algorithm>
# include <string>

using namespace std;
class Person {

    public:
        int age;
        string name;

        Person(string name, int age) {
            this->age = age;
            this->name = name;
        }

        bool operator<(Person other) const {
            if (this->age < other.age) {
                return true;
            }
            return false;
        }

        bool operator>(Person other) const {
            if (this->age > other.age) {
                return true;
            }
            return false;
        }
};

int main() {
    std::vector<Person> persons;
    persons.push_back(Person("A", 2));
    persons.push_back(Person("C", 3));
    persons.push_back(Person("B", 1));
    persons.push_back(Person("A", 4));
```

```
1  **Java**
2  ```Java
3  import java.util.*;
4
5  class Person implements Comparable<Person> {
6      public String name;
7      public int age;
8
9      Person(String name, int age) {
10         this.name = name;
11         this.age = age;
```



```
12     }
13
14     @Override
15     public int compareTo(Person p) {
16         if (this.age < p.age) {
17             return -1;
18         } else if (this.age == p.age) {
19             return 0;
20         }
21
22         return 1;
23     }
24
25 }
26
27 class CompByName implements Comparator<Person> {
28
29     public int compare(Person a, Person b)
30     {
31         return a.name.compareTo(b.name);
32     }
33 }
34
35 class CompByNameThenAge implements Comparator<Person> {
36
37     public int compare(Person a, Person b)
38     {
39         int val = a.name.compareTo(b.name);
40         if (val == 0) {
41             if (a.age > b.age) {
42                 return -1;
43             } else if (a.age == b.age) {
44                 return 0;
45             }
46
47             return 1;
48         }
49
50         return val;
51     }
52 }
53
54
55 class CompByAge implements Comparator<Person> {
56
57     public int compare(Person a, Person b)
58     {
59         if (a.age < b.age) {
60             return -1;
61         } else if (a.age == b.age) {
62             return 0;
63         }
64
65         return 1;
66     }
67 }
68
```

```

69 public class Main {
70     public static void main(String[] args) {
71
72         ArrayList<Person> list = new ArrayList<>();
73
74         list.add(new Person("A", 2));
75         list.add(new Person("C", 3));
76         list.add(new Person("B", 1));
77         list.add(new Person("A", 4));
78
79         // Collections.sort(list);
80         Collections.sort(list, new CompByNameThenAge());
81
82         for (int i=0; i < list.size(); i++) {
83             System.out.println(list.get(i).name + " " +
84                 list.get(i).age);
85         }
86     }
87 }
88 ...
89

```

```

In [ ]: 1 lessthan(a1,a2):
        2     return a1 < a2
        3
        4 lessthan(1,2) -> true
        5 lessthan(2,2) -> false
        6
        7 x = 3
        8 y = 2
        9 lessthan(x,y) -> false so is x==y or is x>y
       10     lessthan(y,x) -> true -> x > y
       11     lessthan(y,x) -> false -> equal

```

```
In [ ]: 1
```

```
In [ ]: 1
```

```
In [ ]: 1
```

Question

<https://leetcode.com/problems/largest-number/> (<https://leetcode.com/problems/largest-number/>)

TC: $O(n \log n)$

SC: $O(1)$

```

// Type your code here, or Load an example.
#include <vector>
#include <algorithm>
#include <string>

using namespace std;
class Person {

public:
    int age;
    string name;

    Person(string name, int age) {
        this->age = age;
        this->name = name;
    }

    bool operator<(Person other) const {
        if (this->age < other.age) {
            return true;
        }
        return false;
    }

    bool operator>(Person other) const {
        if (this->age > other.age) {
            return true;
        }
        return false;
    }
};

int main() {
    std::vector<Person> persons;
    persons.push_back(Person("A", 2));
    persons.push_back(Person("C", 3));
    persons.push_back(Person("B", 1));
    persons.push_back(Person("A", 4));

    //a<b -> a.func(b)

    // std::sort(persons.begin(), persons.end());
    // std::sort(persons.begin(), persons.end(), std::greater<Person>
    ());
    std::sort(persons.begin(), persons.end(), [](Person a, Person b)
    {
        return a.age > b.age;
    });
}

```

```

// for(auto p: persons) {
//     std::cout << p.name << " " << p.age << endl;
// }

std::vector<int> nums = {3,30,34,5,9};
// std::sort(nums.begin(), nums.end(), [](int n1, int n2) {
//     auto s1 = to_string(n1);
//     auto s2 = to_string(n2);
//     return s1 > s2;
// });

std::sort(nums.begin(), nums.end(), [](int n1, int n2) {
    auto s1 = to_string(n1);
    auto s2 = to_string(n2);
    return s1+s2 > s2+s1;
});

sort(a1, a2, less())
#     3 5 9 30 34 // assume bubble sort

#     5 3 9 30 34 swap
#     5 9 3 30 34 swap
#     5 9 3 30 34 no swap 330 > 303 -> true
#     5 9 3 34 30 swap

#     9 5 3 34 30 swap
#     9 5 3 34 30 no swap
#     9 5 34 3 30 swap
#         .....

for(auto num: nums) {

```

Question

<https://leetcode.com/problems/h-index/> (<https://leetcode.com/problems/h-index/>)

In []:

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