

## **CS 540: Introduction to Artificial Intelligence Homework # 8**

**Assigned: 4/09  
Due: 4/16 before class**

### **Hand in your homework:**

There are five questions in this homework. Please answer the questions in a single pdf file. Please typeset your homework, do not submit handwritten+scan answers. The pdf file should be submitted on Canvas.

### **Late Policy:**

All assignments are due at the beginning of class on the due date. One (1) day late, defined as a 24-hour period from the deadline (weekday or weekend), will result in 10% of the total points for the assignment deducted. So, for example, if a 60-point assignment is due on a Wednesday 9:30 a.m., and it is handed in between Wednesday 9:30 a.m. and Thursday 9:30 a.m., 6 points will be deducted. Two (2) days late, 25% off; three (3) days late, 50 off. No homework can be turned in more than three (3) days late. Written questions and program submission have the same deadline.

### **Collaborative Policy:**

You are to complete this assignment individually. However, you are encouraged to discuss the general algorithms and ideas with classmates, TAs, and instructor in order to help you answer the questions. You are also welcome to give each other examples that are not on the assignment in order to demonstrate how to solve problems. But we require you to:

- not explicitly tell each other the answers
- not to copy answers or code fragments from anyone or anywhere
- not to allow your answers to be copied
- not to get any code on the Web

In those cases where you work with one or more other people on the general discussion of the assignment and surrounding topics, we suggest that you specifically record on the assignment the names of the people you were in discussion with.

### Question 1: Resolution [9 points]

Given the knowledge base

$$p \implies (q \implies r)$$

use resolution to prove the query

$$(p \wedge q) \implies (q \implies r).$$

Be sure to show what you convert to CNF (do not skip steps), and how you perform each resolution step.

### Question 2: Translation from English to First Order Logic [13 points]

1. (7 points) Consider the following axioms:

- Every child loves Santa.
- Everyone who loves Santa loves any reindeer.
- Rudolph is a reindeer, and Rudolph has a red nose.
- Anything which has a red nose is weird or is a clown.
- No reindeer is a clown.
- Scrooge does not love anything which is weird.
- (Conclusion) Scrooge is not a child.

Give the First Order Logic (FOL) sentences. You may define your FOL predicates and functions.

2. (6 points) Consider the following axioms:

- Every Austinite who is not conservative loves some armadillo.
- Anyone who wears maroon-and-white shirts is an Aggie.
- Every Aggie loves every dog.
- Nobody who loves every dog loves any armadillo.
- Clem is an Austinite, and Clem wears maroon-and-white shirts.
- There is a conservative Austinite.

Give the First Order Logic (FOL) sentences. You may define your FOL predicates and functions.

### Question 3: First Order Logic [8 points]

You are a homicide detective and receive news of the murder of your teacher, Chuck. His students Abby (aka A), Ben (aka B), and Chris (aka C) are the only suspects. You bring them in for questioning. Here's what they tell you:

- Abby says that Ben and Chuck were friends, and Chris and Chuck were not friends.
- Ben says he and Chuck were not friends.
- Chris says that Ben and Chuck were friends.

As an astute detective you make the following assumptions about the world:

- Friends don't murder each other.
- There is no more than one murderer.

- If a person isn't a murderer, they don't lie.
1. (2.5 points) Write a set of sentences in FOL representing the knowledge in the six English sentences above. Note: You may have more than one FOL sentence representing one English sentence, if necessary, and you may include the knowledge given in sentence 6 directly into your representation of sentences 1-3. Use the following predicates:  $M(x)$  means  $x$  is a murderer, and  $F(x)$  means  $x$  is a friend of Chuck. Represent 5 sentences using the equality predicate.
  2. (4 points) Write all of your sentences from (a) in conjunctive normal form (CNF). Instead of using your representation of sentence (5) from (a), convert to CNF the equivalent sentence:  

$$(\neg M(A) \vee \neg M(B)) \wedge (\neg M(A) \vee \neg M(C)) \wedge (\neg M(B) \vee \neg M(C))$$
  3. (1.5 points) Chris later tells you that he was a friend of Chuck. Write an FOL sentence that represents this new piece of information.

### Question 4: Forward Chaining and backward Chaining [10 points]

1. (5 points) Use forward chaining to solve the following problem:

Given:

$A$

$B$

$C$

$A \wedge B \Rightarrow D$

$B \wedge D \Rightarrow F$

$F \Rightarrow G$

$A \wedge E \Rightarrow H$

$A \wedge C \Rightarrow E$  Is  $H$  true? Draw a tree to illustrate the search for a proof.

2. (5 points) Use backward chaining on the following KB to prove  $Q$ :

$P \Rightarrow Q$

$E \Rightarrow B$

$R \Rightarrow Q$

$M \wedge N \Rightarrow Q$

$A \wedge B \Rightarrow P$

$A \Rightarrow M$

$C \Rightarrow M$

$D \Rightarrow N$

$D$

$A$

Draw a tree to illustrate the search for a proof. Mark the nodes that are satisfied in this KB. What is the proof of  $Q$ ? (Please show the steps)

### Question 5: Clustering [20 points]

Consider the following information about distances in miles between pairs of 10 U.S. cities:

The coordinates (latitude, longitude) of these cities are:

BOS (42.4, 71.1),

NY (41.7, 74.0),

DC (38.9, 77.0),

MIA (25.8, 80.2),  
SLC (40.8, 111.9),  
SEA (47.6, 122.3),  
SF (37.8, 122.4),  
LA (34.1, 118.2),  
DEN (39.7, 105.0),  
ATL (33.7, 84.3).

Please directly use the Euclidean distance when solving Question 5.1 and Question 5.2.

1. (10 points) Perform hierarchical clustering using single-linkage and the above data.
  - (a) Show the resulting dendrogram.
  - (b) What clusters of cities are created if you want 3 clusters?
2. (10 points) Show the results of one iteration of k-means clustering assuming  $k = 2$  and the initial cluster centers are defined as  $c1 = (50, 90)$  and  $c2 = (30, 100)$ 
  - (a) Give the list of cities in the initial 2 clusters.
  - (b) Give the coordinates of the new cluster centers.
  - (c) Give the list of cities in the 2 clusters based on the new cluster centers computed in the (b).