WaveCrest: a statistical approach to reconstruct gene expression trajectory in ordered single cell RNA-seq experiments

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1 Introduction

WaveCrest (as detailed in Chu* and Leng* et al., 2015 (1)) is a statistical approach to reconstruct gene expression trajectory in single cell RNA-seq experiments with ordered conditions. WaveCrest contains two modules - the first module implements an extended nearest insertion (ENI) algorithm that searches for optimal cell orders, and the second module implements a spline fitting module that can be used to identify additional dynamic genes.

2 Run WaveCrest

Before analysis can proceed, the WaveCrest package must be loaded into the working space:

> library(WaveCrest)

2.1 Required inputs

Data: The object Data should be a G-by-S matrix containing the expression values for each gene and each cell, where G is the number of genes and S is the number of cells. These values should exhibit estimates of gene expression across cells. Counts of this nature may be obtained from RSEM (2), Cufflinks (3), or a similar approach. Cross-cell library size normalization should be performed. A cross-cell library size normalization by median-by-ratio normalization are shown in section 2.2.

Conditions: The object Conditions should be a factor of length S that indicates to which condition each cell belongs. Note the order of levels in the factor should represent the order in the RNA-seq experiments.

The object WaveCrestExData is a simulated data matrix containing 200 rows of genes and 120 columns of cells. The genes are named g1, g2, ... and the cells are named s1, s2, ...

```
> data(WaveCrestExData)
> str(WaveCrestExData)
num [1:200, 1:120] 99.7 134.6 105.5 83 103.3 ...
- attr(*, "dimnames")=List of 2
    ..$ : chr [1:200] "g1" "g2" "g3" "g4" ...
    ..$ : chr [1:120] "s1" "s2" "s3" "s4" ...
```

Here we simulated 4 time points (conditions), each has 30 cells. To specify which condition each cell belongs, we define:

Downstream analysis by WaveCrest requires the conditions to be specified as a factor. In particular, levels of the factor need to be sorted along the time/spatial course. For example, to generate a factor with ordered conditions from t1 to t4, we define:

```
> Conditions <- factor(CondVector, levels=c("t1","t2","t3","t4"))
> str(Conditions)
Factor w/ 4 levels "t1","t2","t3",..: 1 1 1 1 1 1 1 1 1 1 1 ...
> levels(Conditions)
[1] "t1" "t2" "t3" "t4"
```

2.2 Normalization

WaveCrest requires cross-cell normalization to be applied to adjust for sequencing depth differences among different cells. Here, the library size factors may be obtained via the function MedianNorm, which implements the median-by-ratio normalization introduced in DESeq (4).

```
> Sizes <- MedianNorm(WaveCrestExData)
> str(Sizes)
Named num [1:120] 1 1 1 1 1 ...
- attr(*, "names")= chr [1:120] "s1" "s2" "s3" "s4" ...
```

Note that in a case that none of the genes are expressed in all cells (any gene has at least one zero counts) due to technical dropouts, the MedianNorm() function may return NA estimates. The option alternative = TRUE in MedianNorm function may be applied to address this issue. For example,

```
> Sizes <- MedianNorm(WaveCrestExData,alternative = TRUE)
> str(Sizes)
num [1:120] 1 1 1 1 1 ...
```

To obtain the normalized expression matrix for visualization purpose or other downstream analyses, we may use the GetNormalizedMat() function:

```
> DataNorm <- GetNormalizedMat(WaveCrestExData, Sizes)</pre>
```

Note the WaveCrest analysis requires normalized expression estimates.

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2.3 Recover the cell orders

WaveCrest reconstructs gene expression trajectory in ordered single cell RNA-seq experiments using an ENI algorithm. A list of key markers should be provided for the reconstruction. Such markers may be defined from differential expression analysis and/or prior knowledge (1). As an example, we define the first 8 genes in the example data set as the key markers:

```
> Markers <- rownames(DataNorm)[1:8]
> print(Markers)
[1] "g1" "g2" "g3" "g4" "g5" "g6" "g7" "g8"
```

Take a look at the key markers following the original cell order:

```
> par(mfrow=c(3,3))
> frame()
> legend("top", levels(Conditions),col=1:4,pch=1,ncol=1)
  for(i in 1:8) {
                plot(DataNorm[Markers[i],],col=as.numeric(Conditions),
                                            ylab="Normalized expression", xlab="Original order",main=Markers[i])}
                                                                                                                          g2
                                                                                g1
                                                          Normalized expression
                                                                                                     Normalized expression
                                                                120
                                                                                                          130
                                     o t2
                                                                110
                                     o t3
                                                                                                          120
                                     o t4
                                                                100
                                                                                                          9
                                                                             40
                                                                                    80
                                                                                            120
                                                                                                                               80
                                                                                                                                      120
                                                                           Original order
                                                                                                                     Original order
                                      g3
                                                                                g4
                                                                                                                          g5
                Normalized expression
                                                          Normalized expression
                                                                                                     Normalized expression
                      120
                                                                95
                                                                                                          100
                      110
                                                                85
                                                                                                          90
                                          80
                                                                             40
                                                                                    80
                                                                                                                               80
                           0
                                  40
                                                 120
                                                                                            120
                                                                                                                       40
                                                                                                                                      120
                                Original order
                                                                           Original order
                                                                                                                     Original order
                                                                                g7
                                      g6
                                                                                                                           g8
                Normalized expression
                                                          Normalized expression
                                                                                                     Normalized expression
                                                                140
                                                                                                          115
                      120
                                                                130
                                                                                                          105
                                                                120
                      105
                                                                                                          92
                                          80
                                                                             40
                                                                                    80
                                                                                            120
                                                                                                                       40
                                                                                                                               80
                                Original order
                                                                           Original order
                                                                                                                     Original order
```

Figure 1: Key markers used in the ENI step. The y axis shows normalized expression. The x axis shows cells following original order.

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Once the marker list is provided, the WaveCrestENI() function can be used to reconstruct the cell order. A 2-opt algorithm is also implemented in the WaveCrestENI() function to avoid finding local maxima. To run the ENI and 2-opt algorithm on our example data set:

- > ENIRes <- WaveCrestENI(Markers, WaveCrestExData, Conditions, N=1000)
 > str(ENIRes)
- int [1:120] 22 19 14 13 30 16 23 25 20 27 ...

Here N is used to specify the number of iterations to run in the 2-opt algorithm. The default value for N is 20000. In this example we set it to 1000 to reduce the run-time. In empirical analysis we recommend users to increase N to improve performance. The output of the WaveCrestENI() function is a numerical vector that indicates order of the cells. To visualize the 8 key markers following recovered cell order:

```
> par(mfrow=c(3,3))
> frame()
> legend("top", levels(Conditions),col=1:4,pch=1,ncol=1)
  for(i in 1:8) {
               plot(DataNorm[Markers[i], ENIRes], col=as.numeric(Conditions),
                                           ylab="Normalized expression", xlab="Recovered order",
                                           main=Markers[i])}
                                                                              g1
                                                                                                                       g2
                                                         Normalized expression
                                                                                                  Normalized expression
                                                              120
                                    o t1
                                    o t2
                                                              110
                                                                                                       120
                                    o t3
                                    o t4
                                                              8
                                                                                                       110
                                                                           40
                                                                                  80
                                                                                         120
                                                                                                             0
                                                                                                                    40
                                                                                                                           80
                                                                                                                                  120
                                                                       Recovered order
                                                                                                                Recovered order
                                     g3
                                                                              g4
                                                                                                                       g5
                                                         Normalized expression
               Normalized expression
                                                                                                  Normalized expression
                     120
                                                              95
                     110
                                                              82
                                                                                                       90
                     9
                                 40
                                         80
                                                                           40
                                                                                  80
                                                                                         120
                                                                                                             0
                                                                                                                           80
                              Recovered order
                                                                       Recovered order
                                                                                                                 Recovered order
                                     g6
                                                                              g7
                                                                                                                       g8
                Normalized expression
                                                         Normalized expression
                                                                                                  Normalized expression
                                                              140
                                                                                                        115
                     120
                                                              130
                                                                                                       105
                                                              120
                     105
                                                                                                       92
                                         80
                                                                           40
                                                                                  80
                                                                                                                    40
                                                                                                                           80
                                 40
                              Recovered order
                                                                       Recovered order
                                                                                                                 Recovered order
```

Figure 2: Key markers used in the ENI step. The y axis shows normalized expression. The x axis shows cells following WaveCrest recovered cell order.

2.4 Identify addtional dynamic genes based on the recovered order

WaveCrest also provides a function WaveCrestIden() to detect additional dynamic genes based on the recovered order. This allows users to 'rescue' genes that were not considered by prior studies (if the markers were picked based on prior knowledge) or were missed by prior analysis (if the markers were picked based on differential expression results, etc.). To identify additional dynamic genes, WaveCrest fits a polynomial regression on each gene's rescaled expression (z-score), following the recovered cell order. Genes with low fitting errors are considered to be top dynamic genes.

To run WaveCrestIden() on all remaining genes in our example data set:

- > DataNormRemain <- DataNorm[setdiff(rownames(DataNorm), Markers),]
- > IdenRes <- WaveCrestIden(DataNormRemain, ENIRes)
- > IdenRes[1:5] # top 5 genes

```
g16 g12 g20 g14 g13
0.04877703 0.05635579 0.08616845 0.12269853 0.15784240
```

The WaveCrestIden() function outputs mean square errors of the gene specific fittings. Genes are sorted increasingly by their mean square errors. To visualize the top 5 genes identified by the WaveCrestIden() function:

```
> par(mfrow=c(3,3))
> frame()
> legend("top", levels(Conditions),col=1:4,pch=1,ncol=1)
> for(i in 1:5) {
              plot(DataNorm[names(IdenRes)[i],ENIRes],col=as.numeric(Conditions),
                                      ylab="Normalized expression", xlab="Recovered order",
                                      main=names(IdenRes)[i])}
                                                                    g16
                                                                                                         g12
                                                  Normalized expression
                                                                                       Normalized expression
                                o t1
                                o t2
                                                                                            98
                                                       108
                                o t3
                                                                                            94
                                o t4
                                                       102
                                                                                            90
                                                                  40
                                                                         80
                                                                                                             80
                                                            0
                                                                               120
                                                                                                      40
                                                                                                                   120
                                                               Recovered order
                                                                                                    Recovered order
                               g20
                                                                    g14
                                                                                                         g13
                                                                                       Normalized expression
              Normalized expression
                                                  Normalized expression
                   120
                                                                                            98
                                                       102
                                                                                            94
                                                       96
                                                                                            90
                                          120
                                                                         80
                                                                               120
                                                                                                             80
                                                                                                                   120
                             40
                                    80
                                                                  40
                          Recovered order
                                                               Recovered order
                                                                                                   Recovered order
```

Figure 3: Top dynamic markers identified by WaveCrest. The y axis shows normalized expression. The x axis shows cells following WaveCrest recovered order.

3 Session info

```
> print(sessionInfo())
R version 3.2.1 (2015-06-18)
Platform: x86_64-apple-darwin13.4.0 (64-bit)
Running under: OS X 10.10.5 (Yosemite)
locale:
[1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
attached base packages:
              graphics grDevices utils
[1] stats
                                            datasets methods
                                                                base
other attached packages:
[1] WaveCrest_0.0.1
                        Oscope_0.99.1
                                            BiocParallel_1.2.14 cluster_2.0.1
[5] EBSeq_1.11.1
                        testthat_0.11.0
                                            gplots_2.17.0
                                                                blockmodeling_0.1.8
loaded via a namespace (and not attached):
 [1] gtools_3.5.0
                                               crayon_1.3.1
                                                                    bitops_1.0-6
                          digest_0.6.8
 [5] futile.options_1.0.0 KernSmooth_2.23-14
                                               gdata_2.17.0
                                                                    futile.logger_1.4.1
 [9] BiocStyle_1.6.0
                         lambda.r_1.1.7
                                               tools_3.2.1
                                                                    parallel_3.2.1
[13] caTools_1.17.1
                          memoise_0.2.1
```

References

- [1] Li-Fang Chu, Ning Leng, Jue Zhang, Zhonggang Hou, Danny Mamott, David T Vereide, Christina Kendziorski, Ron Stewart, and James A Thomson. Single cell rna-seq reveals the molecular dynamics and uncovers novel regulators of human embryonic stem cell differentiation to definitive endoderm. *Submitted*, 2015.
- [2] B Li and C N Dewey. Rsem: accurate transcript quantification from rna-seq data with or without a reference genome. BMC Bioinformatics, 12:323, 2011.
- [3] C Trapnell, A Roberts, L Goff, G Pertea, D Kim, D R Kelley, H Pimentel, S L Salzberg, J L Rinn, and L Pachter. Differential gene and transcript expression analysis of rna-seq experiments with tophat and cufflinks. *Nature Protocols*, 7(3):562–578, 2012.
- [4] S Anders and W Huber. Differential expression analysis for sequence count data. Genome Biology, 11:R106, 2010.