

Sets with indices

I	Set of nurses
T	Set of days
S	Set of shifts
r	Index for rosters
$R(i)$	Set of alternative rosters for nurse i

Decision variables MP:

$slack_{ts}$	slack for shift s on day t
$motivation_{its}^r$	Motivation of nurse i in shift s on day t if assigned to roster r
λ_{ir}	if nurse i is assigned to roster r

Decision variables SP:

x_{its}	1 if physician i works shift s on day t , 0 otherwise
$mood_{it}$	mood of nurse i on day t
$motivation_{its}$	Motivation of nurse i in shift s on day t

Parameter:

$demand_{ts}$	Demand in shift s on day t
Max_W	Number of maximum allowed consecutive working days
M	Big number
α	parameter to control

Master Problem:

$$(MP) \quad \min \quad \sum_t \sum_s slack_{ts} \quad (1)$$

$$(2)$$

subject to:

$$\sum_i \sum_r motivation_{its}^r \lambda_{ir} + slack_{ts} \geq demand_{ts} \quad \forall t, s \quad (3)$$

$$\sum_r \lambda_{ir} = 1 \quad \forall i \quad (4)$$

$$\lambda_{ir} \in \mathbb{Z}^+ \quad \forall i, r \quad (5)$$

$$slack_{ts} \geq 0 \quad \forall t, s \quad (6)$$

The corresponding duals from constraint (3) are π_{ts} and μ_i from constraint (4).

Subproblems:

$$\mathcal{SP}(i) \quad \min - \sum_{t,s} \pi_{ts} \text{motivation}_{ts} - \mu_i \quad (7)$$

$$(8)$$

subject to:

$$\text{mood}_t + M \cdot (1 - x_{ts}) \geq \text{motivation}_{ts} \quad \forall t, s \quad (9)$$

$$\text{motivation}_{ts} \geq \text{mood}_t - M \cdot (1 - x_{ts}) \quad \forall t, s \quad (10)$$

$$\text{motivation}_{ts} \leq x_{ts} \quad \forall t, s \quad (11)$$

$$\sum_s x_{ts} \leq 1 \quad \forall t \quad (12)$$

$$\alpha \sum_s x_{ts} + \text{mood}_t = 1 \quad \forall t \quad (13)$$

$$\text{motivation}_{ts} \in [0, 1] \quad \forall t, s \quad (14)$$

$$t \in [0, 1] \quad \forall t \quad (15)$$

$$x_{ts} \in \{0, 1\} \quad \forall t, s \quad (16)$$

$$(17)$$

Note that the index i is dropped in the subproblem formulation in the code.