run_example

June 30, 2021

```
[1]: import numpy as np
  import matplotlib.pyplot as plt
  %matplotlib inline

from sklearn import cluster, datasets, mixture
  from sklearn.preprocessing import StandardScaler

[2]: p =200

[3]: import sklearn
  np.random.seed(9)

# mu = sklearn.datasets.make_blobs(n_samples=p, n_features=2,u_centers=3,shuffle=False)
  mu = sklearn.datasets.make_moons(n_samples=p, noise=0.05,shuffle=False)

Y = mu[0]

plt.scatter(Y[:,0],Y[:,1])
```

[3]: <matplotlib.collections.PathCollection at 0x7f1314441a90>

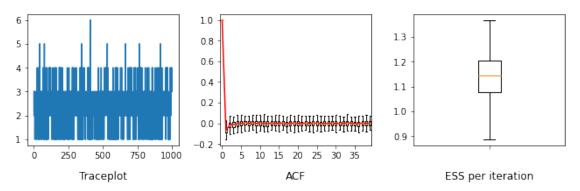
```
1.0
 0.8
 0.6
 0.4
 0.2
 0.0
-0.2
-0.4
-0.6
                   -0.5
                                                             1.5
         -1.0
                              0.0
                                        0.5
                                                  1.0
                                                                       2.0
```

```
[4]: import numba
     from numba import jit
     import importlib
     import gibbs_sampling as gs
[5]: # importlib.reload(gs)
[6]: tree = gs.SpanningTree(Y)
[7]: # burn-in
     # adjust step_size to have the acceptance rate close to 0.3
     _ = tree.runMCMC(100, step_size = 0.02)
    99
    0.4
[8]: # collect Markov chain samples
     trace = tree.runMCMC(1000, step_size = 0.02)
    99
    199
    299
    399
```

```
499
     599
     699
     799
     899
     999
     0.331
 []:
 [9]:
     trace_A = [ gs.getA(trace[i][0]) for i in range(1000)]
[10]: trace_tau = np.array([ trace[i][3] for i in range(1000)])
[11]: mean_tau = np.mean(trace_tau)
[12]: \# use the posterior mean of tau to quickly estimate the marginal connecting
      \rightarrow probability
      tree.params[3] = mean_tau
      prob = tree.computeMarginalProb()
[13]: degree = np.vstack([trace_A[i].sum(0) for i in range(1000)])
 []:
[14]: from statsmodels.tsa.stattools import acf
      import arviz
[15]: acf_mat = np.vstack([ acf(degree[:,i], fft=False, nlags=40) for i in range(p)])
      acf mat[np.isnan(acf mat)]=0
      acf mat[:,0]=1
      ess = np.stack([arviz.ess(degree[:,i]) for i in range(p)])
 []:
[16]: | fig, ax = plt.subplots(1,3, gridspec_kw={'width_ratios': [1, 1,1] })
      fig.set_size_inches([9,3])
      ax[0].plot(degree[:,2])
      ax[0].set_title("Traceplot", y=-0.3)
      # ax[0].plot(np.arange(2000), degreee[:,299]+1)
      ax[1].boxplot(acf_mat[:,:40], showfliers=False,)
      ax[1].plot(np.arange(40)+1, acf_mat[:,:40].mean(0), color='red')
```

```
ax[1].set_xticks( np.arange(8)*5+1)
ax[1].set_xticklabels(np.arange(8)*5)
ax[1].set_title("ACF", y=-0.3)

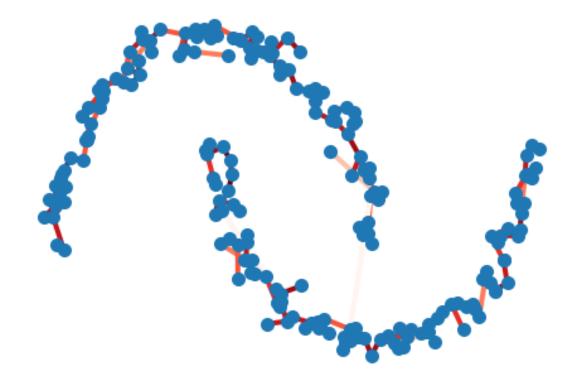
ax[2].boxplot(ess/1000, showfliers=False,)
ax[2].set_xticks( [1])
ax[2].set_xticklabels([""])
ax[2].set_title("ESS per iteration", y=-0.3)
fig.tight_layout(pad=1)
# fig.savefig("benchmark_gibbs.png")
```



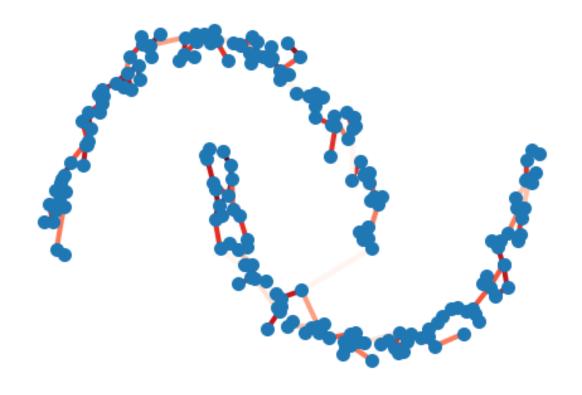
```
[17]: A1 = gs.getA(trace[0][0])
      A2 = gs.getA(trace[499][0])
      A3 = gs.getA(trace[999][0])
[18]: # from pylab import rcParams
      # rcParams['figure.figsize'] = 10, 8
      # rcParams['figure.dpi'] = 300
[19]: import networkx as nx
[20]: width =2
[21]: from matplotlib import cm
      cmap = cm.get_cmap('Reds', 10)
[22]: def pltGraph(A, color='r', usingWeight=True):
          M= nx.Graph(A)
          edges = M.edges()
          weights = [ np.log(prob[u][v]) for u,v in edges]
          if usingWeight:
              nx.draw(M,pos=Y,edge_color=weights,width=4, edge_cmap=cmap,__
       →node_size=100)
```

```
else:
    nx.draw(M,pos=Y,edge_color=color,width=4, node_size=100)
```

```
[23]: f = plt.figure()
pltGraph(A1)
# f.savefig("moons1.png")
```



```
[24]: f = plt.figure()
pltGraph(A3,'red')
# f.savefig("moons2.png")
```



[28]: <matplotlib.colorbar.Colorbar at 0x7f12fb2f06d0>

