

1. Decision Variables

+) $X[i,j,k] = 1$ if staff i work on phase k of day j , 0 otherwise Such that: $1 \leq i \leq N$, $1 \leq j \leq D$, $1 \leq k \leq 4$

2. Constraints

+) Each employee works no more than one shift every day:

$$\sum_{1 \leq k \leq 4} X[i,j,k] \leq 1, \text{ for } 1 \leq i \leq N, 1 \leq j \leq D$$

+) Employees can have a day off after having a night shift on the previous day

$$X[i,j-1,4] + \sum_{1 \leq k \leq 4} X[i,j,k] = 1, \text{ for } 1 \leq i \leq N, 1 \leq j \leq D$$

+) Employees will not work on their off days:

$$\sum_{1 \leq k \leq 4} X[i,j,k] = 0, \text{ for } 1 \leq i \leq N, j \in F[i]$$

+) Each shift will have at least α employees and β at most:

$$\alpha \leq \sum_{1 \leq i \leq N} X[i,j,k] \leq \beta, \text{ for } 1 \leq j \leq D, 1 \leq k \leq 4$$

3. Objective function

$$Z = \max \sum_{1 \leq j \leq D} x[i, j, 4], \text{ for } 1 \leq i \leq N$$

> Minimise Z