CMSC 330: Organization of Programming Languages

OCaml 2 Higher Order Functions

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Door

Tuples

- ▶ Constructed using (e1, ..., en)
- Deconstructed using pattern matching
 - Patterns involve parens and commas, e.g., (p1,p2, ...)
- ▶ Tuples are like C structs
 - · But without field labels
 - Allocated on the heap
- ▶ Tuples can be heterogenous
 - Unlike lists, which must be homogenous
 - (1, ["string1"; "string2"]) is a valid tuple

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Examples With Tuples

Another Example

List And Tuple Types

- ▶ Tuple types use * to separate components
- Examples

```
* (1, 2) :
* (1, "string", 3.5) :
* (1, ["a"; "b"], 'c') :
* [(1,2)] :
* [(1,2); (3, 4)] :
* [(1,2); (1,2,3)] :
```

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List And Tuple Types

- ▶ Tuple types use * to separate components
- Examples

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```
(1, 2): int * int
(1, "string", 3.5): int * string * float
(1, ["a"; "b"], 'c'): int * string list * char
[(1,2)]: (int * int) list
[(1,2); (3, 4)]: (int * int) list
[(1,2); (1,2,3)]: error
Because the first list element has type int * int, but the second has type int * int * int - list elements must all be of the same type
```

Polymorphic Types

- ▶ Some functions we saw require specific list types
 - let plusFirstTwo (x::y::_, a) = (x + a, y + a)
 plusFirstTwo : int list * int -> (int * int)
- ▶ But other functions work for any list

- ▶ OCaml gives such functions polymorphic types
 - hd : 'a list -> 'a
 - this says the function takes a list of any element type 'a, and returns something of that type

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Examples Of Polymorphic Types

Tuples Are A Fixed Size

- This OCaml definition
 - # let foo x = match x with

 (a, b) -> a + b

 | (a, b, c) -> a + b + c;;
- Would yield this error message
 - This pattern matches values of type a * 'b * 'c but is here used to match values of type d * 'e
- ▶ Tuples of different size have different types
 - Thus never more than one match case with tuples

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Conditionals

- ▶ Use if...then...else like C/Java/Ruby
 - · But no parentheses, no elsif, and no end

```
if grade >= 90 then
  print_string "You got an A"
else if grade >= 80 then
  print_string "You got a B"
else if grade >= 70 then
  print_string "You got a C"
else
  print_string "You're not doing so well"
```

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Conditionals (cont.)

- ▶ In OCaml, conditionals return a result
 - · The value of whichever branch is true/false
 - Like ?: in C, C++, and Java

```
# if 7 > 42 then "hello" else "goodbye";;
- : string = "goodbye"
# let x = if true then 3 else 4;;
x : int = 3
# if false then 3 else 3.0;;
This expression has type float but is here used with type int
```

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The Factorial Function

- Using conditionals & functions
 - Can you write fact, the factorial function?

```
let rec fact n =
  if n = 0 then
    1
  else
    n * fact (n-1);;
```

- Notice no return statements
 - · This is pretty much how it needs to be written

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Let Rec

- The rec part means "define a recursive function"
- Let vs. let rec
 - let x = e1 in e2 x in scope within e2
 - let rec x = e1 in e2 x in scope within e2 and e1
- ▶ Why use let rec?
 - If you used let instead of let rec to define fact

```
let fact n =
  if n = 0 then 1
  else n * fact (n-1) in e2
```

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Fact is not bound here!

Let – More Examples

```
▶ let f n = 10;;
let f n = if n = 0 then 1 else n * f (n - 1);;
```

- f 0;; (* 1 *)
- f 1;; (* 10 *)
- ▶ let f x = ... f ... in ... f ...
 - (* Unbound value f *)
- ▶ let rec f x = ... f ... in ... f ...
 - (* Bound value f *)

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Recursion = Looping

- ▶ Recursion is essentially the only way to iterate
 - (The only way we're going to talk about)
- Another example

```
let rec print_up_to (n, m) =
  print_int n; print_string "\n";
  if n < m then print_up_to (n + 1, m)</pre>
```

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Lists and Recursion

- Lists have a recursive structure
 - · And so most functions over lists will be recursive

```
let rec length 1 = match 1 with
   [] -> 0
   | (_::t) -> 1 + (length t)
```

- This is just like an inductive definition
 - > The length of the empty list is zero
 - > The length of a nonempty list is 1 plus the length of the tail
- Type of length?

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More Examples

```
, sum 1 (* sum of elts in 1 *)
let rec sum 1 = match 1 with
      [] -> 0
      | (x::xs) -> x + (sum xs)

, negate 1 (* negate elements in list *)
let rec negate 1 = match 1 with
      [] -> []
      | (x::xs) -> (-x) :: (negate xs)

, last 1 (* last element of 1 *)
let rec last 1 = match 1 with
      [x] -> x
      | (x::xs) -> last xs
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```

A Clever Version of Reverse

```
let rec rev_helper (1, a) = match 1 with
        [] -> a
        | (x::xs) -> rev_helper (xs, (x::a))
let rev 1 = rev_helper (1, [])

Let's give it a try
    rev [1; 2; 3] -
    rev_helper ([1;2;3], []) -
    rev_helper ([2;3], [1]) -
    rev_helper ([3], [2;1]) -
    rev_helper ([], [3;2;1]) -
    [3;2;1]
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```

More Examples (cont.)

```
(* return a list containing all the elements in the
   list 1 followed by all the elements in list m *)

   append (1, m)

let rec append (1, m) = match 1 with
   [] -> m
   | (x::xs) -> x:: (append (xs, m))

rev 1 (* reverse list; hint: use append *)

let rec rev 1 = match 1 with
   [] -> []
   | (x::xs) -> append ((rev xs), [x])

rev takes O(n²) time. Can you do better?

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```

More Examples

```
flattenPairs 1 (* ('a * 'a) list -> 'a list *)
let rec flattenPairs 1 = match 1 with
   [] -> []
   | ((a, b)::t) -> a :: b :: (flattenPairs t)

take (n, 1) (* return first n elts of 1 *)
let rec take (n, 1) =
   if n = 0 then []
   else match 1 with
      [] -> []
   | (x::xs) -> x :: (take (n-1, xs))

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```

Working With Lists

- Several of these examples have the same flavor
 - Walk through the list and do something to every element
 - · Walk through the list and keep track of something
- ▶ Recall the <u>following example code</u> from Ruby:

```
a = [1,2,3,4,5]

b = a.collect { |x| -x }
```

- · Here we passed a code block into the collect method
- Wouldn't it be nice to do the same in OCaml?

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Anonymous Functions

▶ Recall code blocks in Ruby

```
(1..10).each { |x| print x }
```

- Here, we can think of { |x| print x } as a function
- ▶ We can do this (and more) in Ocaml

```
range_each (1,10) (fun x -> print_int x)
```

```
• where
let rec range_each (i,j) f =
    if i > j then ()
    else
    let _ = f i in (* ignore result *)
    range_each (i+1,j) f
```

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Anonymous Functions

- ▶ Passing functions around is very common
 - So often we don't want to bother to give them names
- ▶ Use fun to make a function with no name

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All Functions Are Anonymous

► Functions are first-class, so you can bind them to other names as you like

```
let f x = x + 3
let g = f
g 5 = 8
```

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▶ In fact, let for functions is just shorthand

Examples

Currying

- We just saw a way for a function to take multiple arguments
 - The function consumes one argument at a time, returning a function that takes the rest
- ▶ This is called currying the function
 - · Named after the logician Haskell B. Curry
 - But Schönfinkel and Frege discovered it
 - > So it should probably be called Schönfinkelizing or Fregging

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Higher-Order Functions

 In OCaml you can pass functions as arguments, and return functions as results

```
let plus_three x = x + 3
let twice f z = f (f z)
twice plus_three 5
twice : ('a->'a) -> 'a -> 'a

let plus_four x = x + 4
let pick_fn n =
    if n > 0 then plus_three else plus_four
(pick_fn 5) 0
pick_fn : int -> (int->int)
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```

Curried Functions In OCaml

▶ OCaml has a really simple syntax for currying

```
let add x y = x + y
```

· This is identical to all of the following:

```
let add = (fun x -> (fun y -> x + y))
let add = (fun x y -> x + y)
let add x = (fun y -> x+y)
```

- ▶ Thus:
 - add has type int -> (int -> int)
 - add 3 has type int -> int
 - > add 3 is a function that adds 3 to its argument
 - (add 3) 4 = 7
- ► This works for any number of arguments

Curried Functions In OCaml (cont.)

- Because currying is so common, OCaml uses the following conventions:
 - · -> associates to the right
 - > Thus int -> int -> int is the same as
 > int -> (int -> int)
 - · function application associates to the left
 - > Thus add 3 4 is the same as
 - > (add 3) 4

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Mental Shorthand

- You can think of curried types as defining multiargument functions
 - Type int -> float -> float is a function that takes an int and a float and returns a float
 - Type int -> int -> int is a function that takes three ints and returns an int
- ► The bonus is that you can *partially* apply the function to some of its arguments
 - And apply that to the rest of the arguments later

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Another Example Of Currying

▶ A curried add function with three arguments:

```
let add_th x y z = x + y + z
```

• The same as

```
let add_th x = (fun y \rightarrow (fun z \rightarrow x+y+z))
```

- Then...
 - add th has type int -> (int -> int))
 - add th 4 has type int -> (int -> int)
 - add_th 4 5 has type int -> int
 - add th 4 5 6 iS 15

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Implementing this is Challenging!

- Implementing functions that return other functions requires a clever data structure called a closure
 - We'll see how these are implemented later
- ▶ In the meantime, we will explore using higher order functions, and then discuss how they are implemented

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The Map Function

- ▶ Let's write the map function (like Ruby's collect)
 - Takes a function and a list, applies the function to each element of the list, and returns a list of the results

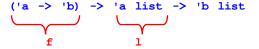
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The Map Function (cont.)

▶ What is the type of the map function?

```
let rec map f l = match l with
    [] -> []
    | (h::t) -> (f h)::(map f t)
```



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Pattern Matching With Fun

match can be used within fun

```
map (fun 1 -> match 1 with (h::_) -> h)
[ [1; 2; 3]; [4; 5; 6; 7]; [8; 9] ]
= [1; 4; 8]
```

- ▶ But use named functions for complicated matches
- ▶ May use standard pattern matching abbreviations

```
map (fun (x, y) \rightarrow x+y) [(1,2); (3,4)]
= [3; 7]
```

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The Fold Function

- Common pattern
 - Iterate through list and apply function to each element, keeping track of partial results computed so far

```
let rec fold f a l = match l with
    [] -> a
    | (h::t) -> fold f (f a h) t
```

- a = "accumulator"
- Usually called fold left to remind us that f takes the accumulator as its first argument
- What's the type of fold?

```
= ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a

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```

Example

Using Fold to Build Reverse

```
let rec fold f a l = match l with
    [] -> a
    | (h::t) -> fold f (f a h) t
```

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▶ Can you build the reverse function with fold?

```
let prepend a x = x::a

fold prepend [] [1; 2; 3; 4] →

fold prepend [1] [2; 3; 4] →

fold prepend [2; 1] [3; 4] →

fold prepend [3; 2; 1] [4] →

fold prepend [4; 3; 2; 1] [] →

[4; 3; 2; 1]
```

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Another Example

```
let rec fold f a 1 = match 1 with
        [] -> a
        | (h::t) -> fold f (f a h) t

let next a _ = a + 1
    fold next 0 [2; 3; 4; 5] →
    fold next 1 [3; 4; 5] →
    fold next 2 [4; 5] →
    fold next 3 [5] →
    fold next 4 [] →

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We just built the length function!

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```