

Incorporating stochastic sensitivity as an uncertainty measure for data assimilation and parcel trajectories in geophysical flows

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Dedication

Abstract

Chapter ?? introduces

Chapter 1

Background

1.1 Lagrangian Dynamics

1.2 Probability Theory

(Brémaud 2020)

1.3 Stochastic Differential Equations

(Kallianpur & Sundar 2014)

1.4 Stochastic Sensitivity

Balasuriya (2020) introduces stochastic sensitivity as a new tool for quantifying the impact of Eulerian uncertainty on Lagrangian trajectories.

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