

random variable: function from sample space to real #

↓  
capital  
letters

$$X: S \rightarrow \mathbb{R}$$

$$\text{ex: } S = \{1, 2, 3, \dots, 6\}$$

$$X(1) = 1$$

$$X(2) = 4$$

$$X(3) = 9$$

ex2: could assign  
1 to evens + 2 to  
odds

ex: coin flipped 5x's.

sequence of H/T a random variable

$$\{(HHTHH), (HTTTT), \dots\}$$

$$X(HTTTH) = 3$$

$$X(HHHTH) = 1$$

number of sets or subsets

} # tails

$$\text{ex2: } \{r_1, r_2, r_3, \dots, r_n\}$$

$$X(r_i) = \text{number of tails} - \text{discrete}$$

$$Y(r_i) = \text{length of tail} \left. \vphantom{\begin{matrix} X(r_i) \\ Y(r_i) \end{matrix}} \right\} \text{continuous}$$

$$Z(r_i) = \text{weight}$$

$$T(r_i) = \text{number of offspring} - \text{discrete}$$

discrete - only countable list of values "staircase"

continuous - use calculus "escalator"

## Discrete Random Variables

every random var has a probability distribution  
- assigns prob of getting that #

ex: flip 2 coins

$$S = \{HH, HT, TH, TT\}$$

$$X(w) = \# \text{ tails}$$



$$P(x) = P(X=x)$$

support of  $X$   
 $X(s) = 0, 1, 2 \leftarrow$  possibilities for  $X(w)$   
 no tails, 1 tail, 2 tails  
 $P(0) = P(X=0) = 1/4$   
 $P(1) = P(X=1) = 1/2$   
 $P(2) = P(X=2) = 1/4$   
 $P(\text{value of random var is 2})$

ex: 3 machines

$P(X \text{ working given random thing})$   
 so w's associated w/ #'s here  
 $\downarrow$

$S = \{www, \text{wwf}, \text{wfw}, \dots\}$   
 associate w/ 2

$$X(s) = \{0, 1, 2, 3\}$$

$$\sum_{x \in X(s)} P(x)$$

$$[0, 1]$$

ex:	0	1	2	3
$P(x)$	0.12	0.27	0.46	0.15

$$P(\text{at least 1}) = 1 - 0.12$$



population mean:

$$\mu = E(X) = \sum_x x P(x)$$

\* long term average of  $X$

ex: Die roll

$$P(x) = 1/6 \quad x \in \{1, 2, \dots, 6\} \rightarrow$$

$$\mu = ?$$

$$E(X) = \sum_{x \in X(s)} x P(x)$$

$$\begin{aligned}
 &= 1 \cdot 1/6 + 2 \cdot 1/6 + 3 \cdot 1/6 + \\
 &\quad 4 \cdot 1/6 + 5 \cdot 1/6 + 6 \cdot 1/6 \\
 &= 1/6 (1 + 2 + 3 + 4 + 5 + 6)
 \end{aligned}$$

ex: machine

0	1	2	3
0.12	0.27	0.46	0.15

1 = one working

$$\begin{aligned}
 \sum x P(x) &= 0(0.12) + 1(0.27) + \\
 &\quad 2(0.46) + 3(0.15) \\
 &= 1.64
 \end{aligned}$$

2=two working  
3=three working