



北京邮电大学软件学院

School Of software Engineering Of BUPT

厚德 博学 敬业 乐群



Operating Systems

Lecture 8 Virtual Memory

Jinpengchen

Email: jpchen@bupt.edu.cn



Catalog Description

- ⊕ Background
- ⊕ Demand Paging
- ⊕ Page Replacement
- ⊕ Allocation of Frames
- ⊕ Thrashing



Background

- ❖ Instructions must be loaded into memory before execution.
- ❖ Solutions in last chapter : Program entire → Physical memory
- ❖ Sometimes, **jobs** may be **too big** or **too many**.

How to expand the main memory?

- ❖ Physically? **COST TOO HIGH!**
- ❖ Logically? **✓**



Background

Virtual memory: Why and How?

- ❑ Some code may get no, or only little, opportunity of execution,
 - for example, code for error handlers
- ❑ Some data may get no opportunity of access
- ❑ Locality of reference (程序的局部性原理), 1968, Denning
 - ✓ Temporal locality (时间局部性)
 - ✓ Spatial locality (空间局部性)
- ❑ Idea: partly loading (部分装入)、demand loading (按需装入)、replacement (置换)



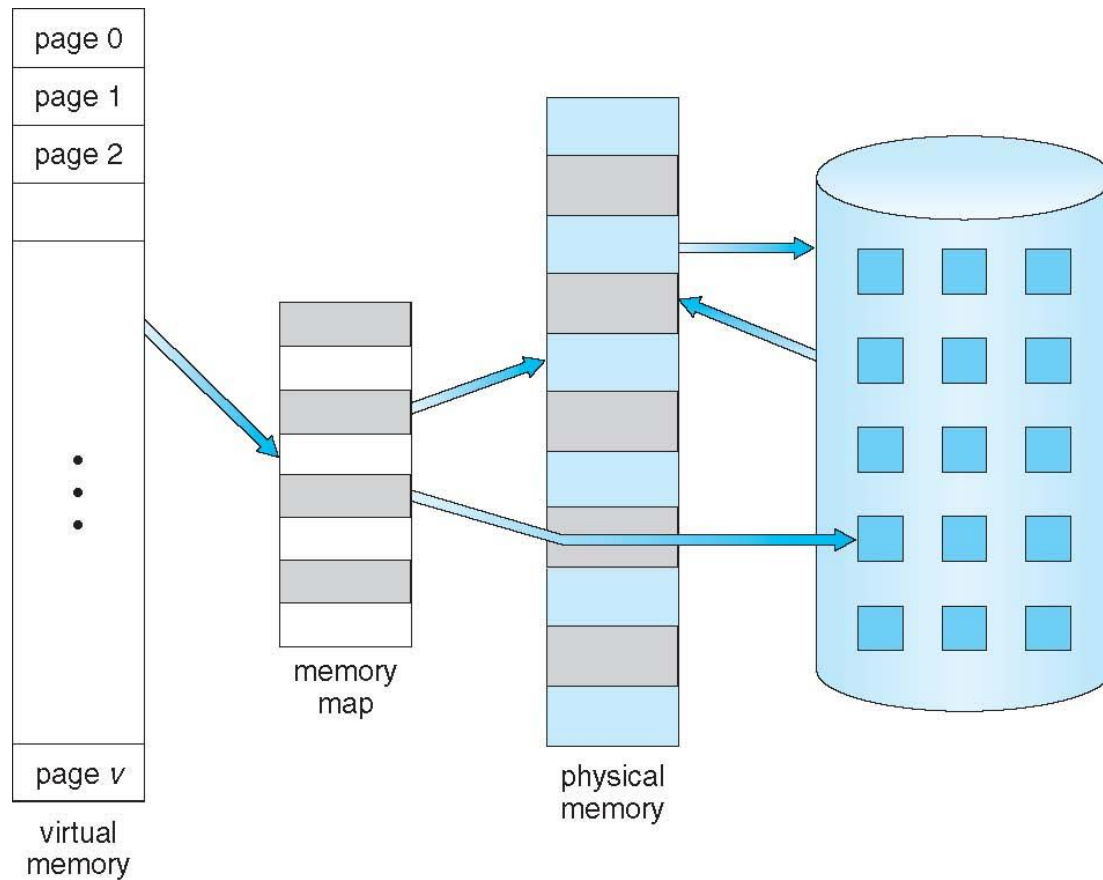
Background

- Virtual Memory (虚拟存储器) 是指具有请求调页功能和置换功能，能从逻辑上对内存容量加以扩充的一种存储器系统
 - Logical size:
 - 从系统角度看：内存容量 + 外存容量
 - 从进程角度看：地址总线宽度范围内；内存容量 + 外存容量
 - Speed: close to main memory
 - Cost per bit: close to secondary storage (disks)
- Virtual memory : separation of user logical memory from physical memory.
 - Only part of the program needs to be in memory for execution
 - Logical address space can therefore be much larger than physical address space
 - Allows address spaces to be shared by several processes
 - Allows for more efficient process creation



Background

Virtual Memory That is Larger Than Physical Memory





Background

- ✚ Virtual memory can be implemented via:
 - ✚ Demand paging
 - ✓ Paging technology + pager (请求调页) and page replacement
 - ✓ Pager VS. swapper
 - the unit of swapping in/out is not the entire process but page.
 - ✚ Demand segmentation



Background

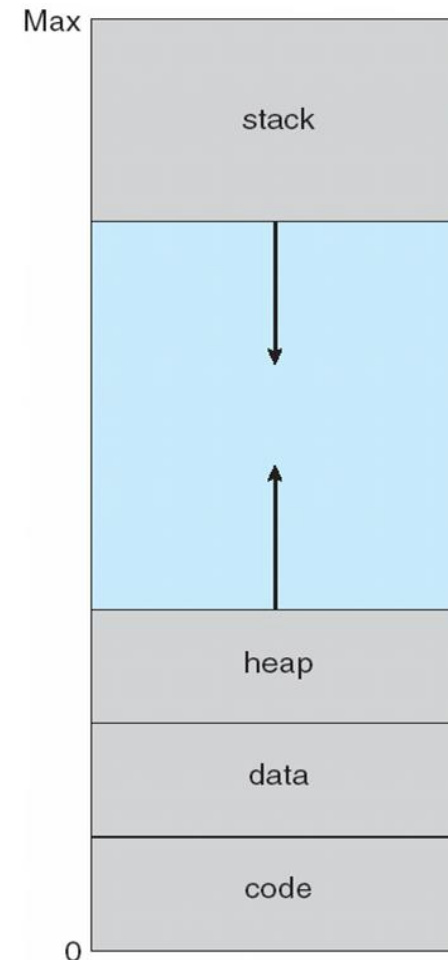
- ✿ 虚拟存储器的特征
 - ✦ 多次性：最重要的特征
 - ✓ 一个作业被分成多次装入内存运行
 - ✦ 对换性
 - ✓ 允许在进程运行的过程中，（部分）换入换出
 - ✦ 虚拟性
 - ✓ 逻辑上的扩充
 - ✦ 虚拟性是以多次性和对换性为基础的。
 - ✦ 多次性和对换性是建立在离散分配的基础上的



Background

Virtual-address Space (虚拟地址空间)

- ❖ The virtual address space of a process refers to the logical (or virtual) view of how a process is stored in memory.
 - ✓ Typically: $0 \sim \text{xxx}$ & exists in contiguous memory
- ❖ In fact, the physical memory are organized (partitioned) in page frames & the page frames assigned to a process may not be contiguous \Rightarrow MMU

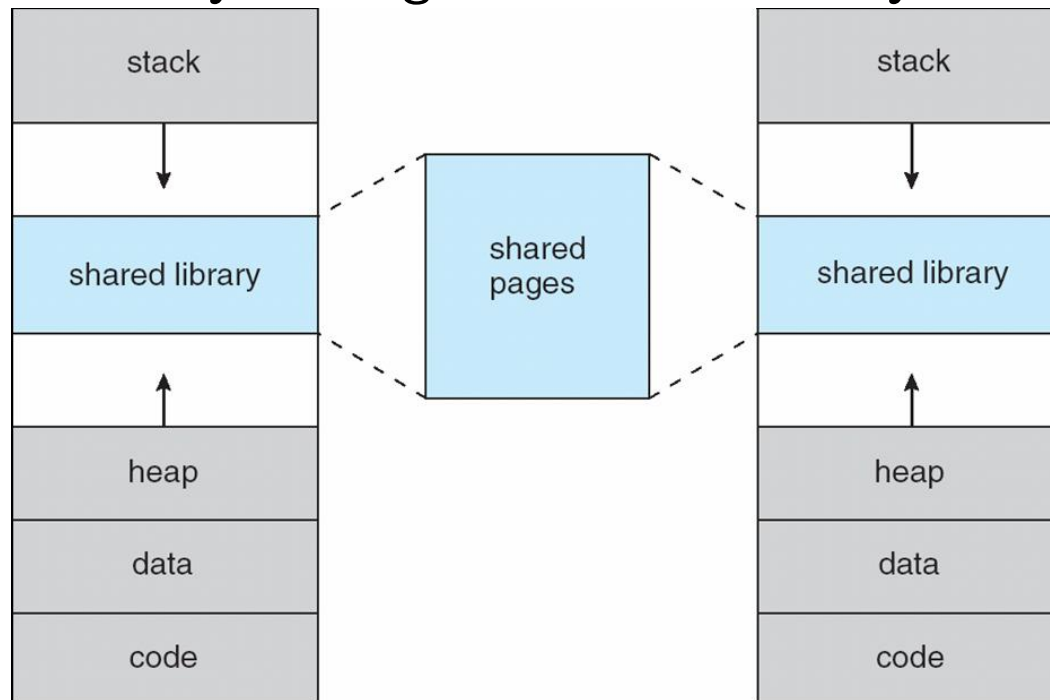




Background

Some benefits

Shared library using virtual memory



Shared memory

Speeding up process creation



Background

Some benefits

- ❑ Programmers need not care about memory limitations
- ❑ More programs could be run simultaneously
- ❑ Less I/O needed, each user program would run faster



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Demand Paging

- Do not load the entire program in physical memory at program execution time.
NO NEED!
- Bring a page into memory only when it is needed
 - Less I/O needed
 - Less memory needed
 - Faster response
 - More users
- A page is needed \Leftarrow Reference to it
 - Invalid reference \Rightarrow Abort
 - Not-in-memory \Rightarrow Bring to memory



Demand Paging

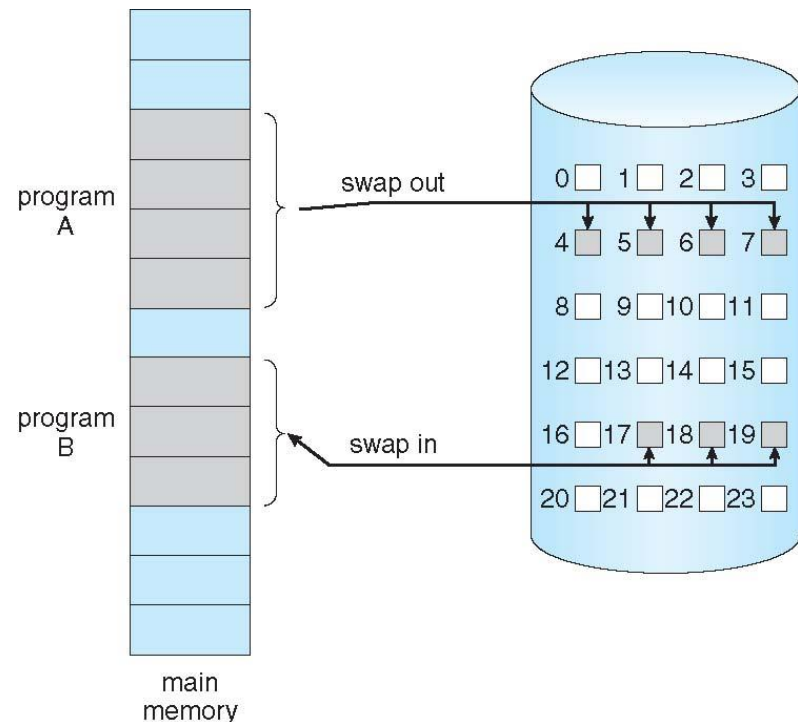
Swapper VS. Pager

- ❑ A swapper manipulates the entire processes
- ❑ Lazy swapper

Never swaps a page into memory unless the page will be needed

✓ Swapper that deals with individual pages is a **pager**

Example: Transfer of
a Paged Memory to
Contiguous Disk Space





Demand Paging

- ✚ Basic Concepts (Hardware support)
 - ✚ The modified page table mechanism
 - ✚ Page fault
 - ✚ Address translation
 - ✚ Secondary memory (as swap space)



Demand Paging

✚ The modified page table mechanism

✚ Valid-Invalid Bit (PRESENT bit)

- ✓ Each page table entry is associated with a valid-invalid bit

$v \Rightarrow$ in-memory & legal,

$i \Rightarrow$ not-in-memory

- ✓ Initially, the valid-invalid bit is set to i on all entries
- ✓ During address translation, if the valid-invalid bit in page table entry is $i \Rightarrow$ page fault

✚ Reference bits (for pager out)

✚ Modify bit (or dirty bit)

✚ Secondary storage info (for pager in)

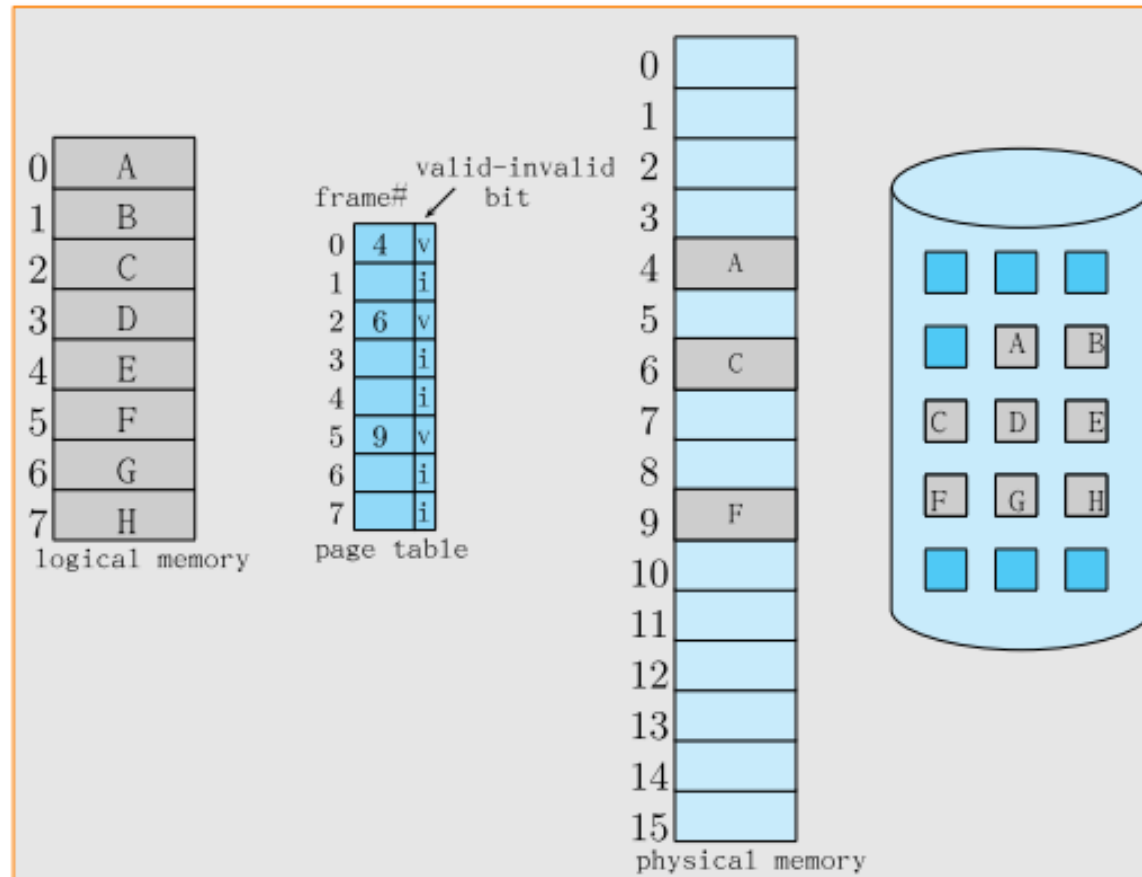
Frame #	valid-invalid bit
	v
	v
	v
	v
	i
	i
	i

page table



Demand Paging

- ✱ The modified page table mechanism
 - ✱ Page table when some pages are not in main memory

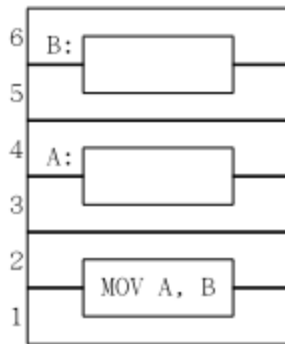




Demand Paging

❖ Page Fault (缺页故障)

- ❖ First reference to a page will trap to OS:
 - ✓ page fault(缺页故障/异常/中断)
- ❖ Page fault trap (缺页异常)
 - ✓ Exact exception (trap), 精确异常
 - Restart the process in the exactly same place and state.
 - Re-execute the instruction which triggered the trap
- ❖ Execution of one instruction may cause multiply page faults



- ❖ Page fault may occur at every memory reference
- ❖ One instruction may cause multiply page faults while fetching instruction or r/w operators

Example: One instruction and 6 page faults



Demand Paging

❁ Page Fault (缺页故障)

❁ Page Fault Handling:

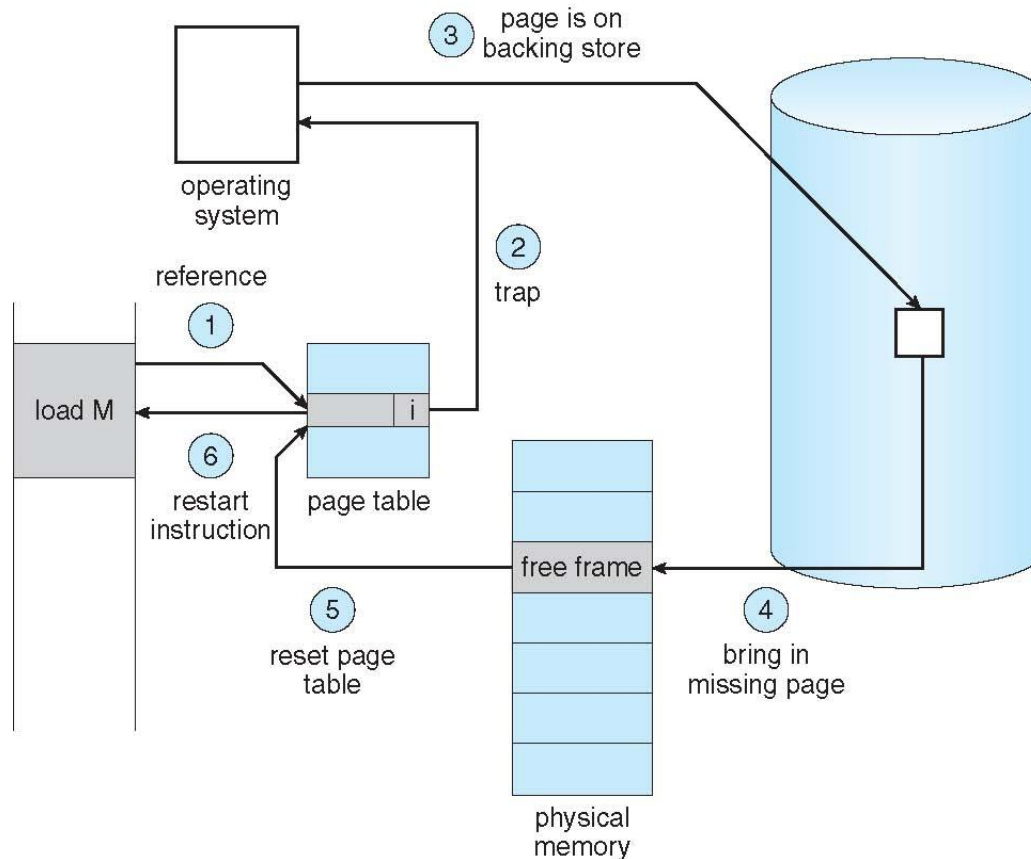
- ✓ OS **looks at** an internal table to decide:
 - Invalid reference \Rightarrow abort
 - Just not in memory \Rightarrow **bring to memory**
- ✓ **Get** an empty frame from the free frame list
- ✓ **Swap** page into frame
 - Pager out & pager in
- ✓ **Modify** the internal tables & Set validation bit = v
- ✓ **Restart** the instruction that caused the page fault



Demand Paging

Page Fault (缺页故障)

Steps in Handling a Page Fault





Demand Paging

❖ Page Fault (缺页故障)

❖ Restart instruction

$C = A + B$

- ✓ 1. fetch the instruction
- ✓ 2. fetch A
- ✓ 3. fetch B
- ✓ 4. Add A and B
- ✓ 5. Store the sum in C (C not in memory)

❖ Problem can be ignored

- ✓ Repetition
- ✓ 1 instruction causes N page faults



Demand Paging

- ✧ Address translation

- ✓ Address translation hardware + page fault handling

- ✧ Resume the execution

- ✦ Context save (保存现场)

- Before OS handling the page fault, the state of the process must be saved

- ✓ Example: record its register values, PC

- ✦ Context restore (恢复现场)

- The saved state allows the process to be resumed from the line where it was interrupted.

- ✦ NOTE: distinguish the following **two** situations

- ✓ Illegal reference \Rightarrow The process is terminated
 - ✓ Page fault \Rightarrow Load in or pager in



Demand Paging

Performance of Demand Paging

- Let p = Page Fault Rate ($0 \leq p \leq 1.0$)
 - ✓ If $p = 0$, no page faults
 - ✓ If $p = 1.0$, every reference is a fault, **Pure Demand Page**

Effective Access Time (EAT)

$$\begin{aligned} \text{EAT} &= (1 - p) \times \text{memory access} \\ &+ p \times \text{page fault time} \end{aligned}$$

$$\begin{aligned} \text{page fault time} &= \text{page fault overhead} \\ &+ \text{swap page out}(\text{optional}) \\ &+ \text{swap page in} \\ &+ \text{restart overhead} \end{aligned}$$



Demand Paging

❁ Performance of Demand Paging

❁ Example

✓ Memory access time = 200ns

✓ Average page-fault service time = 8ms

$$\begin{aligned} \text{EAT} &= (1-p) \times 200 + p \times 8\text{ms} = (1-p) \times 200 + p \times 8,000,000 \\ &= 200 + p \times 7,999,800 \end{aligned}$$

✓ If one access out of 1,000 causes a page fault, then

$$p = 0.001$$

$$\text{EAT} = 8,199.8\text{ns} = 8.2\mu\text{s}$$

This is a slowdown by a factor of $8.2\mu\text{s}/200\text{ns} = 40!!$

✓ If we want performance degradation < 10%, then

$$\text{EAT} = 200 + p \times 7,999,800 < 200 (1 + 10\%) = 220$$

$$p \times 7,999,800 < 20$$

$$p < 20/7,999,800 \approx 0.0000025$$



Demand Paging

❖ Performance of Demand Paging

❖ Method for better performance

✓ To keep the fault time low

- Swap space, faster than file system
- Only dirty page is swapped out, or
- Demand paging only from the swap space, or
- Initially demand paging from the file system, swap out to swap space, and all subsequent paging from swap space

✓ Keep the fault rate extremely low

- Localization of program executing
Time, space



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Page Replacement

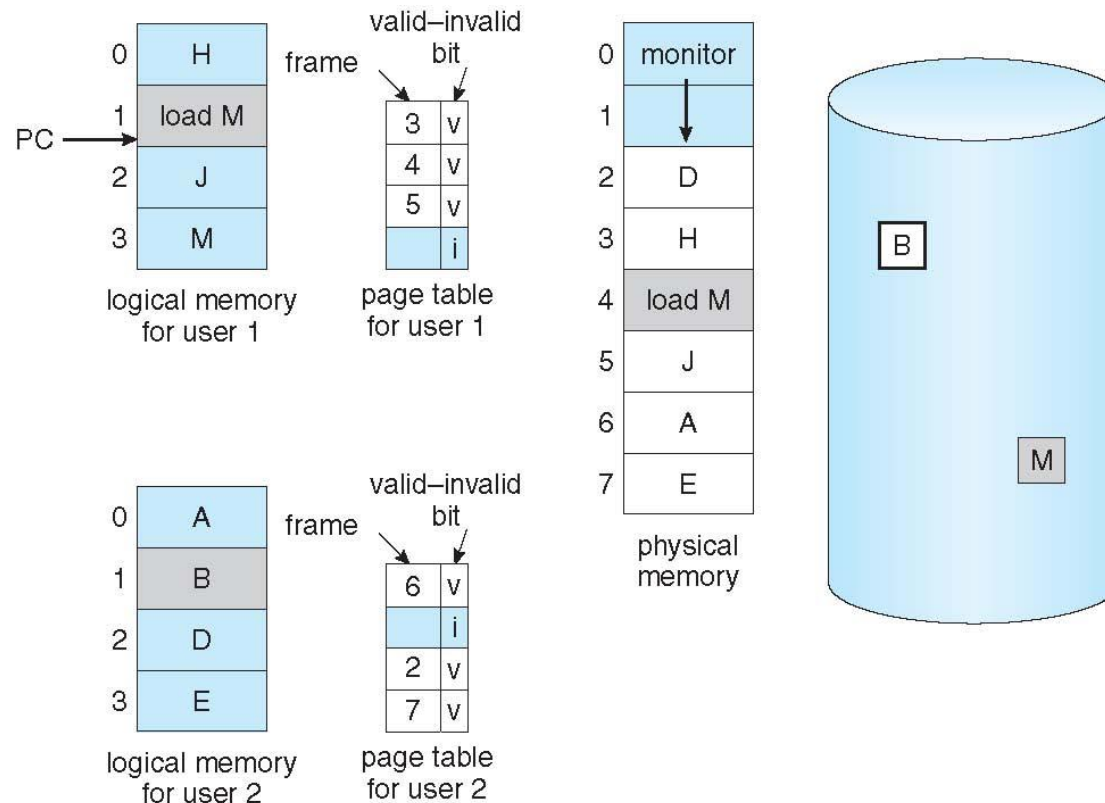
- ✚ What happens if there is no free frame?
 - ✚ Find some page in memory, but not really in use, swap it out
 - ✓ Algorithm?
 - ✓ Performance?
 - want an algorithm which will result in minimum number of page faults
 - ✓ Same page may be brought into memory several times



Page Replacement

Need of Page Replacement (页面置换)

- Free page frame is managed by OS using free-frame-list
- Over-allocation**: No free frames; All memory is in use.





Page Replacement

✚ What happens if there is no free frame?

✚ **Solution:**

Page replacement (页面置换)

Prevent over-allocation of memory by modifying page-fault service routine to include page replacement



Page Replacement

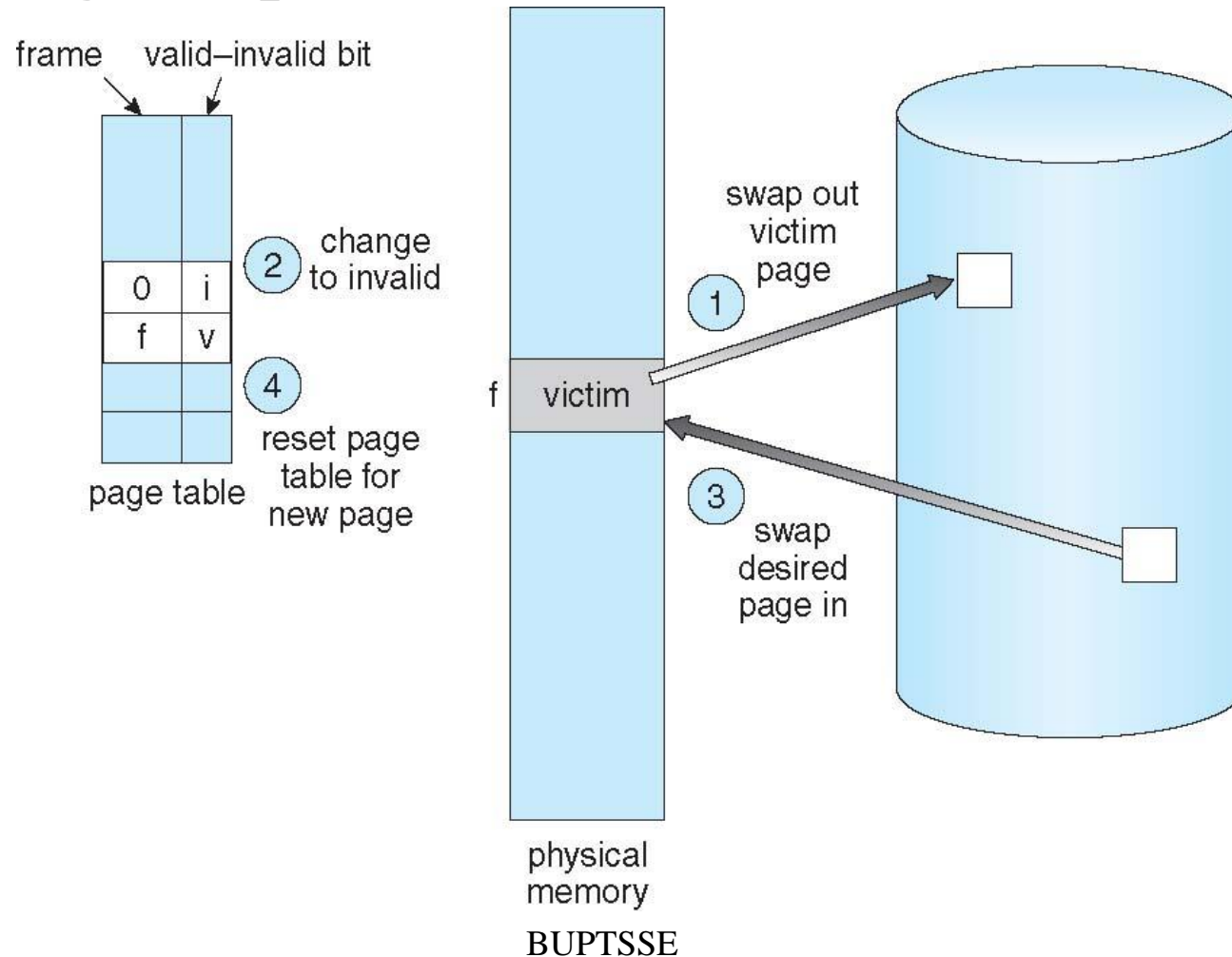
❖ Basic Page Replacement

- ❖ **Find** the location of the desired page on disk
- ❖ **Find** a free frame:
 - ✓ If there is a free frame, use it
 - ✓ If there is no free frame, use a page replacement algorithm to select a victim frame
- ❖ **Bring** the desired page into the (newly) free frame;
Update the page and frame tables
- ❖ **Restart** the process



Page Replacement

Basic Page Replacement





Page Replacement

Basic Page Replacement

- ❏ **NO MODIFY, NO WRITTEN** (to disk/swap space)
 - ✓ Use **modify (dirty) bit** to reduce overhead of page transfers
 - Only modified pages are written to disk
 - ✓ This technique also applies to read-only pages
 - For example, pages of binary code
- ❏ Page replacement completes separation between logical memory and physical memory
 - ✓ Large virtual memory can be provided on a smaller physical memory
- ❏ Demand paging, to obtain the lowest page-fault rate, two major problems
 - ✓ Frame-allocation algorithms
 - ✓ Page-replacement algorithms



Page Replacement

Page Replacement Algorithms

- ❏ **GOAL**: to obtain the lowest page-fault rate
- ❏ Different algorithms are evaluated by running it on a particular string of memory references (**reference string**) and computing the number of **page faults** on that string
- ❏ A **reference string** is a sequence of addresses referenced by a program

Example:

✓ An address reference string:

0100 0432 0101 0612 0102 0103 0104 0101 0611 0103
0104 0101 0610 0102 0103 0104 0101 0609 0102 0105

✓ Assuming page size = 100B, then its corresponding page reference string is:

1 4 1 6 1 6 1 6 1 6 1

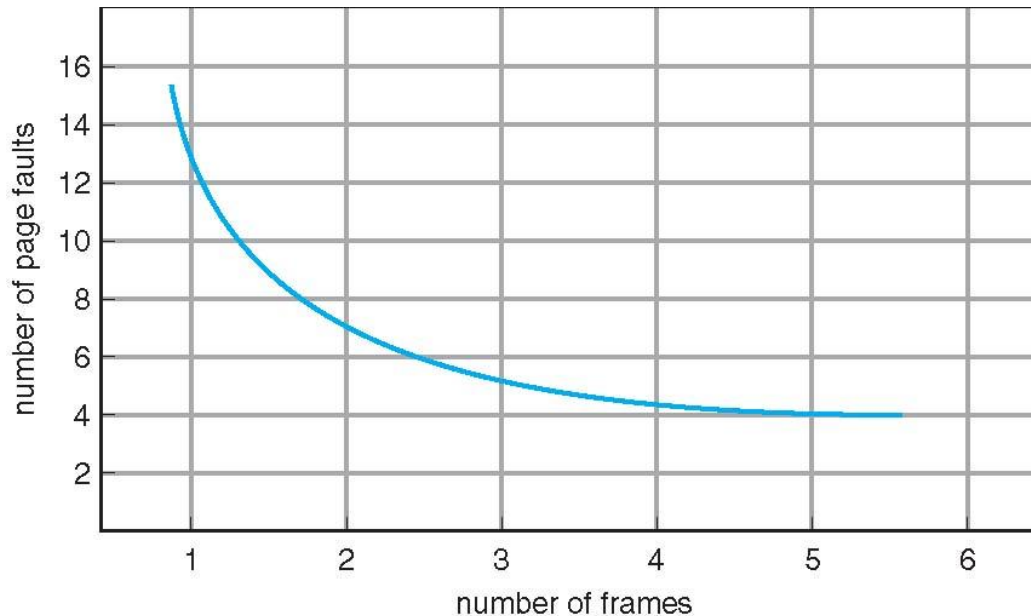


Page Replacement

Page Replacement Algorithms

How many page faults?

- ✓ Determined by the number of page frames assigned to the process
- ✓ For the upper example: 1 4 1 6 1 6 1 6 1 6 1
 - If ≥ 3 , then only 3 page faults
 - If $= 1$, 11 pages faults



Graph of Page Faults Versus The Number of Frames



Page Replacement

❖ Page Replacement Algorithms

❖ In all our examples, the reference strings are

✓ 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

✓ 7, 0, 1, 2, 0, 3, 0, 4, 2, 3, 0, 3, 2,
1, 2, 0, 1, 7, 0, 1



First-In-First-Out (FIFO) Algorithm

- ✚ The **simplest** page-replacement algorithm: **FIFO**
 - ✚ For each page: a time when it was brought into memory
 - ✚ For replacement: **the oldest page is chosen**
 - ✚ Data structure: a FIFO queue
 - ✓ Replace the page at the head of the queue
 - ✓ Insert a new page at the end of the queue
 - ✚ Example 1: **15 page faults, 12 page replacements**

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2
	0	0	0
		1	1

2	2	4	4	4	0
3	3	3	2	2	2
1	0	0	0	3	3

0	0
1	1
3	2

7	7	7
1	0	0
2	2	1

page frames



First-In-First-Out (FIFO) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
 - 3 frames (3 pages can be in memory at a time per process)

1	1	4	5	
2	2	1	3	9 page faults
3	3	2	4	

- 4 frames

1	1	5	4	
2	2	1	5	10 page faults
3	3	2		
4	4	3		

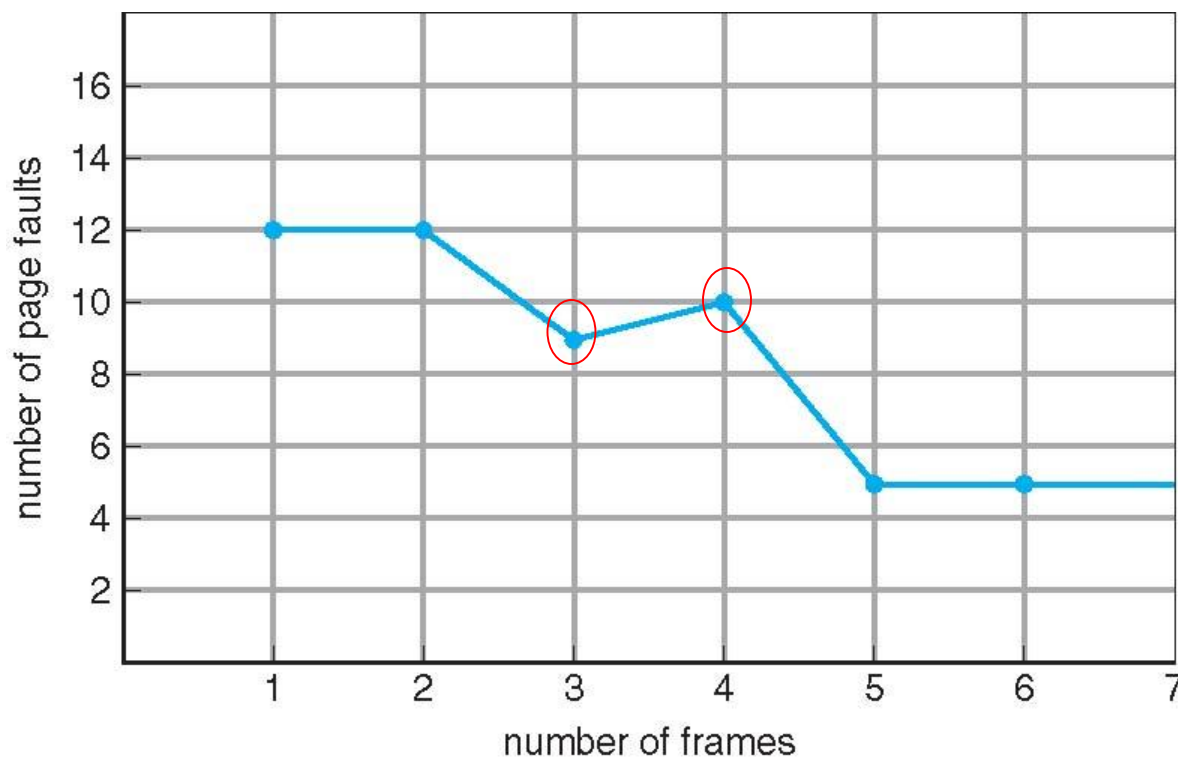


First-In-First-Out (FIFO) Algorithm

More memory, better performance? MAY BE NOT!!

❖ **Belady's anomaly** (贝莱迪异常现象):

more frames \Rightarrow more page faults



FIFO
illustrating
Belady's
Anomaly



Optimal Algorithm

Optimal page-replacement algorithm:

Replace page that will not be used for longest period of time

- It has the lowest page-fault rate

- It will never suffer from Belady's anomaly

Example 1: 9 page faults, 6 page replacements

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		2		2		2		2				7		
	0	0	0		0		4		0		0		0				0		
		1	1		3		3		3		1						1		

page frames



Optimal Algorithm

4 frames example

1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

1	4
2	6 page faults
3	
4	5

OPT: Difficult to implement

❏ How to know the future knowledge of the reference string?

❏ So, it is **only used for measuring** how well other algorithm performs



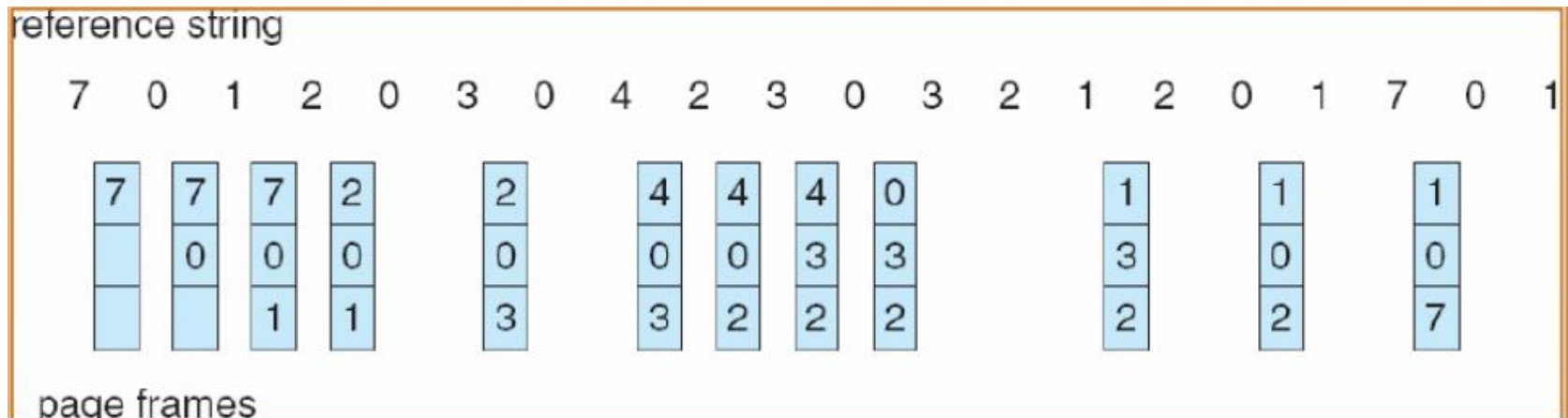
Least Recently Used (LRU) Algorithm

- LRU: an approximation of the OPT algorithm

Use the recent past as an approximation of the near future

- ❖ To replace the page that **has not been used for the longest period of time**
- ❖ For each page: a time of its last use
- ❖ For replace: the oldest time value

- Example 1: 12 page faults, 9 page replacements





Least Recently Used (LRU) Algorithm

Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5

1	1	1	1	5
2	2	2	2	2
3	5	5	4	4
4	4	3	3	3

8 page faults



Least Recently Used (LRU) Algorithm

HOW to implement LRU replacement?

❏ Counter implementation

- ✓ Every page entry has a counter;
every time page is referenced through this entry, copy the clock into the counter
- ✓ When a page needs to be changed, look at the counters to determine which are to be changed

❏ Stack implementation – keep a stack of page numbers in a double link form:

- ✓ When a page is referenced: Move it to the top
 - Requires 6 pointers to be changed
- ✓ Each update is a bit more expensive
- ✓ No search for replacement



Least Recently Used (LRU) Algorithm

- Use of a Stack to Record the Most Recent Page References

reference string

4 7 0 7 1 0 1 2 1 2 7 1 2

2
1
0
7
4

stack
before
a

7
2
1
0
4

stack
after
b

↑ ↑
a b



LRU Approximation Algorithms

✧ Reference bit

- ✧ Each page is associated with a bit, initially = 0
- ✧ When page is referenced, this bit is set to 1
- ✧ Replace the one which is 0 (if one exists)
 - ✓ However, we do not know the order

✧ Additional-Reference-Bits Algorithm:

- ✧ Record each entry of a page table with a 8-bit byte
- ✧ At a regular interval, a timer interrupt transfers the control to the OS

Reference bits + time ordering, for example: 8 bits

- ✓ HW modifies the highest bit, only
- ✓ Periodically, right shift the 8 bits for each page
- ✓ 00000000, ..., 01110111, ..., 11000100, ..., 11111111



LRU Approximation Algorithms

- ✿ Second chance (clock) Algorithm
 - ✦ Need **only 1 reference bit**, modified FIFO algorithm
 - ✦ Clock replacement
 - ✓ First, a page is selected by FIFO
 - ✓ If the page to be replaced (in clock order) has reference bit = 0, then replace
 - ✓ If the page to be replaced (in clock order) has reference bit = 1, then:
 - set reference bit 0
 - leave page in memory
 - replace next page (in clock order), subject to same rules

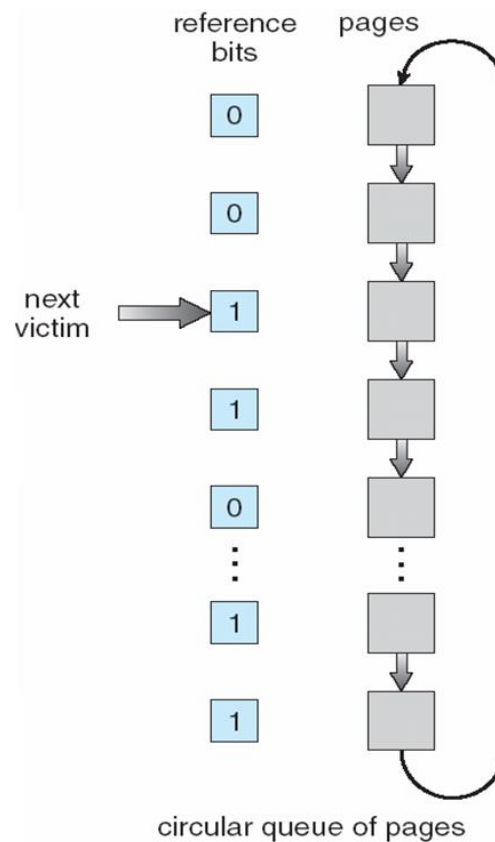


LRU Approximation Algorithms

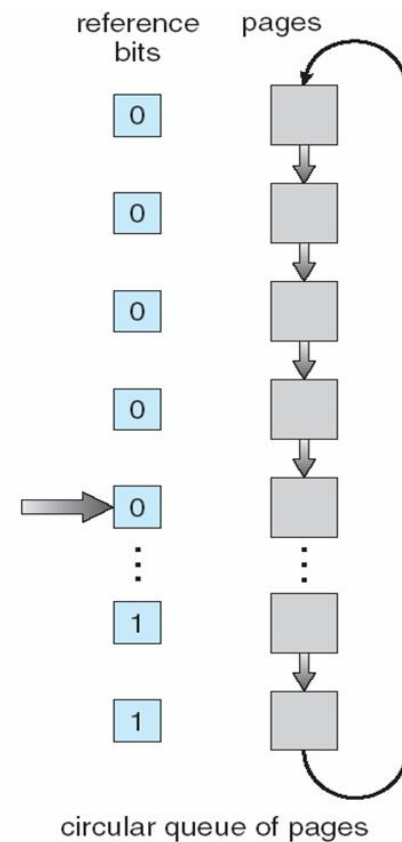
Second chance (clock) Algorithm

Implementation: Clock replacement

✓ Clock order



(a)



(b)



Counting Algorithms

❁ Counting algorithms:

Keep a counter of the number of references that have been made to each page

❁ LFU(Least Frequently Used) Algorithm:

replaces page with the smallest count

✓ Problem: heavily used initially, then never used

✓ Solution: shift the counts right by 1 bit to decay the average usage count

❁ MFU(Most Frequently Used) Algorithm: based on the argument that the page with the smallest count was probably just brought in and has yet to be used



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Allocation of Frames

Minimum the number of pages

- ❑ Each process needs the minimum number of pages
- ❑ Determined by ISA (Instruction-Set Architecture)
 - ✓ We must have enough frames to hold all the different pages that any single instruction can reference
- ❑ Example: IBM 370
 - 6 pages to handle MOVC instruction:
 - ✓ Instruction is 6 bytes, might span 2 pages
 - ✓ 2 pages to handle from
 - ✓ 2 pages to handle to
- ❑ Two major allocation schemes
 - ✓ Fixed allocation; priority allocation
- ❑ Two replacement policy
 - ✓ Global vs. local



Allocation of Frames

Fixed allocation

✚ Equal allocation

- ✚ For example, if there are 100 frames and 5 processes, give each process 20 frames.

frame number for any process = m/n

m = total memory frames

n = number of processes



Allocation of Frames

Fixed allocation

✦ Proportional allocation

✦ Allocate according to the size of process

✓ example:

s_i = size of process p_i

$S = \sum s_i$

m = total number of frames

a_i = allocation for $p_i = \frac{s_i}{S} \times m$

$m = 64$

$s_1 = 10$

$s_2 = 127$

$a_1 = \frac{10}{137} \times 64 \approx 5$

$a_2 = \frac{127}{137} \times 64 \approx 59$



Allocation of Frames

✚ Priority Allocation

- ✚ Use a proportional allocation scheme **using priorities** rather than size
- ✚ If process P_i generates a page fault,
 - ✓ Select for replacement one of its frames
 - ✓ Select for replacement a frame from a process with lower priority number



Allocation of Frames

✚ Replacement policy: Global vs. Local Allocation

✚ Global replacement

process selects a replacement frame from the set of all frames; one process can take a frame from another

✓ **Problem:** a process cannot control its own page-fault rate

✚ Local replacement

✓ each process selects a frame from only its own set of allocated frames

✓ **Problem:** less used pages of memory



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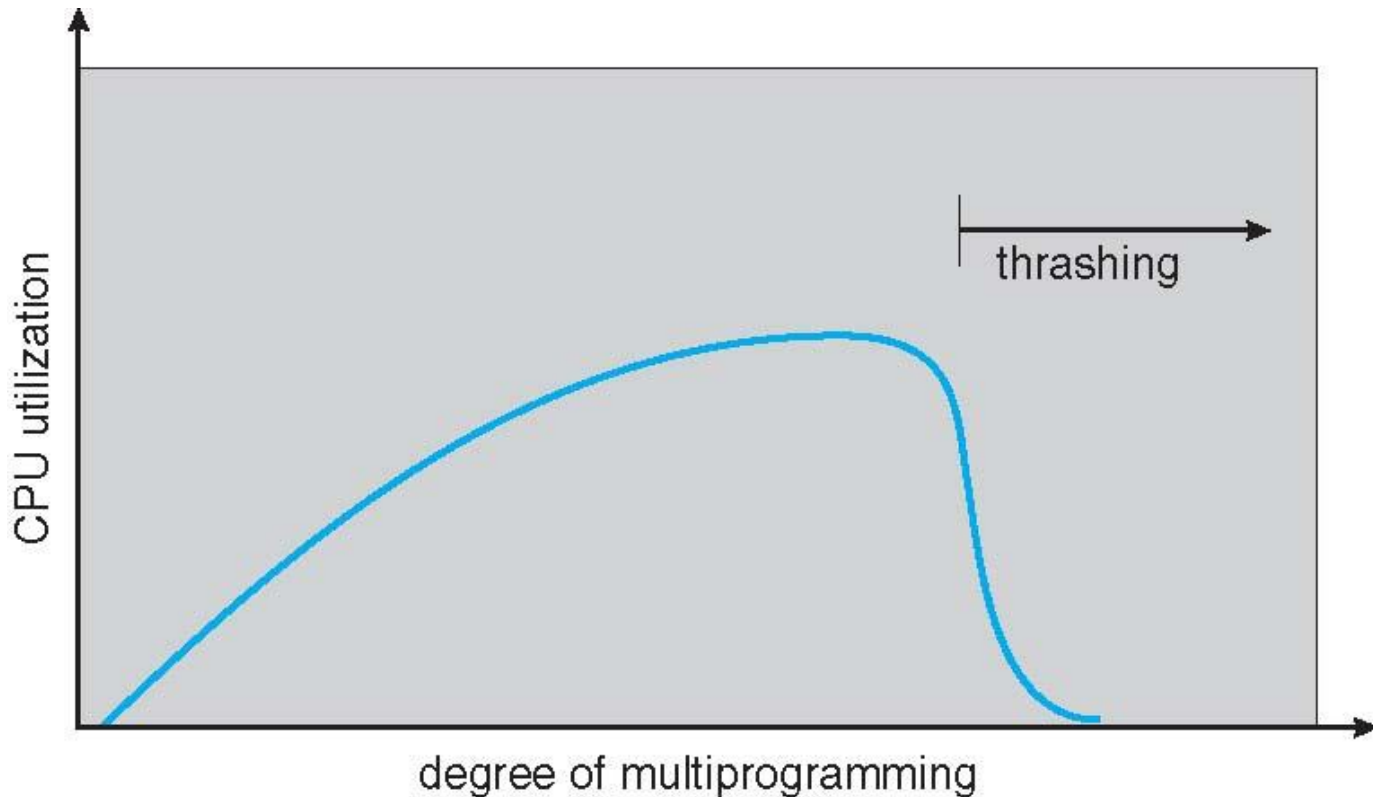
Thrashing (抖动)

- ✦ If a process does not have “enough” pages, the **page-fault rate** is very high. This leads to:
 - ✦ Low CPU utilization
 - ✦ OS thinks that it needs to increase the degree of multiprogramming
 - ✦ Another process is added to the system, getting worse!
- ✦ **Thrashing** \equiv a process is busy swapping pages in and out
 - ✦ Spending more time in swapping than executing



Thrashing (抖动)

✦ **Cause of trashing:** unreasonable degree of multiprogramming (不合理的多道程序度)





Thrashing (抖动)

- ✿ How to limit the effects of thrashing
 - ❏ Local replacement algorithm? not entirely solved.
 - ❏ We must provide a process with as many frames as it needs—locality
 - ❏ How do we know how many frames are needed?
 - ✓ working-set strategy \Leftarrow Locality model
- ✿ Locality model: This is the reason why demand paging works
 - ❏ Process migrates from one locality to another
 - ❏ Localities may overlap
- Why does thrashing occur?
 Σ size of locality > total memory size



Thrashing (抖动)

Working-Set Model (工作集模型)

- ❏ The working-set model is based on the assumption of locality.

- ❏ Let

 - $\Delta \equiv$ working-set window

 - \equiv a fixed number of page references

 - For example: 10,000 instructions

Working set (工作集):

The set of pages in the most recent Δ page references.

- ❏ An approximation of the program's locality.



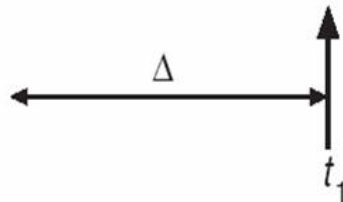
Thrashing (抖动)

Working-Set Model (工作集模型)

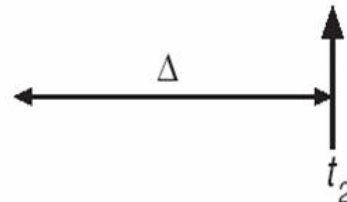
Example: $\Delta = 10$

page reference table

... 2 6 1 5 7 7 7 7 5 1 6 2 3 4 1 2 3 4 4 4 3 4 3 4 4 4 1 3 2 3 4 4 4 3 4 4 4 ...



$WS(t_1) = \{1, 2, 5, 6, 7\}$



$WS(t_2) = \{3, 4\}$

Working set size:

WSS_i (working set of Process P_i) =

total number of pages referenced in the most recent Δ (varies in time)

- ✓ **Varies** in time, depend on the selection of Δ
 - if Δ too small \Rightarrow will not encompass entire locality
 - if Δ too large \Rightarrow will encompass several localities
 - if $\Delta = \infty \Rightarrow$ will encompass entire program



Thrashing (抖动)

- For all processes in the system, currently

$D = \sum WSS_i \equiv$ total demand frames

m : total number of available frames

❏ $D > m \Rightarrow$ Thrashing

❏ Policy:

if $D > m$, then suspend one of the processes



Thrashing (抖动)

❖ Keeping Track of the Working Set

❖ Approximate with: **fixed interval timer + reference bits**

❖ Example: $\Delta = 10,000$

✓ Cause a timer interrupt after every 5000 time units

✓ Keep two in-memory bits for each page

✓ Whenever a timer interrupts, copy and set the values of all reference bits to 0

✓ If one of the bits in memory = 1 \Rightarrow page in working set

❖ Why is this not completely **accurate**?

✓ IN!! But where?

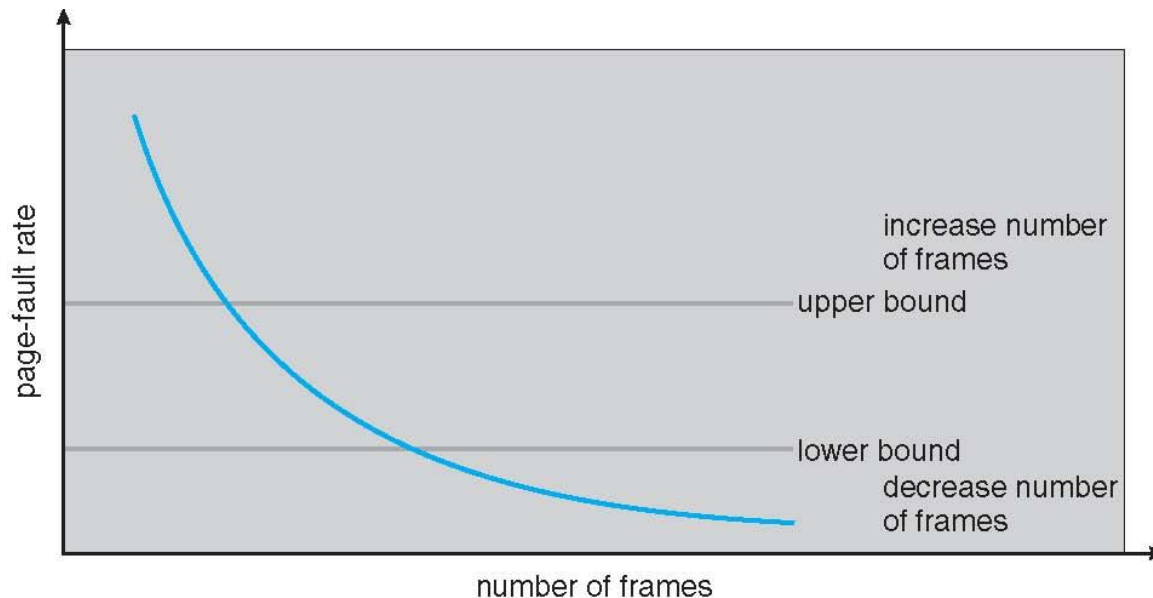
❖ **Improvement:**

✓ 10 bits and interrupt every 1000 time units



Thrashing (抖动)

- ❖ Page-Fault Frequency (缺页频率): helpful for controlling trashing
 - ❖ Trashing has a high page-fault rate.
 - ❖ Establish “acceptable” page-fault rate
 - ✓ If actual rate is too low, process loses frame
 - ✓ If actual rate is too high, process gains frame





End of Chapter 8