

F1/10

Autonomous Racing

Scan Matching - Part 2

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CS 4501
Rice Hall 120

F1/10 2020 Autonomous Racing Teams CS 4501



File Edit View Insert Format Data Tools Add-ons Help Last edit was made 37 minutes ago by anonymous

A set of standard spreadsheet toolbar icons including file, print, zoom, currency, percentage, date/time, font style, font size, bold, italic, underline, and various alignment and border options.

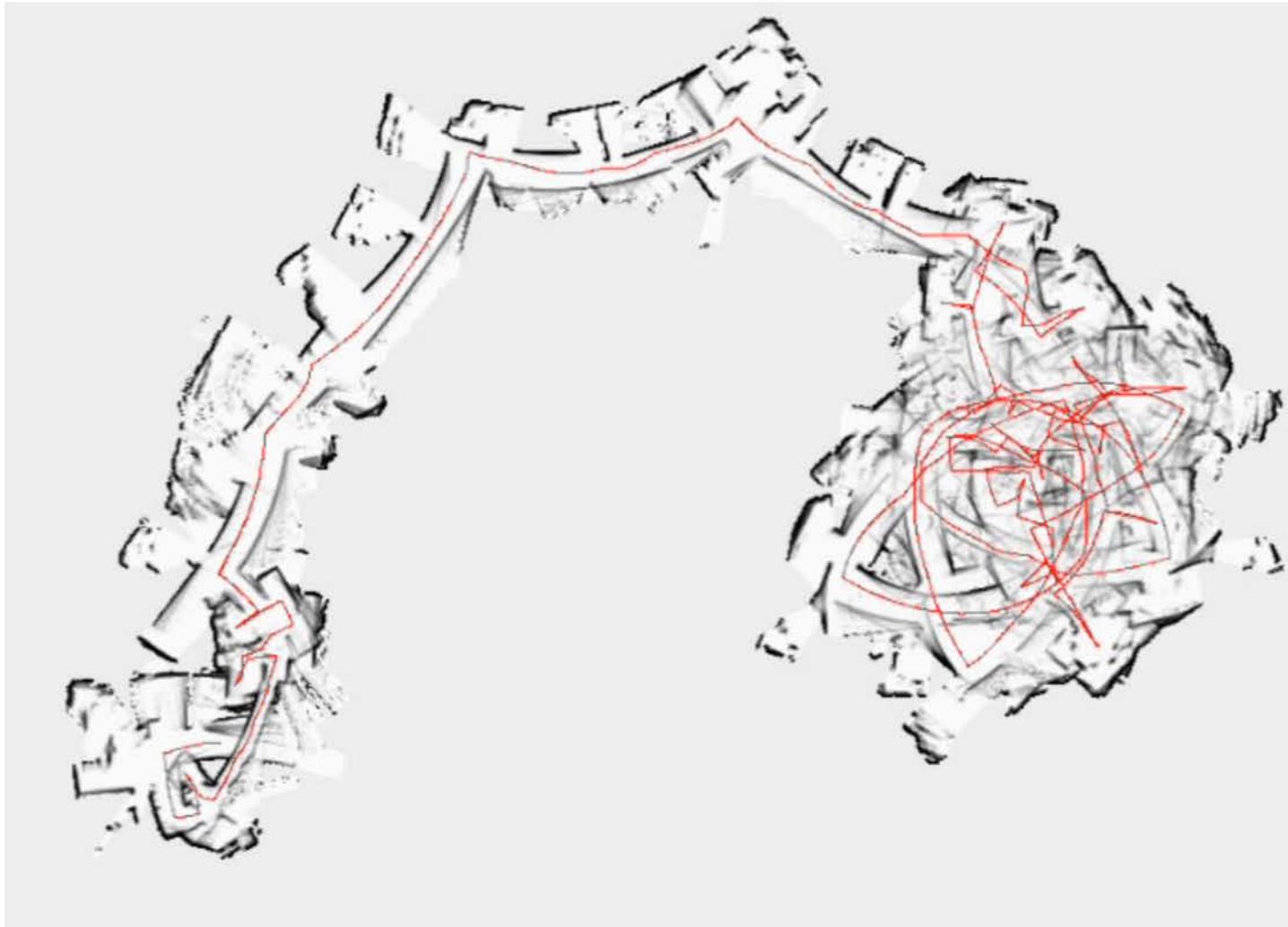
fx Vehicle Number

	A	B	C	D	E	F	G
1	Vehicle Number	Vehicle N/W SSID	Member 1 (First + Last Name)	Member 2 (First + Last Name)	Member 3 (First + Last Name)	Member 4 (First + Last Name)	Color Code (Assigned by TA)
2							
3	1	team_1	Raghava Pamula	Catherine Bradberry	Logan Hylton		
4							
5	2	team_2	Ryan Kann	Wyatt Joyner	Corey Lando	Jack Herd	
6							
7	3	team_3	Rahul Batra	Rashid Lasker	Stephen Shiao	Adeet Patel	
8							
9	4	team_4	Bradley Knaysi	Peng Zhang	Emory Ducote		
10							
11	5	team_5	Jaspreet Ranjit	Jack Schumann	Hsing Chun Lin	Micah Harris	
12							
13	6	team_6	Sean Shih	Chris Han			
14							
15	7	team_7	Kaiying Shan	Hanzhi Zhou			
16							
17	8	team_8	Michael Tang	Catherine Im	Austin Bunting		
18							
19	9	team_9					

Scan Matching



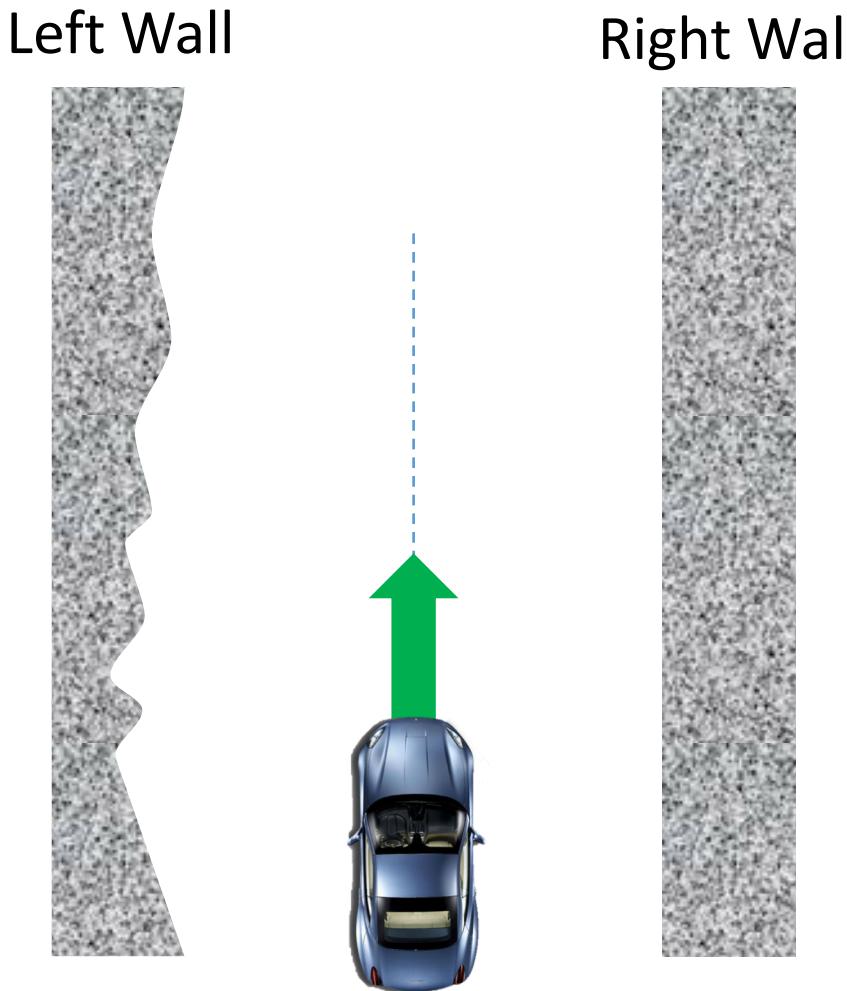
Raw Odometry



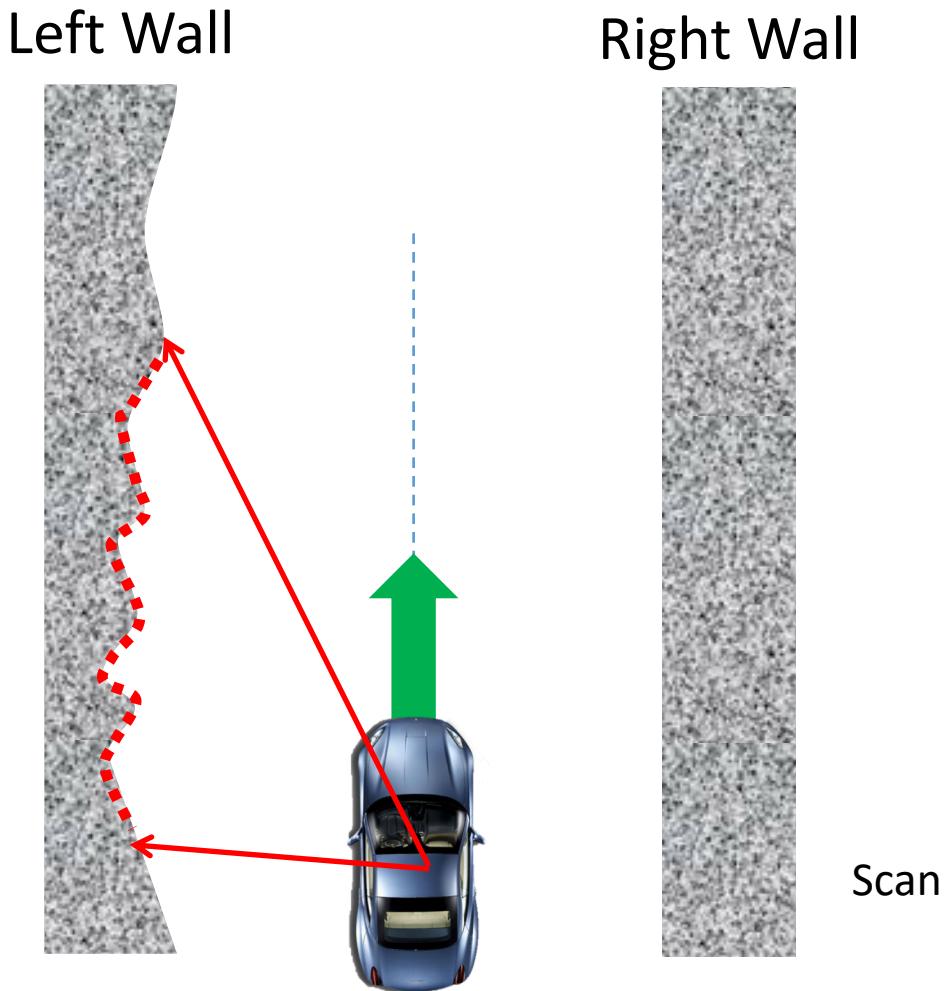
Odometry with LIDAR

- Odometry = Estimation of position (x, y, z) and attitude (θ, φ, ψ)
- In what follows, will use “position” as short for “position and attitude”

LIDAR for odometry: Scan matching

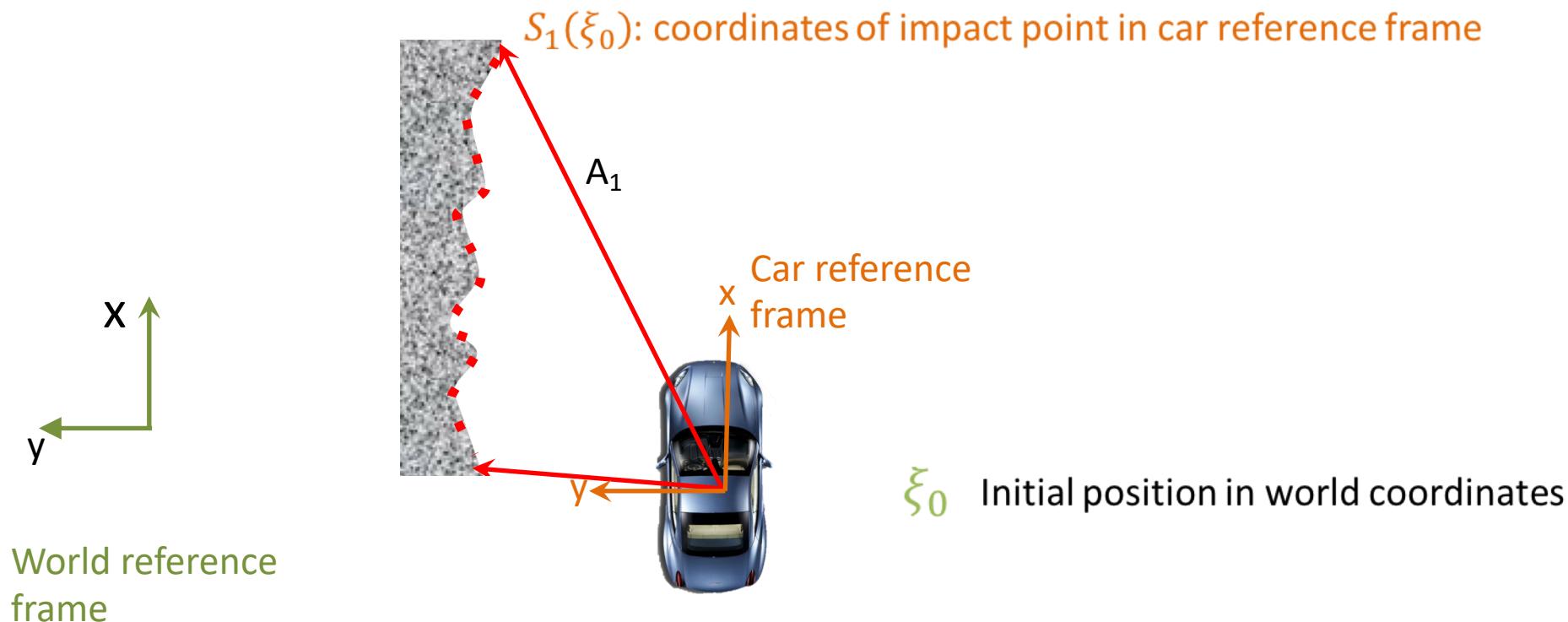


LIDAR for odometry: Scan matching

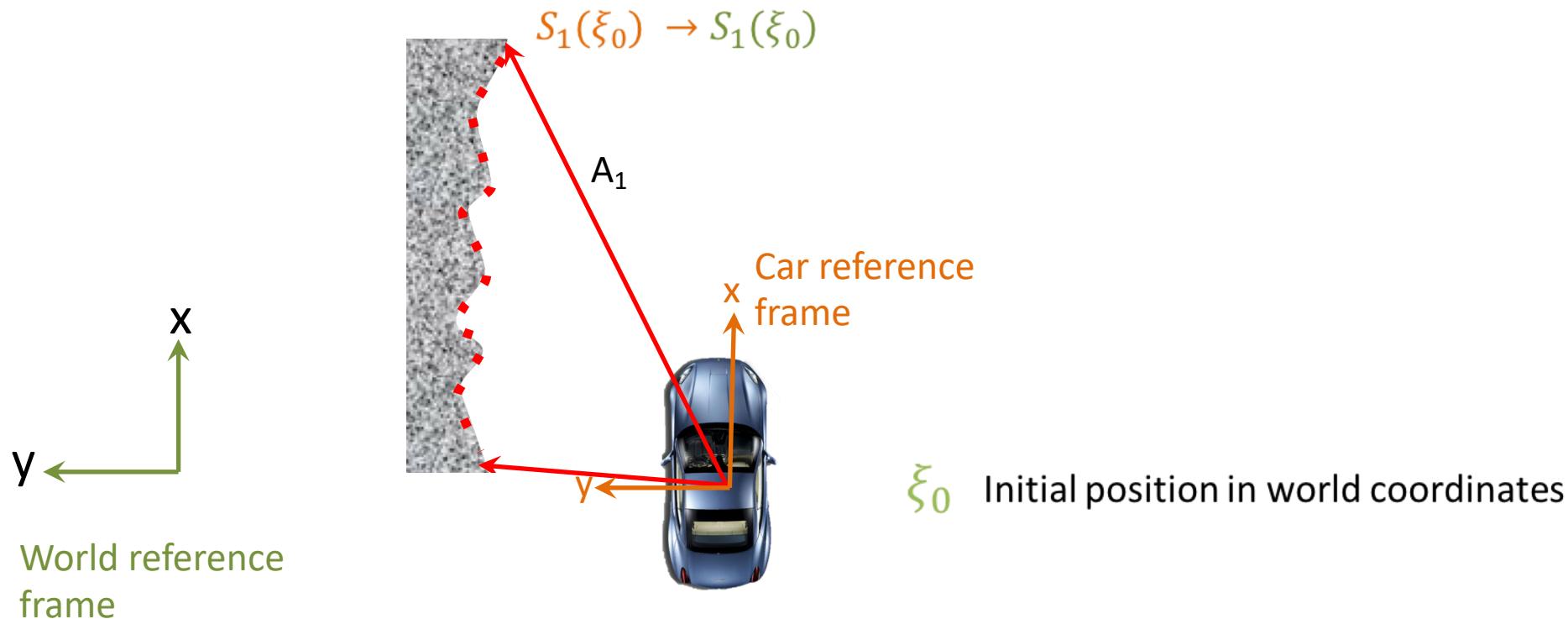


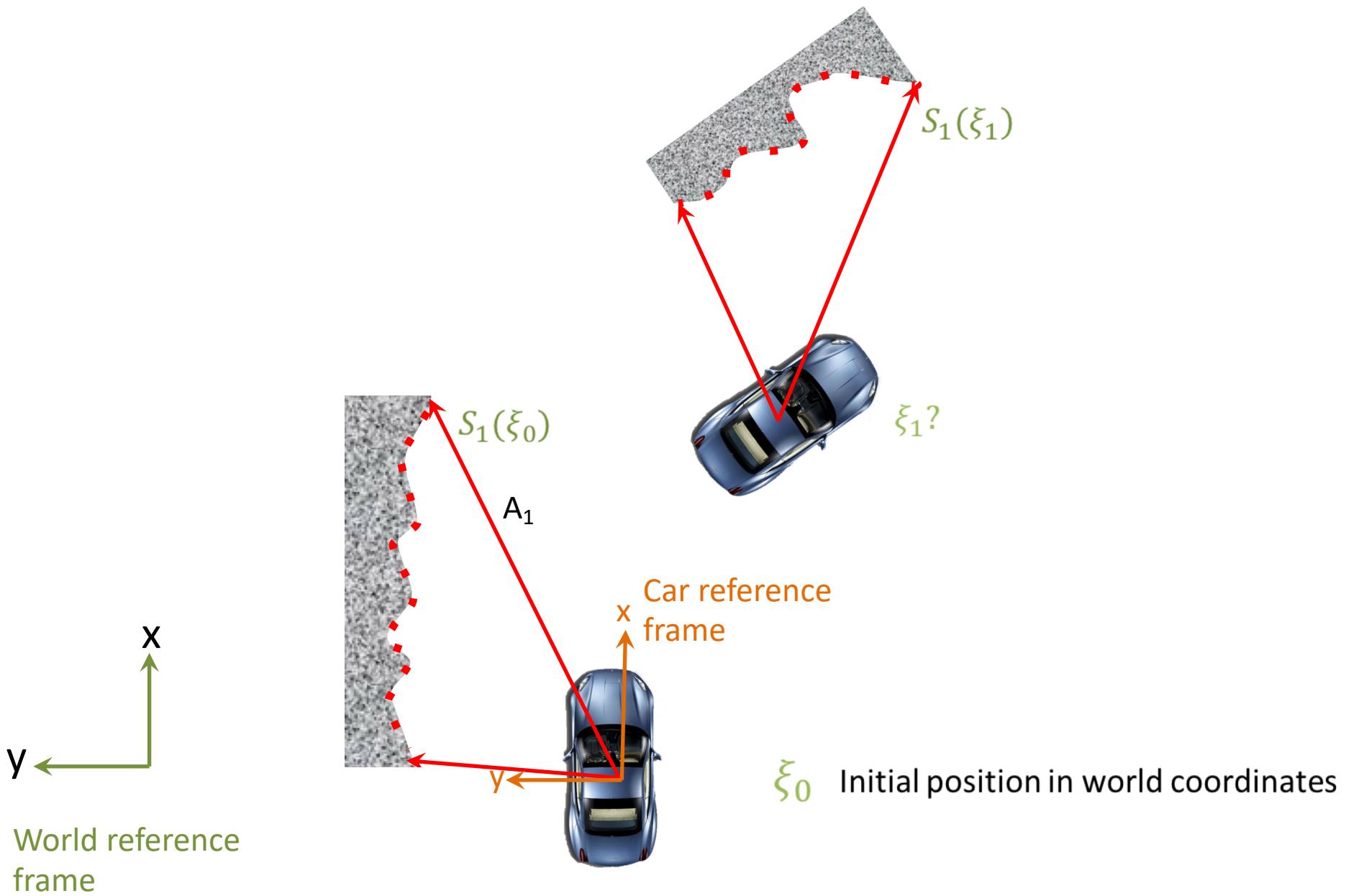
Scan 1

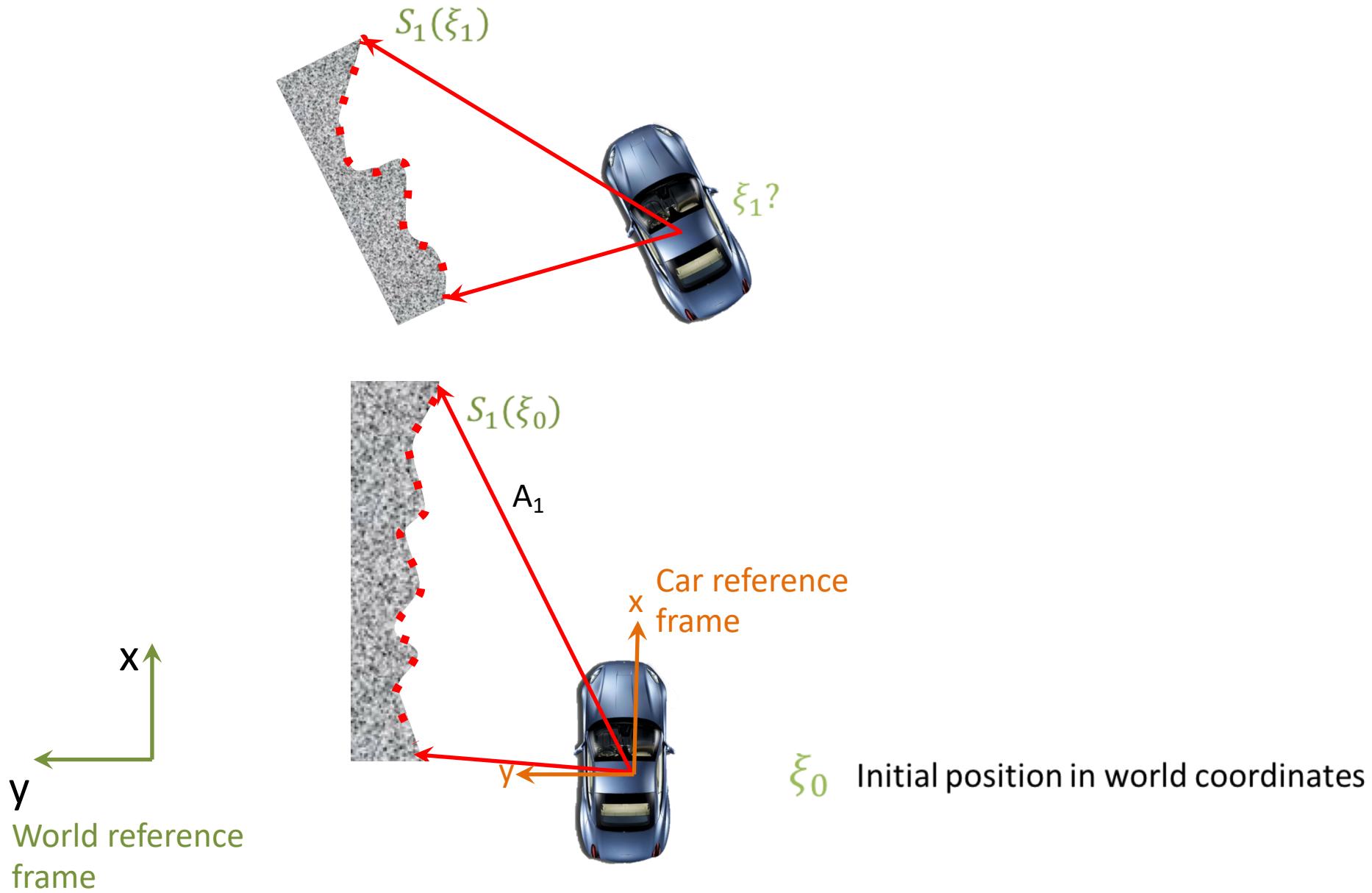
LIDAR for odometry: Scan 1

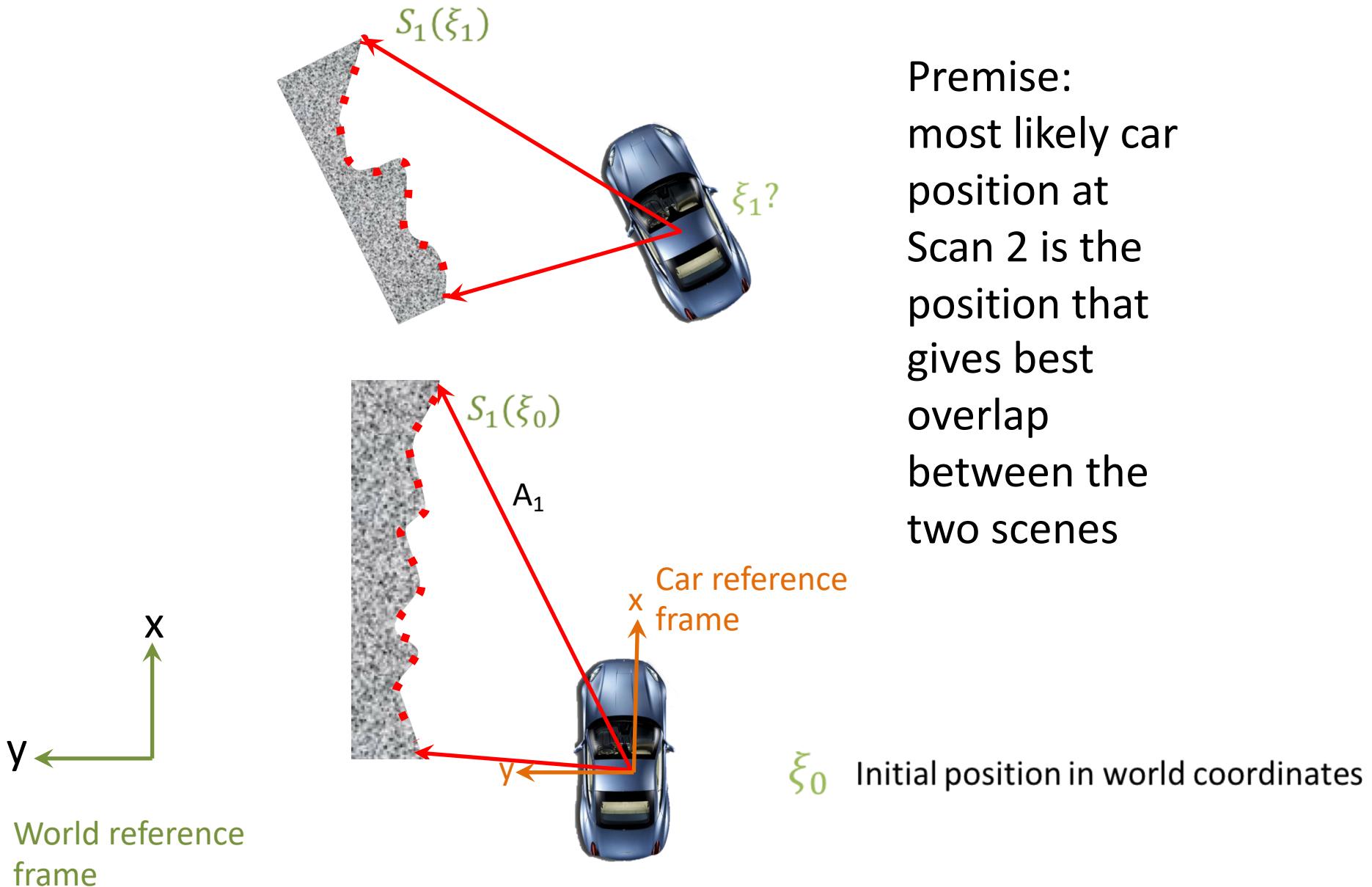


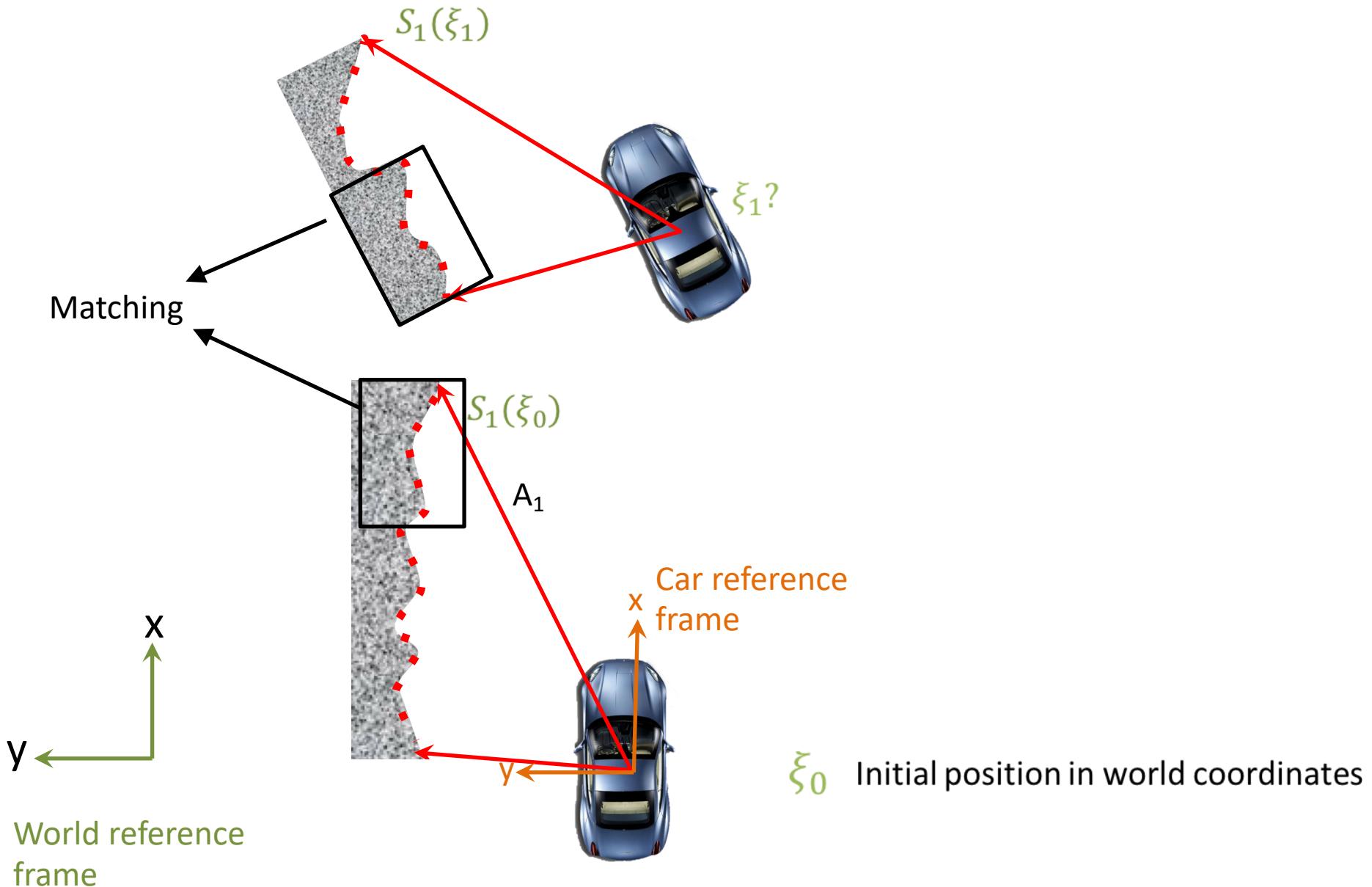
LIDAR for odometry: Scan 1

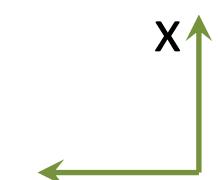


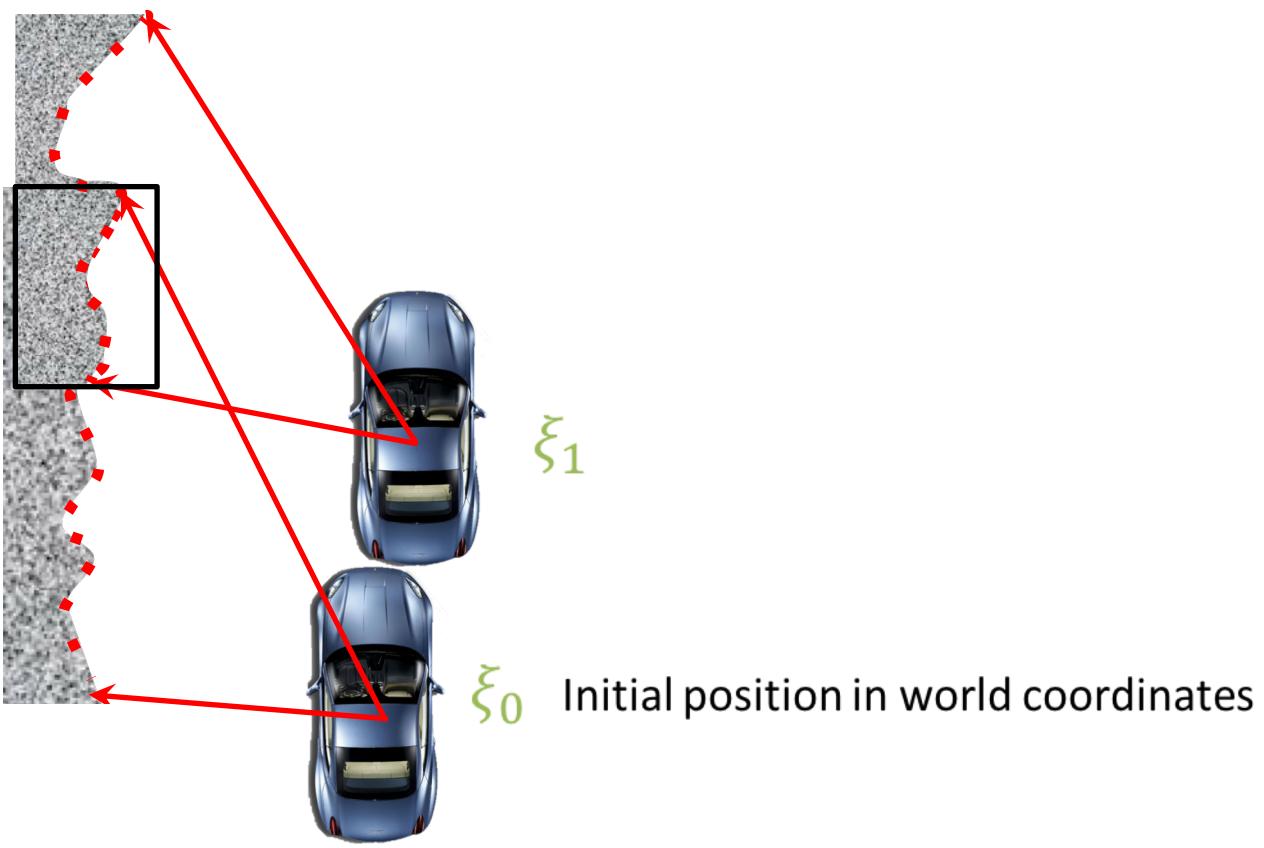




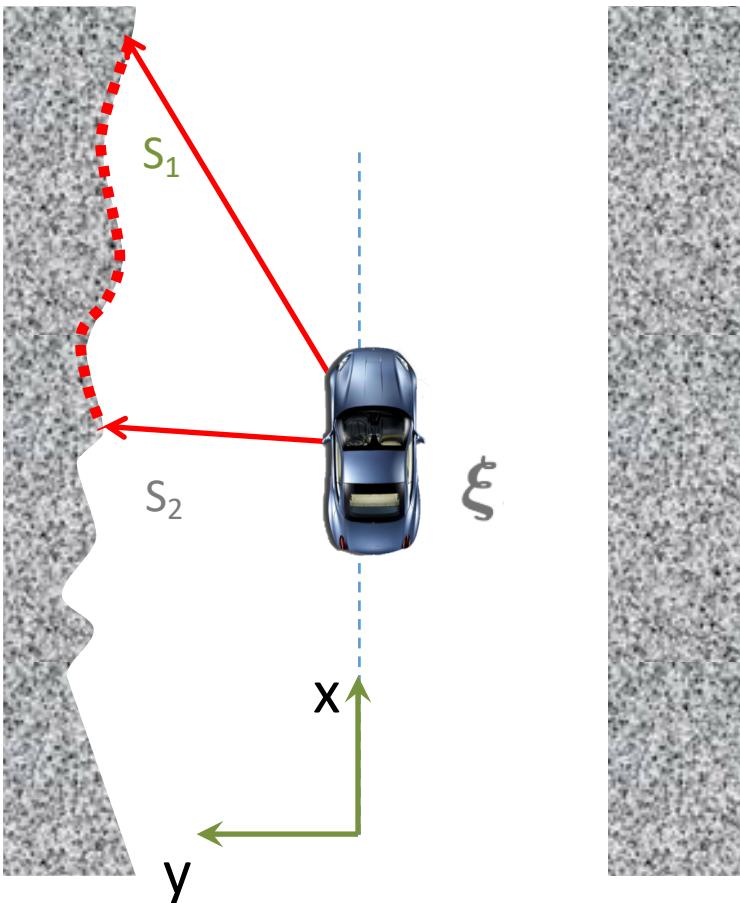




 World reference frame



Scan matching: optimization



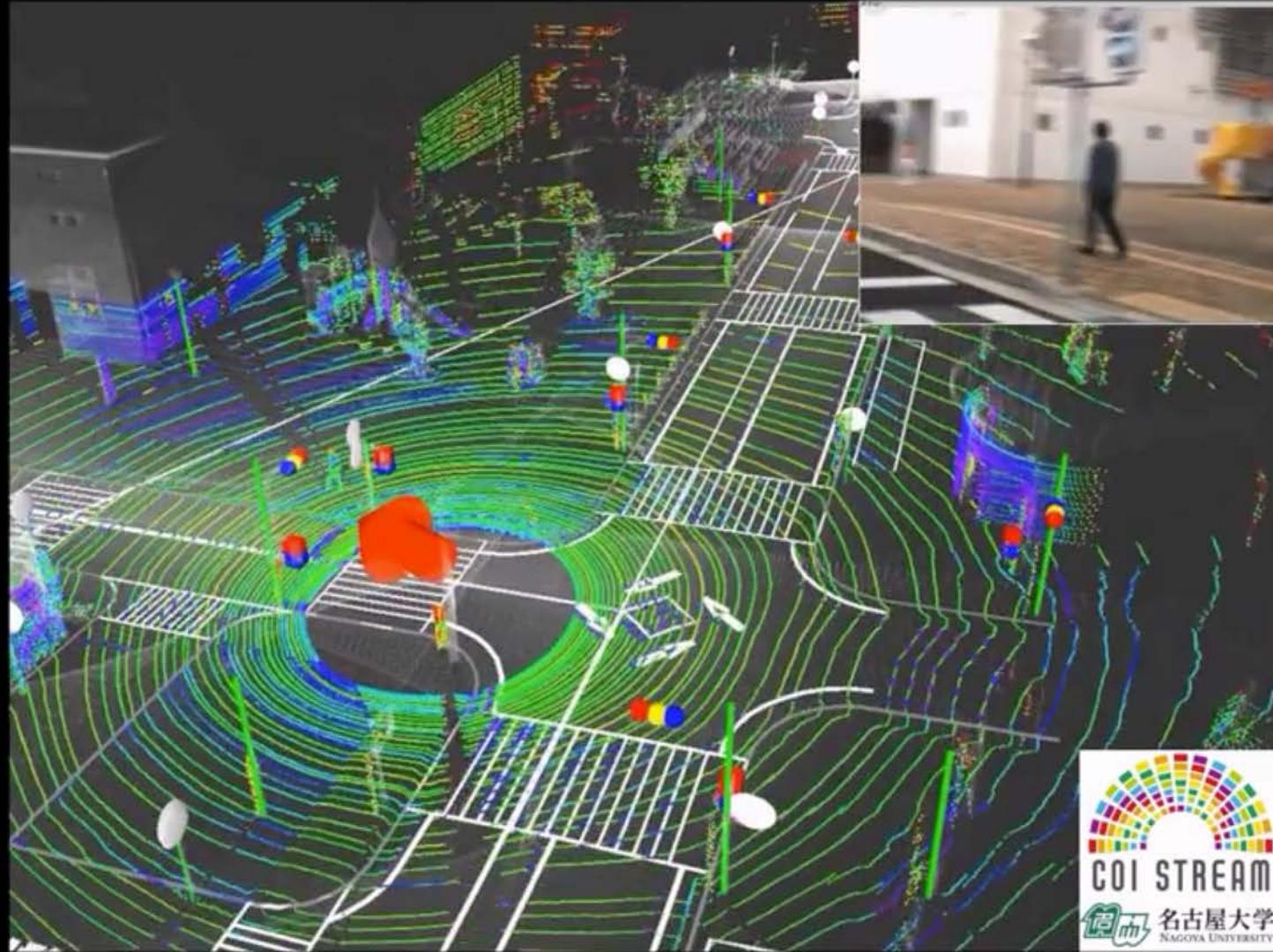
Impact coordinates of i^{th} step in world frame

Total of n steps ($n = 1084$)

$$\xi^* = \underset{\xi}{\operatorname{argmin}} \sum_{i=1}^n [1 - M(\mathbf{S}_i(\xi))]^2$$

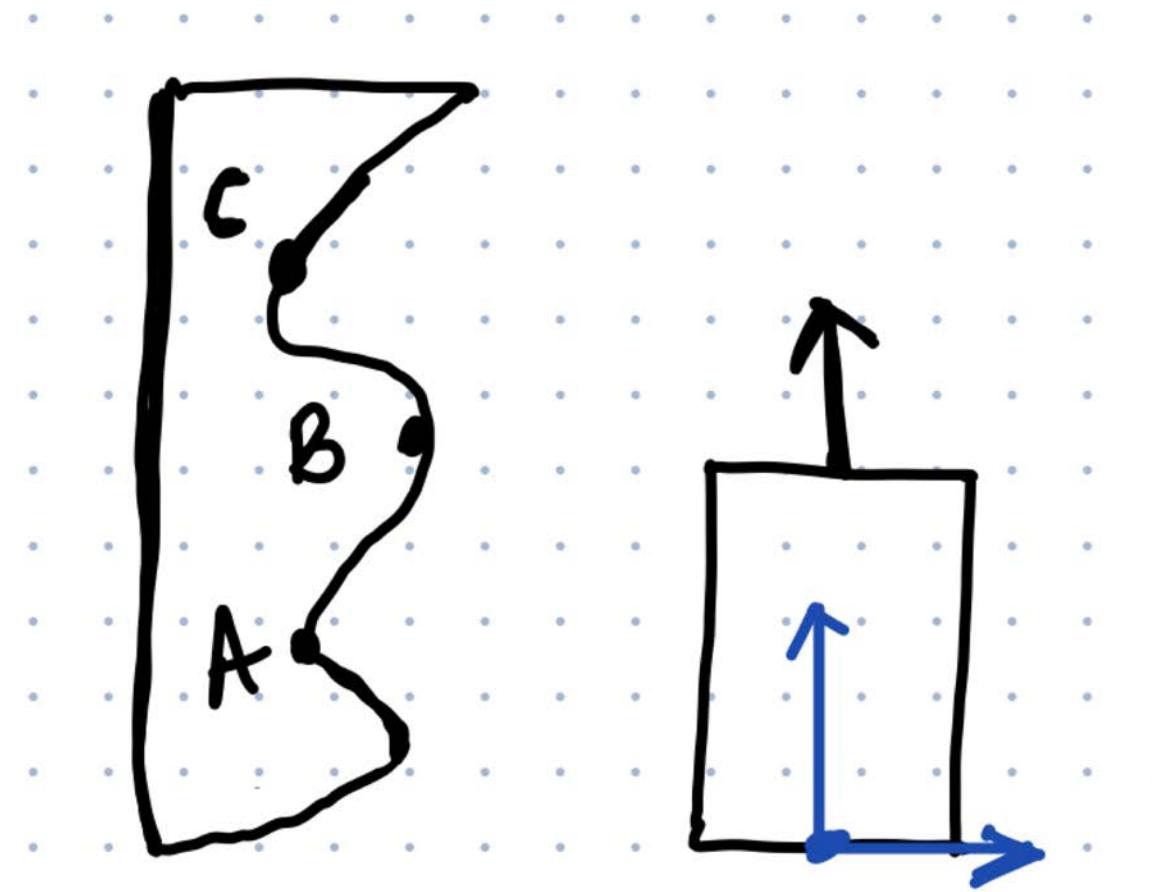
Measure of match





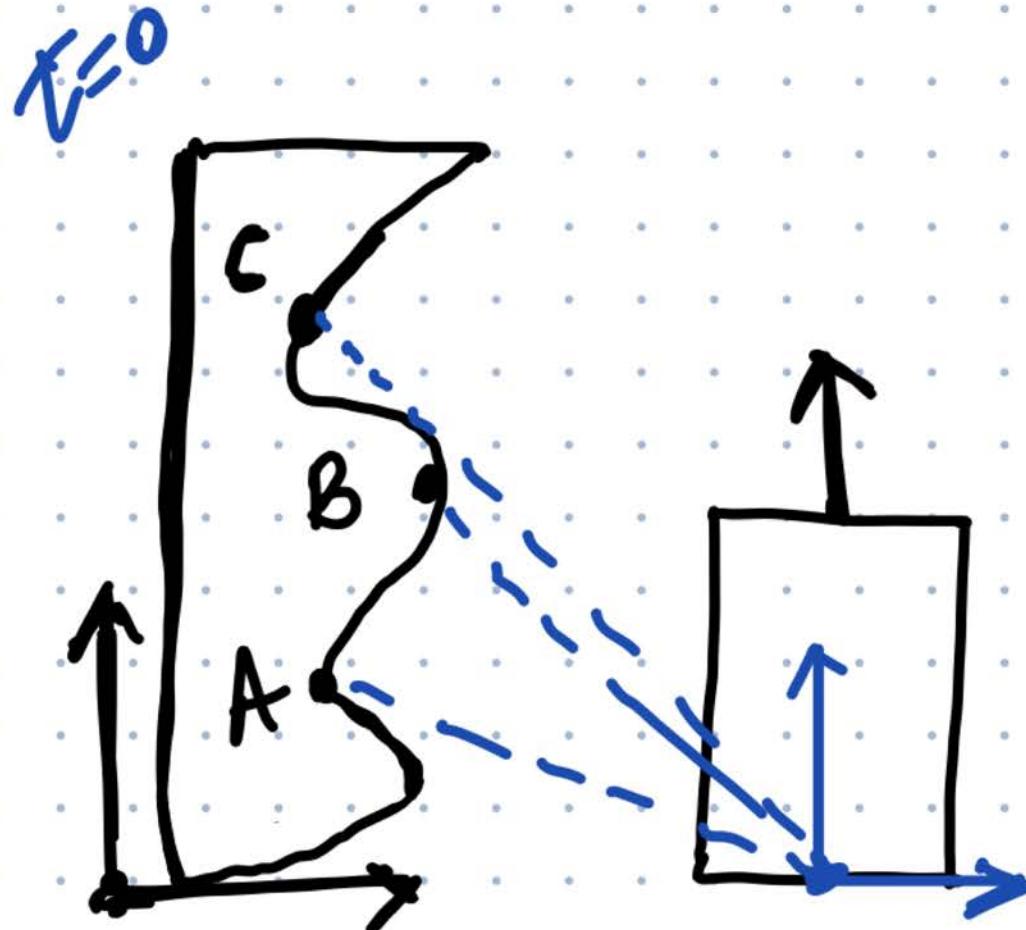
Problem Setup

Let's say my robot is in some environment with landmarks A, B, C

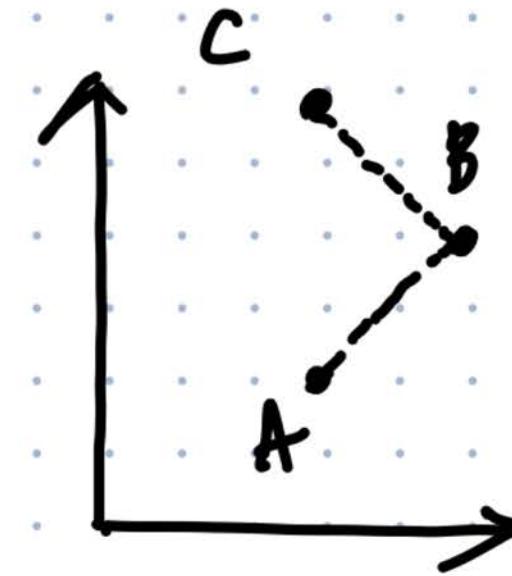


Problem Setup

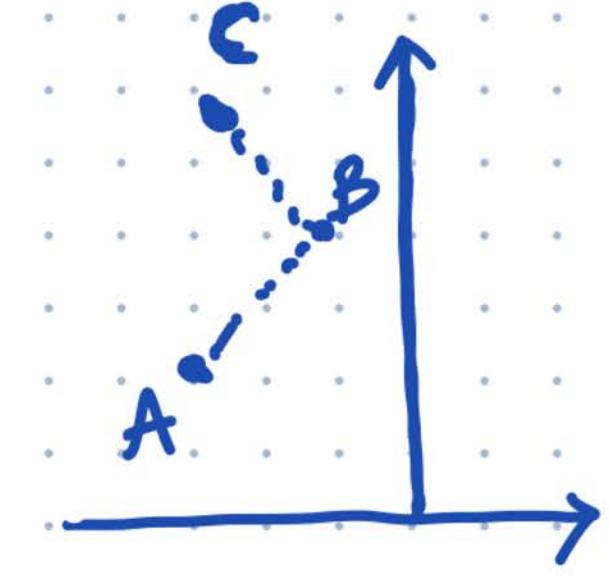
At $t=0$, measurements of distances to A,B,C are taken:



$\langle \text{Global} \rangle$

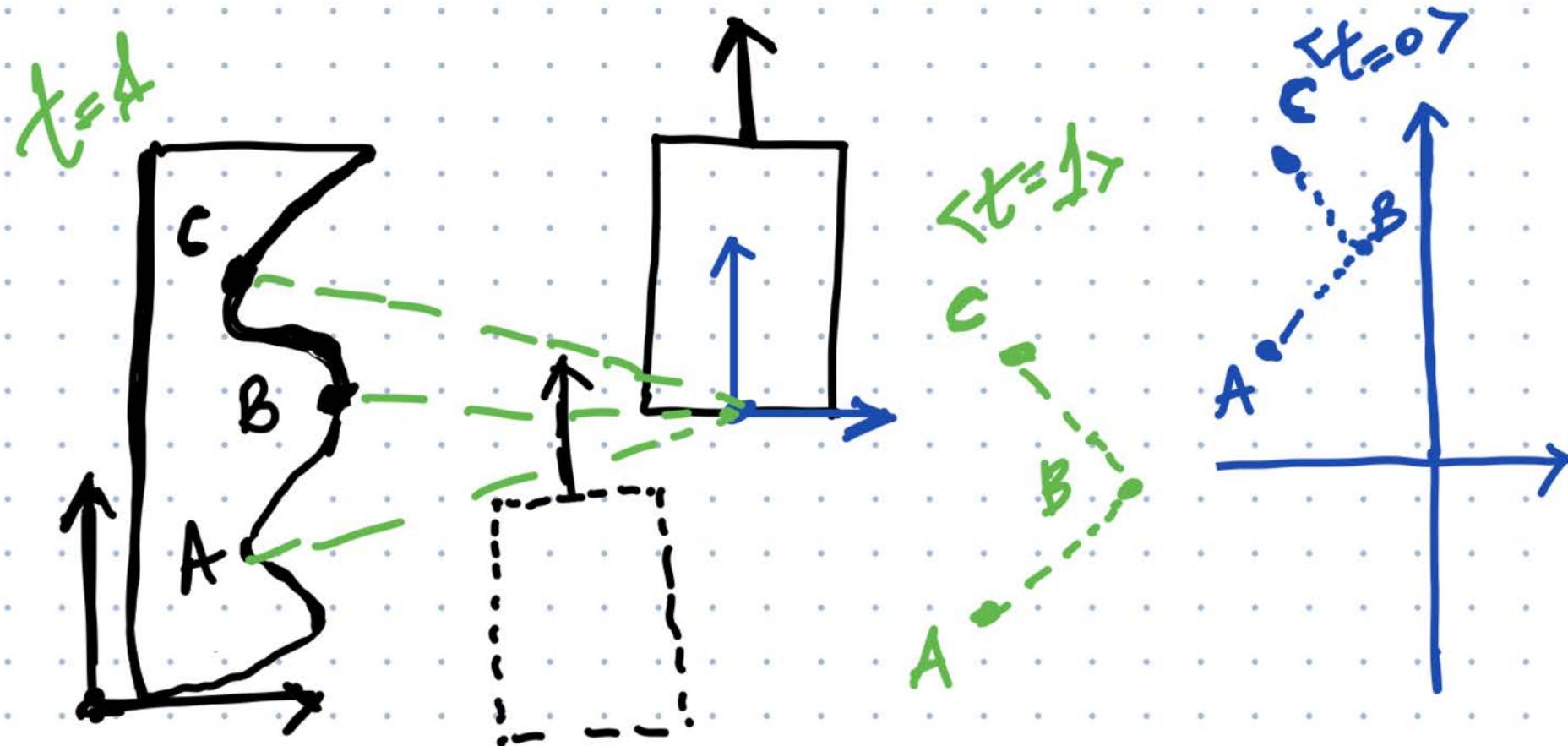


$\langle t=0 \rangle$



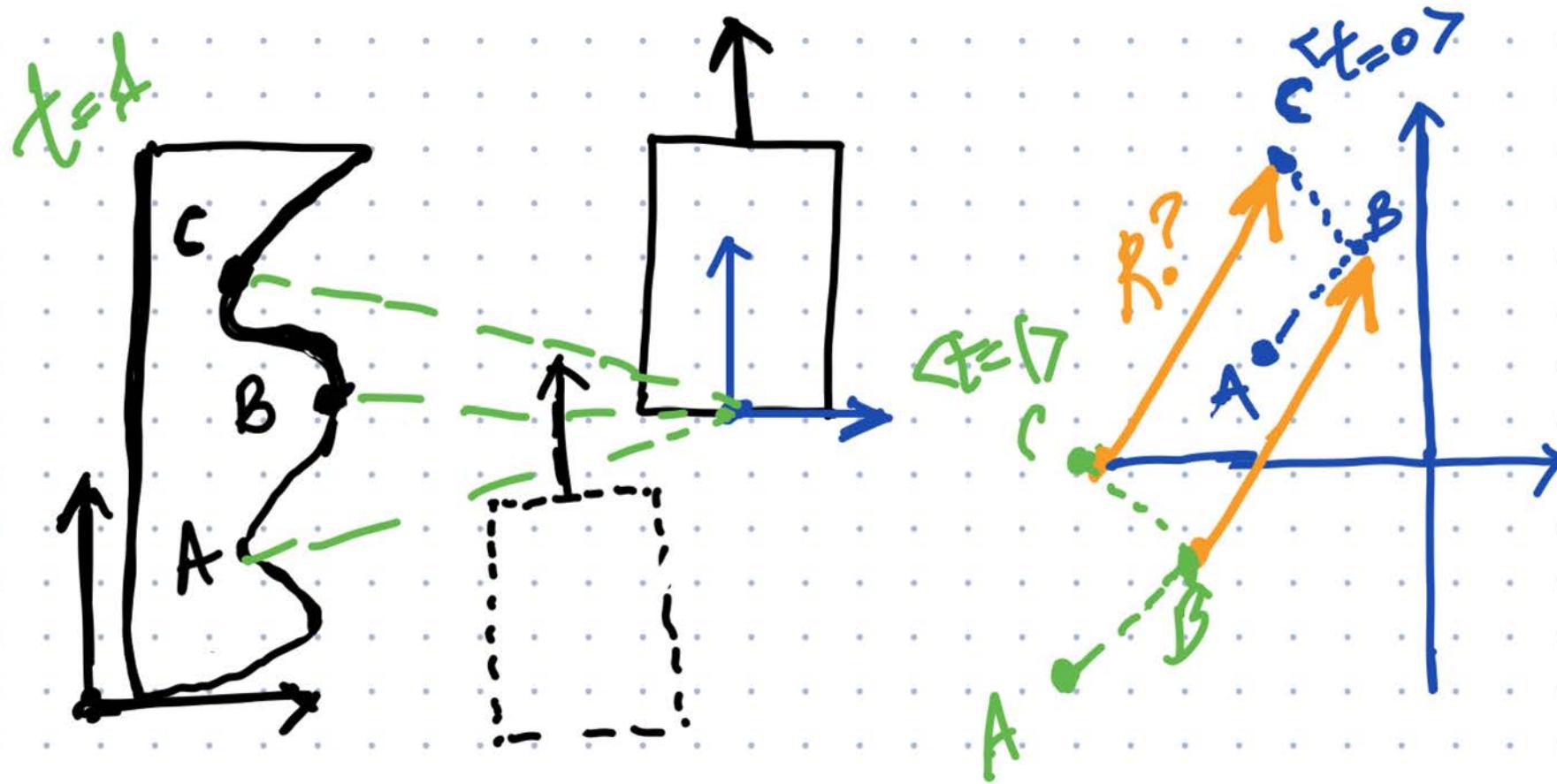
Problem Setup

At $t=1$, moving in some unknown direction, the distances to the landmarks will have changed:



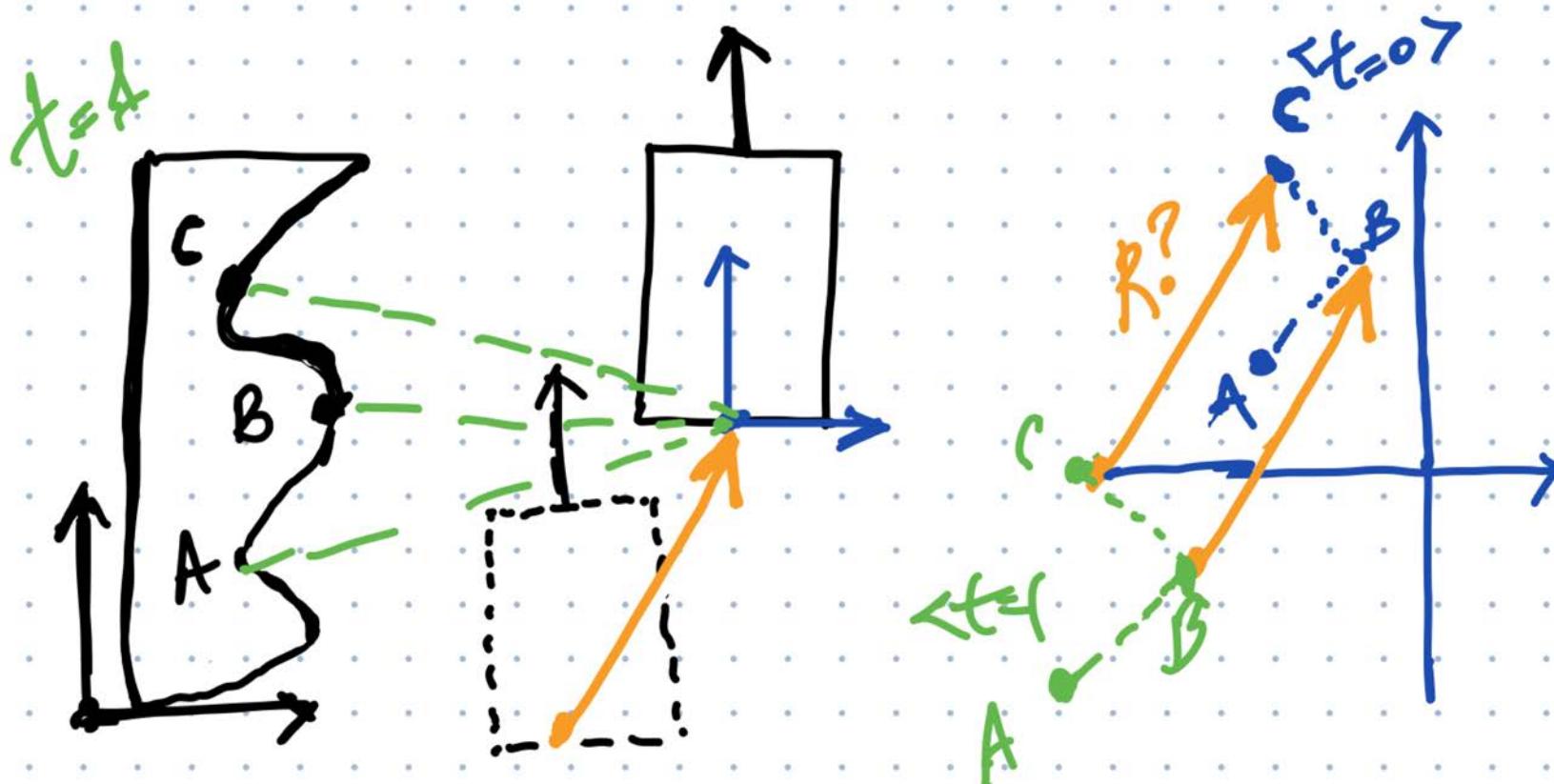
Problem Setup

We want to find transform R , the transforms the two set of points to be the closest:



Problem Setup

Why? The transform R represents how much the robot has moved in time:



How do we find R?

Challenge:

- If we knew A, B, C (landmarks) exactly, then this would be easy
- We don't know which measurement is for which landmark

Solution:

- Assume closest points correspond to each other → “correspondence match”
- Iteratively find the best transform R

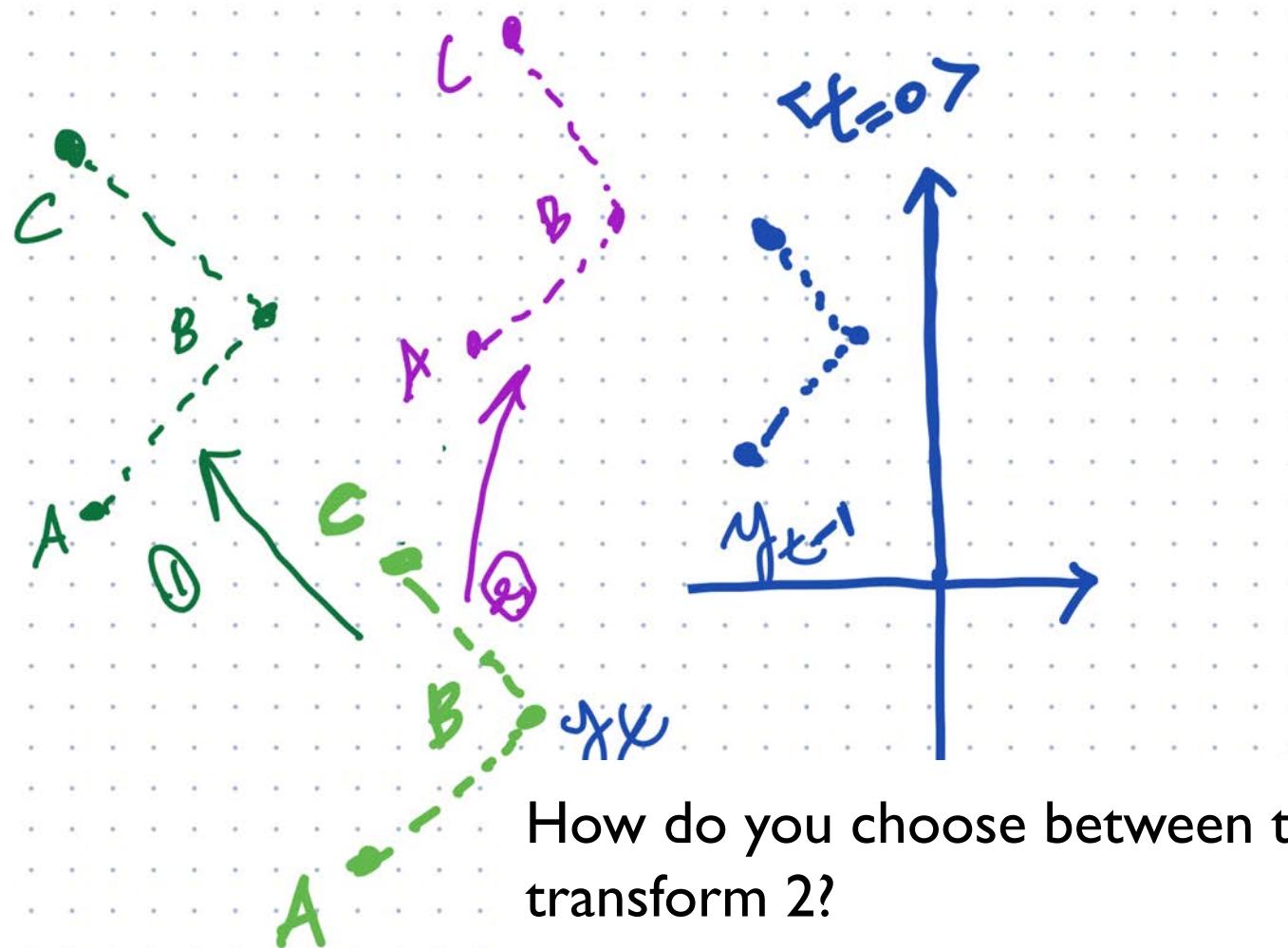
Iterative search for best transform

1. Make some initial “guess” of R (current guess)
2. For each point in new scan ($t=k+1$), find closest point in previous set ($t=k$) (**correspondence search**)
3. Make another “better guess” of R (next guess)
4. Set next guess to current guess, repeat steps 2-4 until converges

What makes a “better guess”? → Need a metric

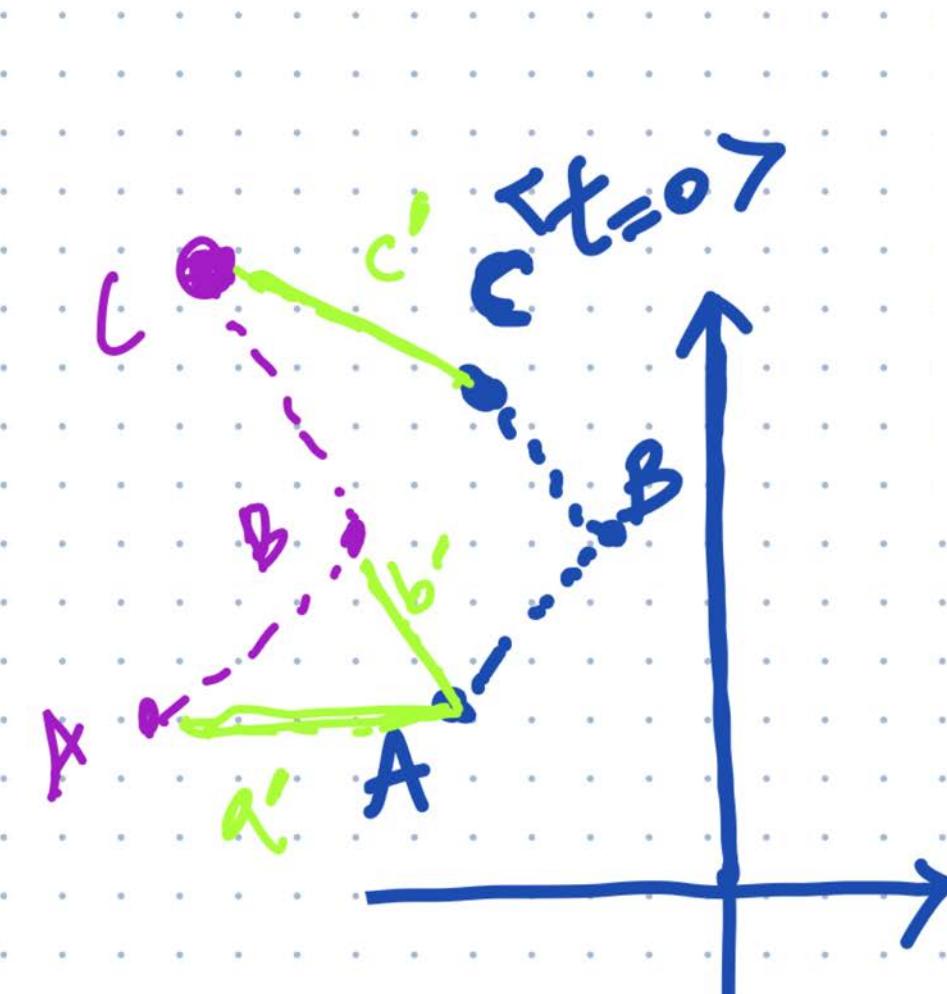
How do you choose between I or II?

(Assume correspondences have been found)



Candidate Match Function

Point-to-scan point

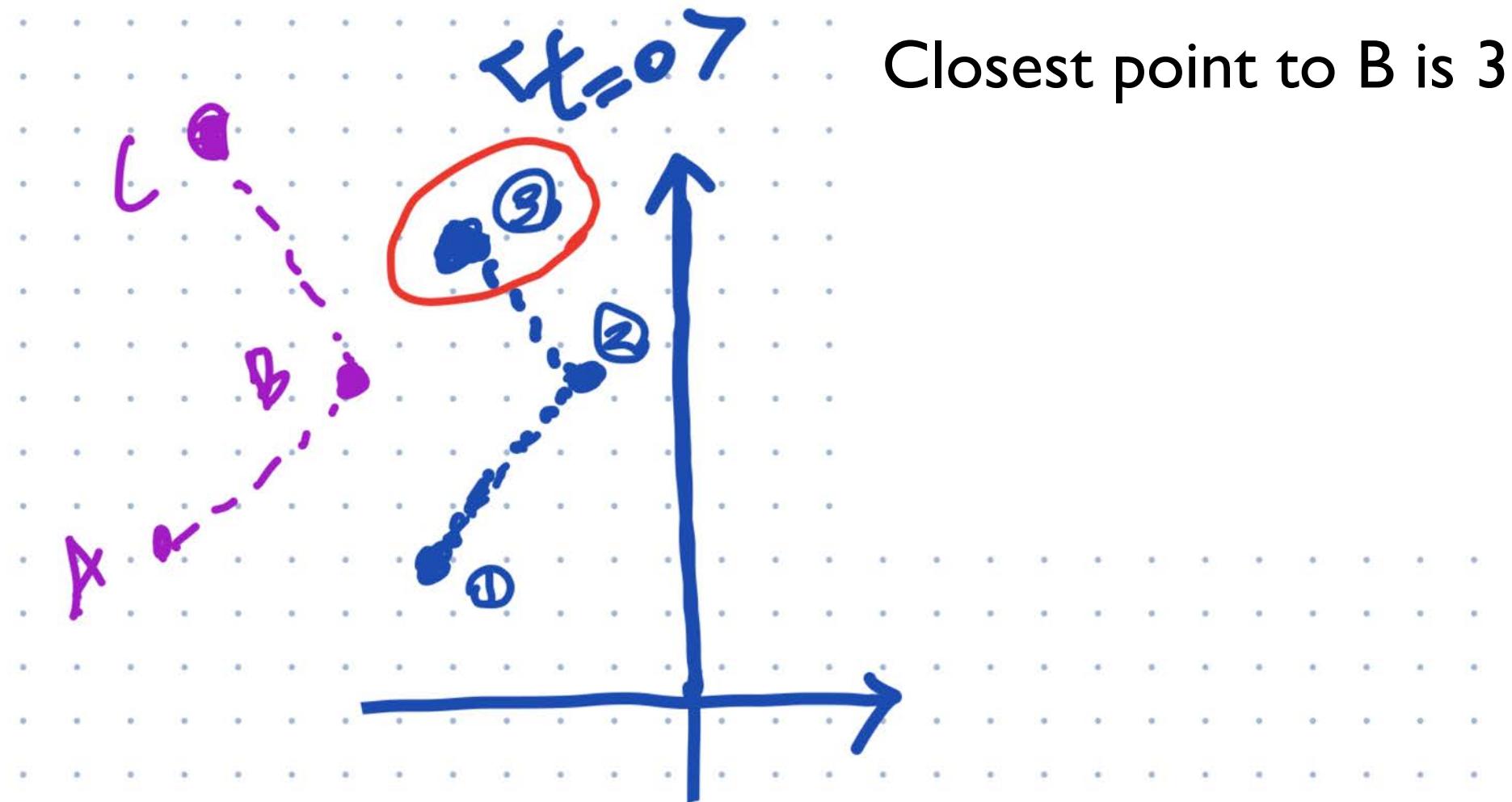


Find closest point and sum the square of distances to the closest point.

$$|a'|^2 + |b'|^2 + |c'|^2$$

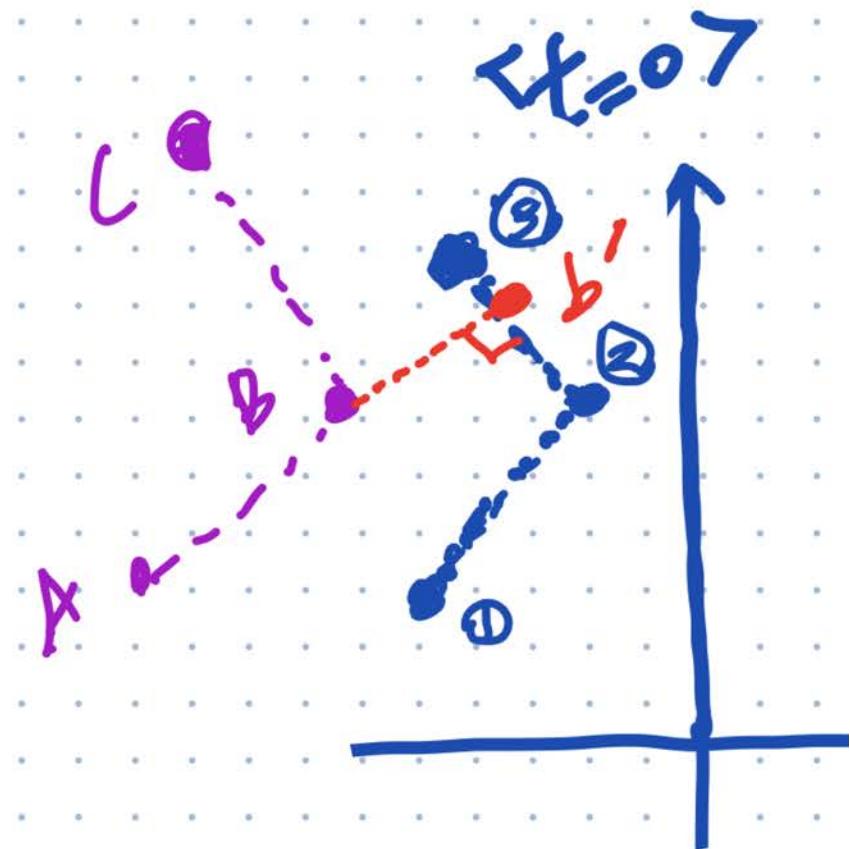
Better Candidate Match Function

Point to projected point (point-to-point) metric:



Better Candidate Match Function

Find projection of point onto reference surface:

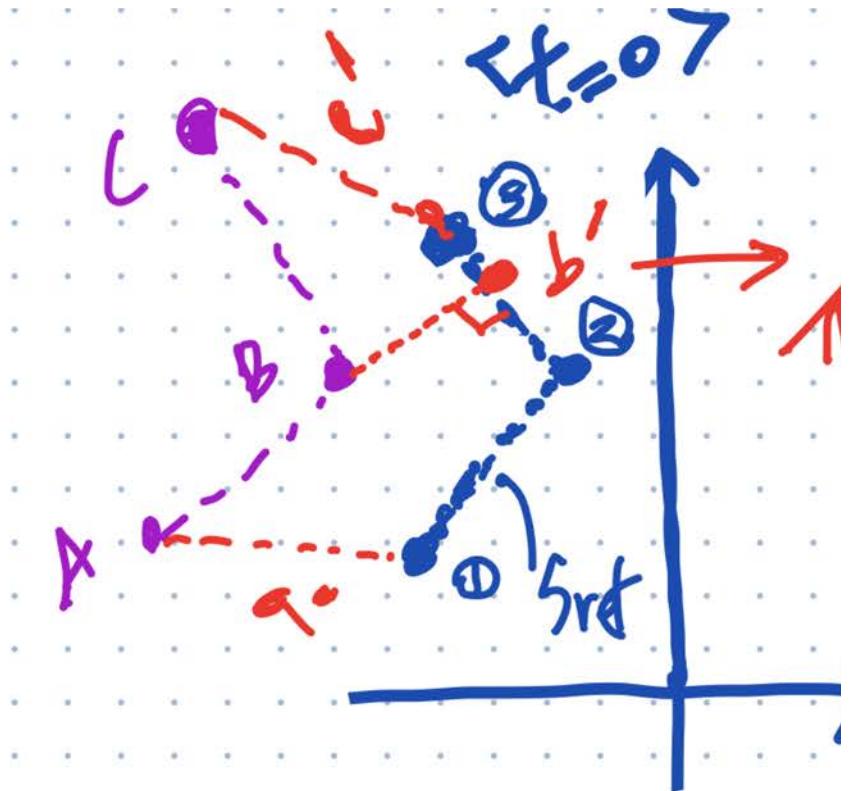


Closest point to B is 3

Find projected **point** on line
segment 2-3, b'

Better Candidate Match Function

Squared sum of projected distances (point-to-point)



Closest point to B is 3

Find projected **point** on line segment 2-3, b'

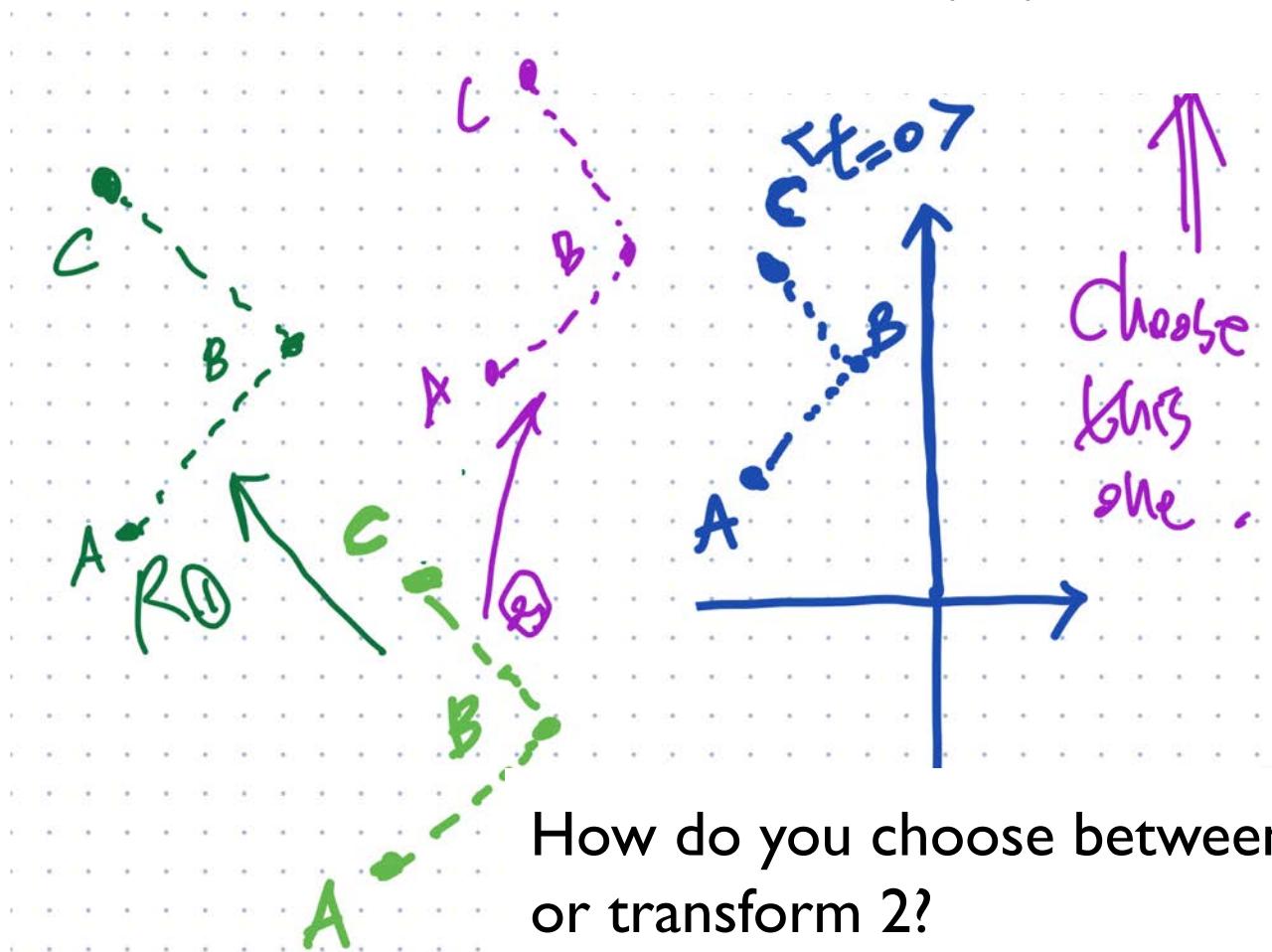
Square the sum of projected distances

$$\text{Score} = \|a'\|^2 + \|b'\|^2 + \|c'\|^2$$

How do you choose between I or II

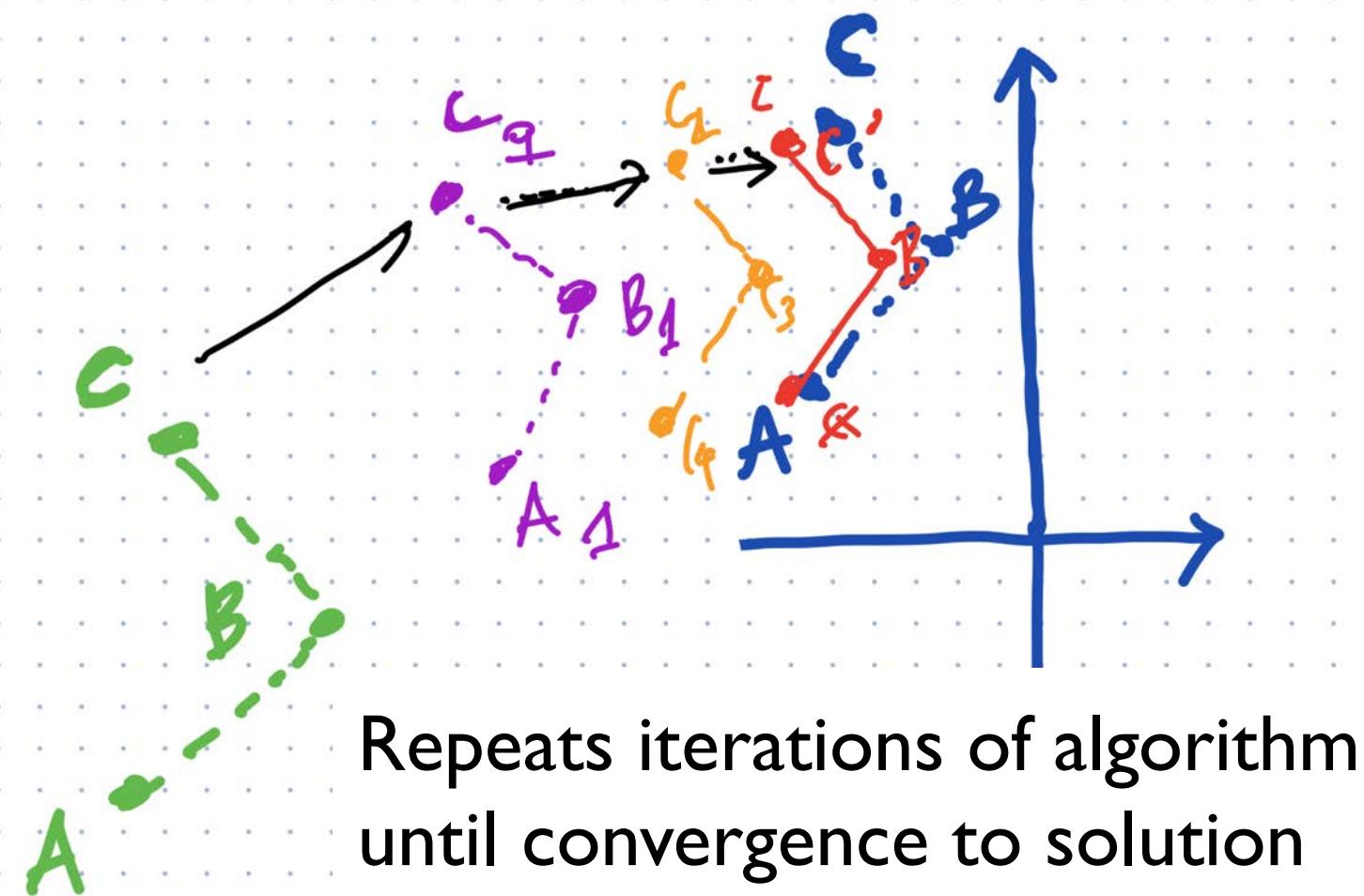
Choose R2

Match Score (R1) > Match Score (R2)



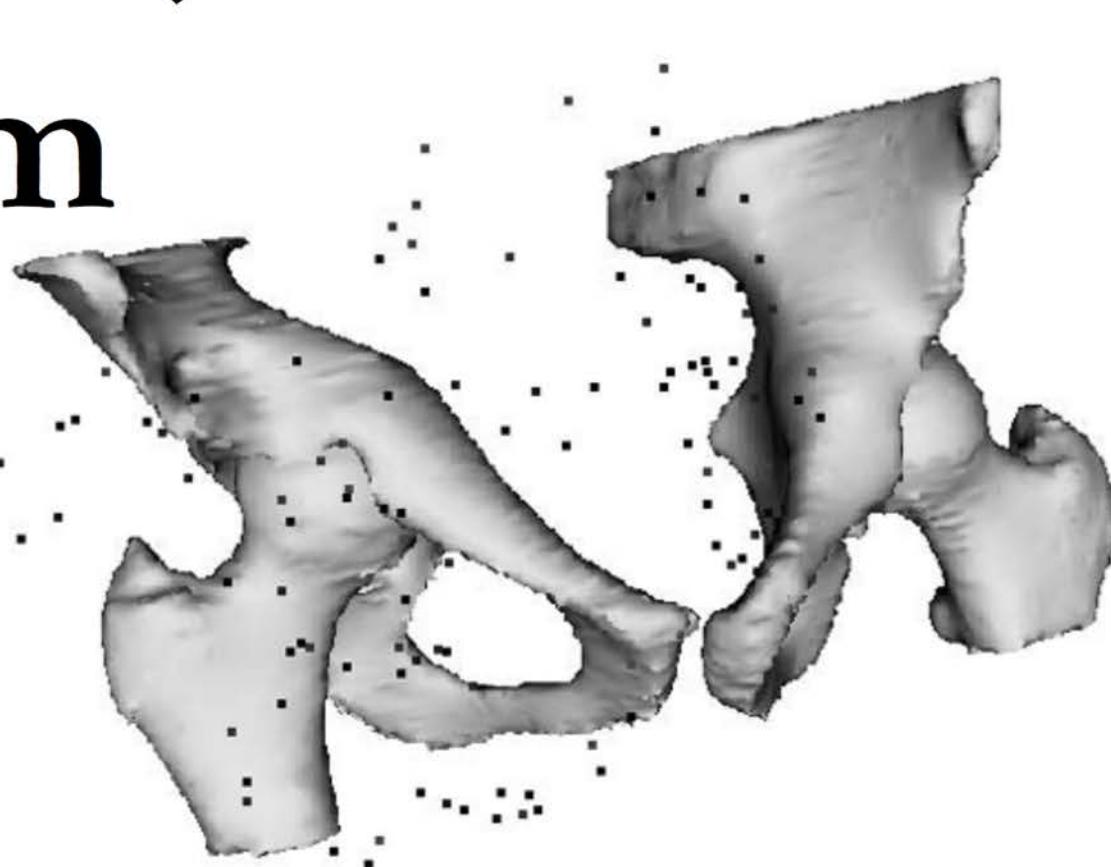
Iterative Matching

Uses point-to-point metric



Iterative Closest Point (ICP)

Algorithm



- Given: two corresponding point sets:

$$X = \{x_1, \dots, x_n\}$$

$$P = \{p_1, \dots, p_n\}$$

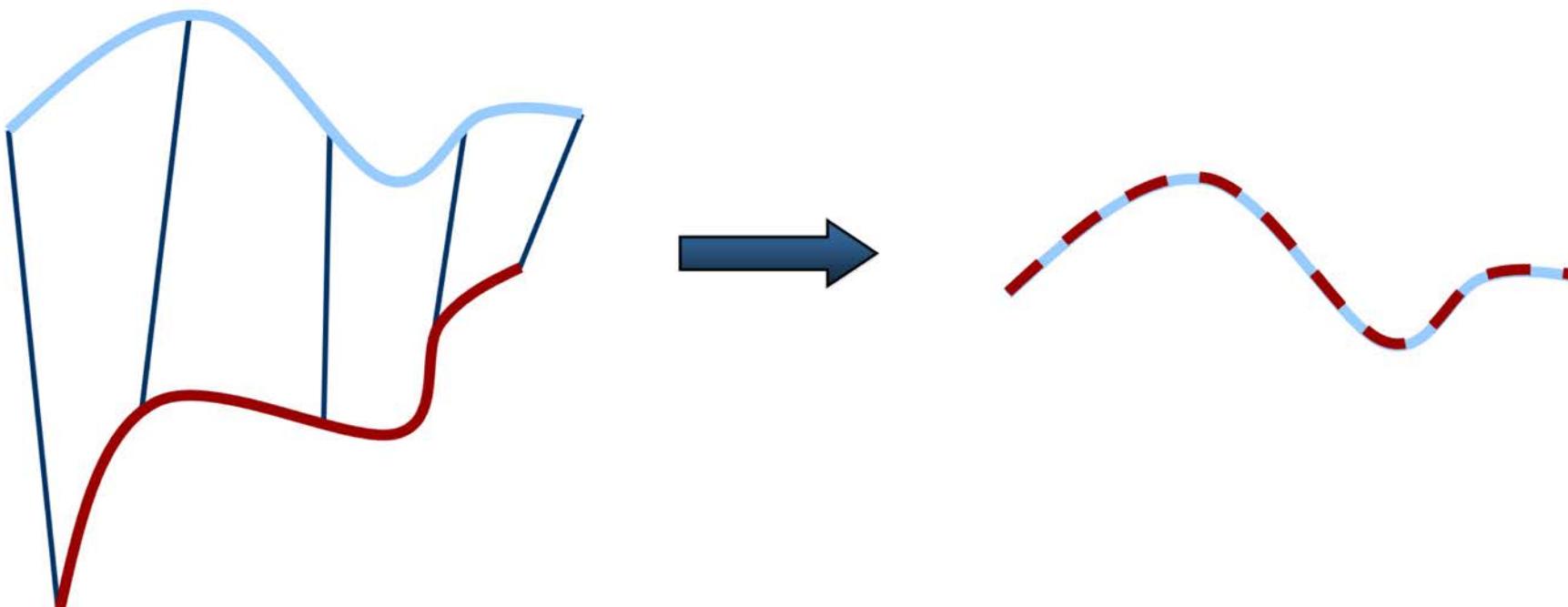
- Wanted: translation t and rotation R that minimizes the sum of the squared error:

$$E(R, t) = \frac{1}{N_p} \sum_{i=1}^{N_p} \|x_i - Rp_i - t\|^2$$

Where x_i and p_i are corresponding points.

Key Idea

- If the correct correspondences are known, the correct relative rotation/translation can be calculated in closed form.



Center of Mass

$$\mu_x = \frac{1}{N_x} \sum_{i=1}^{N_x} x_i \quad \text{and} \quad \mu_p = \frac{1}{N_p} \sum_{i=1}^{N_p} p_i$$

are the centers of mass of the two point sets.

Idea:

- Subtract the corresponding center of mass from every point in the two point sets before calculating the transformation.
- The resulting point sets are:

$$X' = \{x_i - \mu_x\} = \{x'_i\}$$

and

$$P' = \{p_i - \mu_p\} = \{p'_i\}$$

SVD

Let $W = \sum_{i=1}^{N_p} x'_i p_i'^T$

denote the singular value decomposition (SVD) of W by:

$$W = U \begin{bmatrix} \sigma_1 & 0 & 0 \\ 0 & \sigma_2 & 0 \\ 0 & 0 & \sigma_3 \end{bmatrix} V^T$$

where $U, V \in \mathbb{R}^{3 \times 3}$ are unitary, and
 $\sigma_1 \geq \sigma_2 \geq \sigma_3$ are the singular values of W.

SVD

Theorem (without proof):

If $\text{rank}(W) = 3$, the optimal solution of $E(R,t)$ is unique and is given by:

$$R = UV^T$$

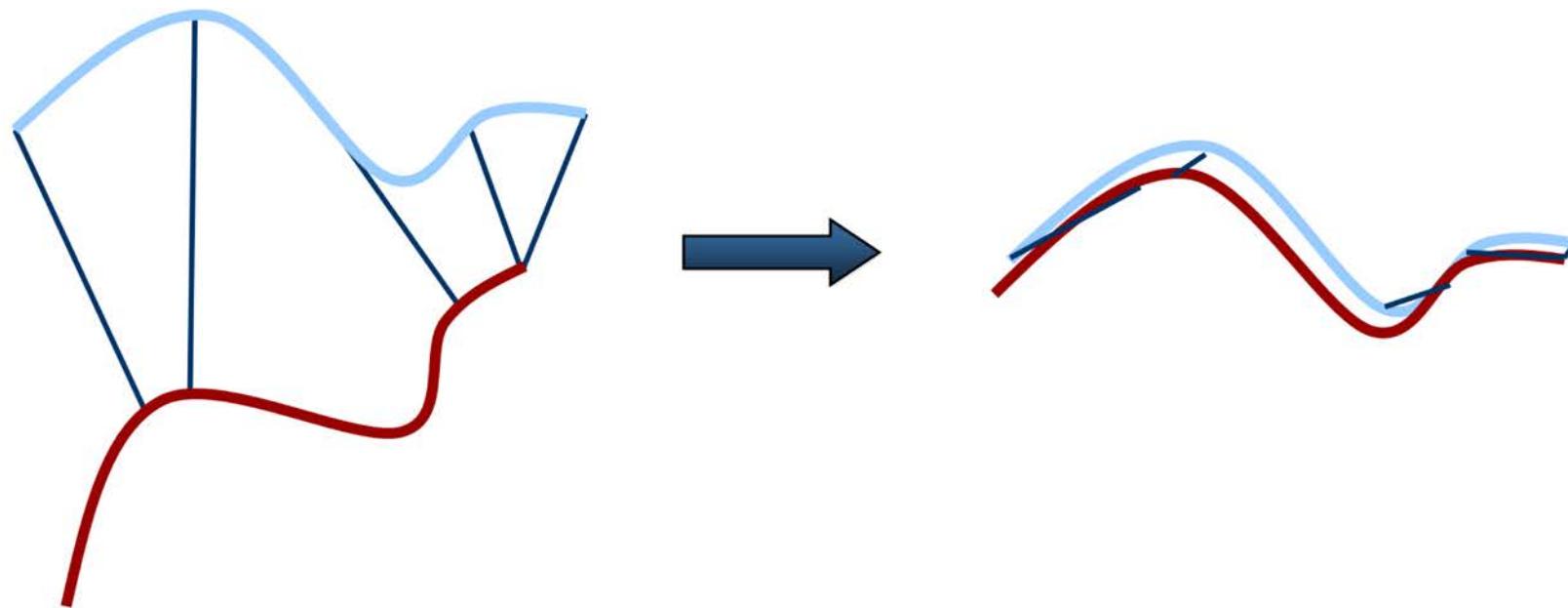
$$t = \mu_x - R\mu_p$$

The minimal value of error function at (R,t) is:

$$E(R, t) = \sum_{i=1}^{N_p} (||x'_i||^2 + ||y'_i||^2) - 2(\sigma_1 + \sigma_2 + \sigma_3)$$

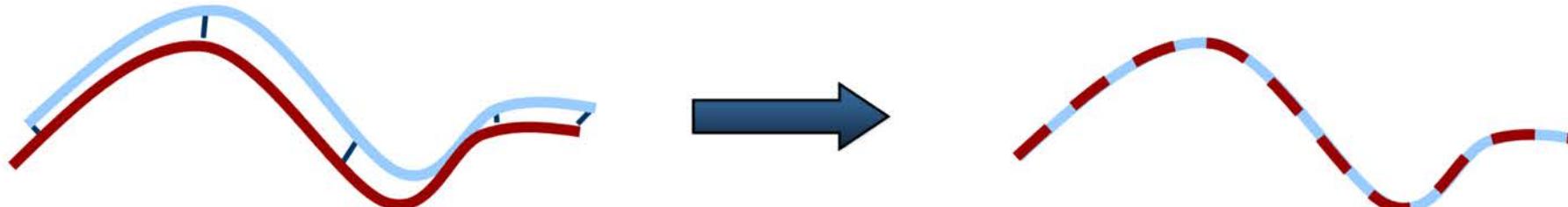
ICP with Unknown Data Association

- If correct correspondences are not known, it is generally impossible to determine the optimal relative rotation/translation in one step



ICP-Algorithm

- Idea: iterate to find alignment
- Iterated Closest Points (ICP)
[Besl & McKay 92]
- Converges if starting positions are “close enough”



ICP-Variants

- Variants on the following stages of ICP have been proposed:
 1. Point subsets (from one or both point sets)
 2. Weighting the correspondences
 3. Data association
 4. Rejecting certain (outlier) point pairs

Performance of Variants

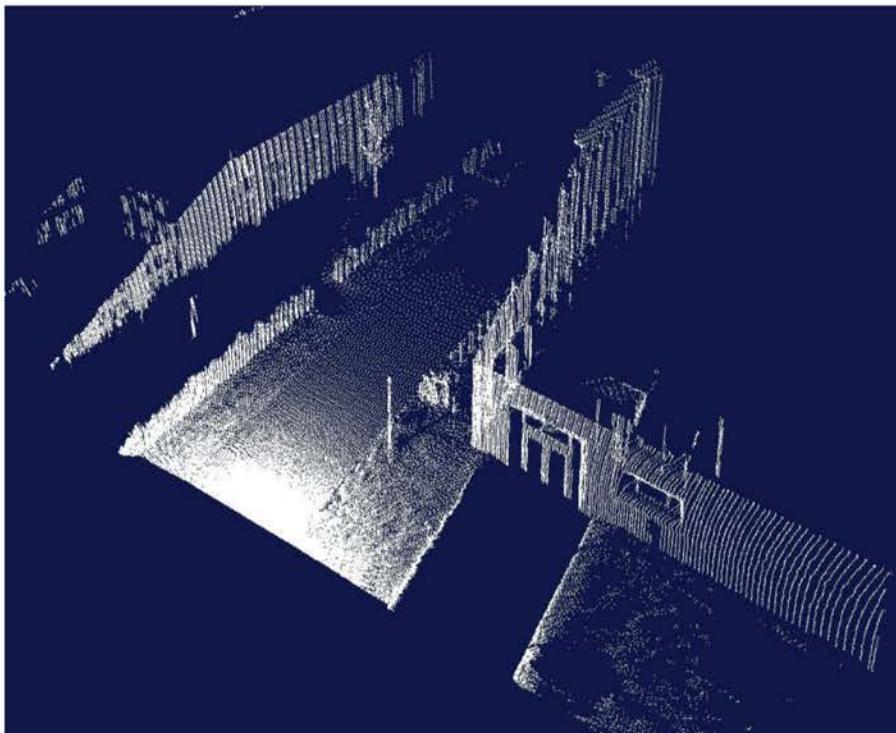
- Various aspects of performance:
 - Speed
 - Stability (local minima)
 - Tolerance wrt. noise and/or outliers
 - Basin of convergence
(maximum initial misalignment)
- Here: properties of these variants

Selecting Source Points

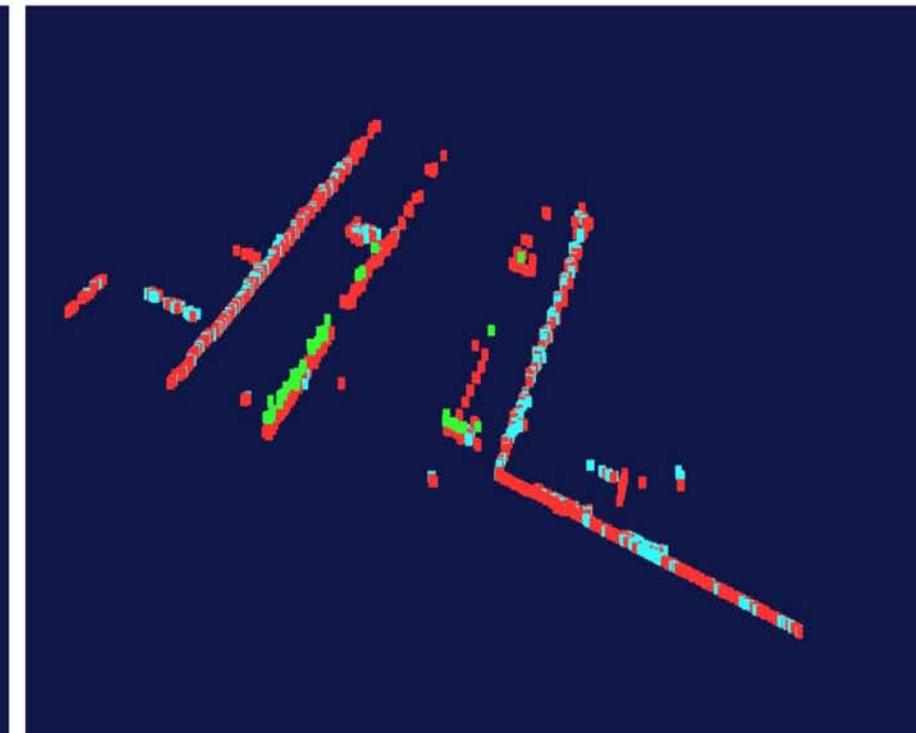
- Use all points
- Uniform sub-sampling
- Random sampling
- Feature based Sampling
- Normal-space sampling
 - Ensure that samples have normals distributed as uniformly as possible

Feature-Based Sampling

- try to find “important” points
- decrease the number of correspondences
- higher efficiency and higher accuracy
- requires preprocessing



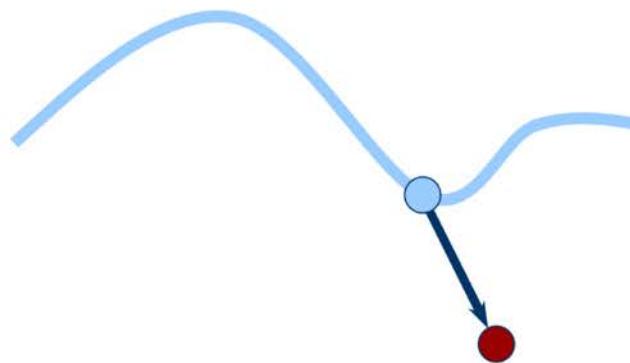
3D Scan (~200.000 Points)



Extracted Features (~5.000 Points)

Closest-Point Matching

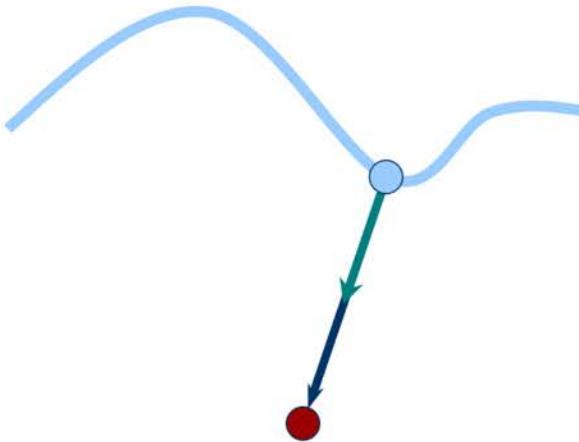
- Find closest point in other the point set



Closest-point matching generally stable,
but slow and requires preprocessing

Normal Shooting

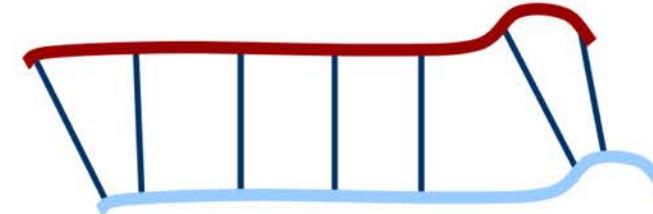
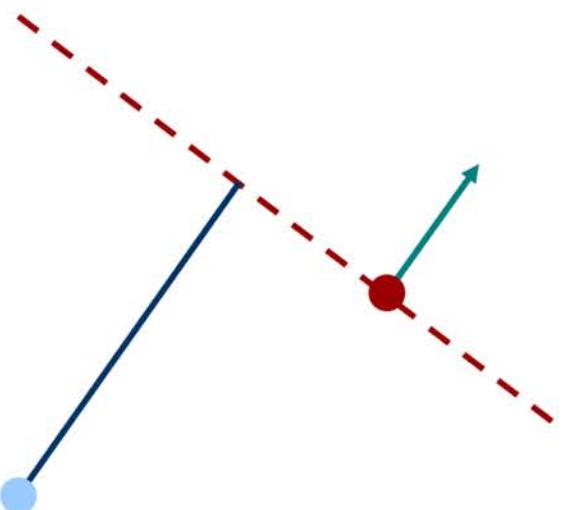
- Project along normal, intersect other point set



Slightly better than closest point for smooth structures, worse for noisy or complex structures

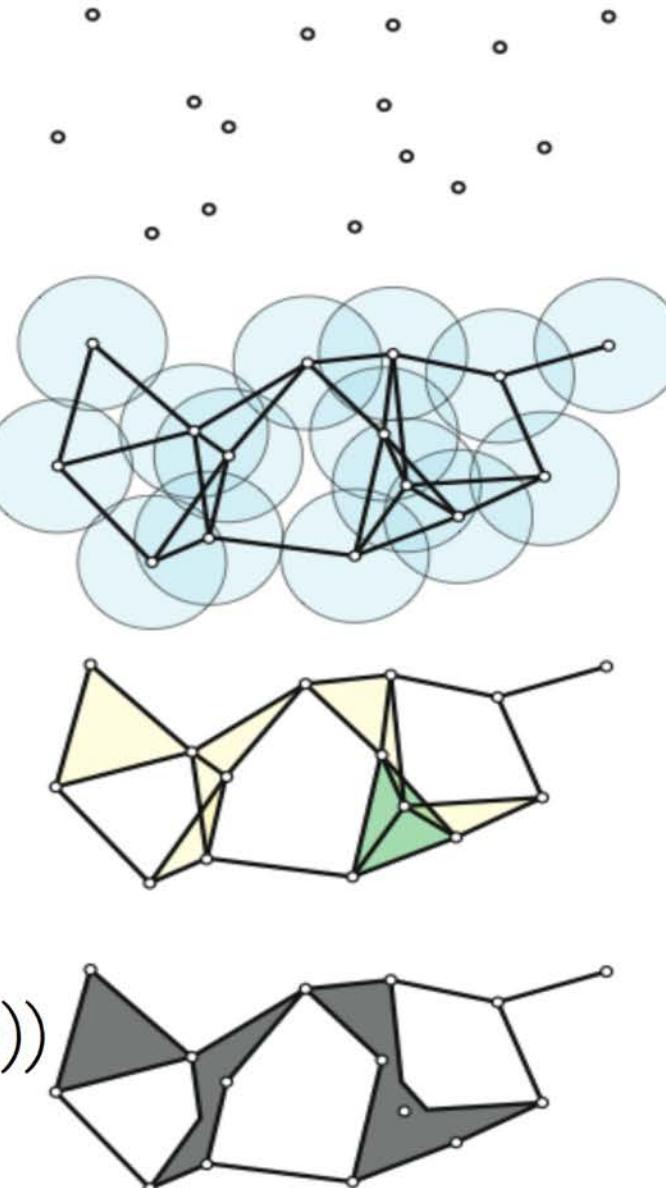
Point-to-Plane Error Metric

- Using point-to-plane distance instead of point-to-point lets flat regions slide along each other [Chen & Medioni 91]



Data Types

- Point sets
- Line segment sets (polylines)
- Implicit curves : $f(x,y,z) = 0$
- Parametric curves : $(x(u),y(u),z(u))$
- Triangle sets (meshes)
- Implicit surfaces : $s(x,y,z) = 0$
- Parametric surfaces $(x(u,v),y(u,v),z(u,v))$



Various Different Ways to Realize Scan-Matching

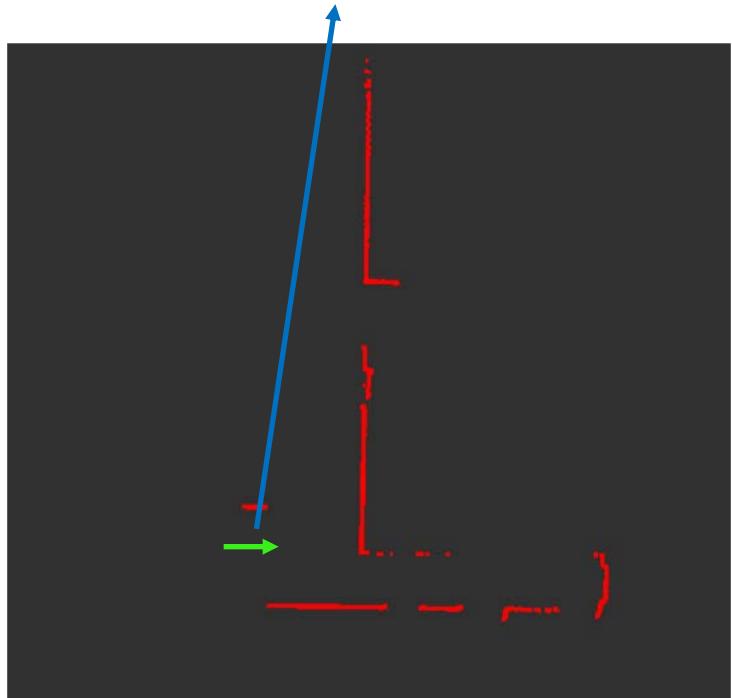
- Iterative closest point (ICP)
- Scan-to-scan
- Scan-to-map
- Map-to-map
- Feature-based
- RANSAC for outlier rejection

ICP Assumptions and Limitations

- Assumes a sufficiently fast scan rate
 - Significant overlap will exist between sequential scans
 - Points with high correspondence will exist
- Assumes surface will be non-smooth and heterogeneous
 - Smooth surface will look the same to the algorithm

Scan Matching

Pose of the Car at $t = t_1$



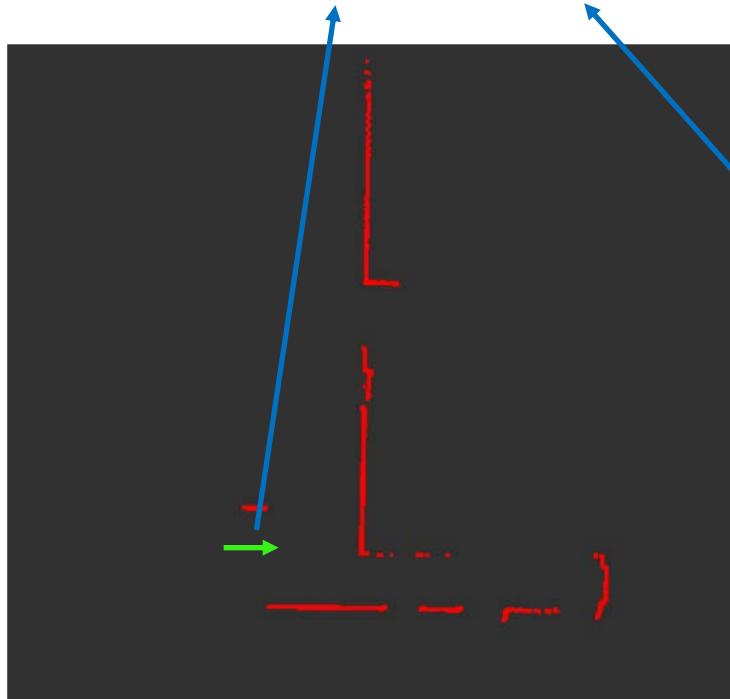
Laser Scans w.r.t car at Time $t = t_1$



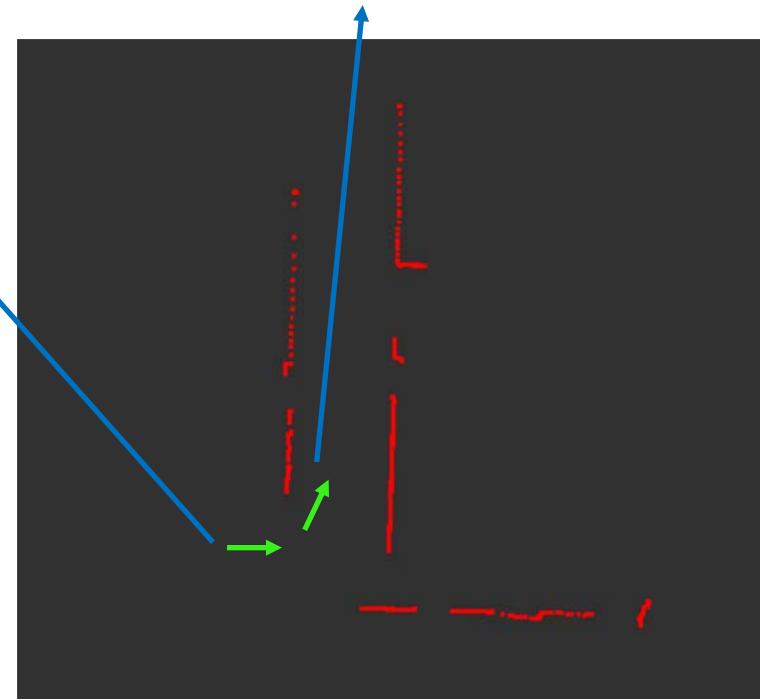
Laser Scans w.r.t car at Time $t = t_2$

Scan Matching

Pose of the Car at $t = t_1$



Pose of the Car at $t = t_2$



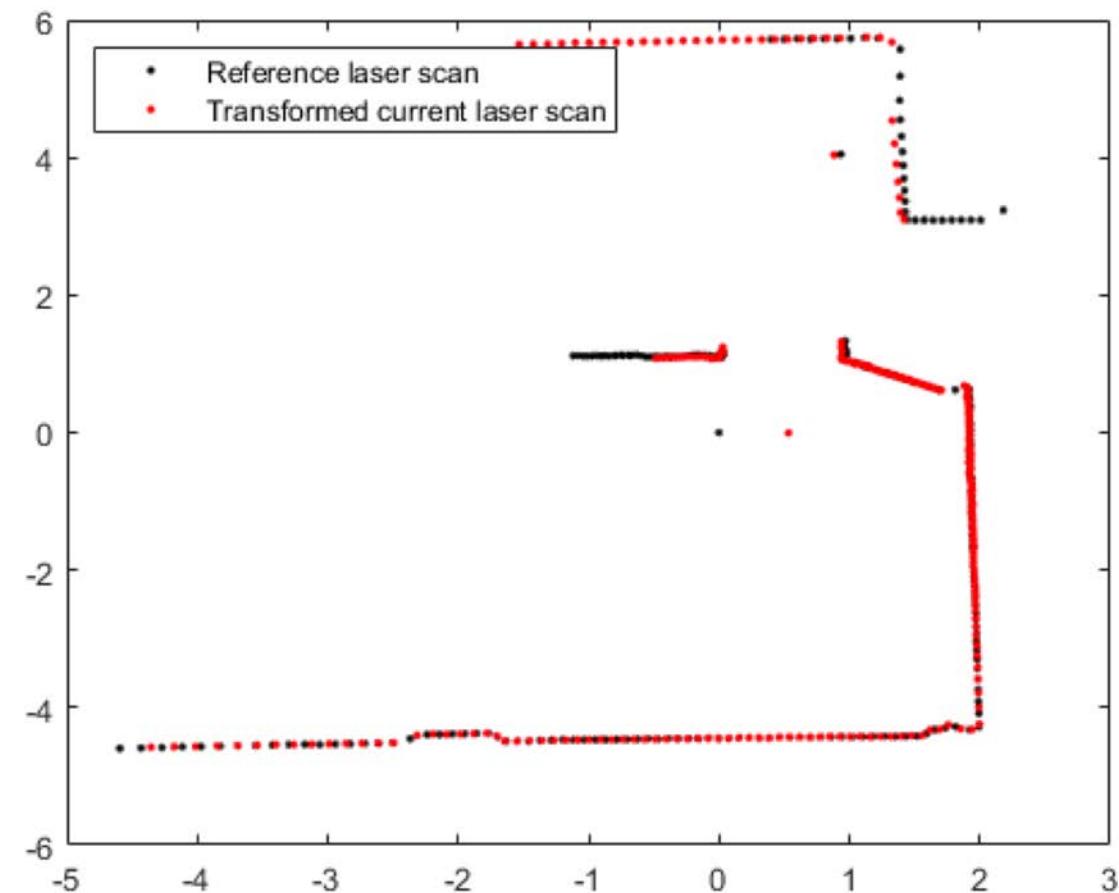
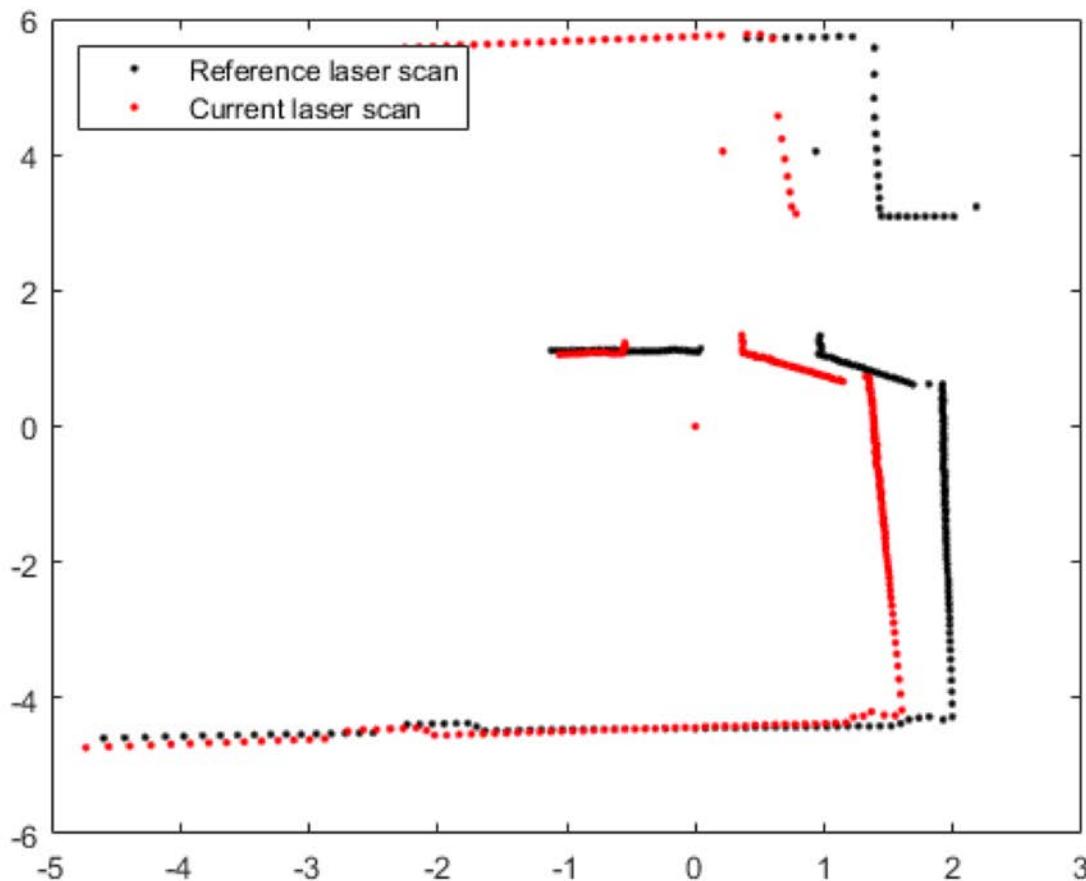
Laser Scans w.r.t car at Time $t = t_1$

Laser Scans w.r.t car at Time $t = t_2$

```
transform = matchScans(currentScan, referenceScan)
```

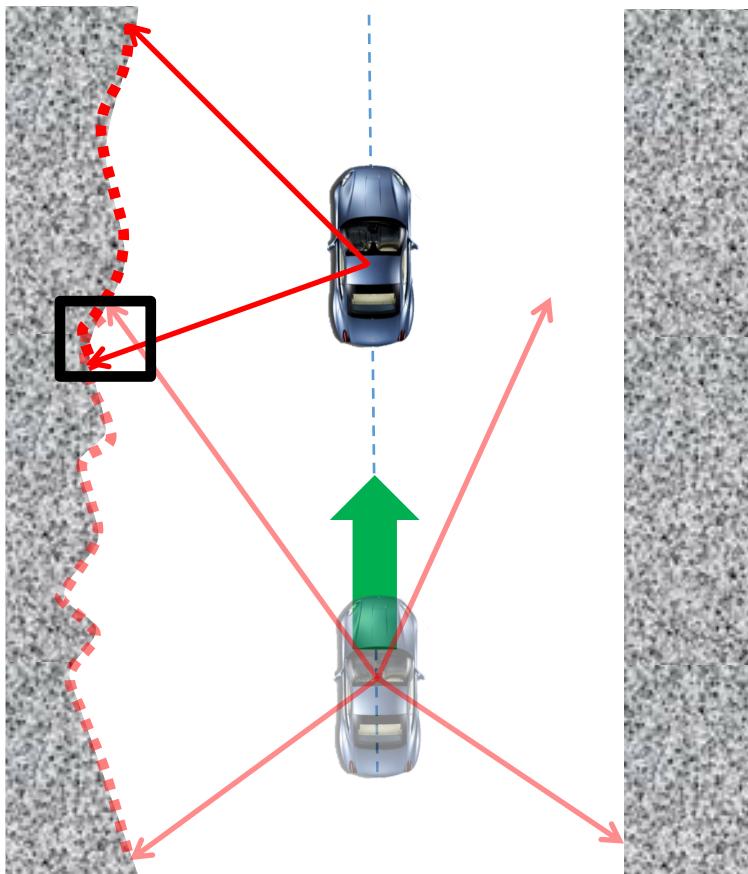
transform = 1×3

0.5348 -0.0065 -0.0336



Scan matching: requirements

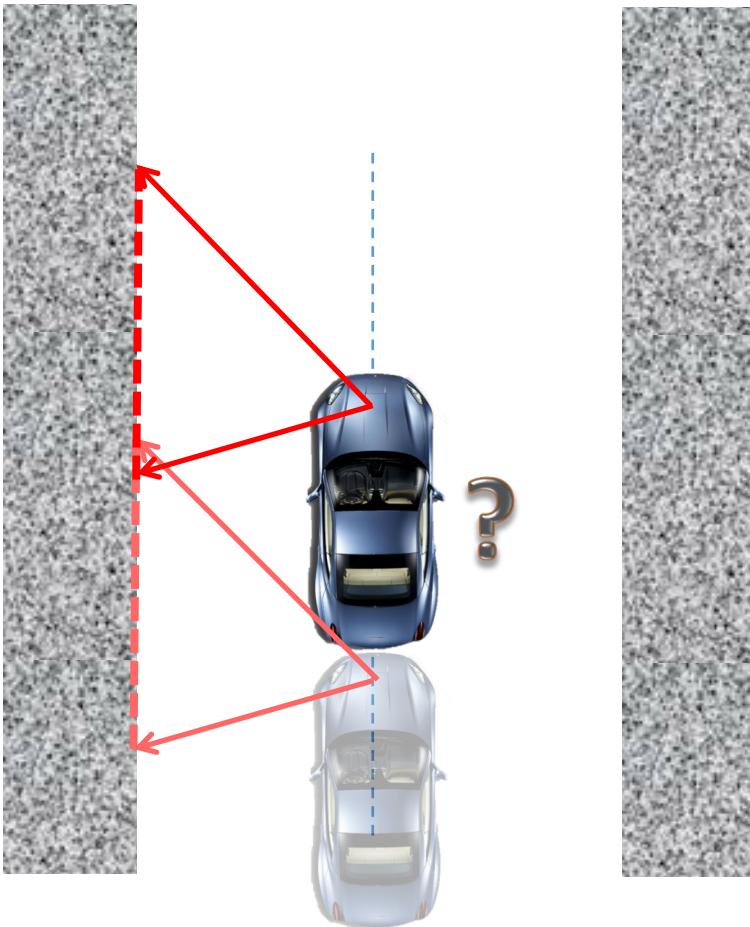
Left Wall



Right Wall

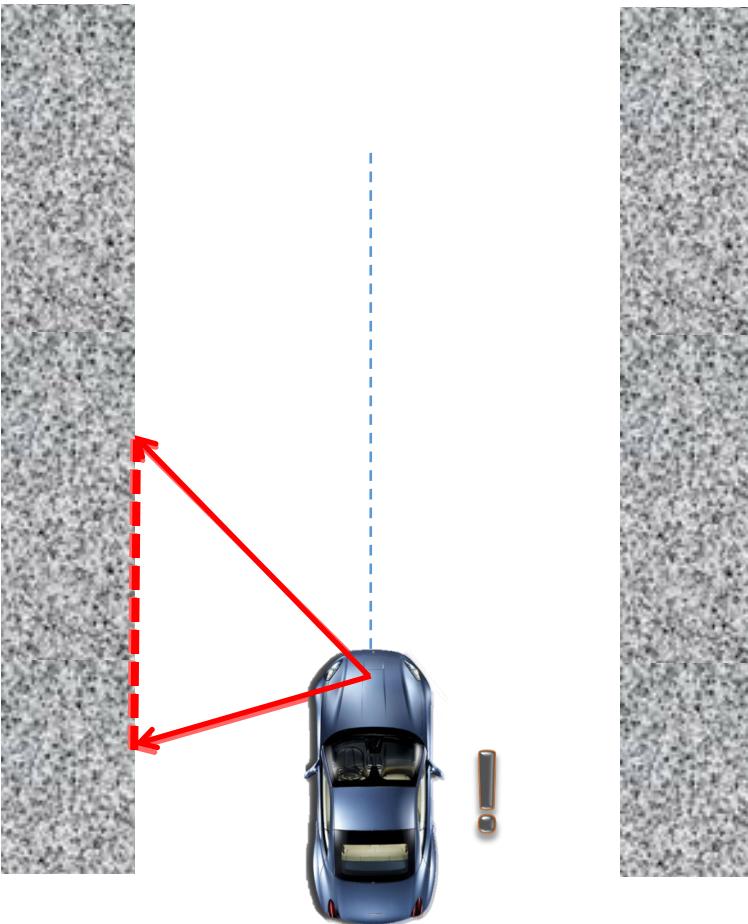
- Sufficiently fast scan rate
- A slow scan rate can lead to few matches between scans.
- Not really a risk for today's LIDARs

Scan matching : requirements



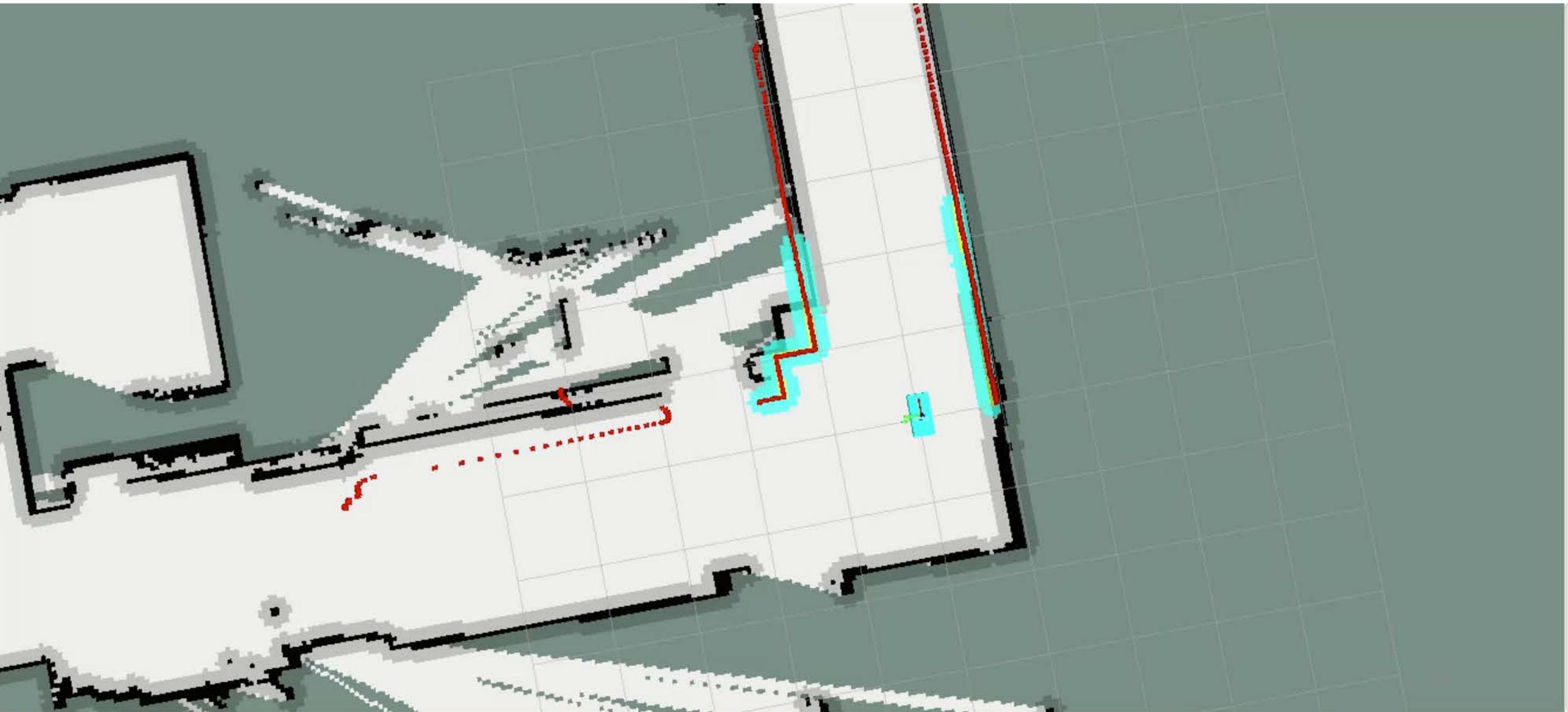
- Non-smooth, or heterogeneous, surfaces.
- Smooth surfaces all look the same to the matching algorithm.

Scan matching : requirements



- Non-smooth, or heterogeneous, surfaces.
- Best match between scans is if car did not move.

Failed scan matching



Order your Melodic Tshirt before the campaign ends May 8th! You can choose US Fulfillment or EU Fulfillment. X



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Package Summary

✓ Released ✗ No API documentation

A ROS node to provide access to SCIP 2.0-compliant Hokuyo laser range finders (including 04LX).

- Maintainer status: maintained
- Maintainer: Chad Rockey <chadrockey AT gmail DOT com>
- Author: Brian P. Gerkey, Jeremy Leibs, Blaise Gassend
- License: LGPL

Package Links

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Package Summary

[!\[\]\(e83f1ece1f519a598f38d7ee921e4a69_img.jpg\) Released](#)[!\[\]\(ad85e0cfbe0a2aa8295ac05c02ee1d63_img.jpg\) Continuous integration](#)[!\[\]\(b60e02e03923f431b60a2a62b0b654f9_img.jpg\) Documented](#)

urg_node

- Maintainer status: maintained
- Maintainer: Tony Baltovski <tony.baltovski AT gmail DOT com>
- Author: Chad Rockey <chadrockey AT gmail DOT com>, Mike O'Driscoll <modriscoll AT clearpath DOT ai>
- License: BSD

Package Links

[Code API](#)[Msg API](#)[FAQ](#)[Changelog](#)[Change List](#)[Reviews](#)[Dependencies \(14\)](#)[Used by \(3\)](#)[Jenkins jobs \(10\)](#)[Distributions](#)[ROS/Installation](#)[ROS/Tutorials](#)[RecentChanges](#)[urg_node](#)[Page](#)[Immutable Page](#)[Info](#)[Attachments](#)[More Actions:](#) [User](#)

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[laser_scan_matcher](#)

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[scan_tools](#): [laser_ortho_projector](#) | [laser_scan_matcher](#) | [laser_scan_sparsifier](#) | [laser_scan_splitter](#) | [ncd_parser](#) | [polar_scan_matcher](#) | [scan_to_cloud_converter](#)

Package Summary

 Released  Continuous integration  Documented

An incremental laser scan matcher, using Andrea Censi's Canonical Scan Matcher (CSM) implementation. See [the web site](#) for more about CSM. NOTE the CSM library is licensed under the GNU Lesser General Public License v3, whereas the rest of the code is released under the BSD license.

- Maintainer status: maintained
- Maintainer: Ivan Drwanovski <cenvroboticslab@gmail.com>, Carlos <ciaramillo@ccnunv.edu>, Isaac

Package Links

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Dependencies (10)

Used by (1)

Jenkins jobs (10)

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laser_scan_matcher: ROS

4.3.6 Scan matching

`~max_iterations (int, default: 10)`

Maximum ICP cycle iterations

`~max_correspondence_dist (double, default: 0.3)`

Maximum distance for a correspondence to be valid

`~max_angular_correction_deg (double, default: 45.0)`

Maximum angular displacement between scans, in degrees

`~max_linear_correction (double, default: 0.50)`

Maximum translation between scans (m)

`~epsilon_xy (double, default: 0.000001)`

A threshold for stopping (m)

`~epsilon_theta (double, default: 0.000001)`

A threshold for stopping (rad)

`~outliers_maxPerc (double, default: 0.90)`

Percentage of correspondences to consider: if 0.90, always discard the top 10% of correspondences with more error

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Package Summary

✓ Released ✓ Continuous integration ✓ Documented

Laser scan processing tools.

- Maintainer status: maintained
- Maintainer: Ivan Dryanovski <ccnyroboticslab AT gmail DOT com>, Carlos
 <ciaramillo AT cs.cuny DOT edu>, Isaac I Y Saito <iisvsaito AT opensource-robotics.tokyo DOT in>

Package Links

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Dependencies (8)

[Jenkins jobs \(10\)](#)

[Page](#)

[Immutable Page](#)

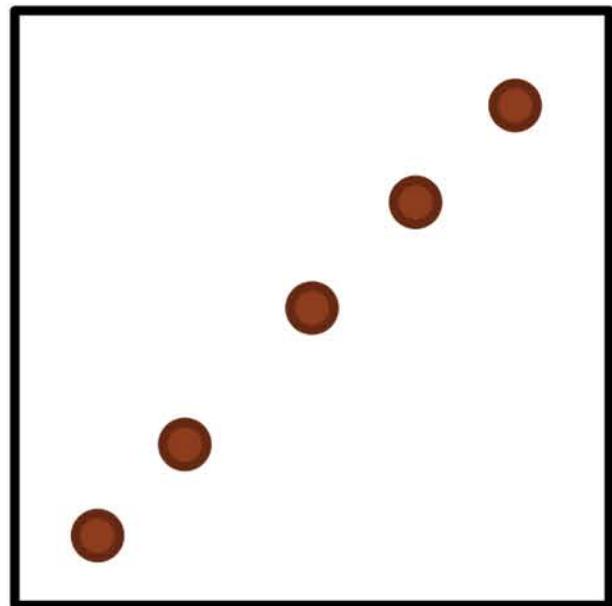
[Info](#)

[Attachments](#)

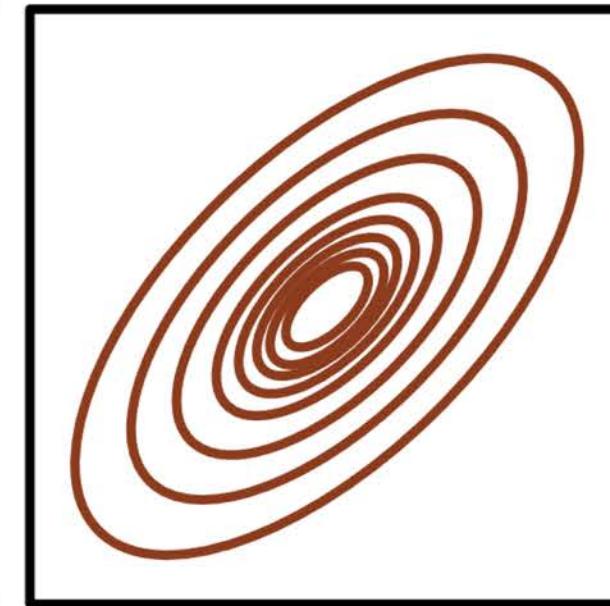
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2

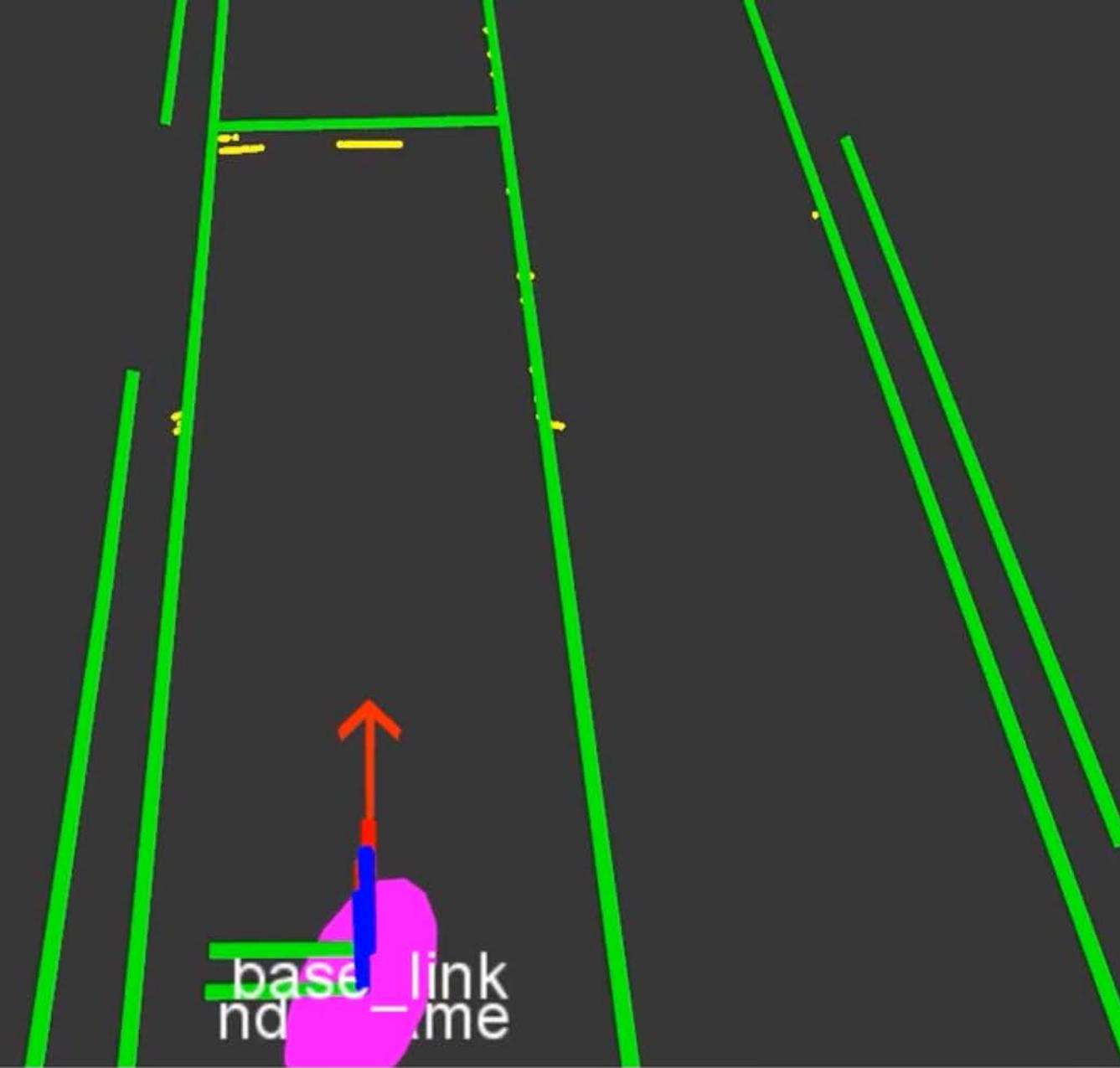
Normal Distribution Transform



n points
measured in a 2D
cell.
 n points,
 $2n$ parameters



Gaussian
approximation
for the 2D cell.
1 distribution,
5 parameters



NDT result is used as likelihood function in particle filtering algorithm.

Road marker matching is also used to improve localization accuracy.

Overall Algorithm

Input data:

- Reference scan, y_{t-1} , current scan y_t , initial guess of **roto-transformation** q_0

Output:

- Transformation q , the converged solution representing the roto-transformation between the scans

Overall Algorithm

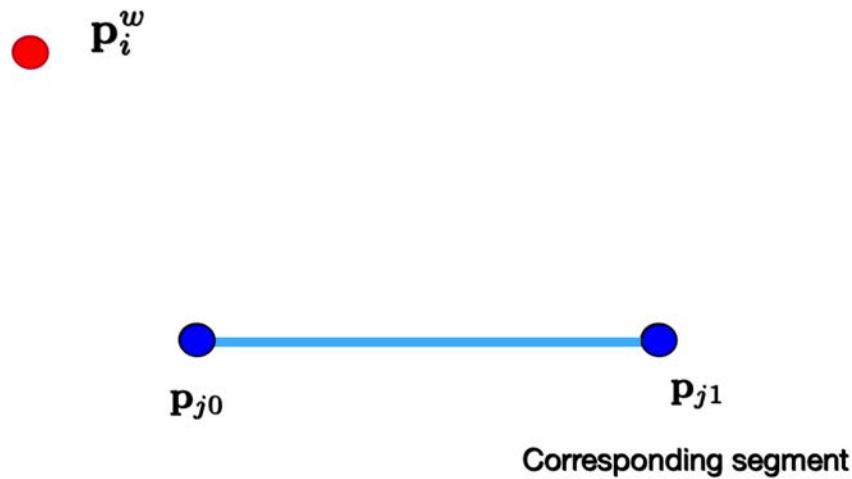
At $t=k$

1. Use previous guess q_k , transform coordinates of current scan into the frame of the previous scan
2. For each point, find closest line segment (**point-to-line correspondence search**)
3. Update transform
 - a. Formulate point-to-line-error objective
 - b. Find transform q_{k+1} that minimizes objective

(Repeat until convergence)

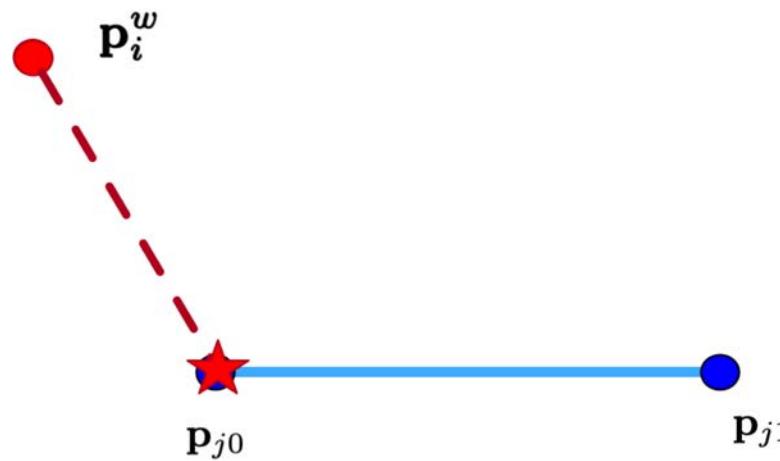
Point-to-point vs Point-to-line

Given a point in current scan and corresponding **line segment**



Point-to-point vs Point-to-line

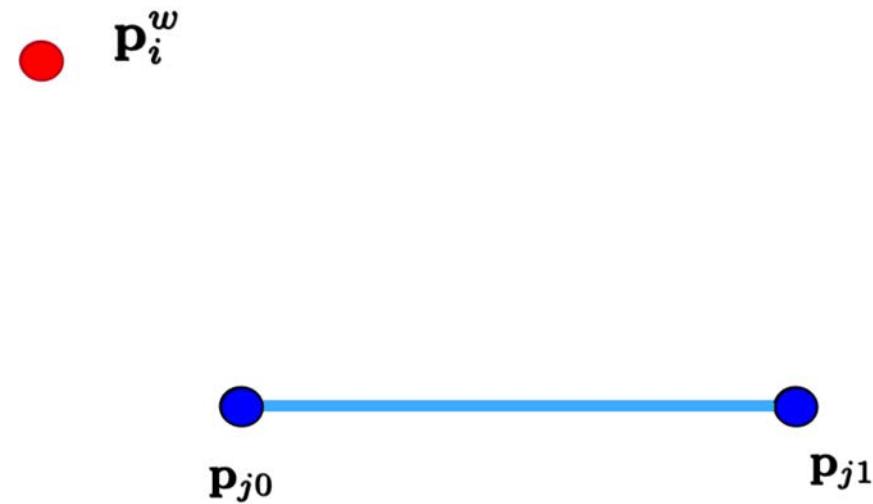
Point-to-point measures the distance as the distance to the nearest **point on the segment**



Projection onto a line segment

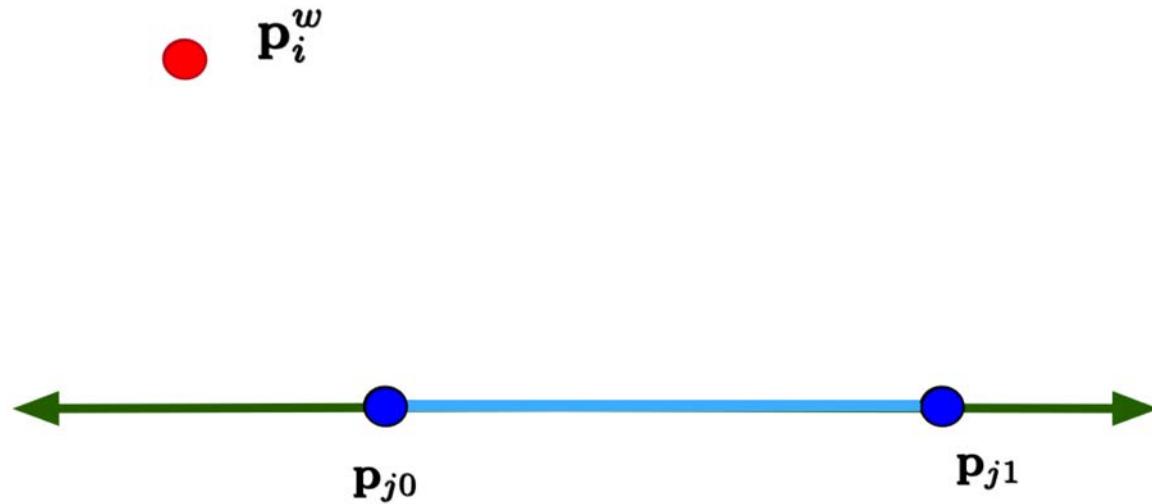
Point-to-point vs Point-to-line

Point-to-line measures the distance as the distance to the nearest **line containing the segment**



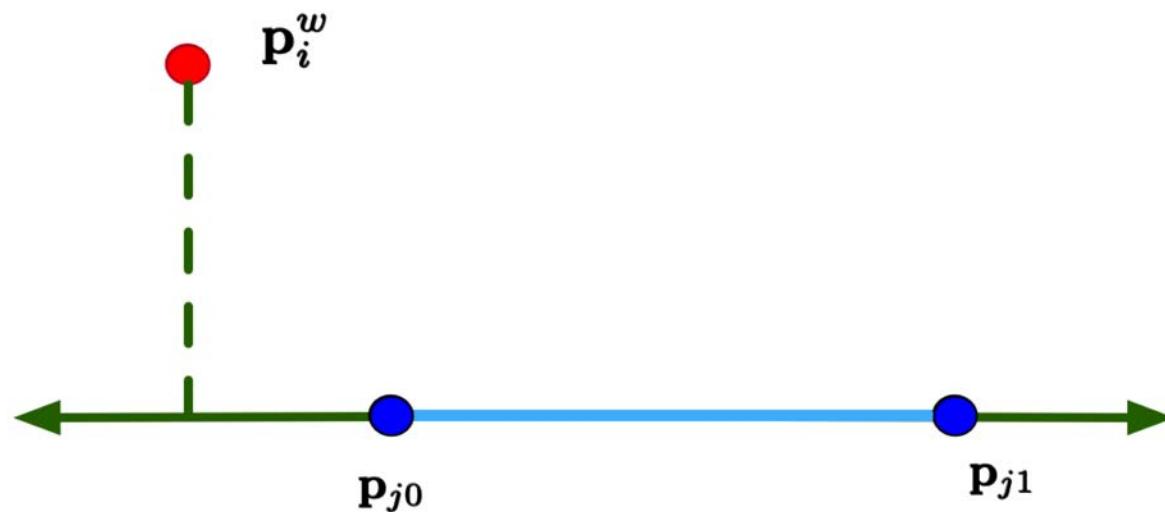
Point-to-point vs Point-to-line

Point-to-line measures the distance as the distance to the nearest **line containing the segment**



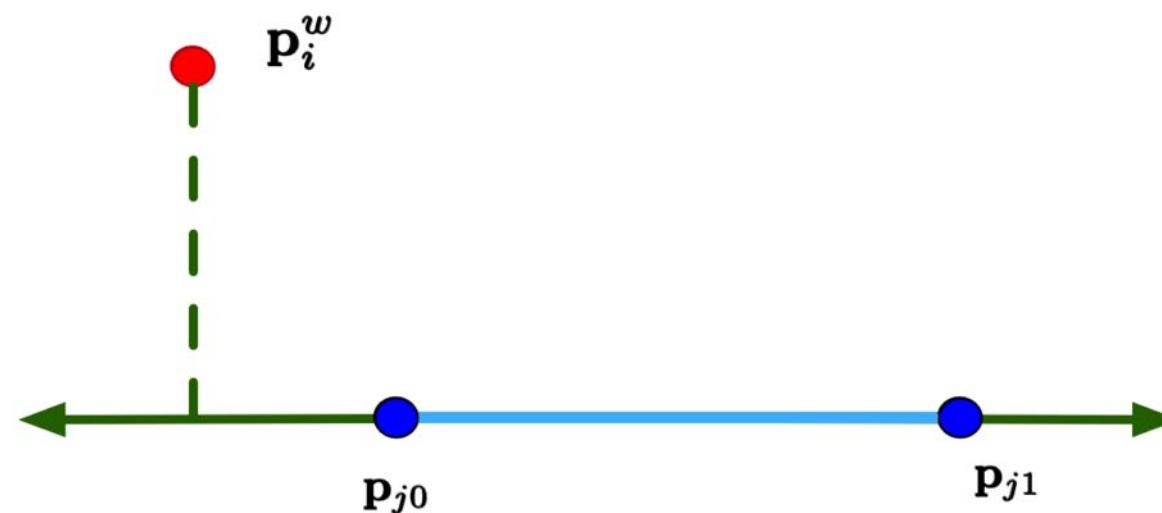
Point-to-point vs Point-to-line

Point-to-line measures the distance as the distance to the nearest **line containing the segment**



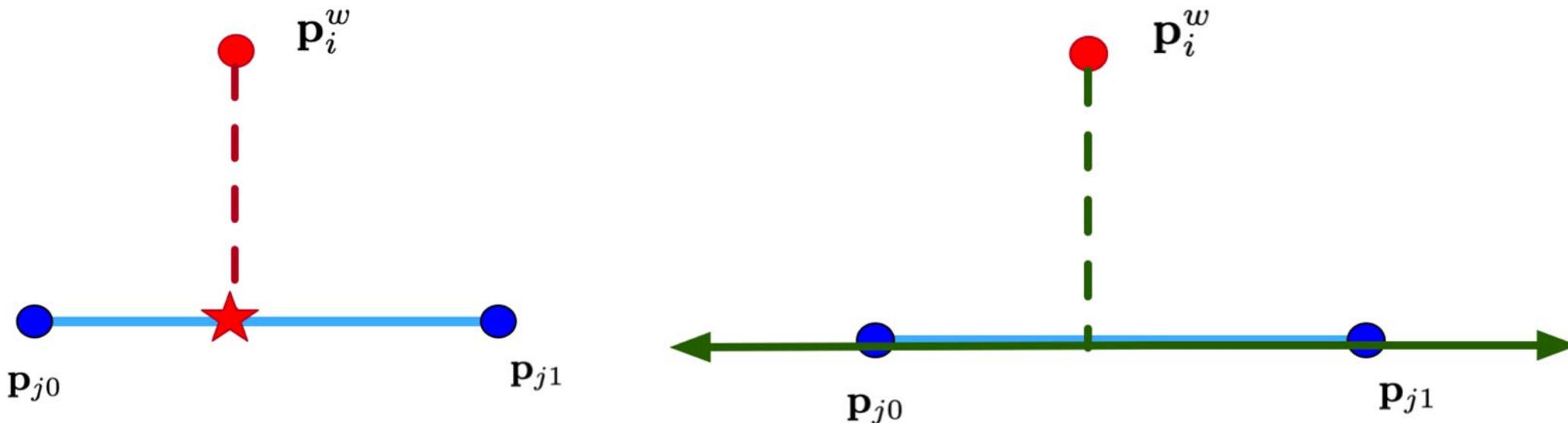
Point-to-line

Point-to-line measures the distance as the distance to the nearest **line containing the segment**

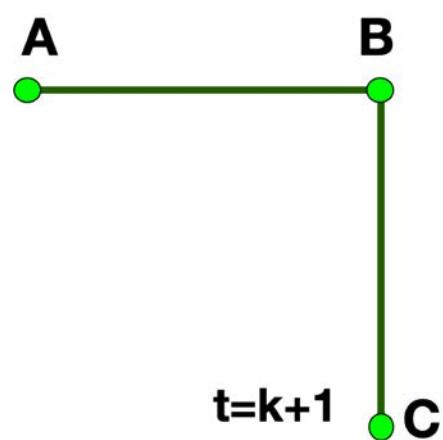
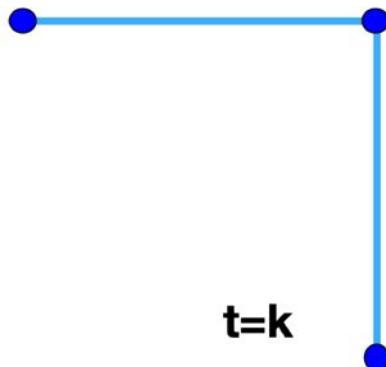


Point-to-point vs Point-to-line

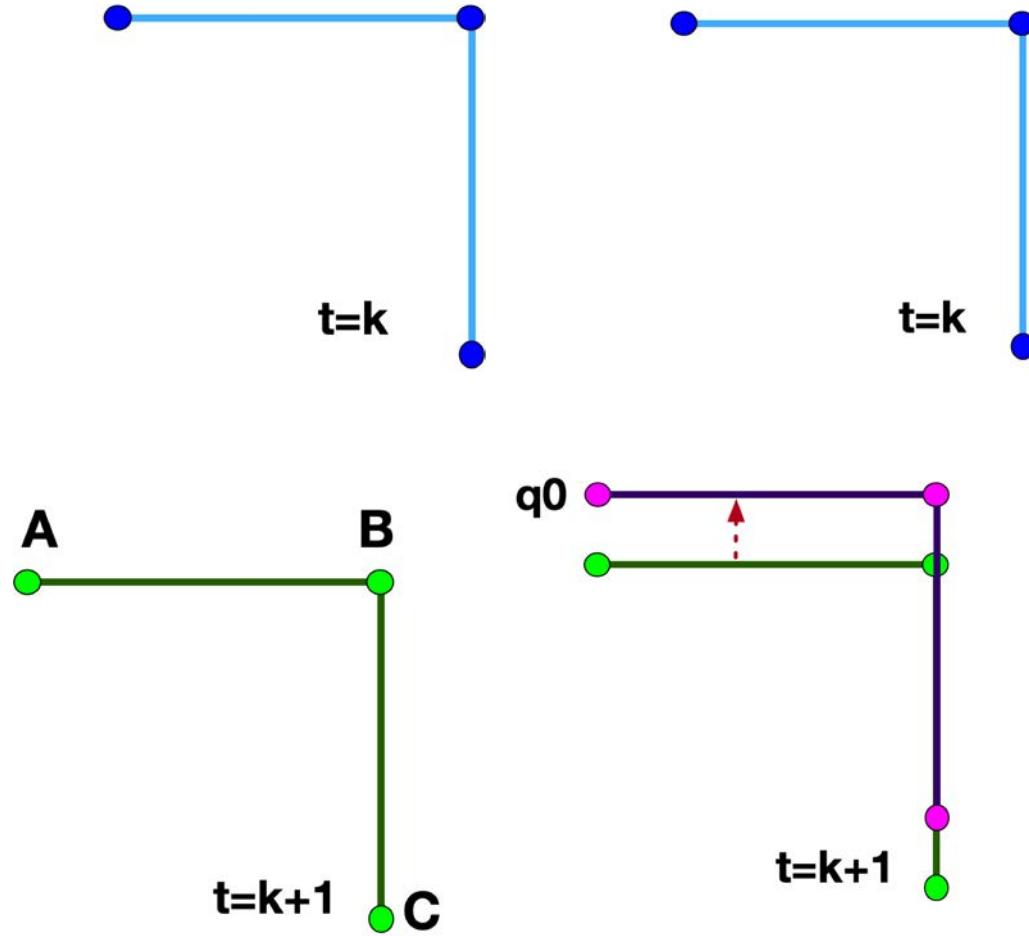
- Point-to-point and point-to-line may coincide in value
- Even in this case,
 - point-to-point **point on the nearest line segment**
 - point-to-line is finding distance to nearest line



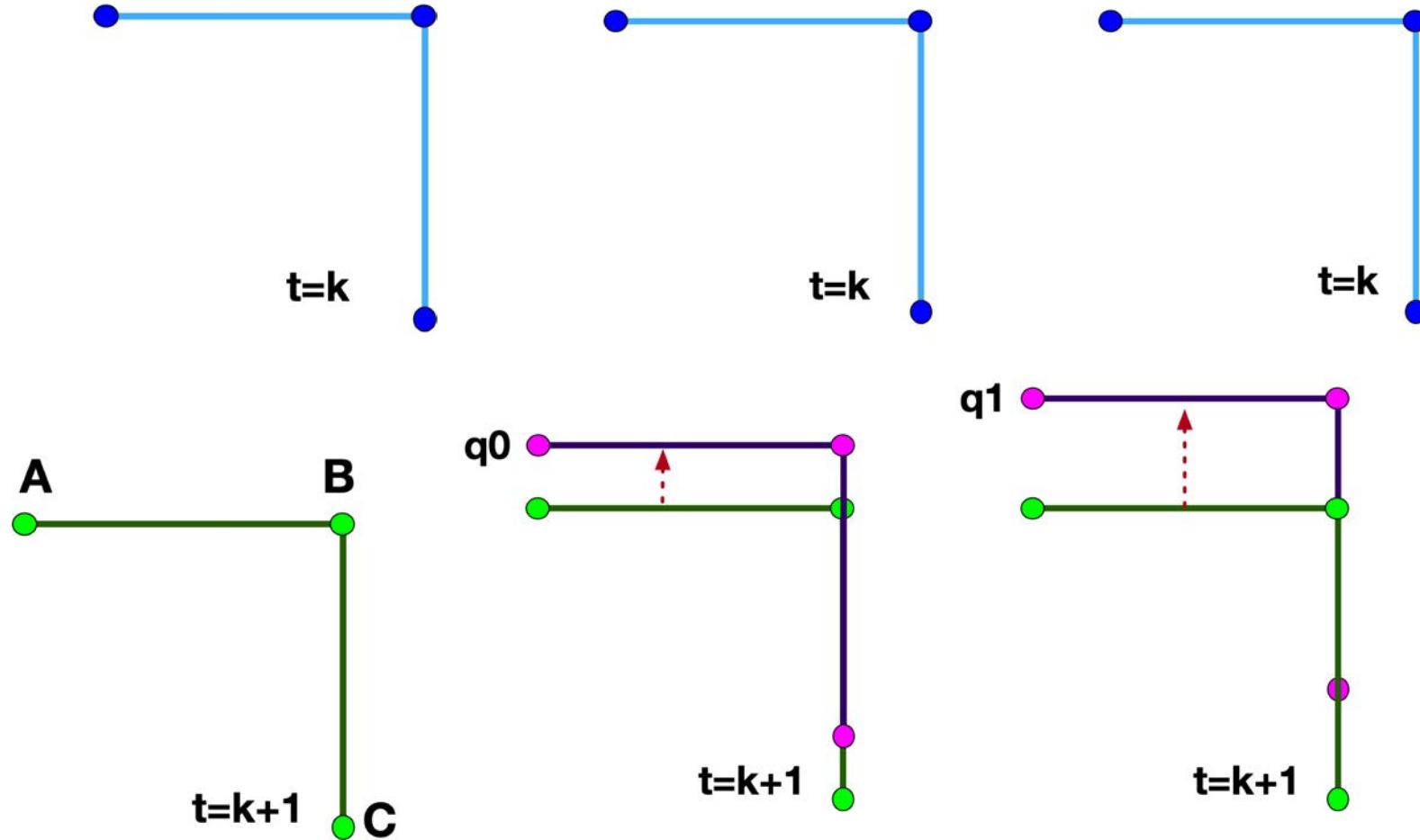
Why is it faster?



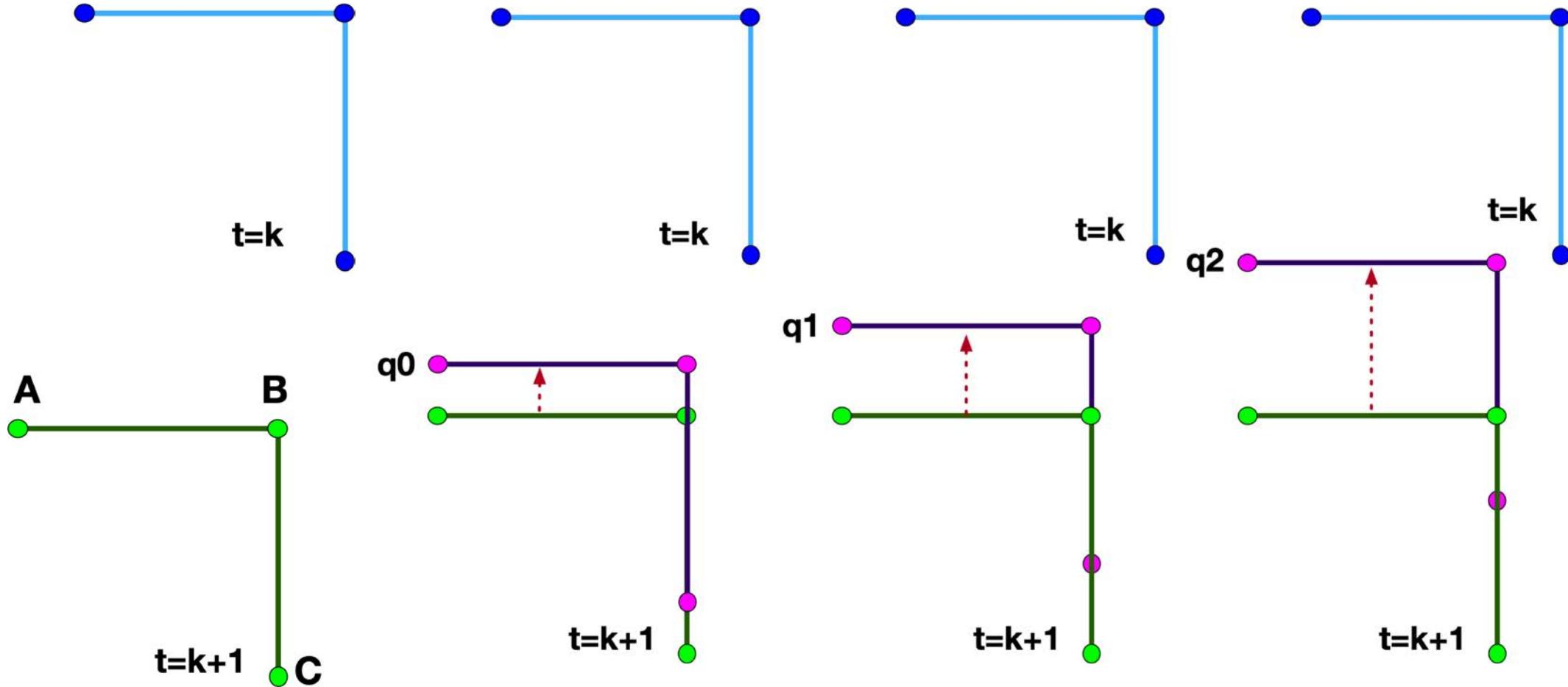
Why is it faster?



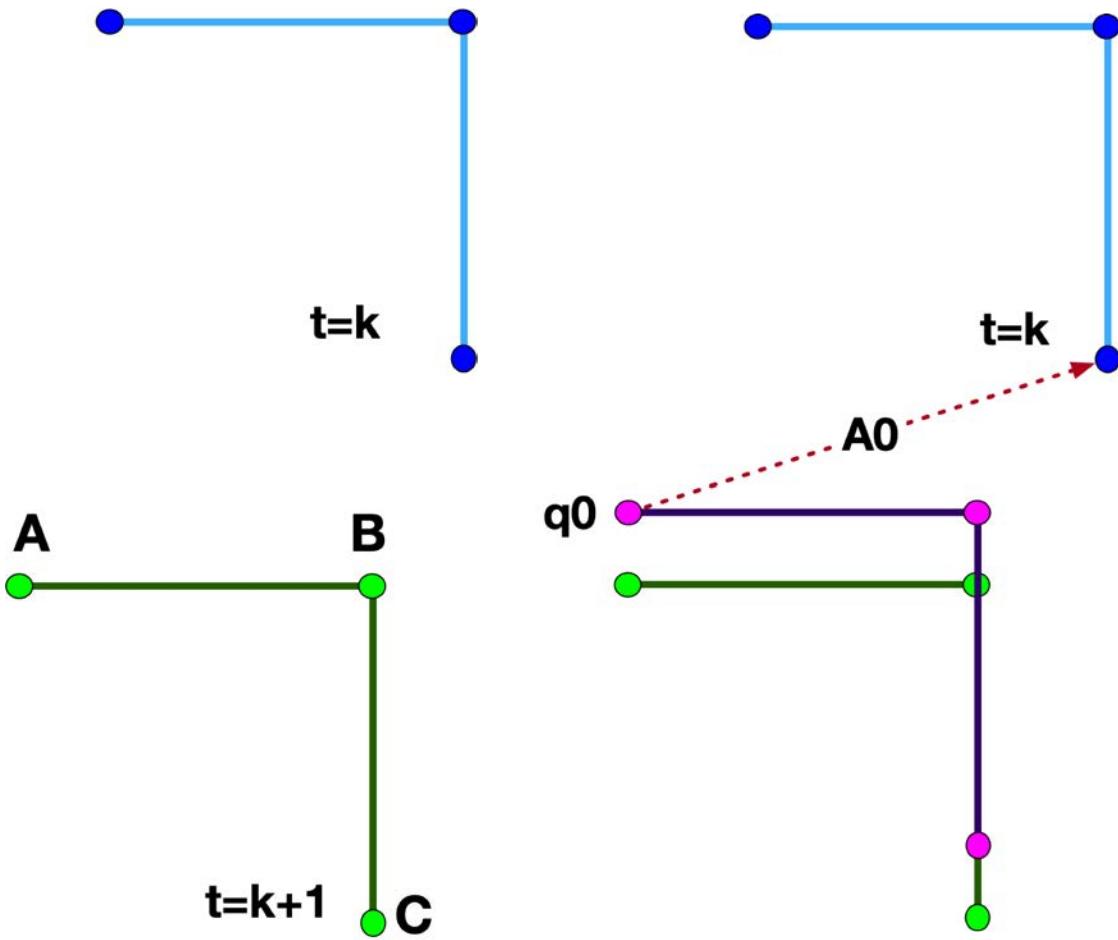
Why is it faster?



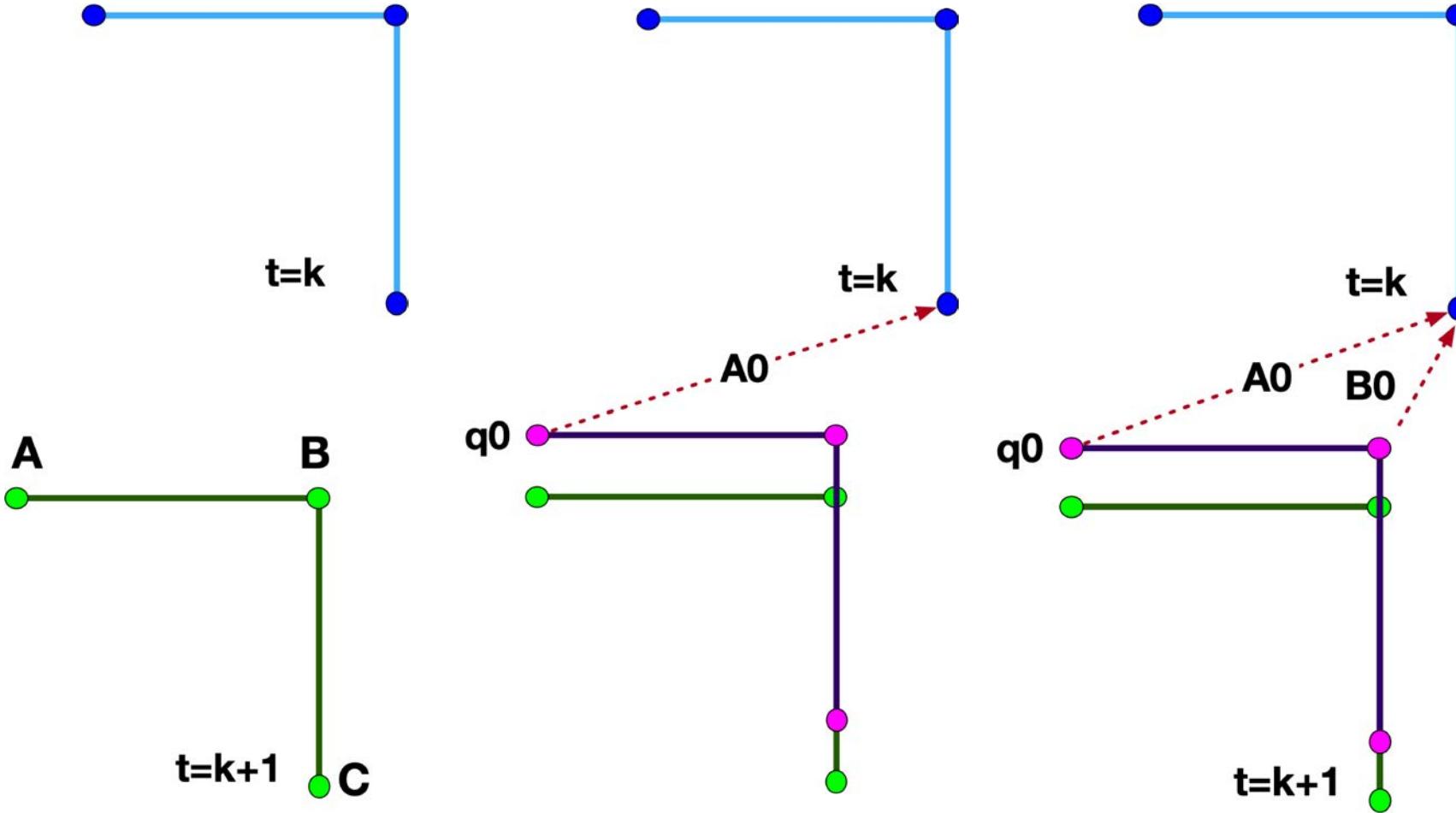
Why is it faster?



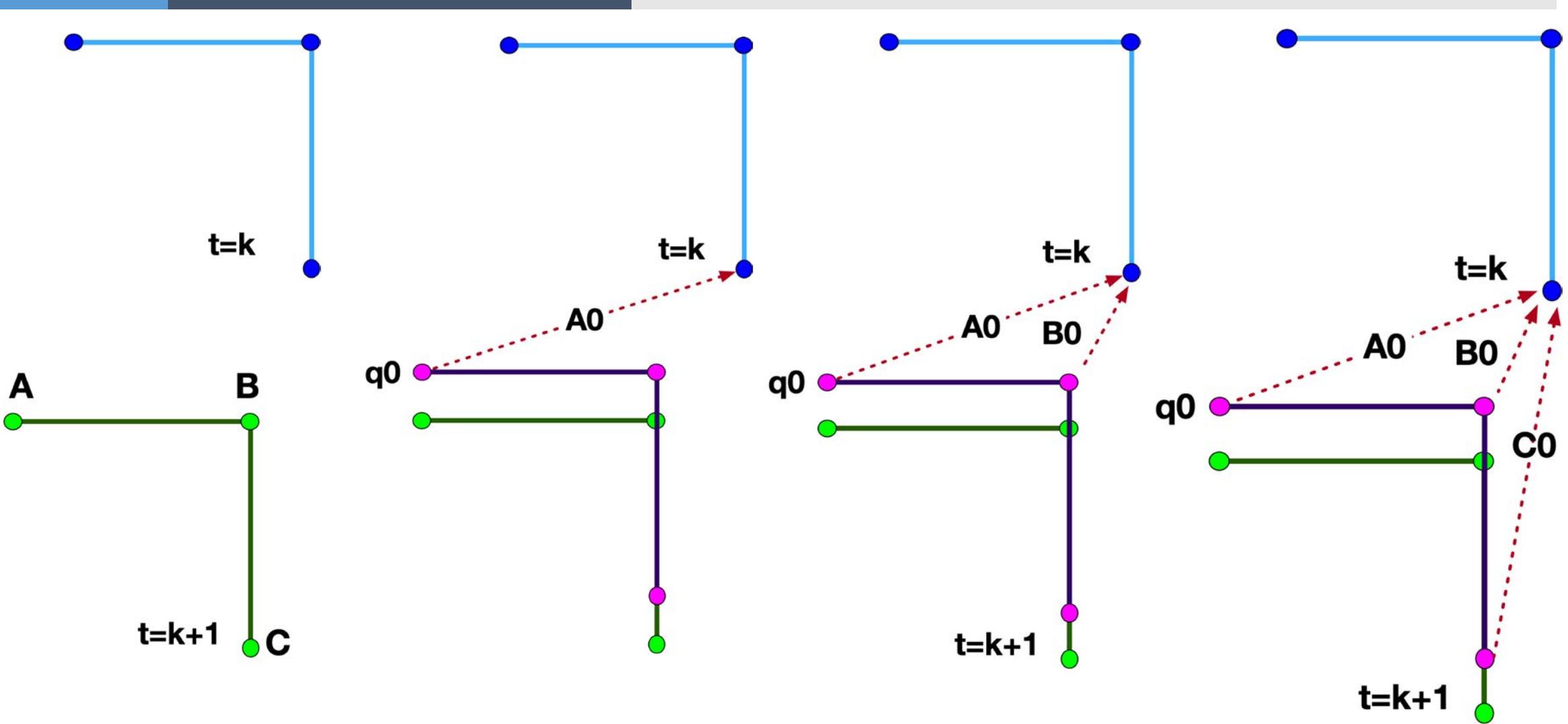
Point-to-point Metric



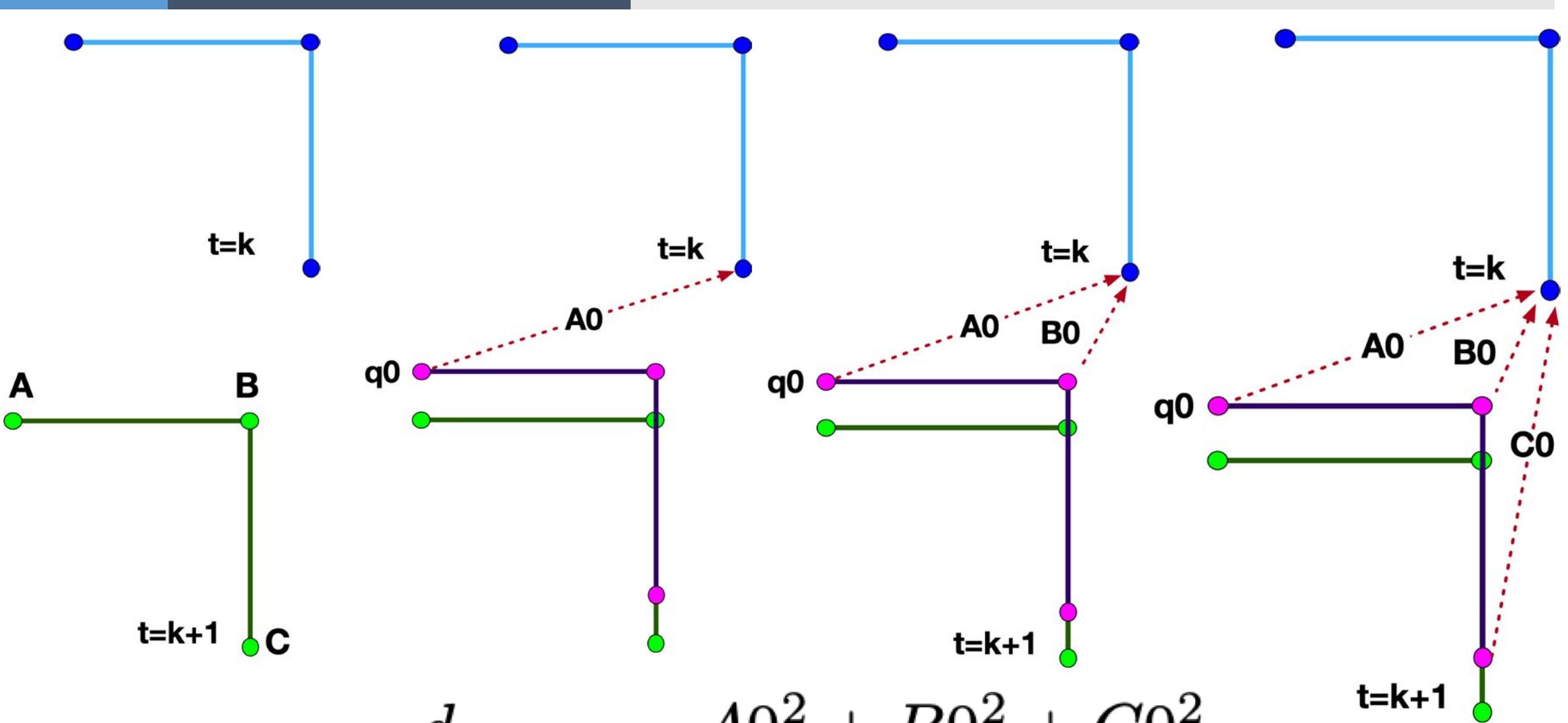
Point-to-point Metric



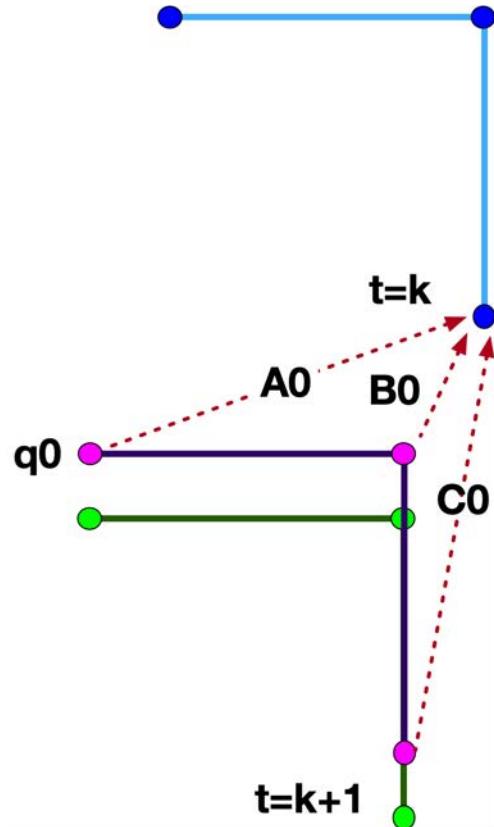
Point-to-point Metric



Point-to-point Metric

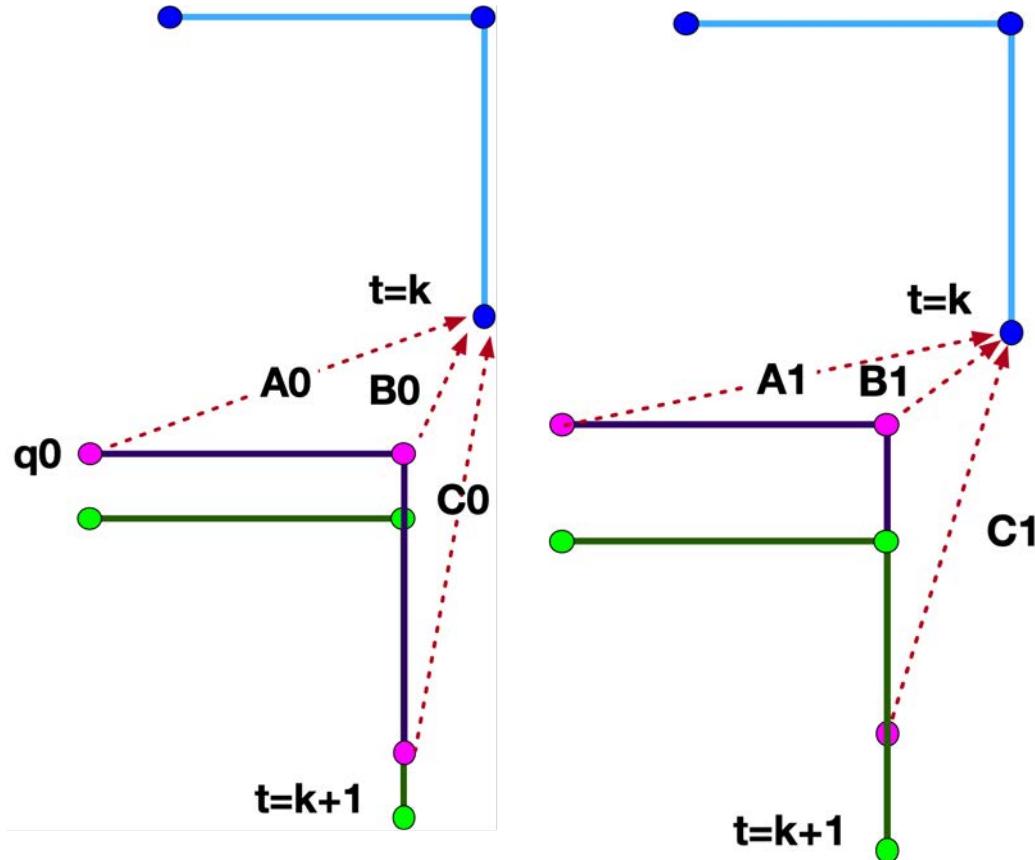


Point-to-point Metric



$$d_{p2p,q_0} = A_0^2 + B_0^2 + C_0^2$$

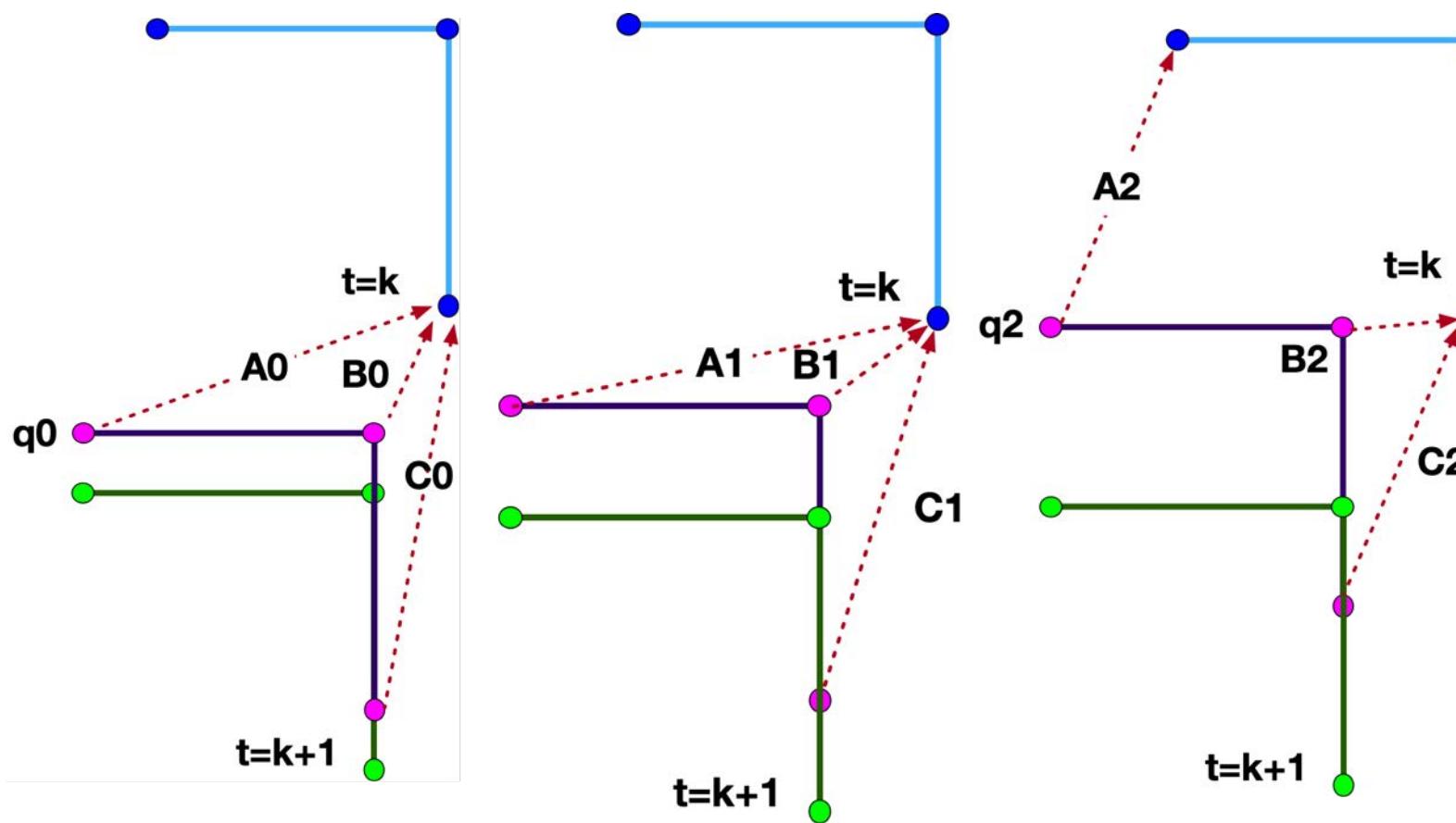
Point-to-point Metric



$$d_{p2p,q0} = A_0^2 + B_0^2 + C_0^2$$

$$d_{p2p,q1} = A_1^2 + B_1^2 + C_1^2$$

Point-to-point Metric

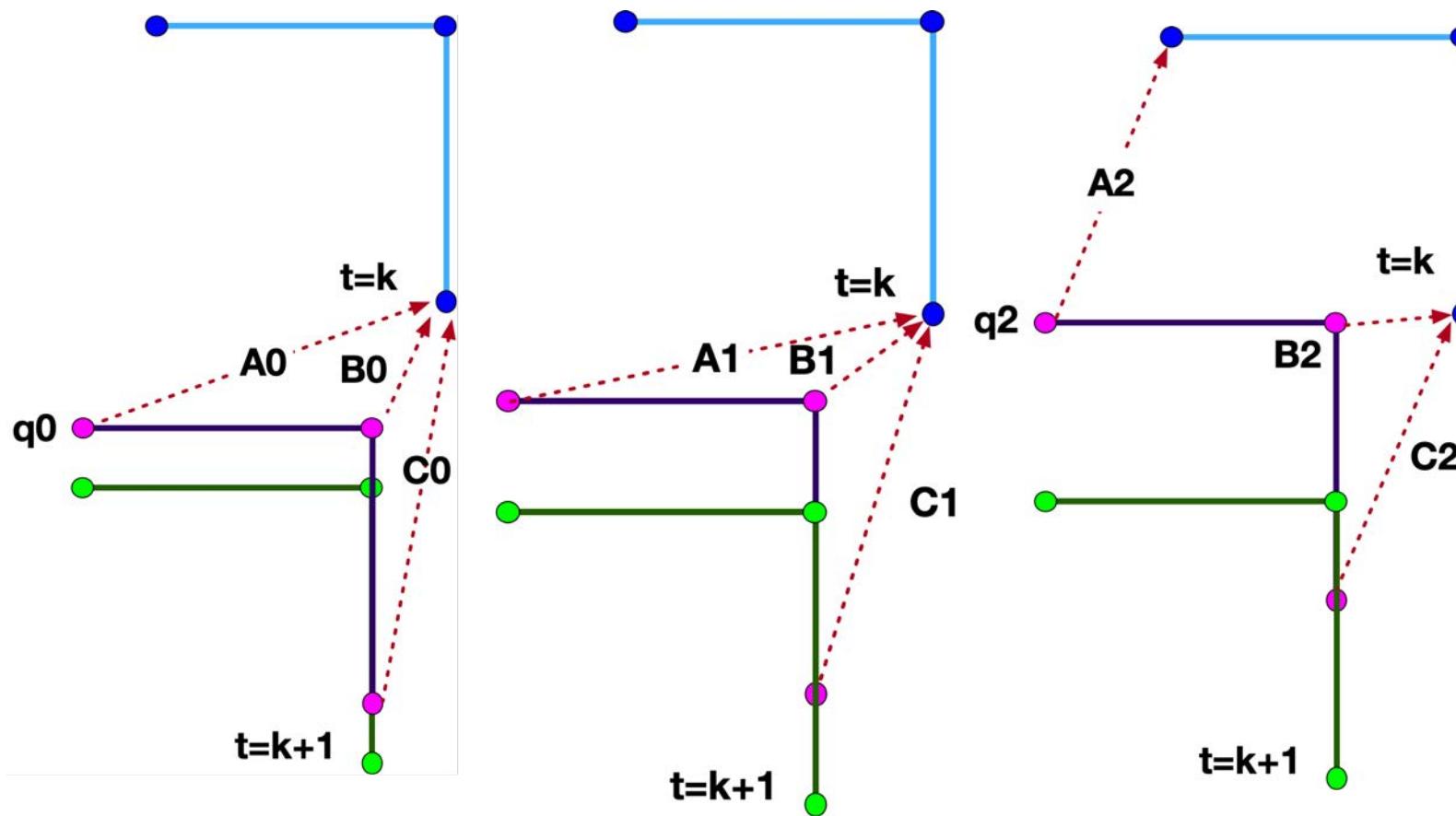


$$d_{p2p,q0} = A_0^2 + B_0^2 + C_0^2$$

$$d_{p2p,q1} = A_1^2 + B_1^2 + C_1^2$$

$$d_{p2p,q2} = A_2^2 + B_2^2 + C_2^2$$

Point-to-point Metric



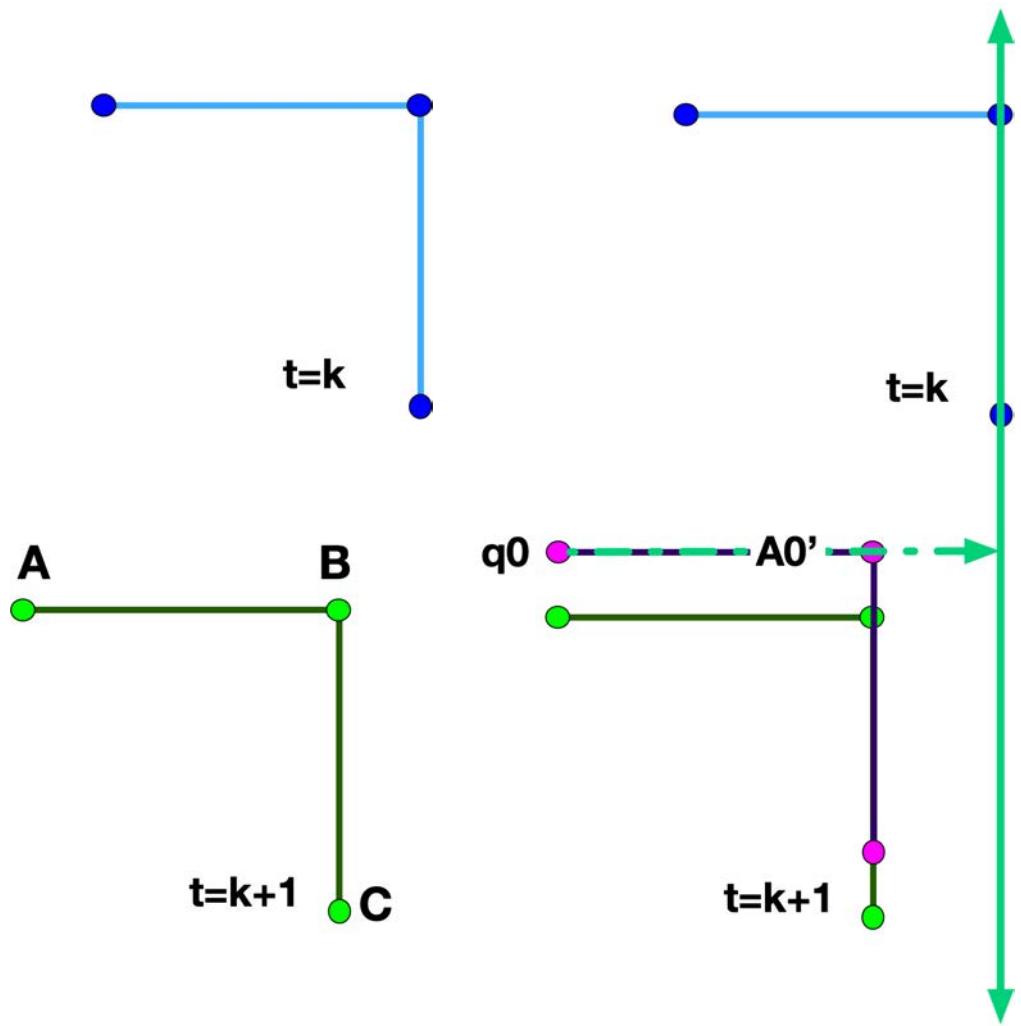
$$d_{p2p,q0} = A0^2 + B0^2 + C0^2$$

$$d_{p2p,q1} = A1^2 + B1^2 + C1^2$$

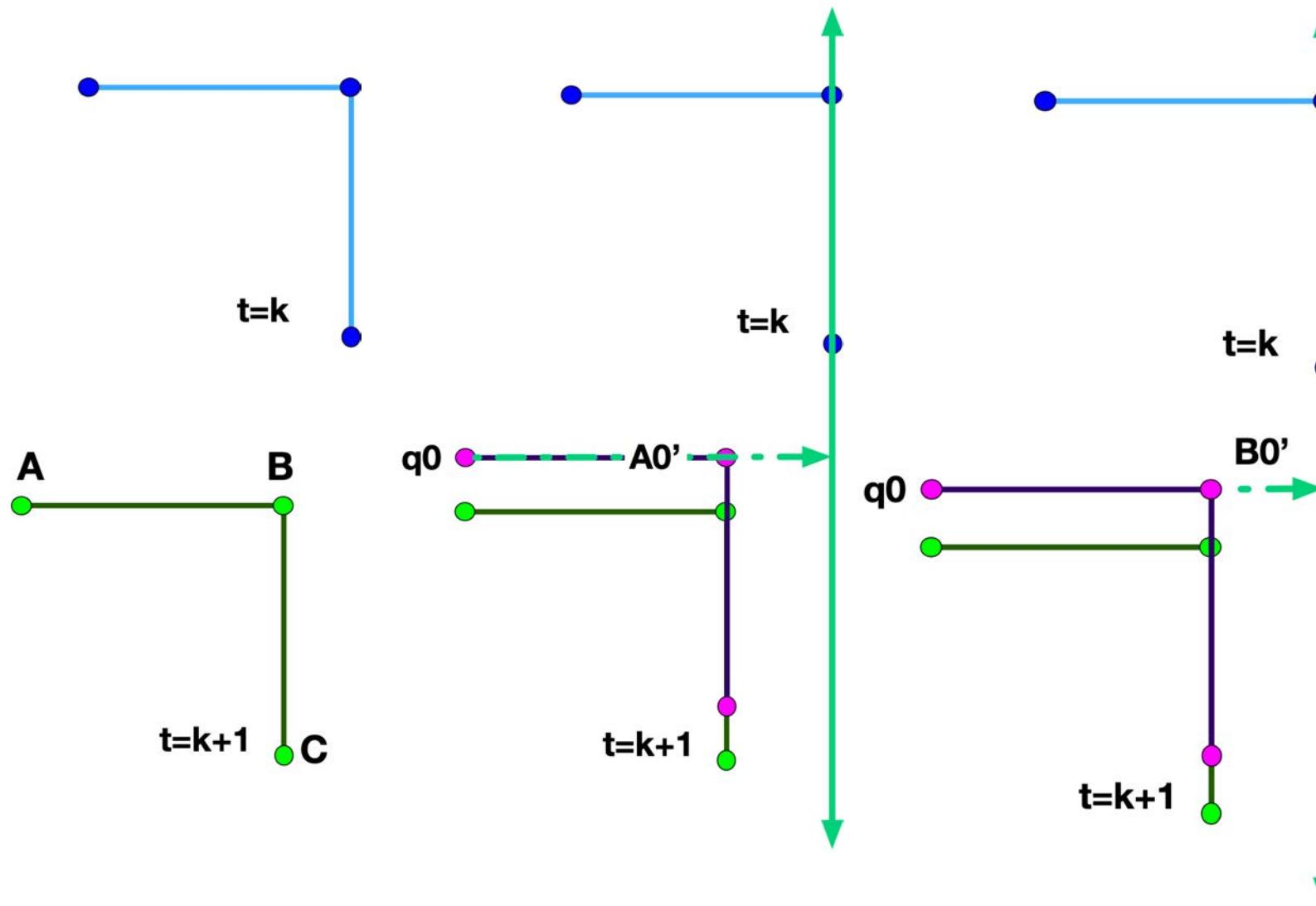
$$d_{p2p,q2} = A2^2 + B2^2 + C2^2$$

$$d_{p2p,q0} \neq d_{p2p,q1} \neq d_{p2p,q2}$$

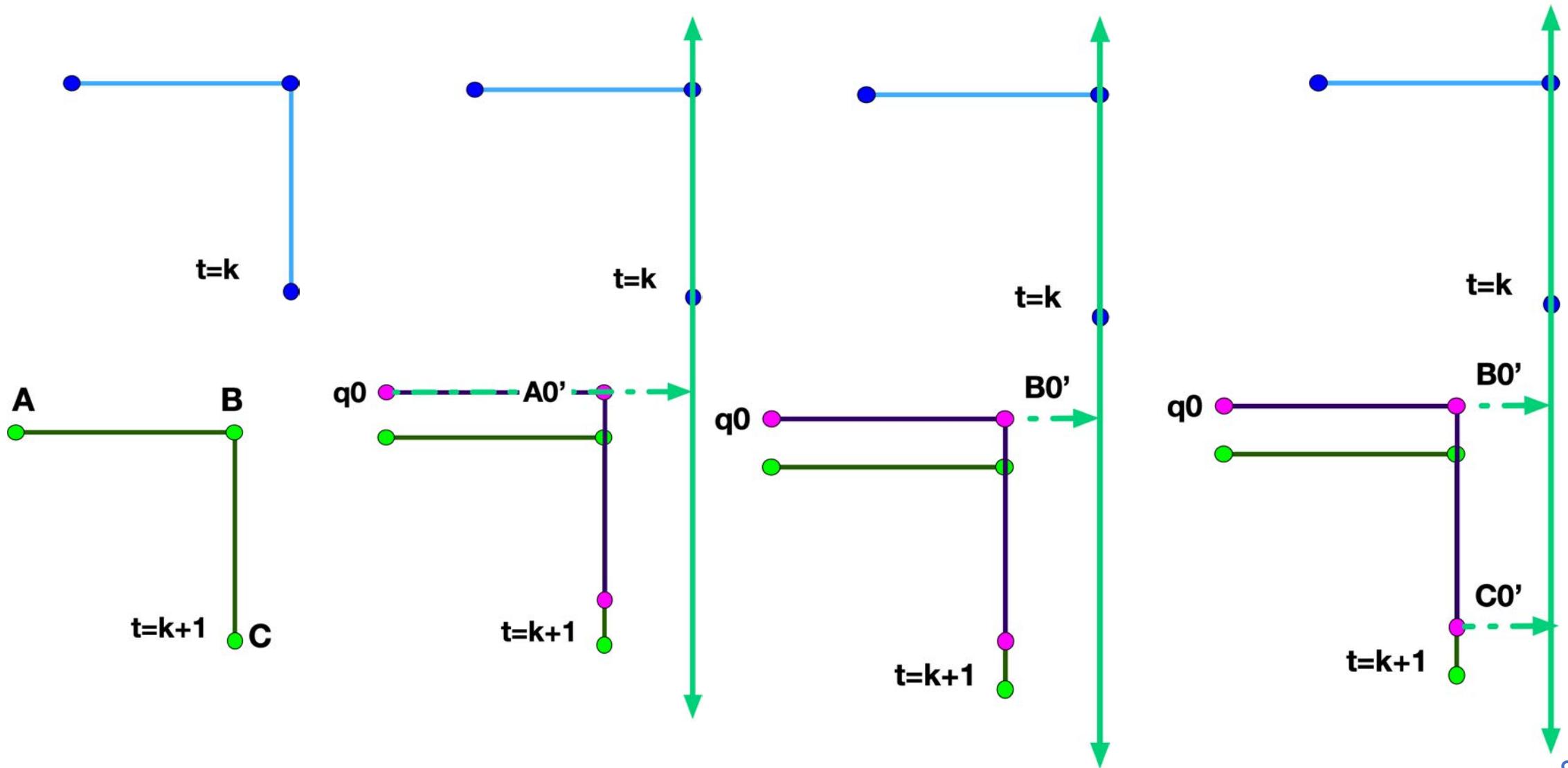
Point-to-line Metric



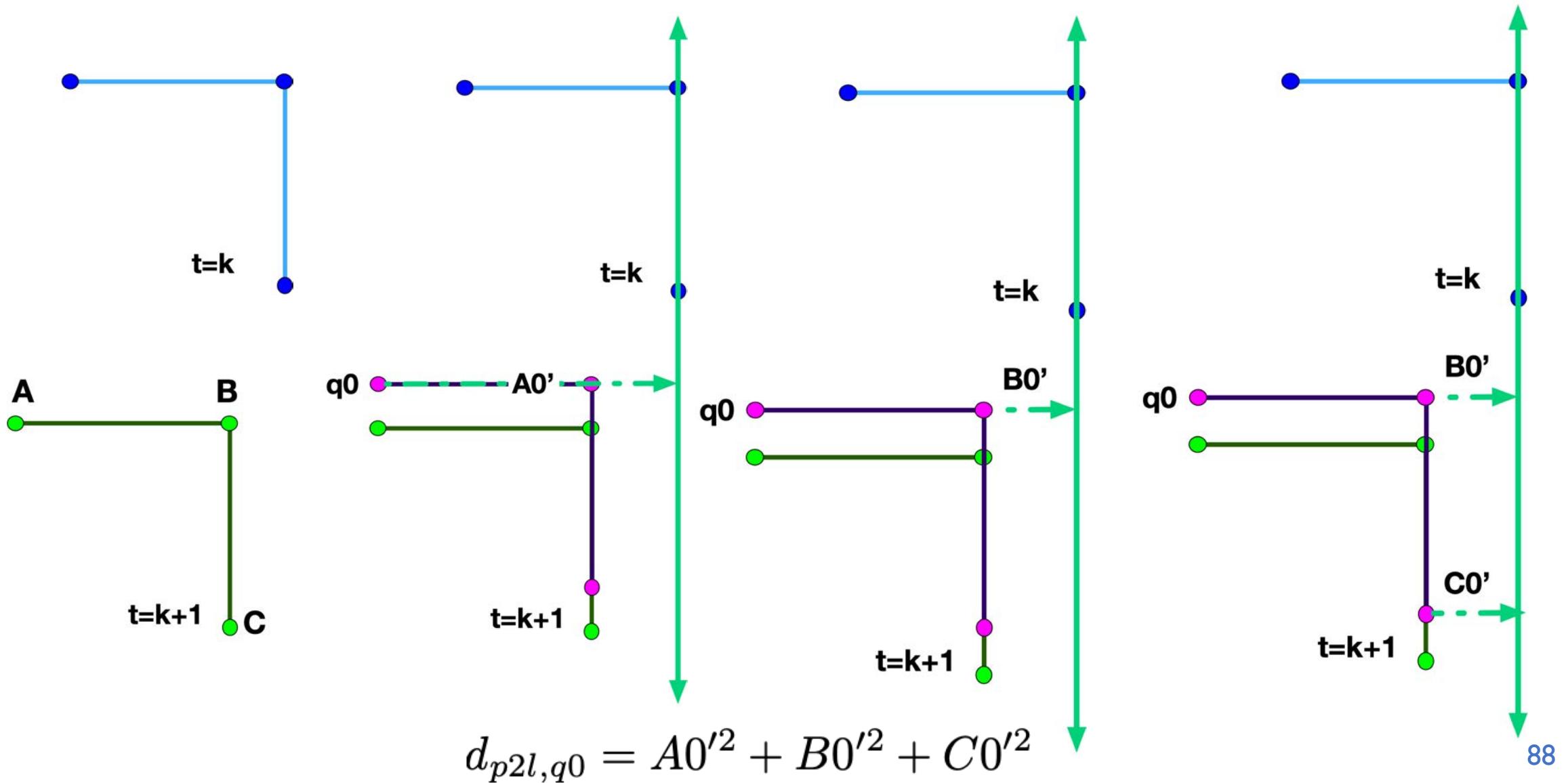
Point-to-line Metric



Point-to-line Metric

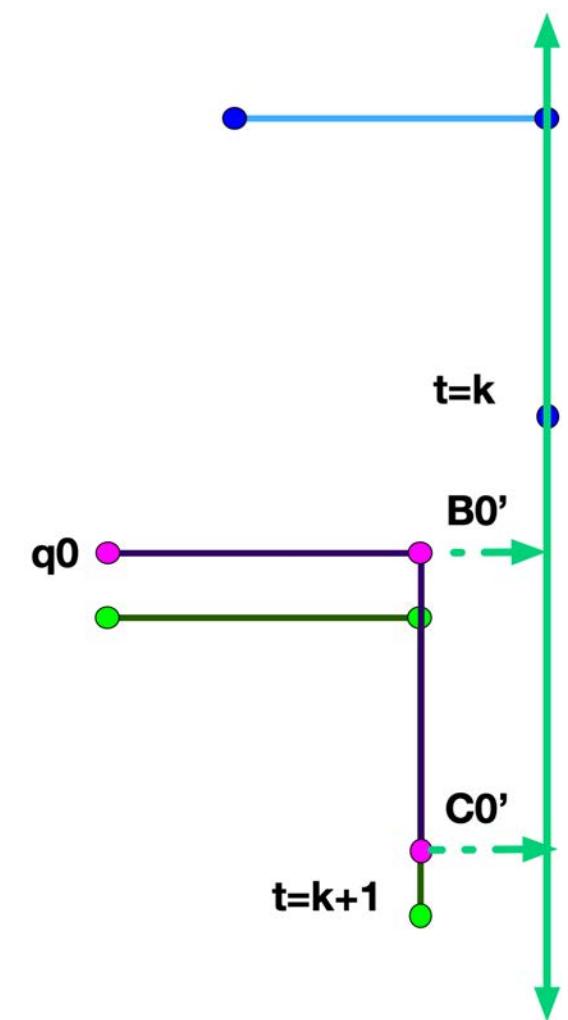


Point-to-line Metric

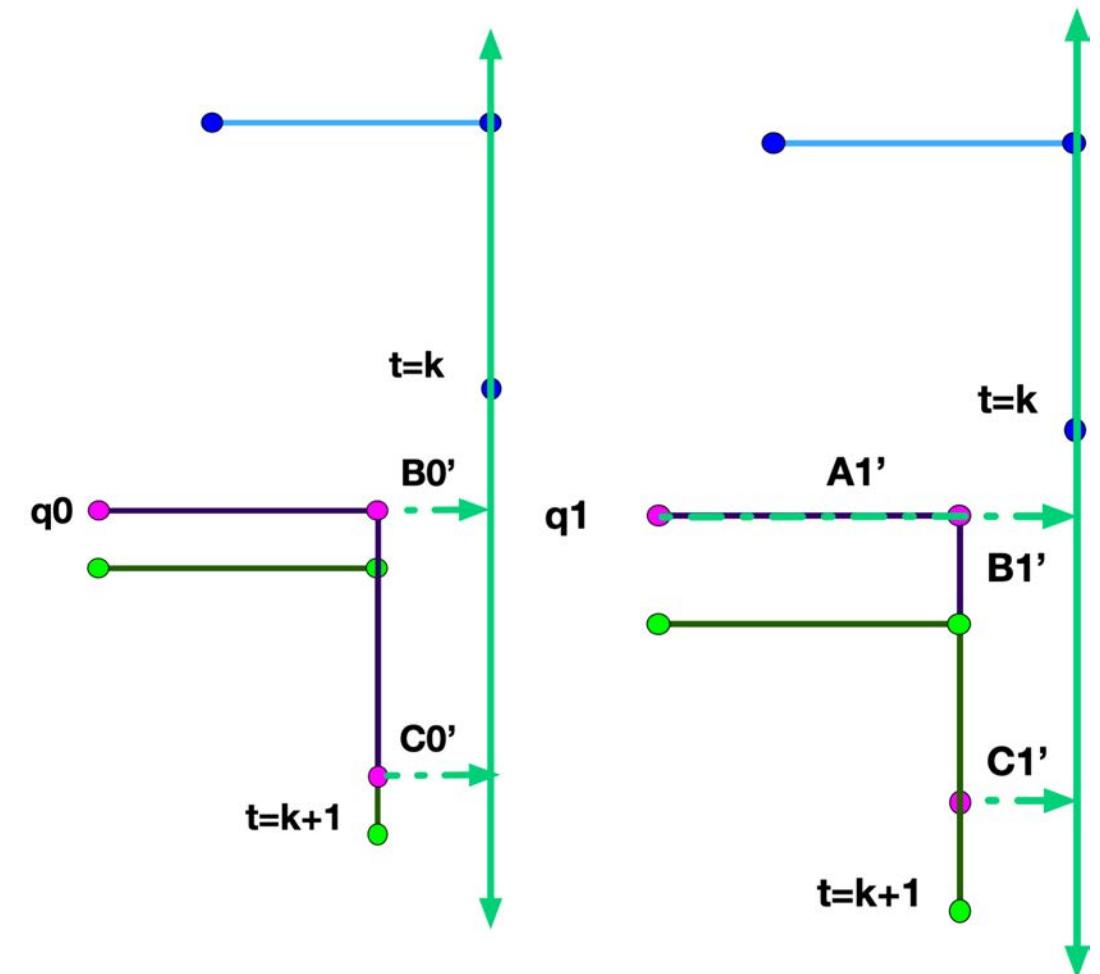


Point-to-line Metric

$$d_{p2l,q0} = A0'^2 + B0'^2 + C0'^2$$

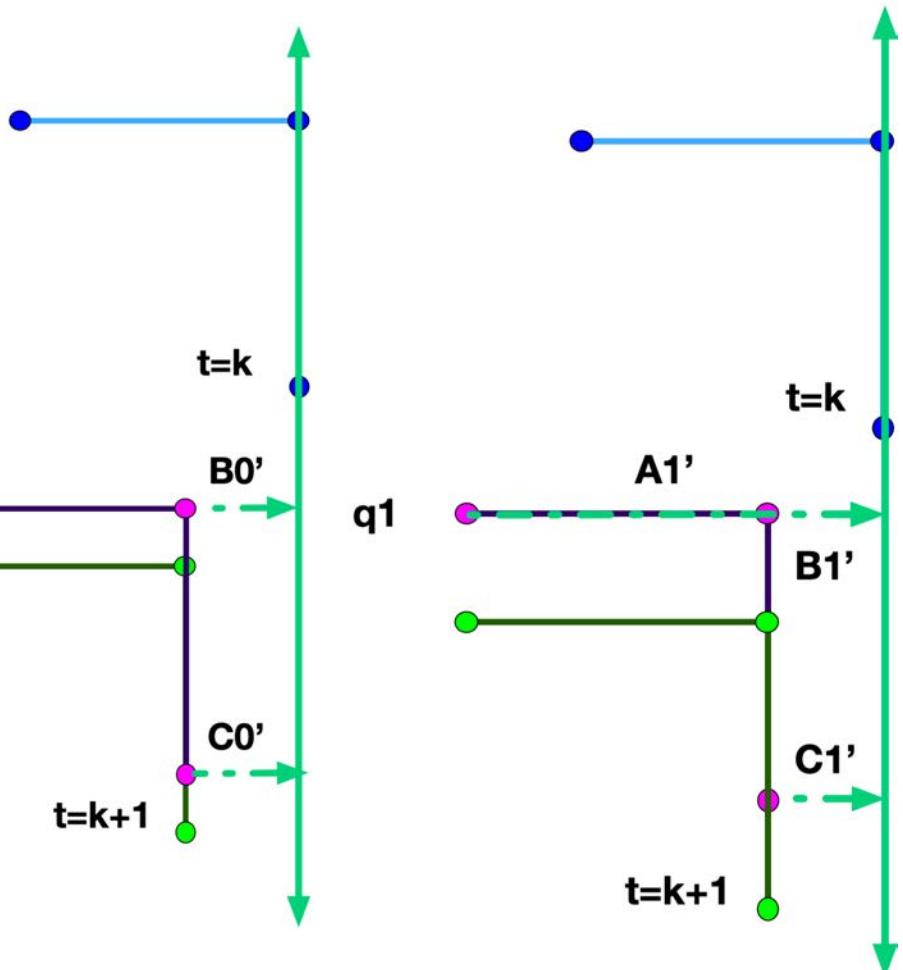


Point-to-line Metric



$$d_{p2l,q_0} = A_{0'}^2 + B_{0'}^2 + C_{0'}^2$$
$$d_{p2l,q_1} = A_{1'}^2 + B_{1'}^2 + C_{1'}^2$$

Point-to-line Metric

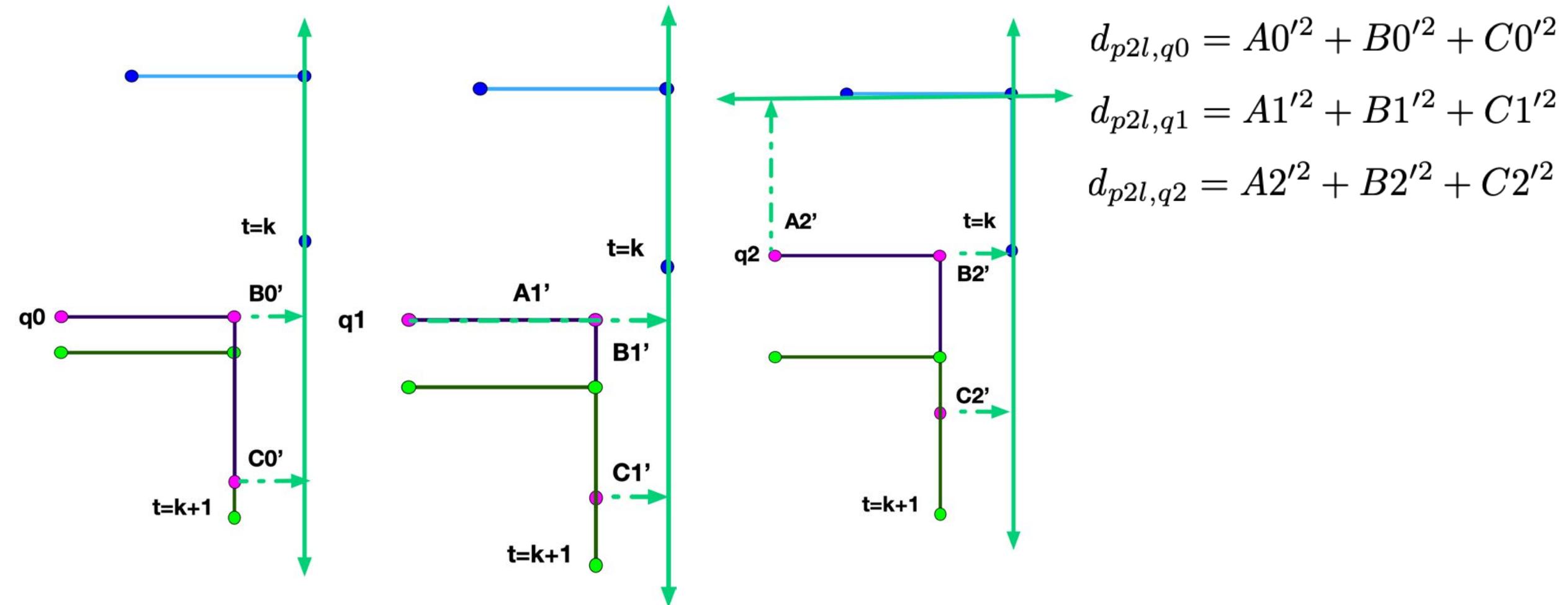


$$d_{p2l,q0} = A0'^2 + B0'^2 + C0'^2$$

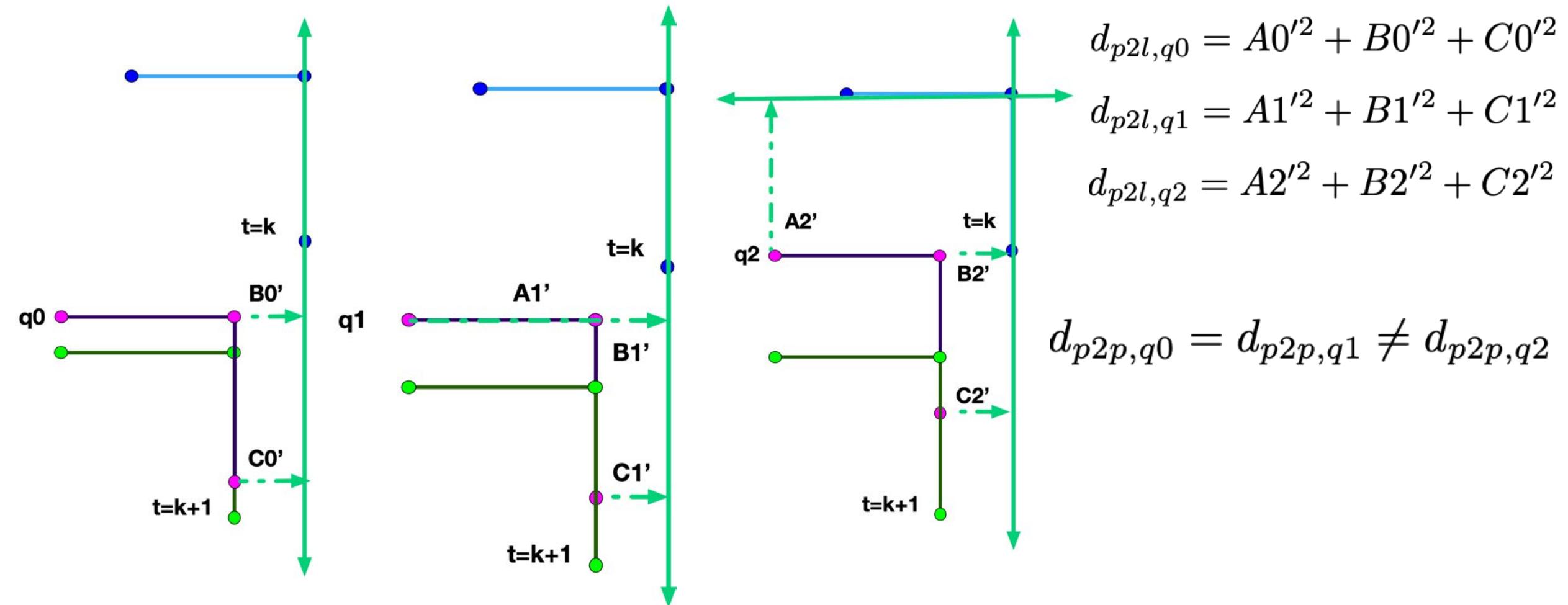
$$d_{p2l,q1} = A1'^2 + B1'^2 + C1'^2$$

$$d_{p2p,q0} = d_{p2p,q1}$$

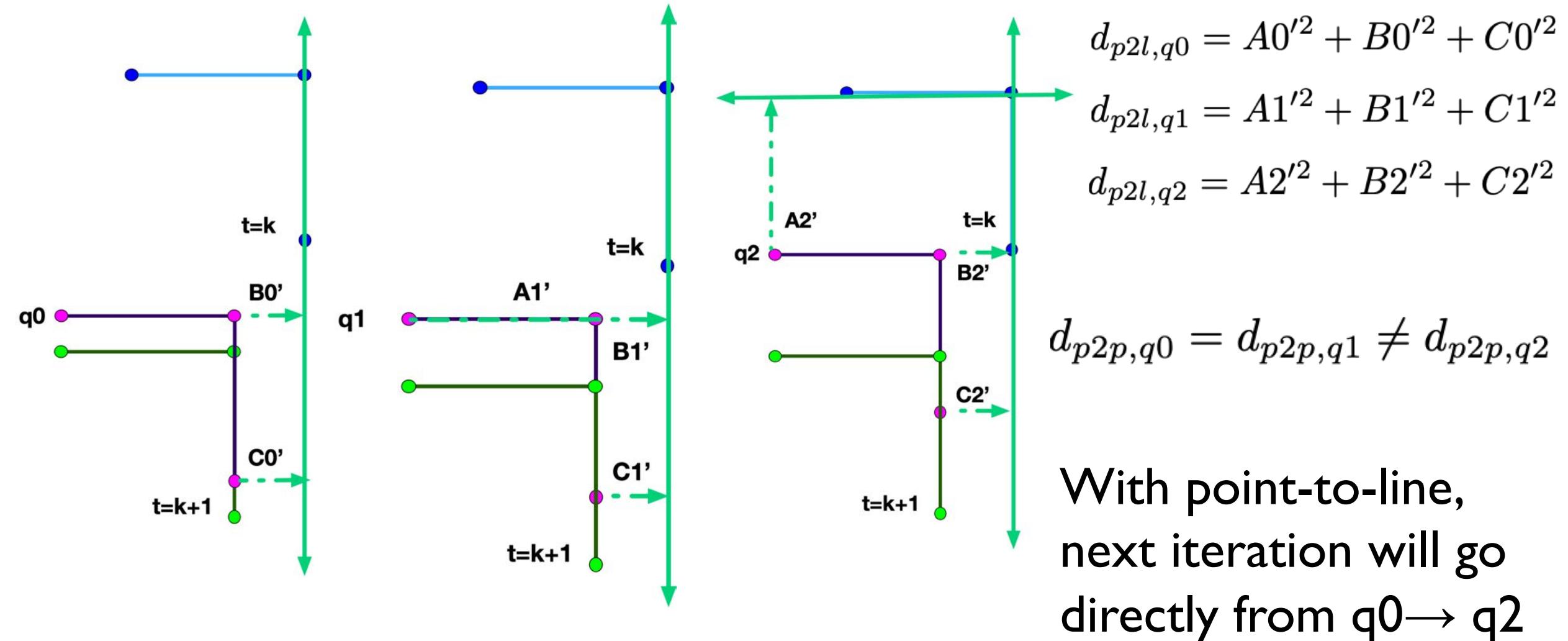
Point-to-line Metric



Point-to-line Metric



Point-to-line Metric



Live Demo: /laserscan & Scan Matching