UNIVERSITY OF WATERLOO

Big Data Infrastructure

CS 489/698 Big Data Infrastructure (Winter 2016)

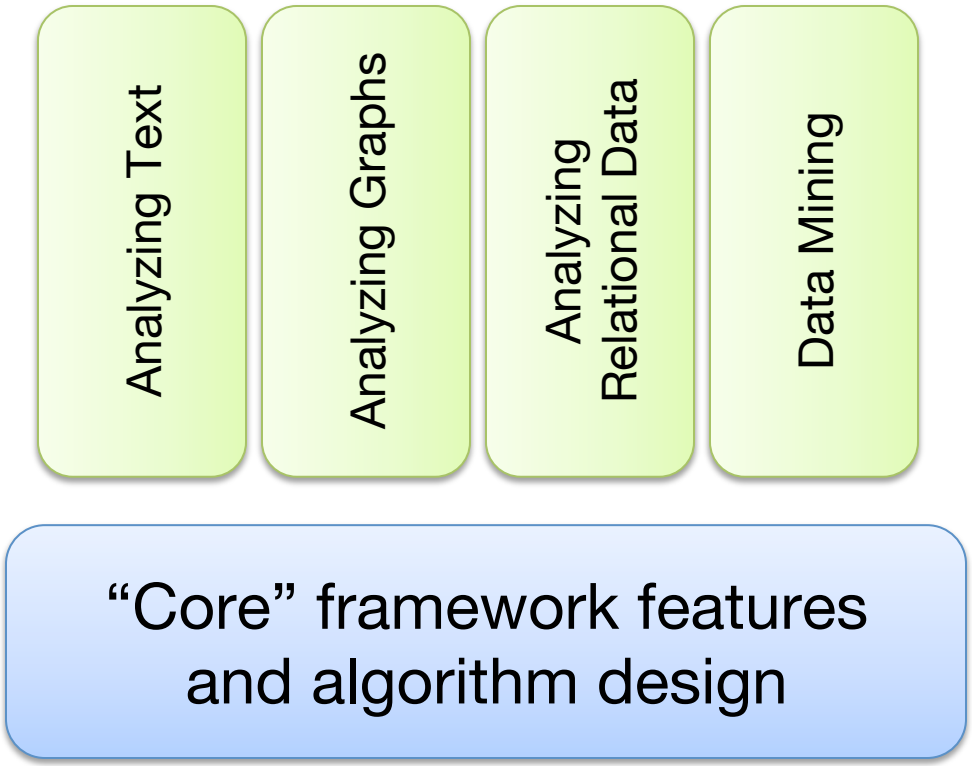
Week 8: Data Mining (1/4)

March 1, 2016

Jimmy Lin
David R. Cheriton School of Computer Science
University of Waterloo

These slides are available at http://lintool.github.io/bigdata-2016w/

Structure of the Course



Supervised Machine Learning

The generic problem of function induction given sample instances of input and output

Focus today

Classification: output draws from finite discrete labels

Regression: output is a continuous value

This is not meant to be an exhaustive treatment of machine learning!

Classification

Source: Wikipedia (Sorting)

Applications

Spam detection

Sentiment analysis

Content (e.g., genre) classification

Link prediction

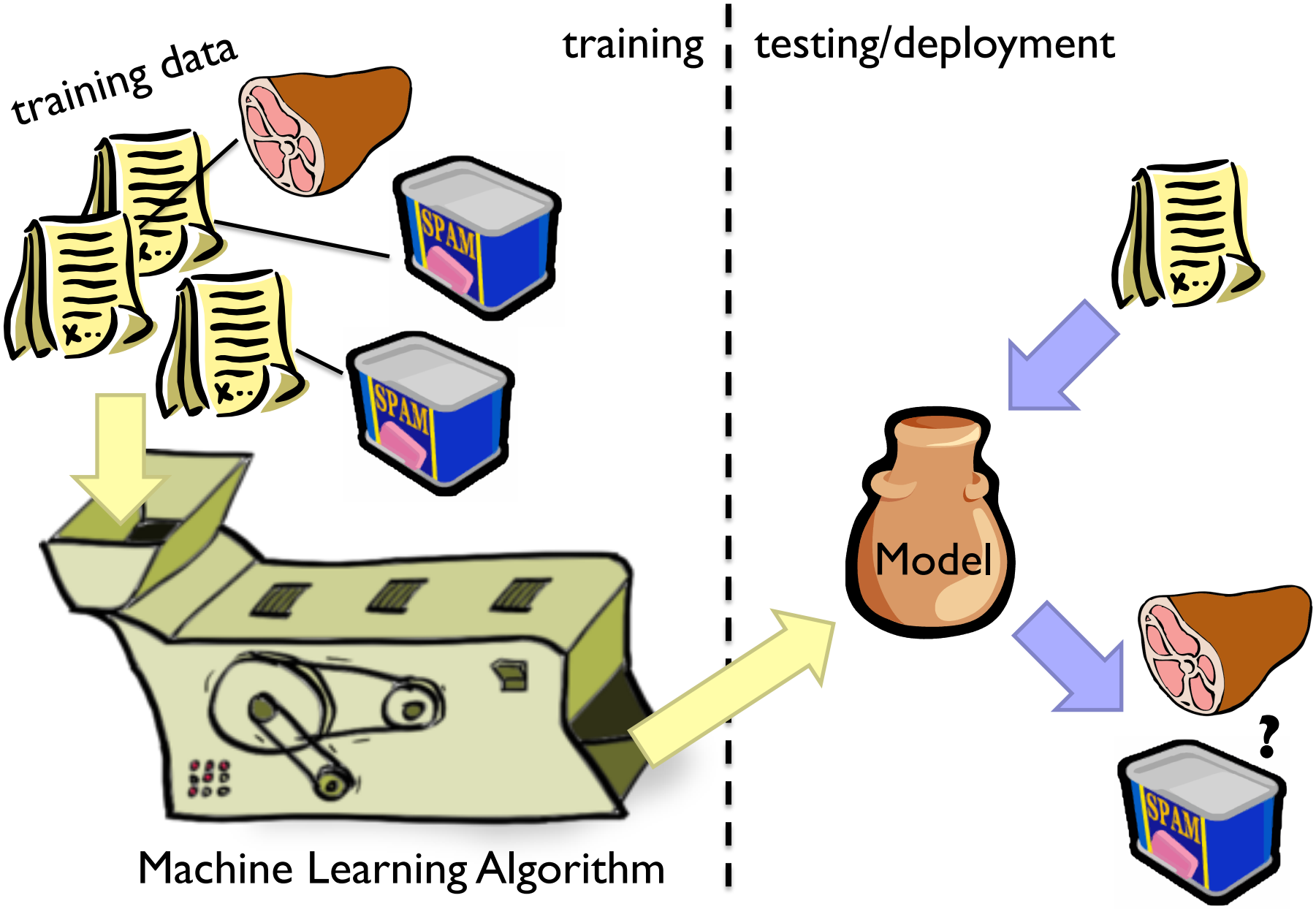
Document ranking

Object recognition

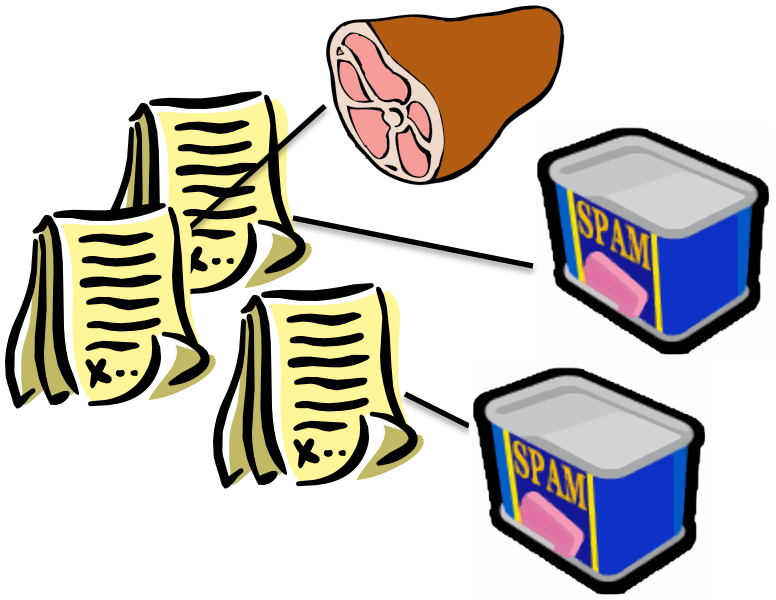
Fraud detection

And much much more!

Supervised Machine Learning



Feature Representations



Who comes up with the features?
How?

Objects are represented in terms of features:

"Dense" features: sender IP, timestamp, # of recipients, length of message, etc.

"Sparse" features: contains the term "viagra" in message, contains "URGENT" in subject, etc.

Applications

Spam detection

Sentiment analysis

Content (e.g., genre) classification

Link prediction

Document ranking

Object recognition

Fraud detection

And much much more!

Features are highly application-specific!

Components of a ML Solution

Data

Features

Model

Optimization

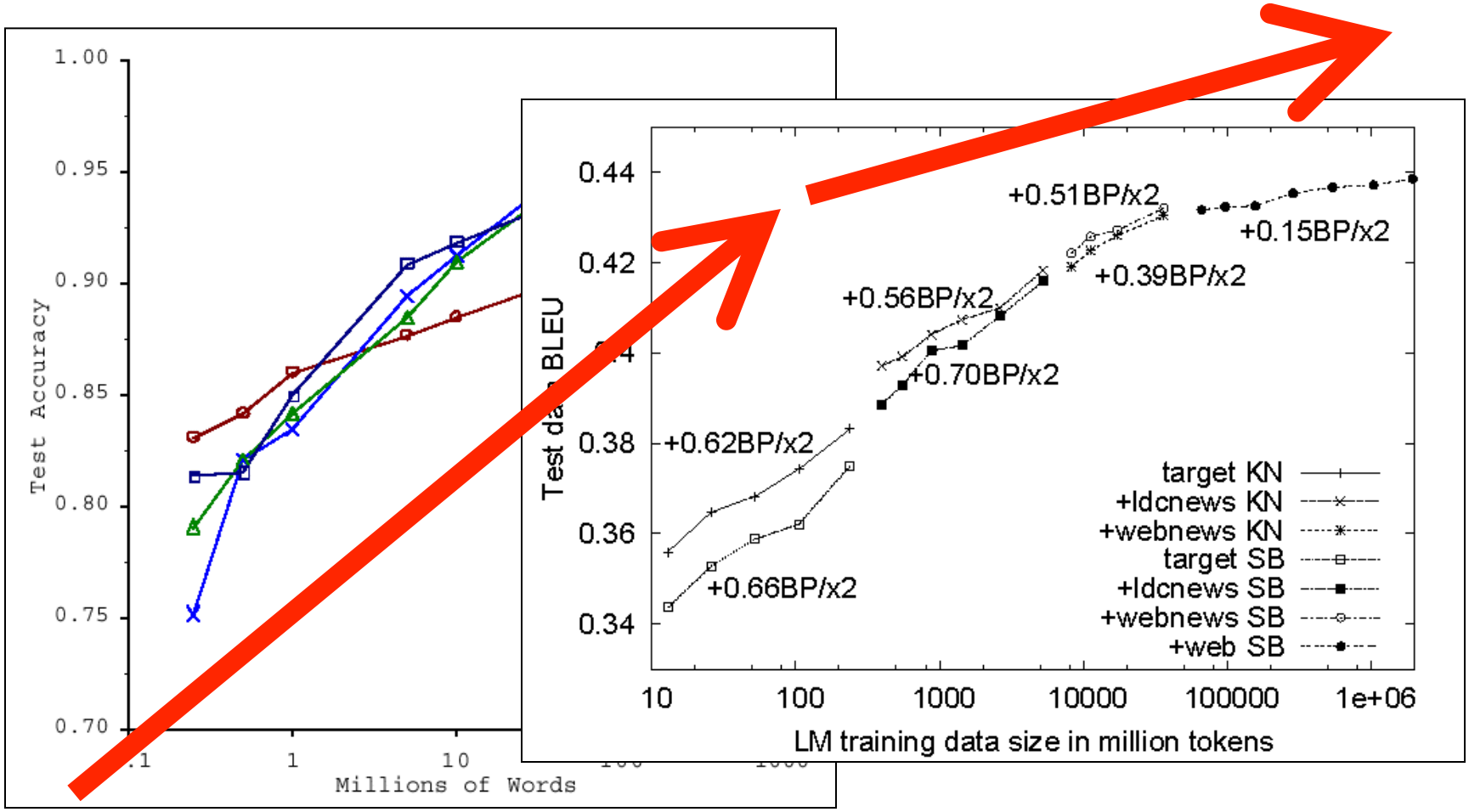
logistic regression, naïve Bayes, SVM, random forests, perceptrons, neural network, etc.

gradient descent, stochastic gradient descent, L-BFGS, etc.

What "matters" the most?

No data like more data!

s/knowledge/data/g;



(Banko and Brill, ACL 2001)
(Brants et al., EMNLP 2007)

Limits of Supervised Classification?

- Why is this a big data problem?
  - Isn't gathering labels a serious bottleneck?
- Solution: crowdsourcing
- Solution: user behavior logs
  - Learning to rank
  - Computational advertising
  - Link recommendation
- The virtuous cycle of data-driven products

Supervised Binary Classification

- Restrict output label to be *binary*
  - Yes/No
  - 1/0
- Binary classifiers form a primitive building block for multi-class problems
  - One vs. rest classifier ensembles
  - Classifier cascades

The Task

- Given $D = \{(\mathrm{x}_i, y_i)\}_i^n$

  label

  (sparse) feature vector

  $\mathrm{x}_i = [x_1, x_2, x_3, \ldots, x_d]$

  $y \in \{0, 1\}$

- Induce $f : X \rightarrow Y$
  - Such that loss is minimized

$$\frac{1}{n} \sum_{i=0}^{n} \ell(f(\mathrm{x}_i), y_i)$$

loss function

- Typically, consider functions of a parametric form:

$$\arg\min_{\theta} \frac{1}{n} \sum_{i=0}^{n} \ell(f(x_i; \theta), y_i)$$

model parameters

Key insight: machine learning as an optimization problem!

(closed form solutions generally not possible)

Gradient Descent: Preliminaries

- Rewrite:

$$\arg\min_{\theta} \frac{1}{n} \sum_{i=0}^{n} \ell(f(\mathrm{x}_i; \theta), y_i) \quad \Rightarrow \quad \arg\min_{\theta} L(\theta)$$

- Compute gradient:
  - "Points" to fastest increasing "direction"

$$\nabla L(\theta) = \left[\frac{\partial L(\theta)}{\partial w_0}, \frac{\partial L(\theta)}{\partial w_1}, \ldots \frac{\partial L(\theta)}{\partial w_d} \right]$$

- So, at any point: *

$$\mathrm{b} = \mathrm{a} - \gamma \nabla L(\mathrm{a})$$

$$L(\mathrm{a}) \geq L(\mathrm{b})$$

* caveats

Gradient Descent: Iterative Update

- Start at an arbitrary point, iteratively update:

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla L(\theta^{(t)})$$

- We have:

$$L(\theta^{(0)}) \geq L(\theta^{(1)}) \geq L(\theta^{(2)}) \dots$$

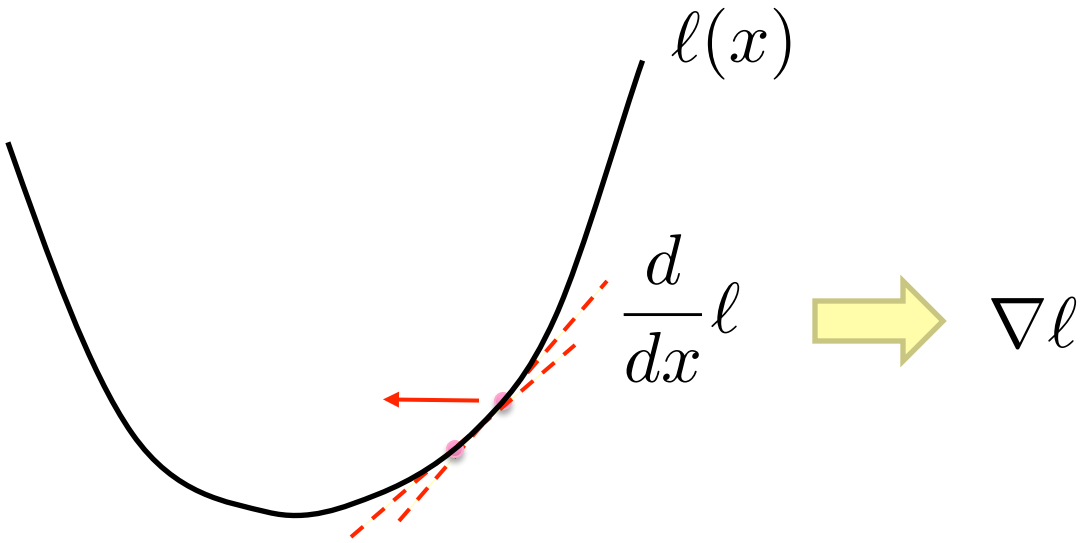
- Lots of details:
  - Figuring out the step size
  - Getting stuck in local minima
  - Convergence rate
  - …

Gradient Descent

Repeat until convergence:

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathrm{x}_i; \theta^{(t)}), y_i)$$

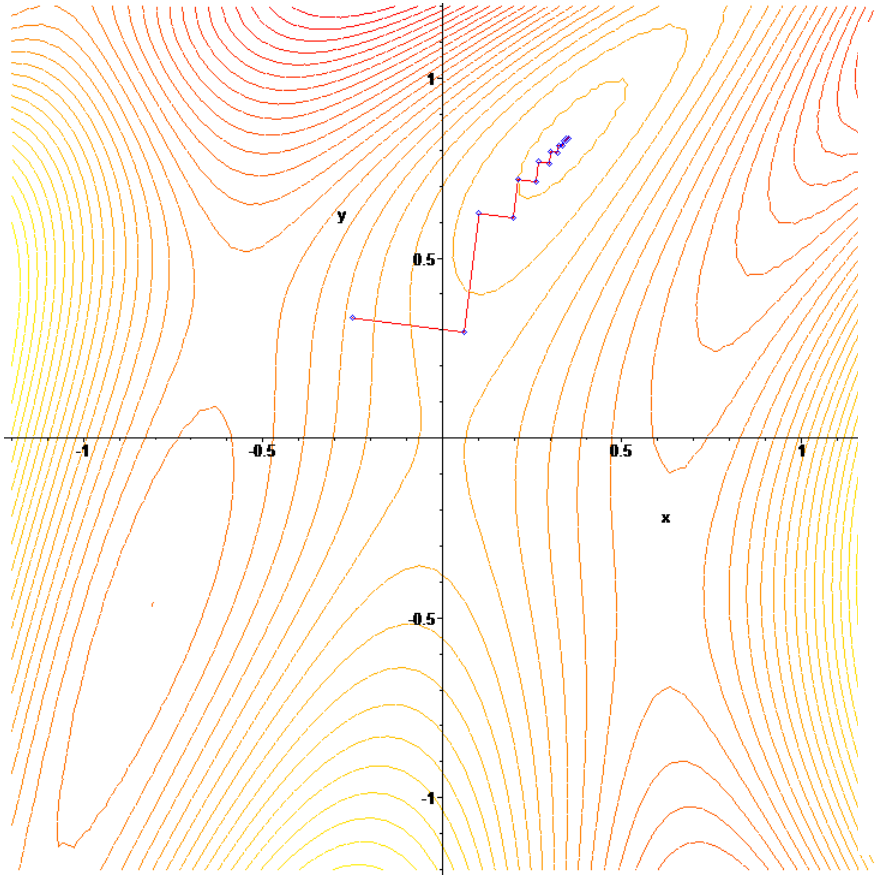
Intuition behind the math...

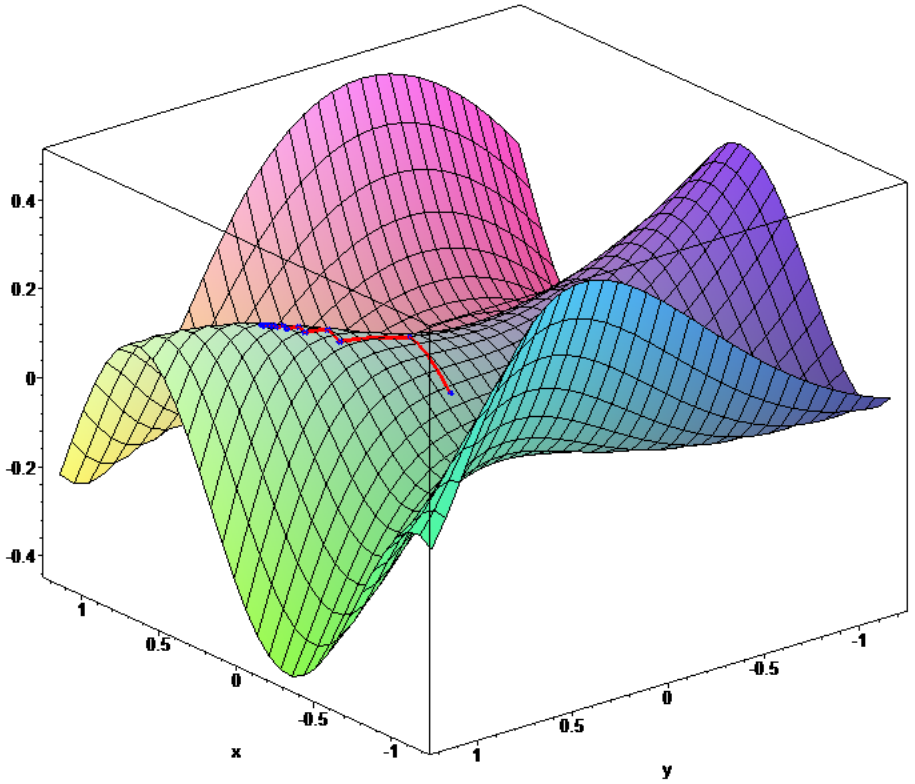


$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathrm{x}_i; \theta^{(t)}), y_i)$$

New weights Old weights

Update based on gradient


y
x
1
0.5
-0.5
-1
-1
-0.5
0.5
1


0.4
0.2
0
-0.2
-0.4
x
1
0.5
0
-0.5
-1
y
1
0.5
0
-0.5
-1

Gradient Descent

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathrm{x}_i; \theta^{(t)}), y_i)$$

Source: Wikipedia (Hills)

Lots More Details...

- Gradient descent is a "first order" optimization technique
  - Often, slow convergence
  - Conjugate techniques accelerate convergence
- Newton and quasi-Newton methods:
  - Intuition: Taylor expansion

$$f(x + \Delta x) = f(x) + f'(x)\Delta x + \frac{1}{2}f''(x)\Delta x^2$$

  - Requires the Hessian (square matrix of second order partial derivatives): impractical to fully compute

Logistic Regression

Source: Wikipedia (Hammer)

Logistic Regression: Preliminaries

- Given $D = \{(\mathrm{x}_i, y_i)\}_i^n$

$$\mathrm{x}_i = [x_1, x_2, x_3, \ldots, x_d]$$
$$y \in \{0, 1\}$$

- Let's define:

$$f(\mathrm{x}; \mathrm{w}) : \mathbb{R}^d \rightarrow \{0, 1\}$$
$$f(\mathrm{x}; \mathrm{w}) = \begin{cases} 1 \text{ if } \mathrm{w} \cdot \mathrm{x} \geq t \\ 0 \text{ if } \mathrm{w} \cdot \mathrm{x} < t \end{cases}$$

- Interpretation:

$$\ln \left[\frac{\Pr(y = 1|\mathrm{x})}{\Pr(y = 0|\mathrm{x})} \right] = \mathrm{w} \cdot \mathrm{x}$$

$$\ln \left[\frac{\Pr(y = 1|\mathrm{x})}{1 - \Pr(y = 1|\mathrm{x})} \right] = \mathrm{w} \cdot \mathrm{x}$$

Relation to the Logistic Function

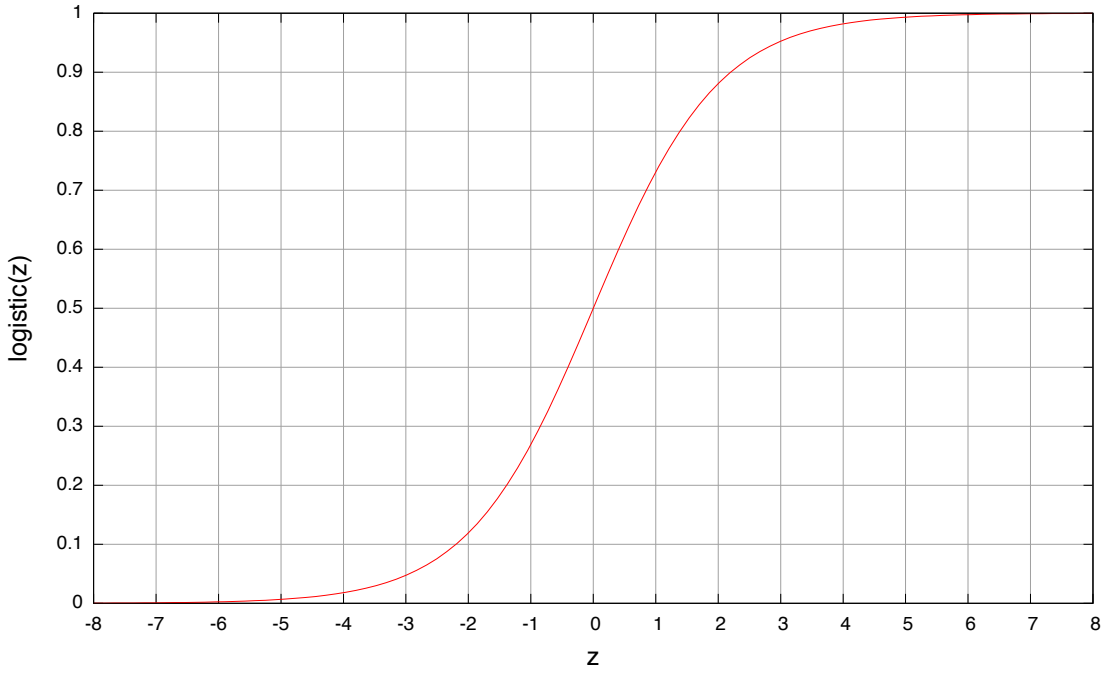
- After some algebra:

$$\Pr(y = 1|x) = \frac{e^{\mathrm{w}\cdot\mathrm{x}}}{1 + e^{\mathrm{w}\cdot\mathrm{x}}}$$

$$\Pr(y = 0|x) = \frac{1}{1 + e^{\mathrm{w}\cdot\mathrm{x}}}$$

- The logistic function:

$$f(z) = \frac{e^z}{e^z + 1}$$



Training an LR Classifier

- *Maximize* the conditional likelihood:

$$\arg\max_{\mathrm{w}} \prod_{i=1}^{n} \Pr(y_i|\mathrm{x}_i, \mathrm{w})$$

- Define the objective in terms of conditional log likelihood:

$$L(\mathrm{w}) = \sum_{i=1}^{n} \ln \Pr(y_i|\mathrm{x}_i, \mathrm{w})$$

  - We know $y \in \{0, 1\}$ so:

$$Pr(y|\mathrm{x}, \mathrm{w}) = Pr(y = 1|\mathrm{x}, \mathrm{w})^{y} Pr(y = 0|\mathrm{x}, \mathrm{w})^{(1-y)}$$

  - Substituting:

$$L(\mathrm{w}) = \sum_{i=1}^{n} \Big(y_i \ln \Pr(y_i = 1|\mathrm{x}_i, \mathrm{w}) + (1 - y_i) \ln \Pr(y_i = 0|\mathrm{x}_i, \mathrm{w}) \Big)$$

LR Classifier Update Rule

- Take the derivative:

$$L(\mathrm{w}) = \sum_{i=1}^{n} \Big(y_i \ln \Pr(y_i = 1 | \mathrm{x}_i, \mathrm{w}) + (1 - y_i) \ln \Pr(y_i = 0 | \mathrm{x}_i, \mathrm{w}) \Big)$$

$$\frac{\partial}{\partial \mathrm{w}} L(\mathrm{w}) = \sum_{i=0}^{n} \mathrm{x}_i \Big(y_i - \Pr(y_i = 1 | \mathrm{x}_i, \mathrm{w}) \Big)$$

- General form for update rule:

$$\mathrm{w}^{(t+1)} \leftarrow \mathrm{w}^{(t)} + \gamma^{(t)} \nabla_{\mathrm{w}} L(\mathrm{w}^{(t)})$$

$$\nabla L(\mathrm{w}) = \left[\frac{\partial L(\mathrm{w})}{\partial w_0}, \frac{\partial L(\mathrm{w})}{\partial w_1}, \ldots \frac{\partial L(\mathrm{w})}{\partial w_d} \right]$$

- Final update rule:

$$\mathrm{w}_i^{(t+1)} \leftarrow \mathrm{w}_i^{(t)} + \gamma^{(t)} \sum_{j=0}^{n} x_{j,i} \Big(y_j - \Pr(y_j = 1 | \mathrm{x}_j, \mathrm{w}^{(t)}) \Big)$$

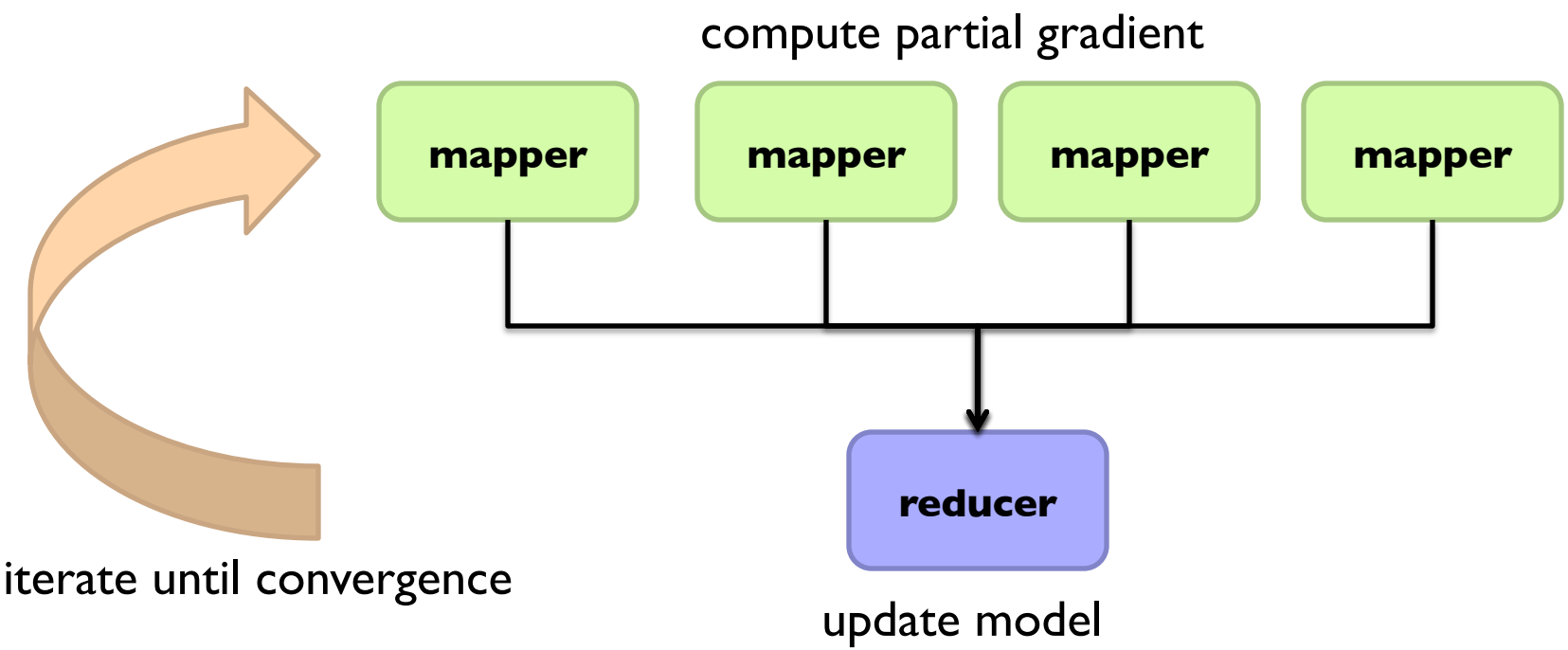
Lots more details…

- Regularization
- Different loss functions
- …

Want more details?
Take a real machine-learning course!

MapReduce Implementation

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \underbrace{\underbrace{\frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathrm{x}_i; \theta^{(t)}), y_i)}_{\text{mappers}}}_{\text{single reducer}}$$



Shortcomings

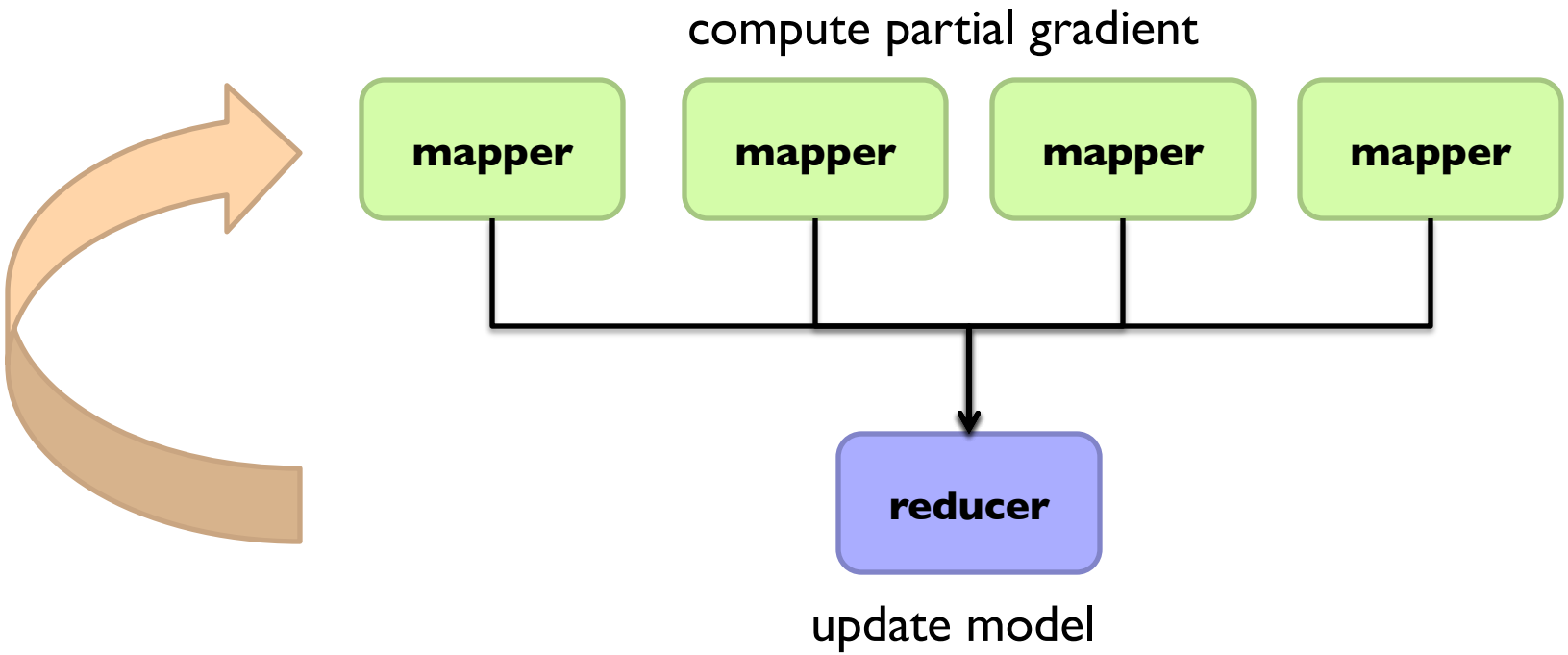
- Hadoop is bad at iterative algorithms
  - High job startup costs
  - Awkward to retain state across iterations
- High sensitivity to skew
  - Iteration speed bounded by slowest task
- Potentially poor cluster utilization
  - Must shuffle all data to a single reducer
- Some possible tradeoffs
  - Number of iterations vs. complexity of computation per iteration
  - E.g., L-BFGS: faster convergence, but more to compute

Spark Implementation

```
val points = spark.textFile(...).map(parsePoint).persist()

var w = // random initial vector
for (i <- 1 to ITERATIONS) {
  val gradient = points.map{ p =>
    p.x * (1/(1+exp(-p.y*(w dot p.x)))-1)*p.y
  }.reduce((a,b) => a+b)
  w -= gradient
}
```

What's the difference?



Source: Wikipedia (Hills)

Source: Wikipedia (Water Slide)

Batch vs. Online

Gradient Descent

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \frac{1}{n} \sum_{i=0}^{n} \nabla \ell(f(\mathrm{x}_i; \theta^{(t)}), y_i)$$

"batch" learning: update model after considering all training instances

Stochastic Gradient Descent (SGD)

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla \ell(f(\mathrm{x}; \theta^{(t)}), y)$$

"online" learning: update model after considering *each* (randomly-selected) training instance

In practice… just as good!

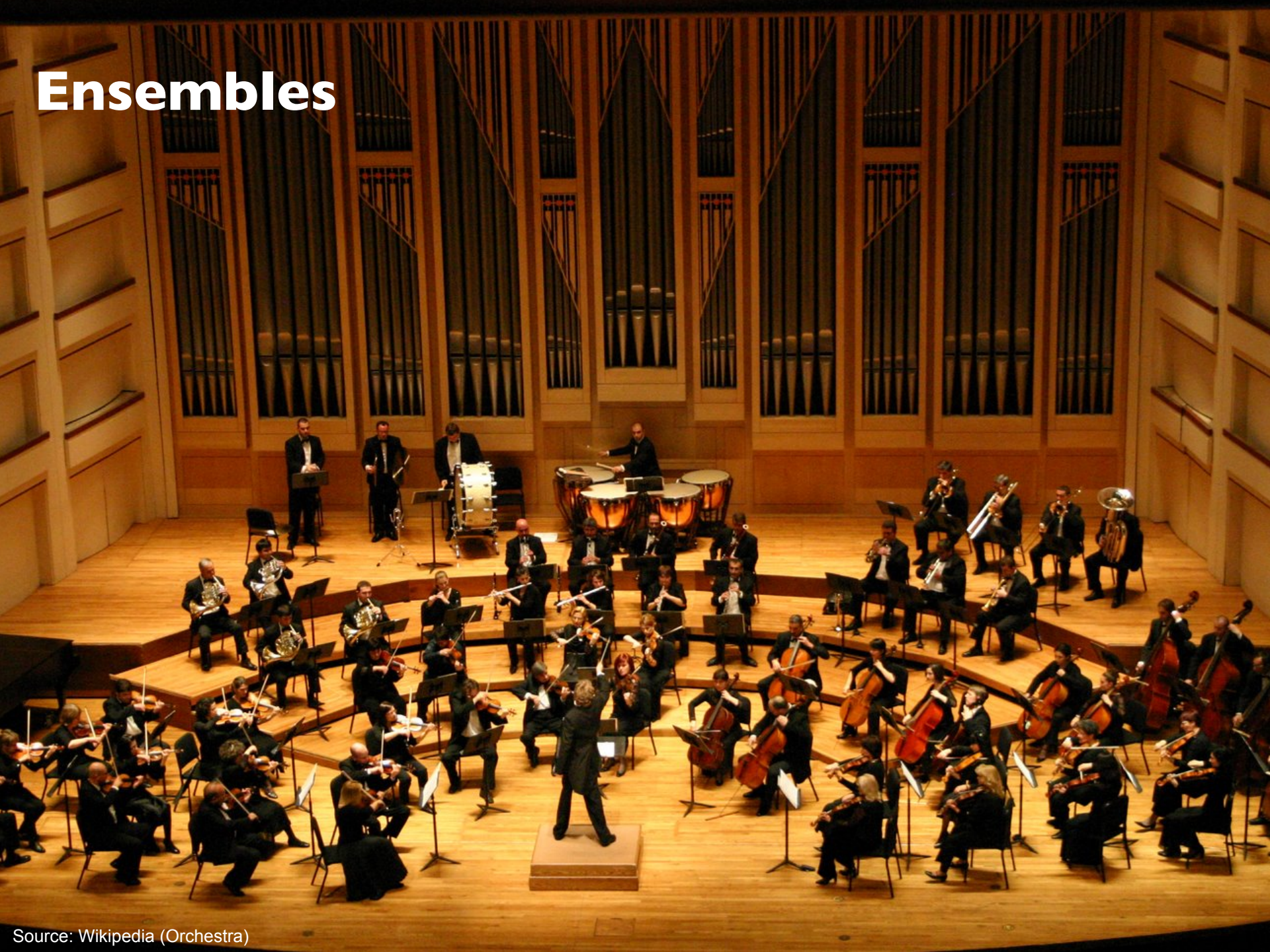
Practical Notes

- Most common implementation:
  - Randomly shuffle training instances
  - Stream instances through learner
- Single vs. multi-pass approaches
- "Mini-batching" as a middle ground between batch and stochastic gradient descent

We've solved the iteration problem!

What about the single reducer problem?

Ensembles



Source: Wikipedia (Orchestra)

Ensemble Learning

- Learn multiple models, combine results from different models to make prediction
- Why does it work?
  - If errors uncorrelated, multiple classifiers being wrong is less likely
  - Reduces the variance component of error
- A variety of different techniques:
  - Majority voting
  - Simple weighted voting:

$$y = \arg\max_{y \in Y} \sum_{k=1}^{n} \alpha_k p_k(y|\mathrm{x})$$

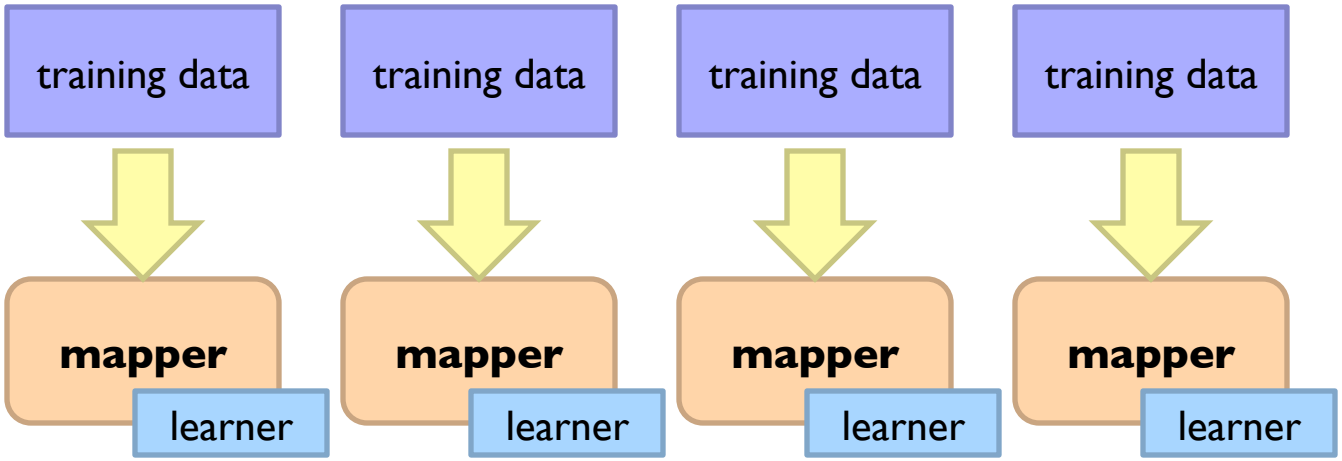
  - Model averaging
  - …

Practical Notes

- Common implementation:
  - Train classifiers on different input partitions of the data
  - Embarrassingly parallel!
- Contrast with other ensemble techniques, e.g., boosting

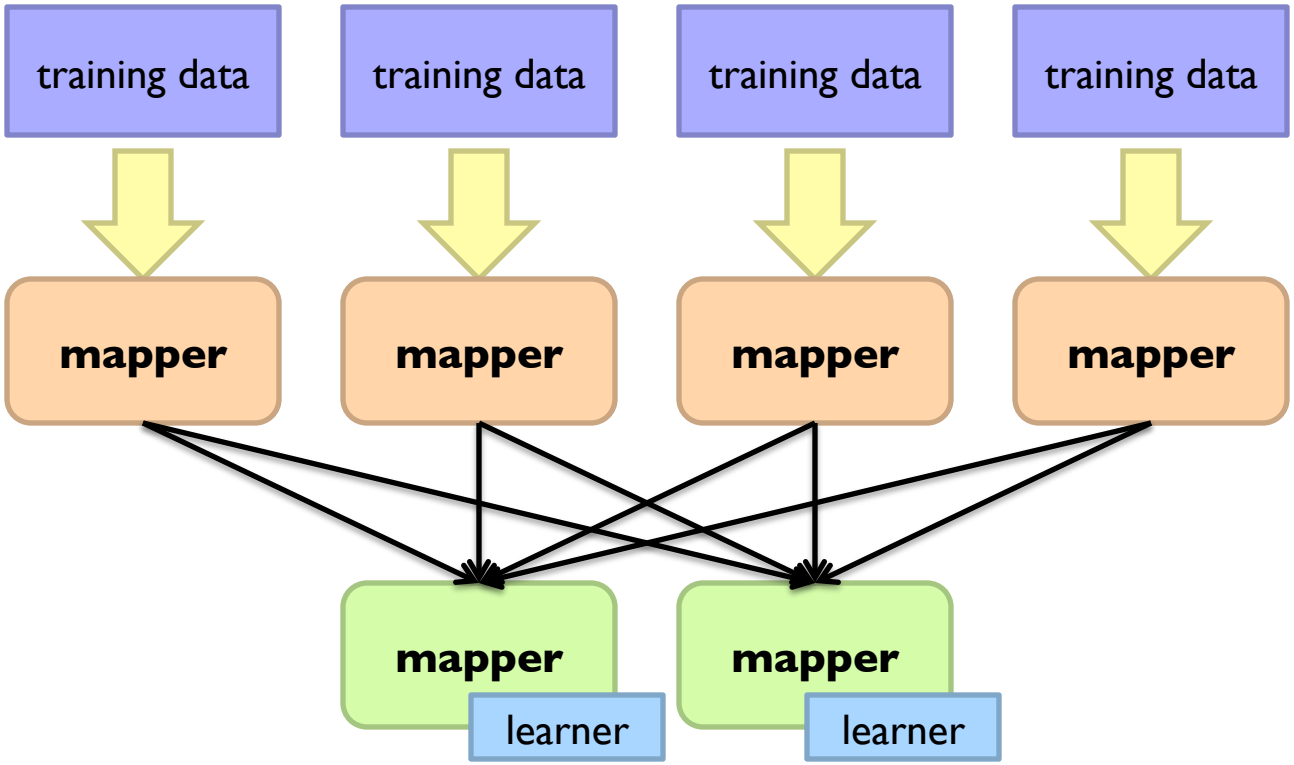
MapReduce Implementation

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla \ell(f(\mathrm{x}; \theta^{(t)}), y)$$



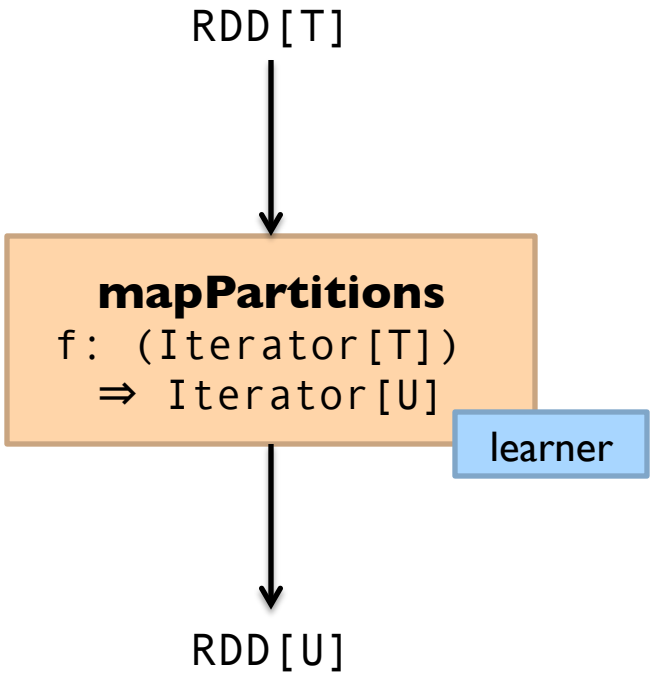
MapReduce Implementation

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla \ell(f(\mathrm{x}; \theta^{(t)}), y)$$



What about Spark?

$$\theta^{(t+1)} \leftarrow \theta^{(t)} - \gamma^{(t)} \nabla \ell(f(\mathrm{x}; \theta^{(t)}), y)$$



MapReduce Implementation: Details

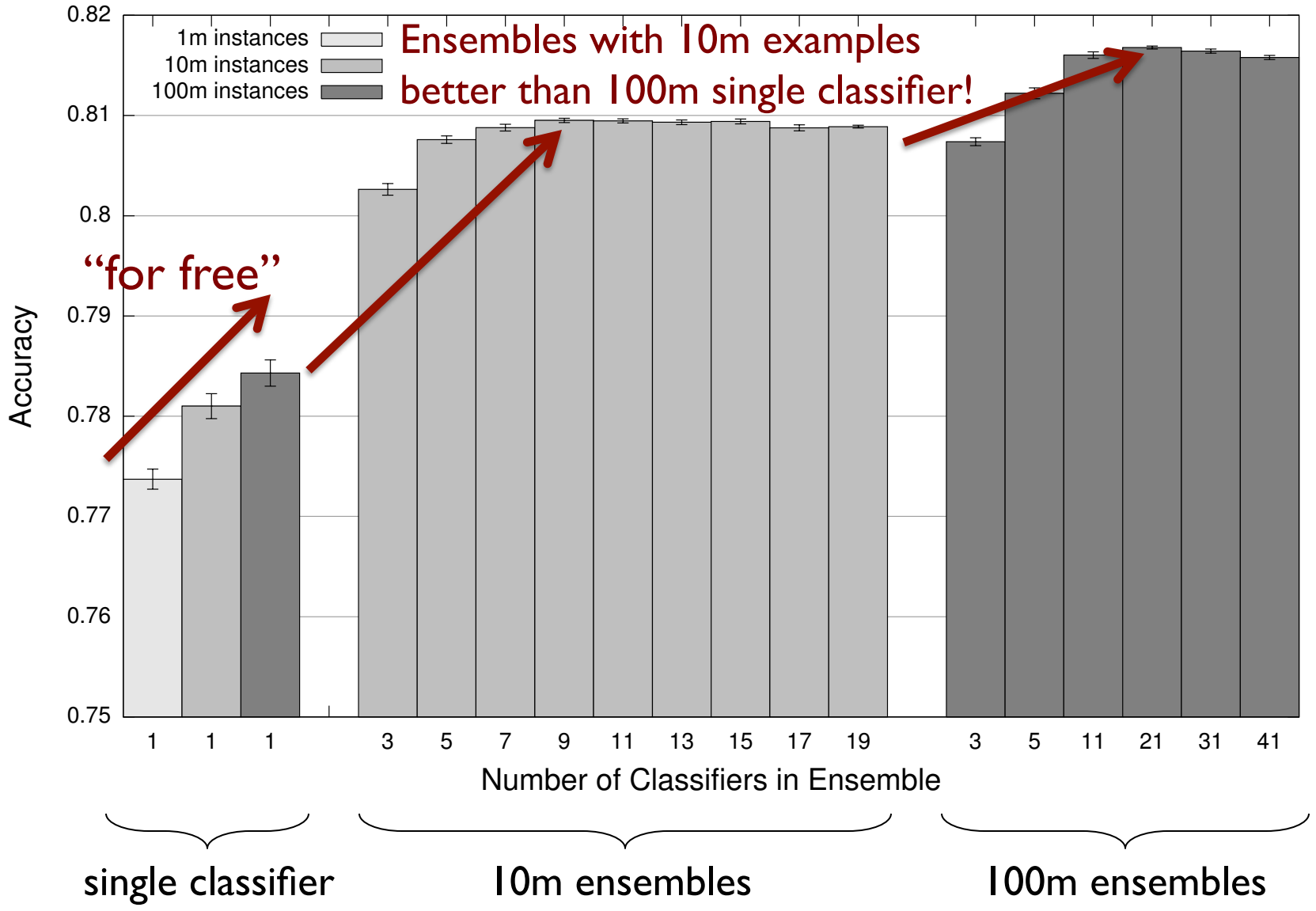
- Two possible implementations:
  - Write model out as “side data”
  - Emit model as intermediate output

Sentiment Analysis Case Study

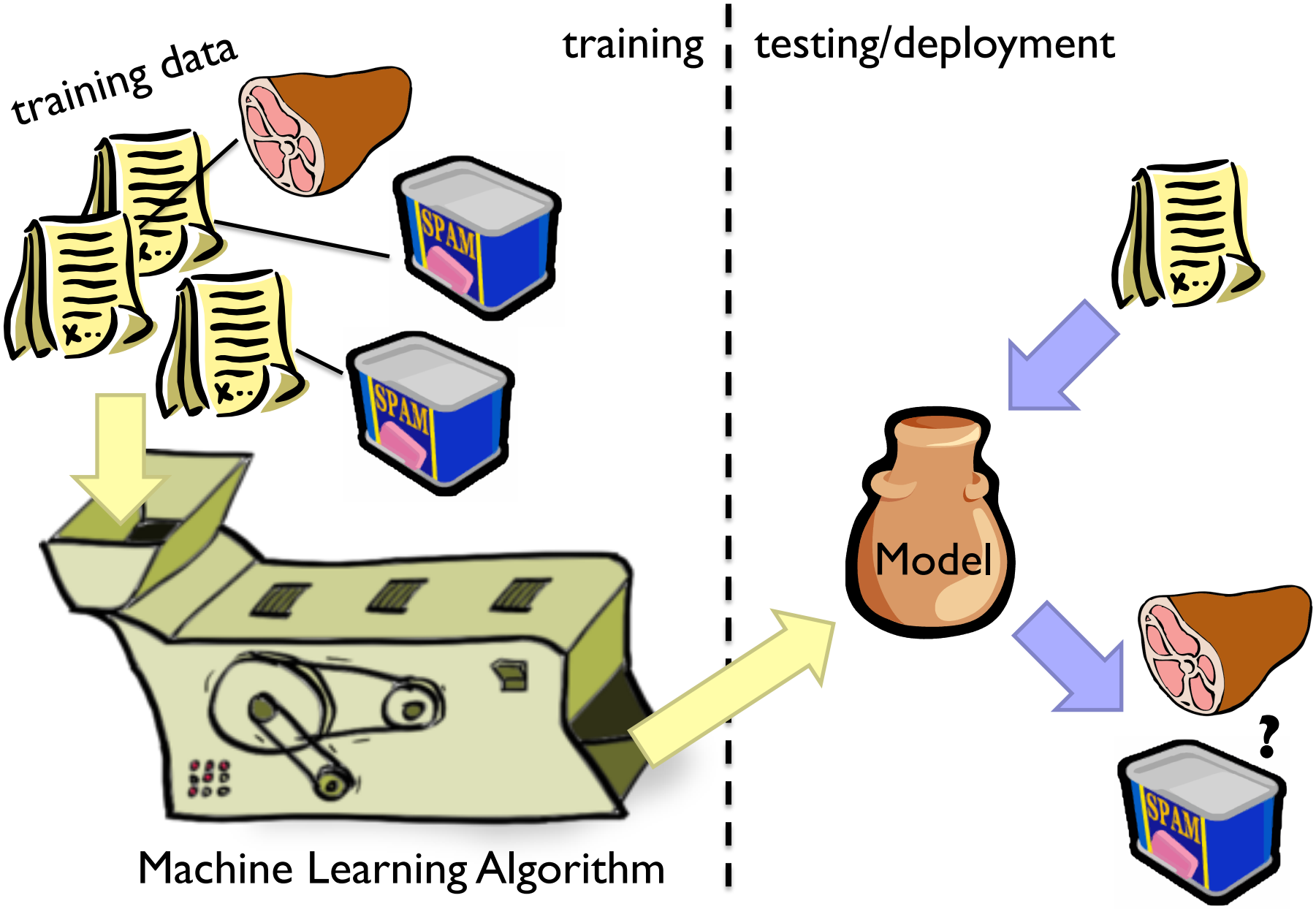
Lin and Kolcz, SIGMOD 2012

- Binary polarity classification: {positive, negative} sentiment
  - Independently interesting task
  - Illustrates end-to-end flow
  - Use the "emoticon trick" to gather data
- Data
  - Test: 500k positive/500k negative tweets from 9/1/2011
  - Training: {1m, 10m, 100m} instances from before (50/50 split)
- Features: Sliding window byte-4grams
- Models:
  - Logistic regression with SGD (L2 regularization)
  - Ensembles of various sizes (simple weighted voting)

Diminishing returns…



Supervised Machine Learning



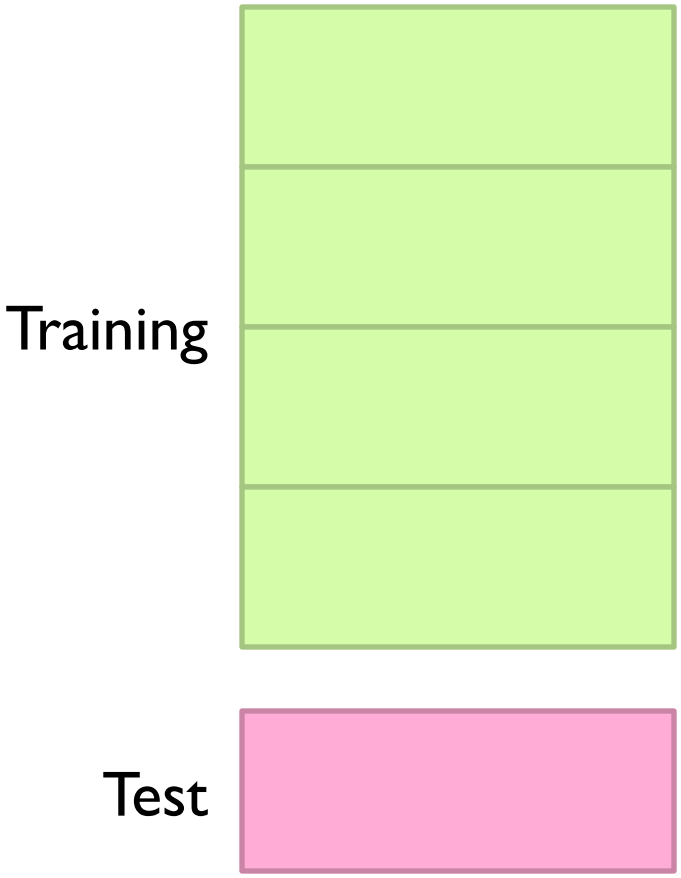
Applied ML in Academia

- Download interesting dataset (comes with the problem)
- Run baseline model
  - Train/test
- Build better model
  - Train/test
- Does new model beat baseline?
  - Yes: publish a paper!
  - No: try again!

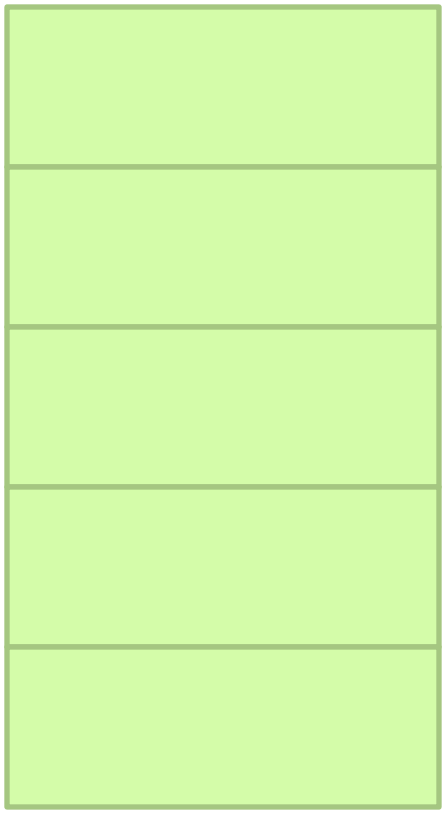
Three Commandants of Machine Learning

Thou shalt not mix training and testing data
Thou shalt not mix training and testing data
Thou shalt not mix training and testing data

Training/Testing Splits

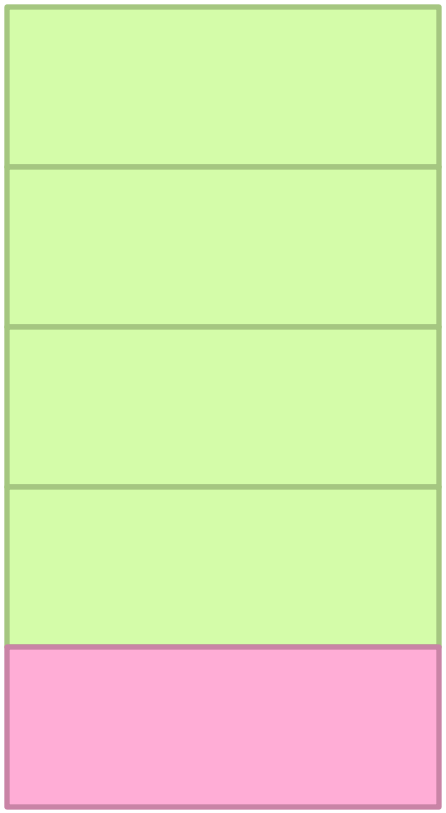


What happens if you need more?



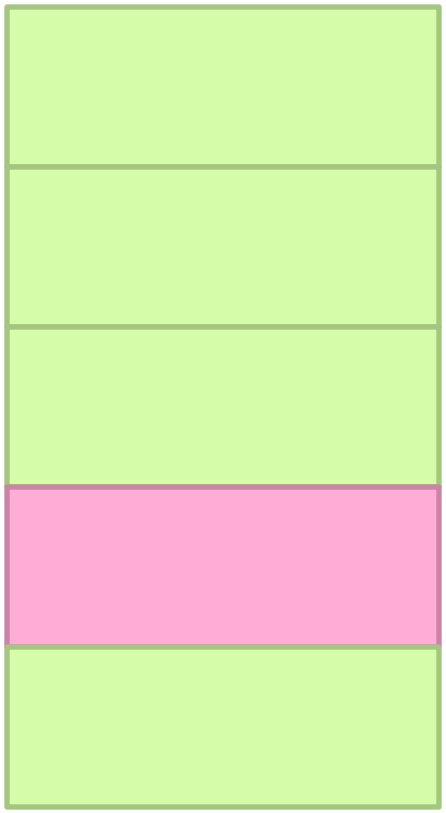
Cross-Validation

Training/Testing Splits



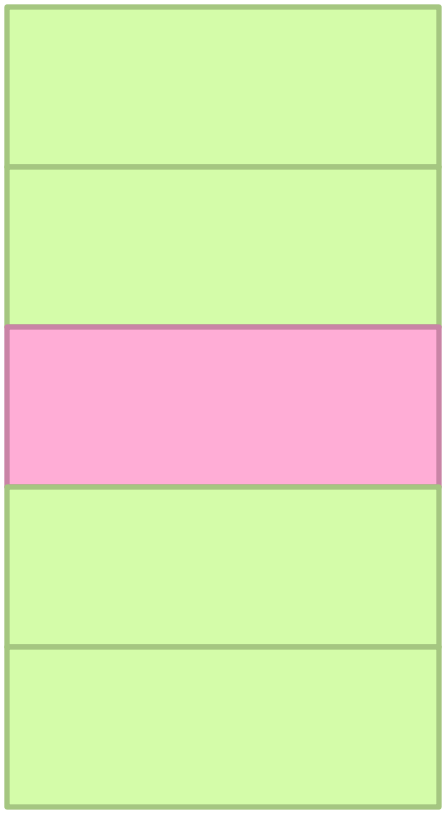
Cross-Validation

Training/Testing Splits



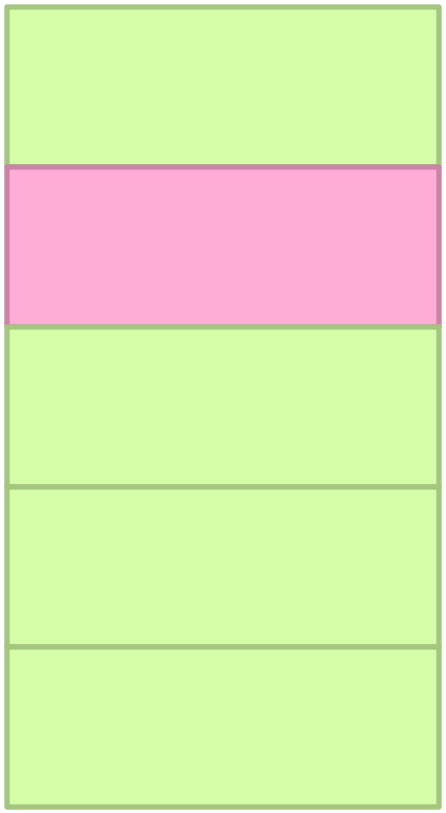
Cross-Validation

Training/Testing Splits



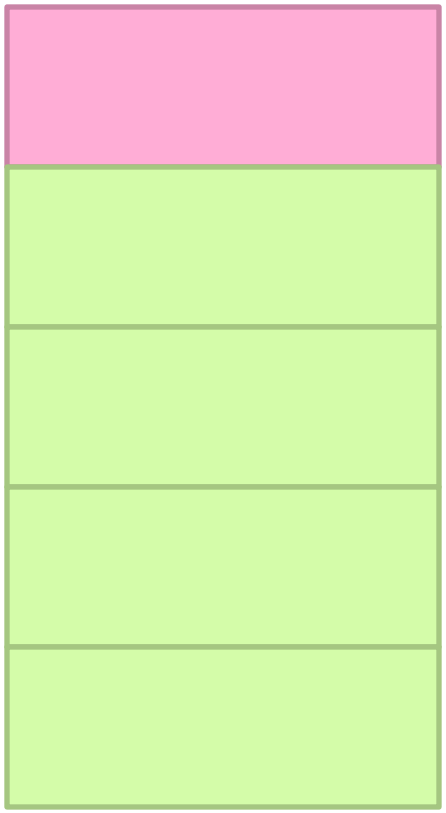
Cross-Validation

Training/Testing Splits



Cross-Validation

Training/Testing Splits



Cross-Validation

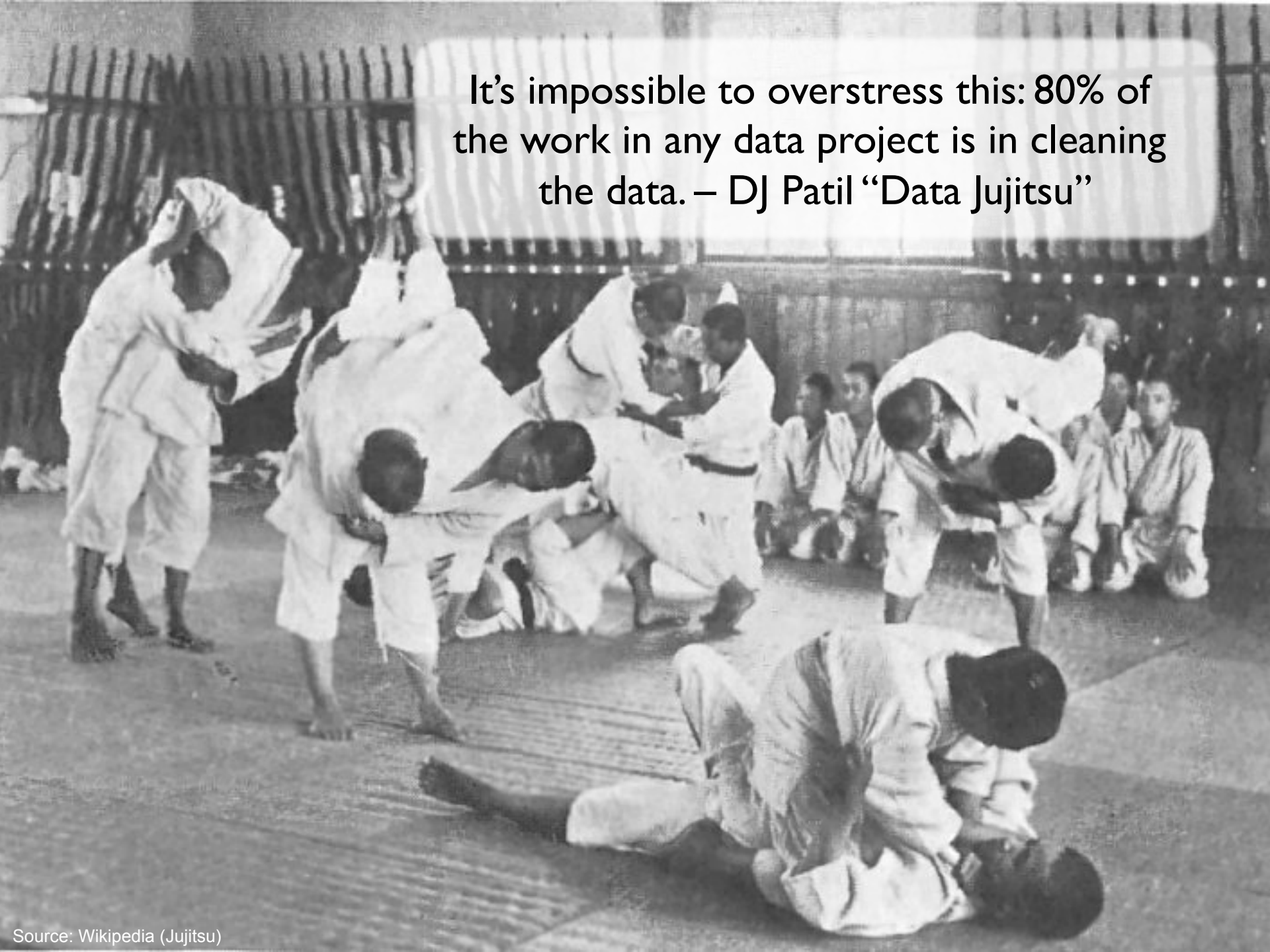
Applied ML in Academia

- Download interesting dataset (comes with the problem)
- Run baseline model
  - Train/test
- Build better model
  - Train/test
- Does new model beat baseline?
  - Yes: publish a paper!
  - No: try again!

Applied ML in Industry

- Formulate the problem (from some vague business goal)
- Find the data
- Prepare and clean the data
- Run data through machine learning library
  - Train/test on retrospective data
- Does the new model beat baseline?
  - Yes: Run live A/B test
  - No: try again!
- Does the new model work in A/B testing?
  - Yes: productionize the model
  - No: try again!

Where's most of the time spent?



Source: Wikipedia (Jujitsu)

The New York Times

TECHNOLOGY

For 'Big Data' Scientists, Hurdle to Insights Is 'Janitor Work'

By STEVE LOHR AUG. 17, 2014

Monica Rogati, Jawbone's vice president for data science, with Brian Wilt, a senior data scientist.

Peter DaSilva for The New York Times

Components of a ML Solution

Data
Features
Model
Optimization

What "matters" the most?

Source: Wikipedia (Japanese rock garden)