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#### Semester Thesis

## Undersampling-Conditioned Diffusion Models for MRI Reconstruction

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#### **ACKNOWLEDGMENTS**

#### INTRODUCTION

#### **BLUBBI**

#### SOME CHAPTER NAME TO BE CHANGED

#### 1 Diffusion Models

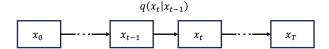
#### 1.1 Forward Diffusion Process

$$q(x_t \mid x_{t-1}) = \mathcal{N}(\sqrt{1 - \beta_t} x_{t-1}, \beta_t I)$$

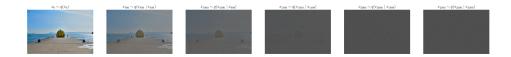
$$q(x_t \mid x_{t-1}) = \mathcal{N}(\sqrt{\alpha_t} x_{t-1}, (1 - \alpha_t) I)$$

$$q(x_t \mid x_0) = \mathcal{N}(\sqrt{\overline{\alpha_t}} x_0, (1 - \overline{\alpha_t}) I)$$

$$\bar{\alpha}_t = \prod_{i=0}^t \alpha_t$$
(1)



**Fig. 1:** Forward Diffusion Process: An image is iteratively destroyed by adding normally distributed noise, according to a schedule. This represents a Markov process where the transition probability  $q(x_t|x_{t-1})$ .



**Fig. 2:** Example of Iterative Image Destruction through Forward Diffusion Process: The indices give the time step in the iterative destruction process, where  $\beta$  was created according to a linear noise variance schedule (5000 steps from in the 0.001 to 0.02 range and picture resolution of 4016 by 6016 pixels).

## CONTENTS

Int	troduction	vii
ВΙ	ubbi	ix
Sc	ome Chapter Name to be changed	хi
	1 Diffusion Models	xi
	1.1 Forward Diffusion Process	xi
	F	age
Lis	st of Figures	χV
Lis	st of Tables	xvii
Lis	stings	xix
1	Introduction	1
2	Blubbi	3

## LIST OF FIGURES

1	Forward Diffusion Process: An image is iteratively destroyed by adding normally	
	distributed noise, according to a schedule. This represents a Markov process	
	where the transition probability $q(x_t x_{t-1})$	xi
2	Example of Iterative Image Destruction through Forward Diffusion Process: The	
	indices give the time step in the iterative destruction process, where $\beta$ was	
	created according to a linear noise variance schedule (5000 steps from in the	
	0.001 to $0.02$ range and picture resolution of 4016 by 6016 pixels)	xi

## LIST OF TABLES

## LISTINGS

INTRODUCTION

# 2 BLUBBI