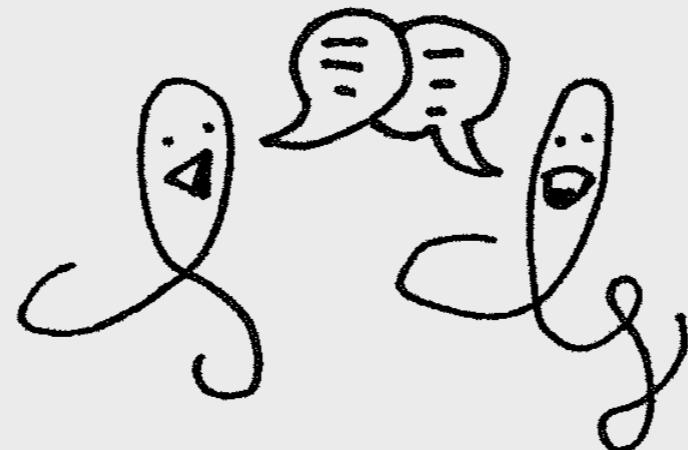
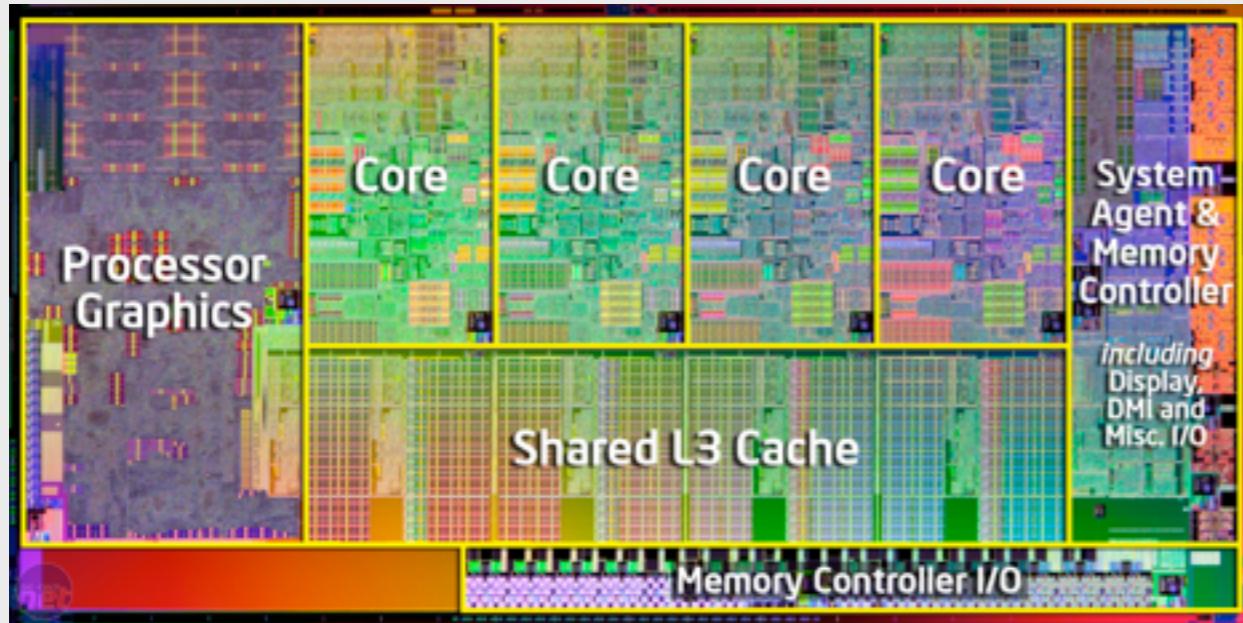


Lattice-based Data Structures for Deterministic Parallel and Distributed Programming



Lindsey Kuper
September 8, 2014

(with illustrations by Jason Reed)



Parallel systems



Distributed systems

My thesis: aka “ $LVars$ ”
Lattice-based data structures
are a general and practical unifying abstraction
for deterministic and quasi-deterministic
parallel and distributed programming.



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spoiler:
deterministic
modulo exceptions

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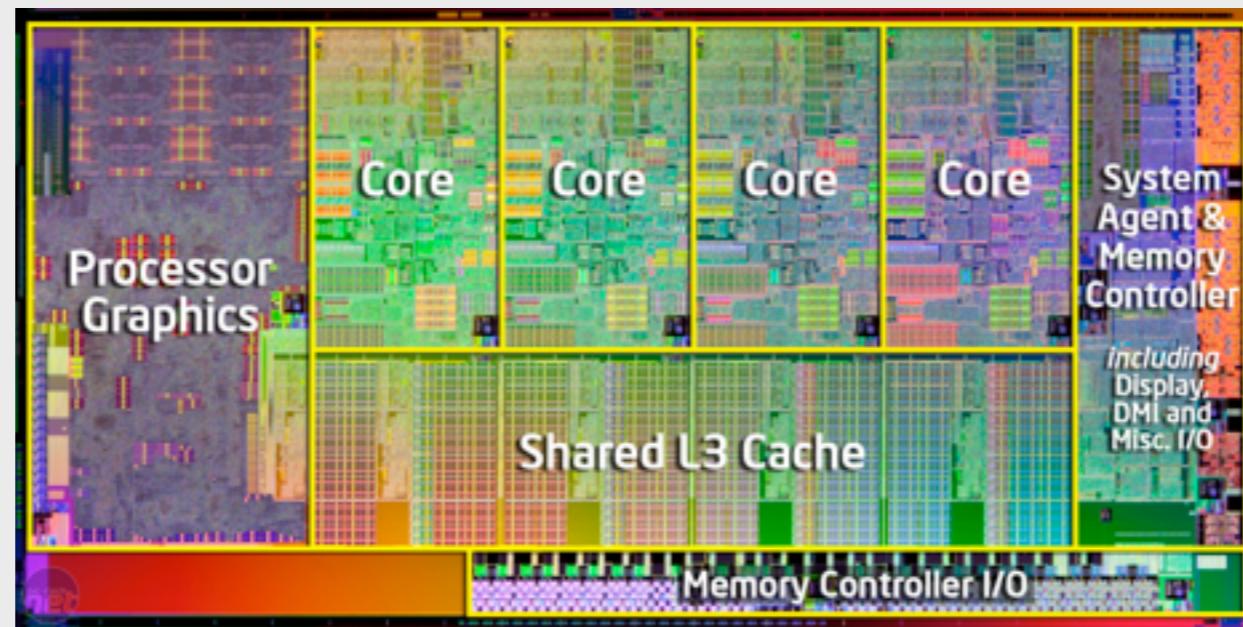


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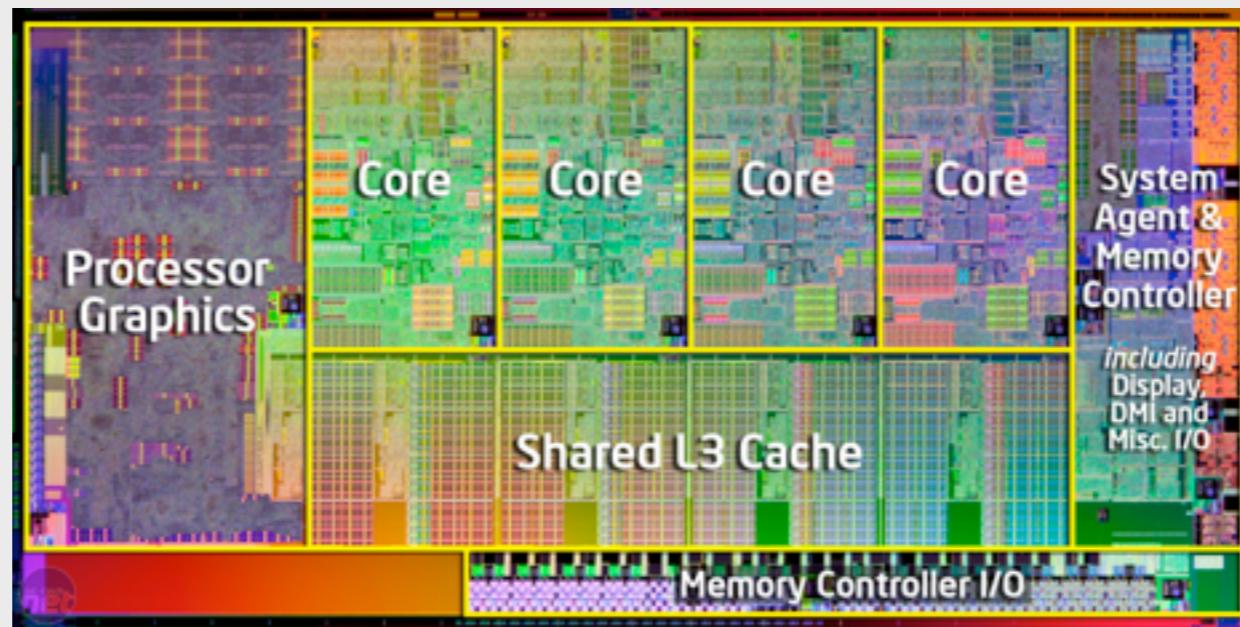


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Deterministic Parallel Programming



(observably)
Deterministic Parallel Programming



```
data Item = Book | Shoes | ...
```



```
data Item = Book | Shoes | ...
```

```
p :: IO (Map Item Int)
```



```
data Item = Book | Shoes | ...
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p :: IO (Map Item Int)  
p = do cart <- newIORef empty
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```
data Item = Book | Shoes | ...  
  
p :: IO (Map Item Int)  
p = do cart <- newIORef empty  
       async (atomicModifyIORef cart  
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```



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       res <- async (readIORef cart)
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```



Terminal = bash = 90x27

bash

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if we want determinism,
we have to learn to *share nicely*

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       wait res
```



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p :: IO (Map Item Int)
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                        readIORef cart)
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main = do v <- p
          print v
```

deterministic

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deterministic...now

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deterministic...now...we hope

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main = do v <- p
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```

```

p :: HasPut e =>
  Par e s (IMap Item s Int)
p = do
  cart <- newEmptyMap
  fork (insert Book 1 cart)
  fork (insert Shoes 1 cart)
  return cart

main = print (runParThenFreeze p)

```

deterministic by construction
 [FHPC '13, POPL '14]

deterministic...now...we hope



The deterministic by construction parallel programming landscape:

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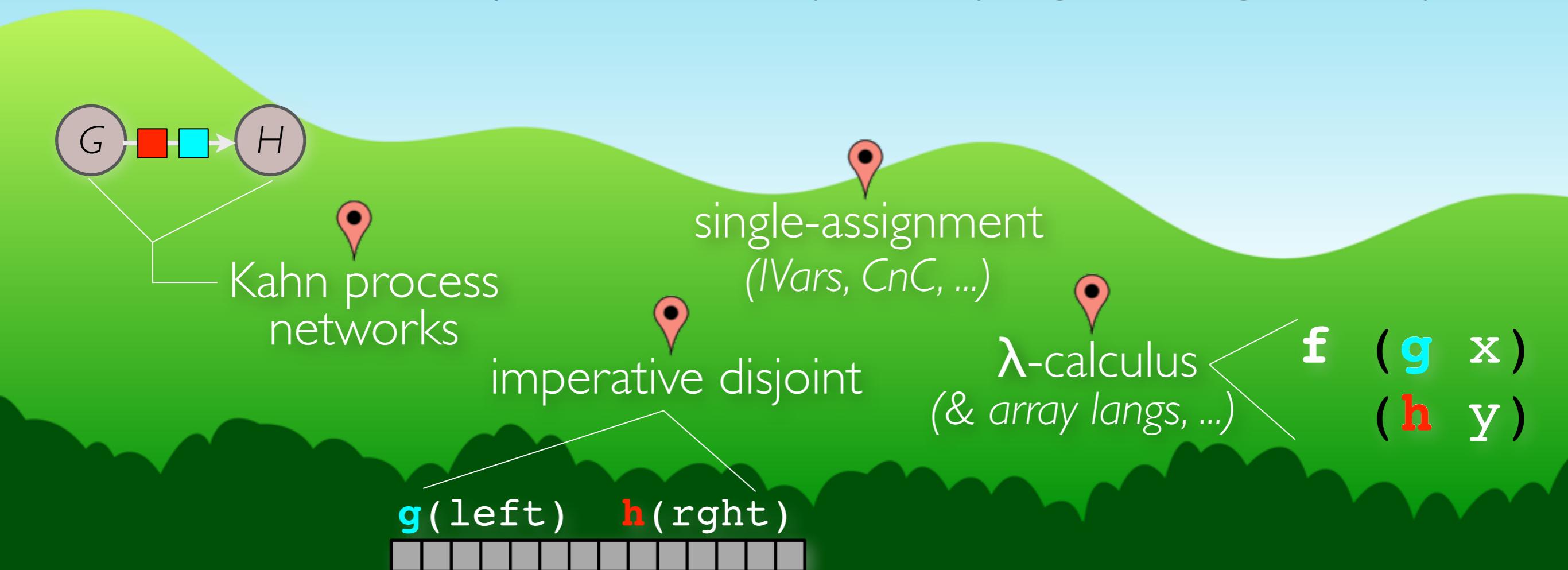
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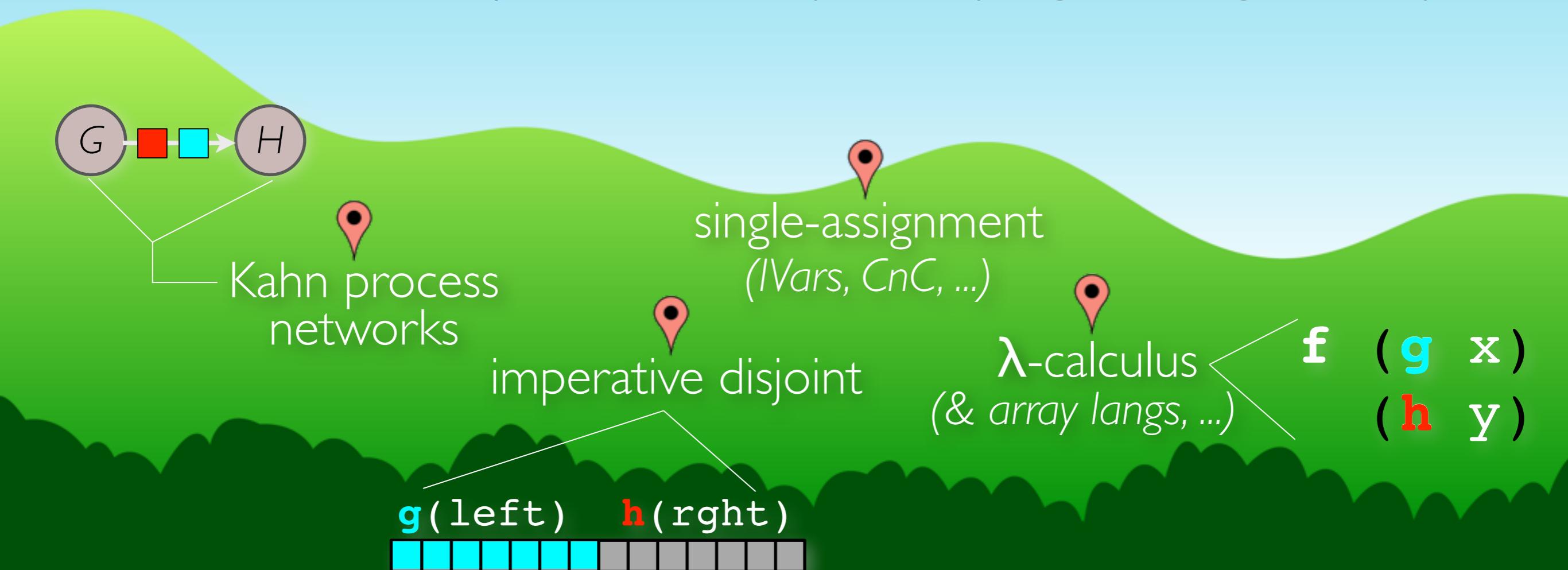
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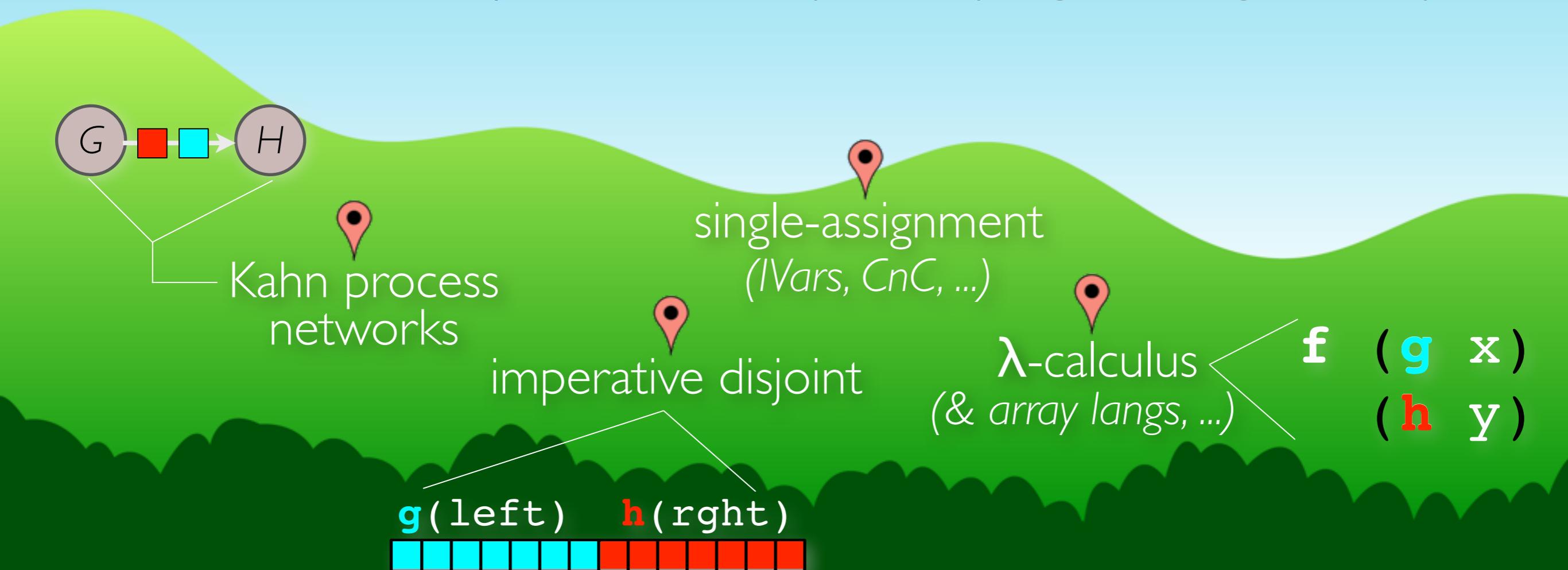
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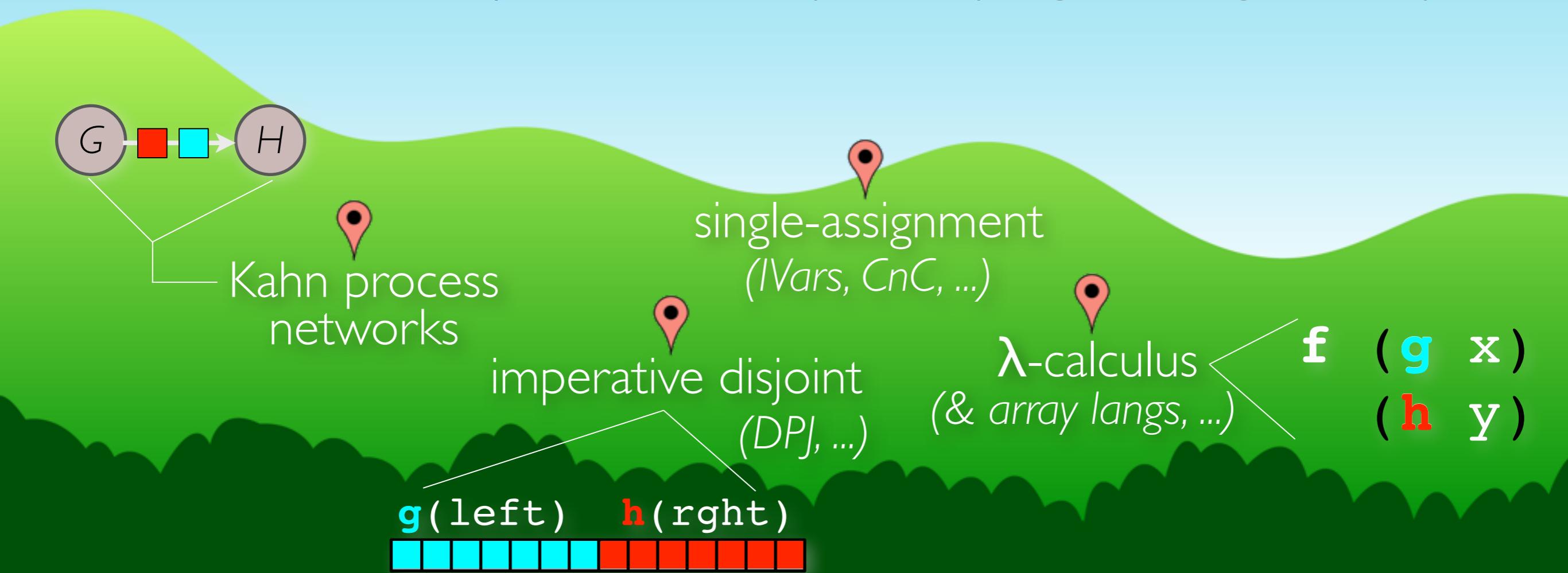
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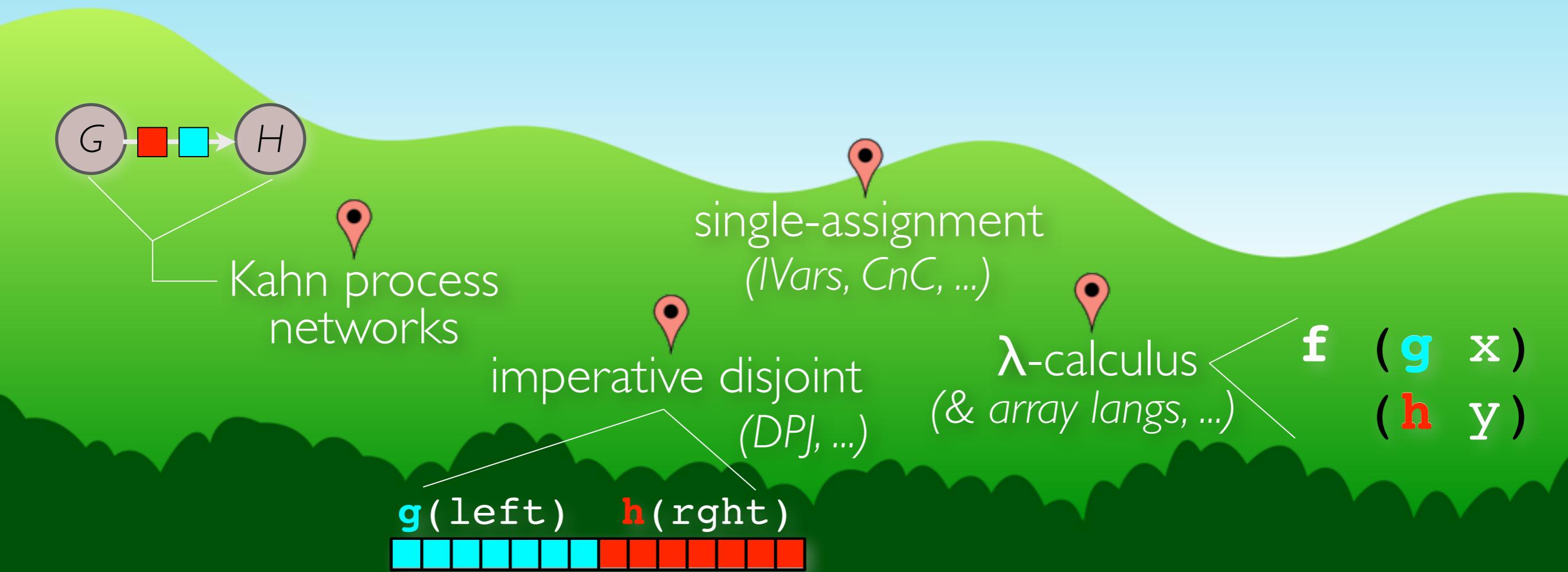
The deterministic by construction parallel programming landscape:



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The deterministic by construction parallel programming landscape:



Can we generalize and *unify* these points in the space?

aka “ $LVars$ ”

Lattice-based data structures

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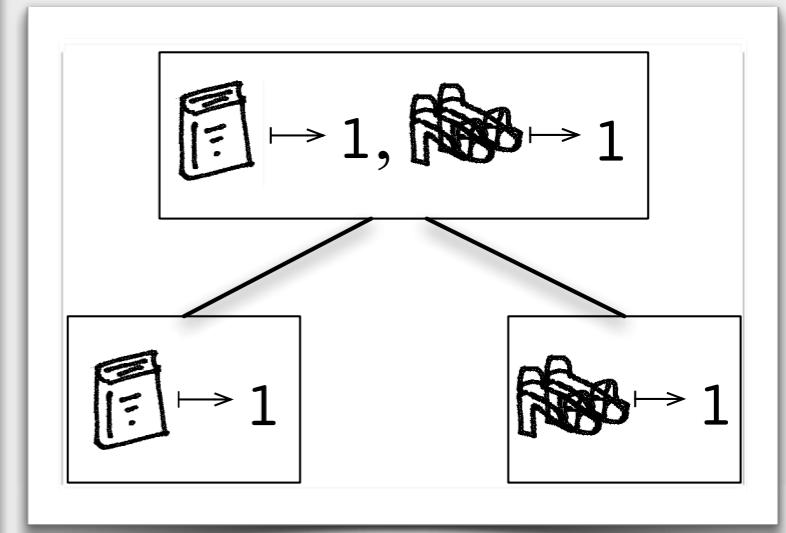
IVars: single writes, blocking (but exact) reads

[Arvind et al., 1989]



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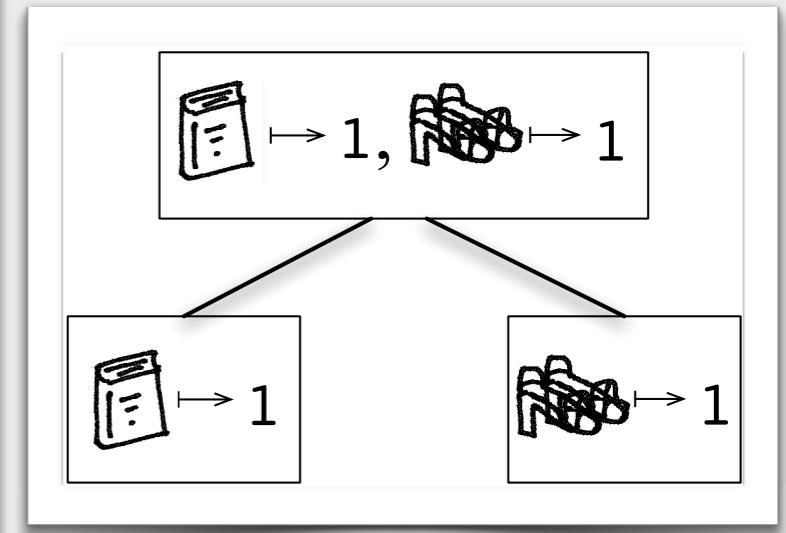
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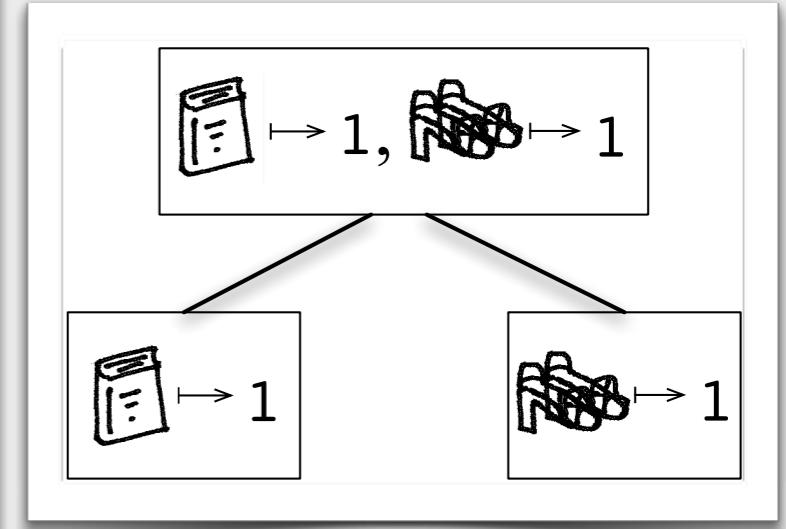
[Arvind et al., 1989]

LVars: multiple commutative and *inflationary* writes,
blocking *threshold* reads



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IVars: single writes, blocking (but exact) reads

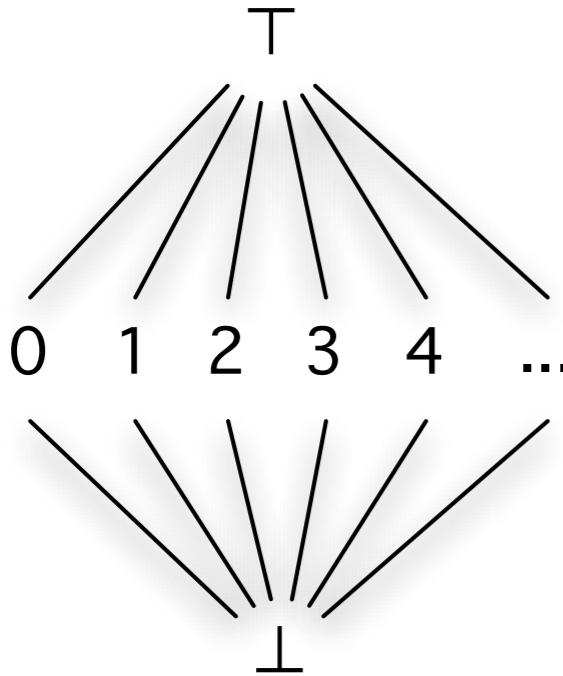
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LVars: multiple commutative and *inflationary* writes,
blocking threshold reads



* actually a bounded join-semilattice

num



Raises an error, since $3 \sqcup 4 = T$

do

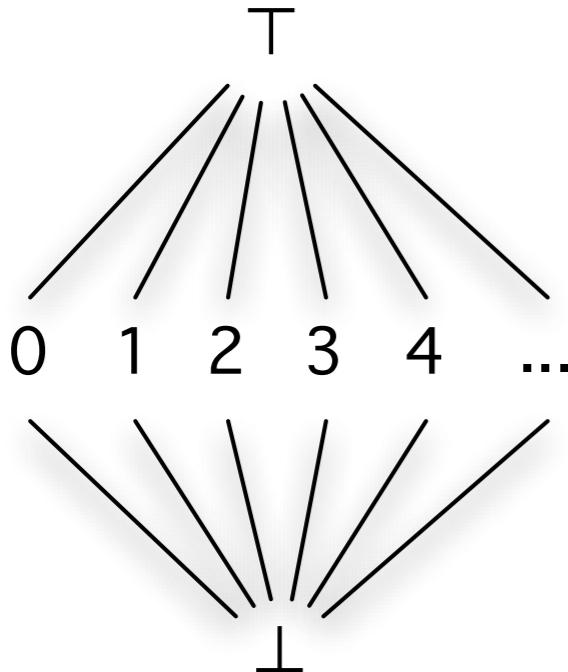
```
fork (put num 3)  
fork (put num 4)
```

Works fine, since $4 \sqcup 4 = 4$

do

```
fork (put num 4)  
fork (put num 4)
```

num



Raises an error, since $3 \sqcup 4 = T$

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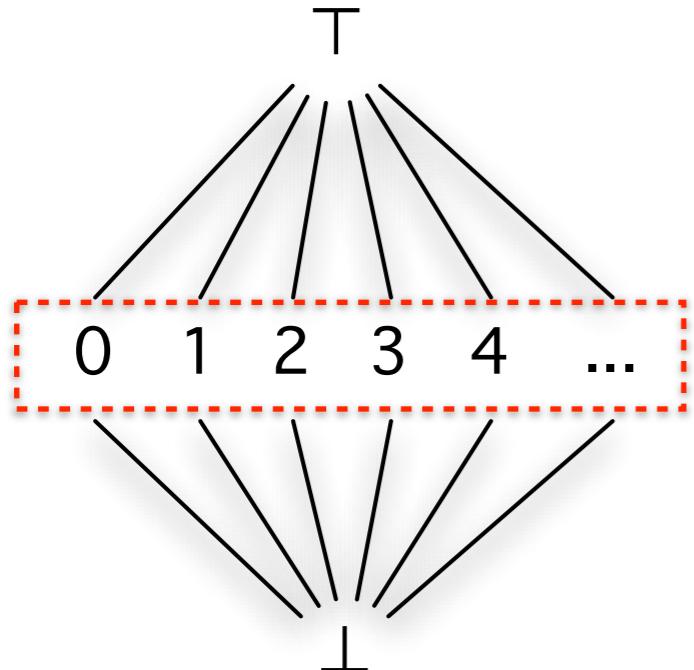
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fork (put num 4)  
fork (put num 4)
```

get blocks until threshold is reached

do

```
fork (put num 4)  
get num
```

num



Raises an error, since $3 \sqcup 4 = T$

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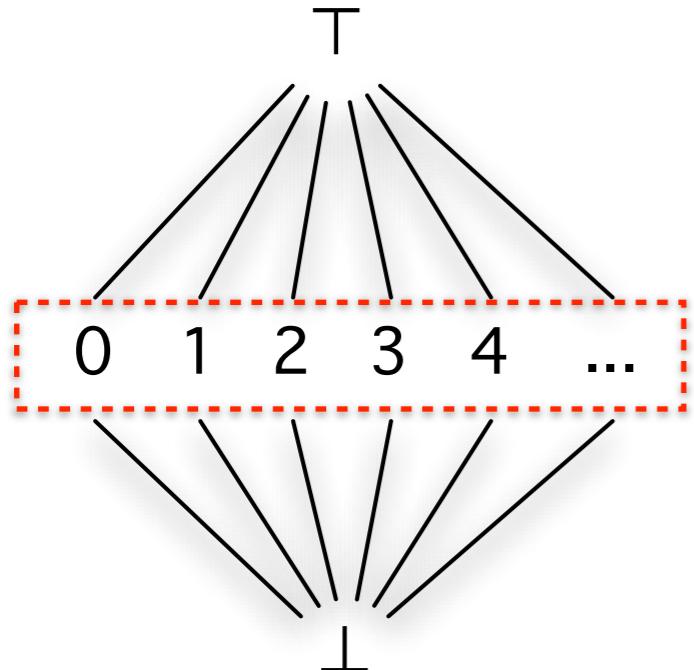
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fork (put num 4)  
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`num`



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Works fine, since $4 \sqcup 4 = 4$

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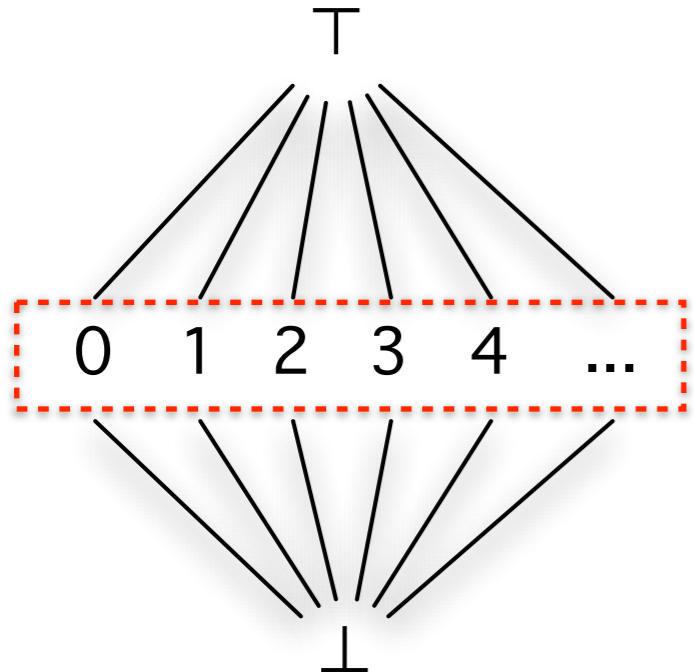
`get` blocks until threshold is reached

do

```
fork (put num 4)  
get num
```

threshold set elements
must be
pairwise incompatible

num



Raises an error, since $3 \sqcup 4 = \top$

do

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Works fine, since $4 \sqcup 4 = 4$

do

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Data structure author's
obligation:

threshold set elements
must be
pairwise incompatible

get blocks until threshold is reached

do

```
fork (put num 4)  
get num
```

counter

T
|
:
3
|
2
|
1
|
⊥

Works fine, since **incrs** commute

do

fork (incr1 counter)
fork (incr42 counter)

counter

T
|
:
3
|
2
|
1
|
—

Works fine, since **incr**s commute
do

fork (incr1 counter)
fork (incr42 counter)

get blocks until threshold is reached

do

fork (incr1 counter)
fork (incr42 counter)
get counter 2

counter

T

:

3

2

1

—

Works fine, since **incr**s commute
do

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fork (incr1 counter)  
fork (incr42 counter)
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get blocks until threshold is reached

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get counter 2
```

counter

T

:

3

2

1

—

—

Works fine, since **incrs** commute
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fork (incr1 counter)  
fork (incr42 counter)
```

get blocks until threshold is reached

do

```
fork (incr1 counter)  
fork (incr42 counter)  
get counter 2
```

unblocks when **counter** is at least 2
exact contents of **counter** not observable



- ✖ Can't see the exact, complete contents of an LVar



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- ✖ Can't iterate over the contents of an LVar



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- ✖ Can't react to writes that we weren't expecting



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handlers,
quiescence,
freezing



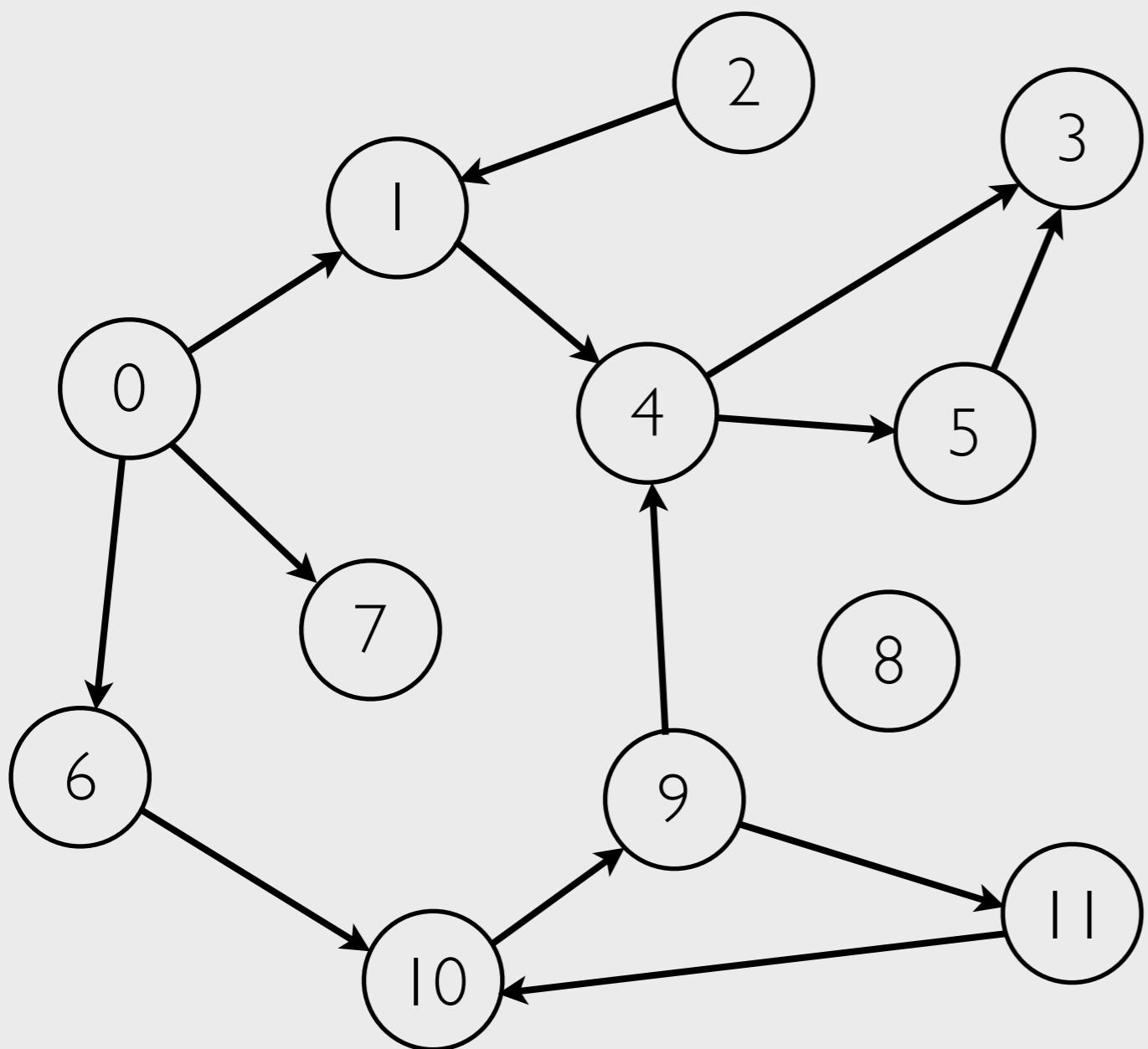
freeze after writing
(or before reading)

aka “ $LVars$ ”
^

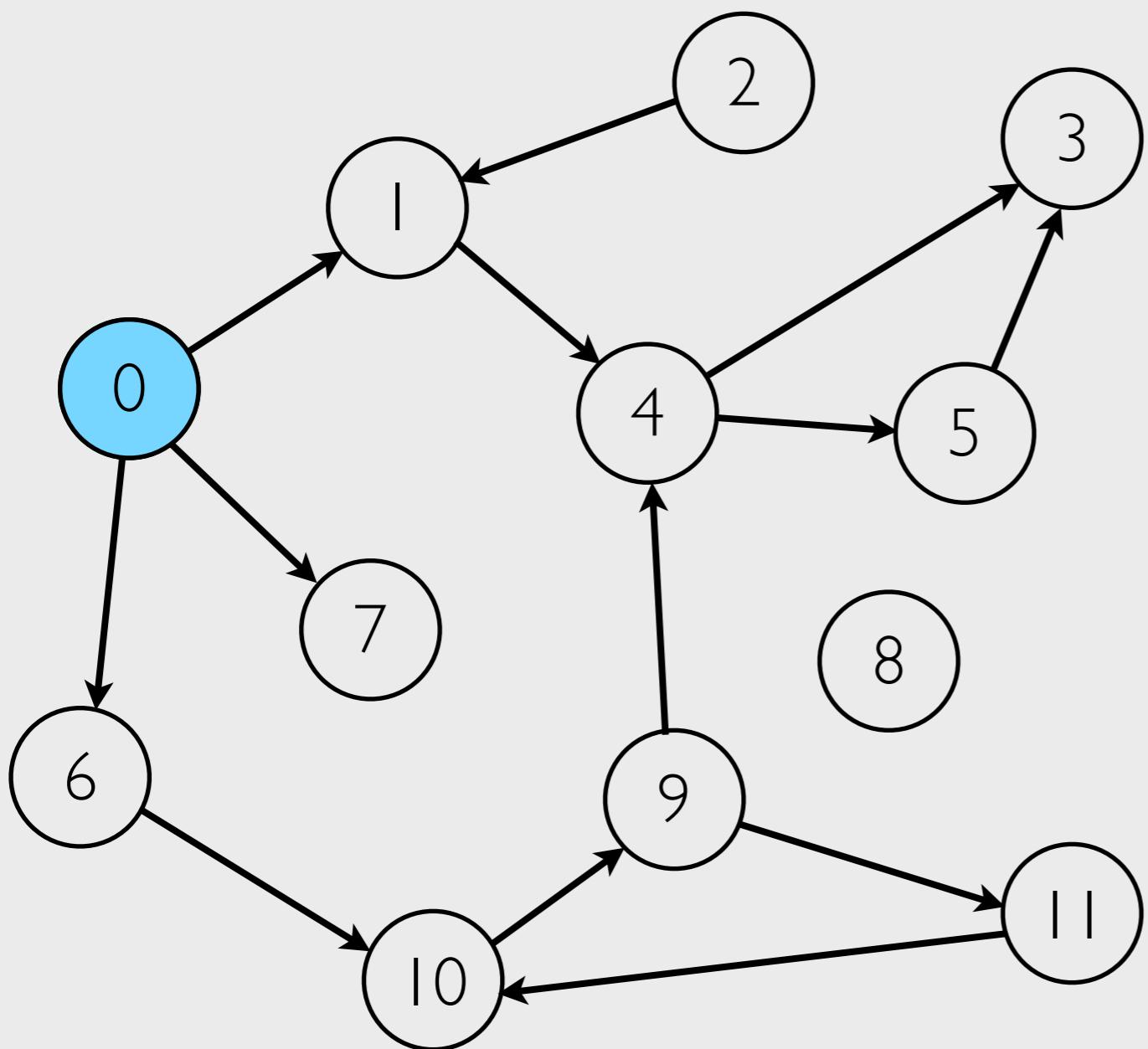
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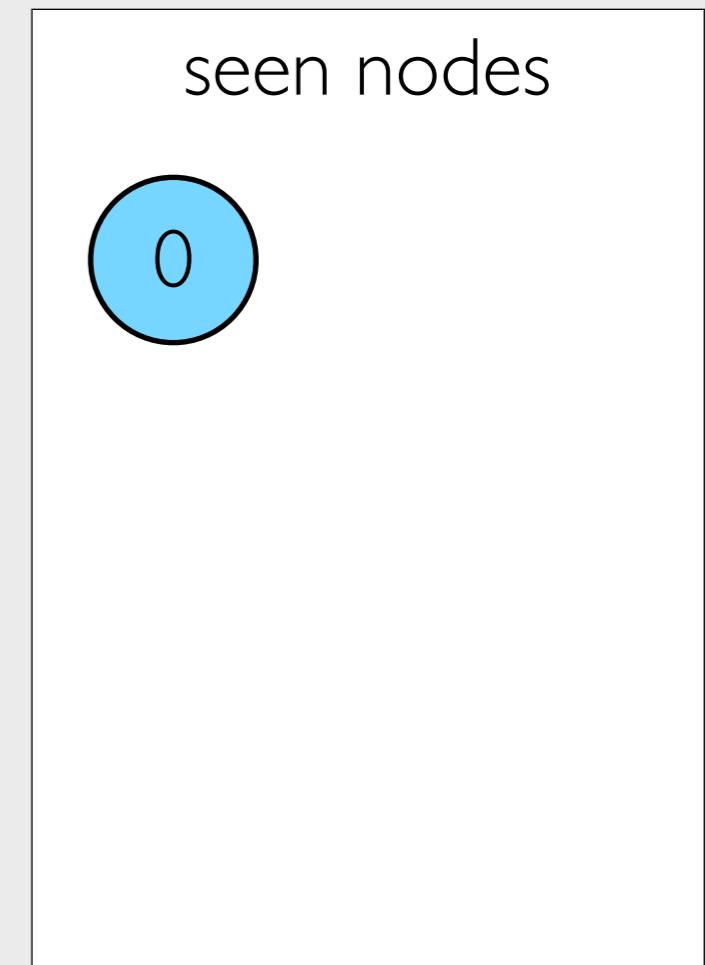
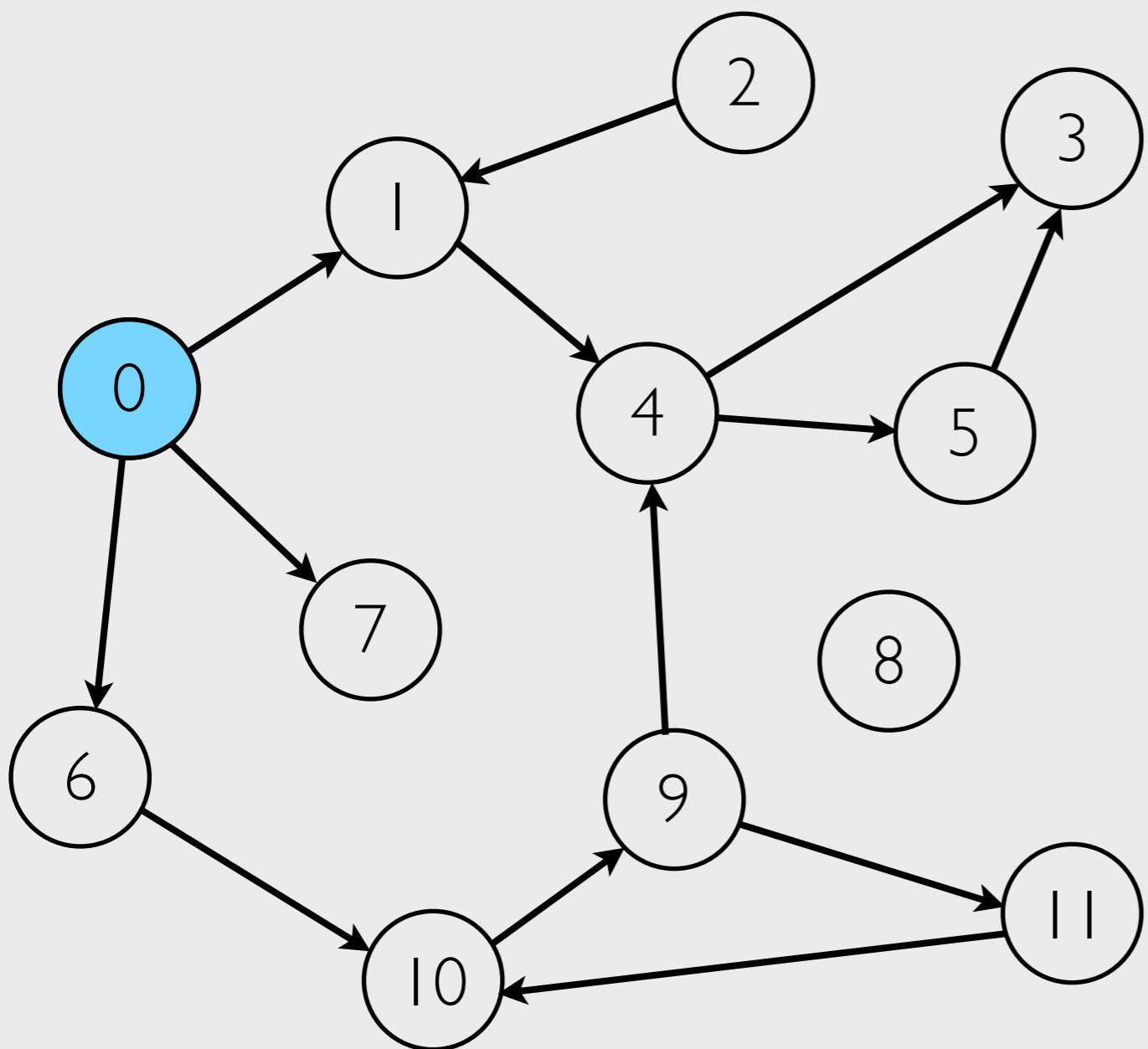


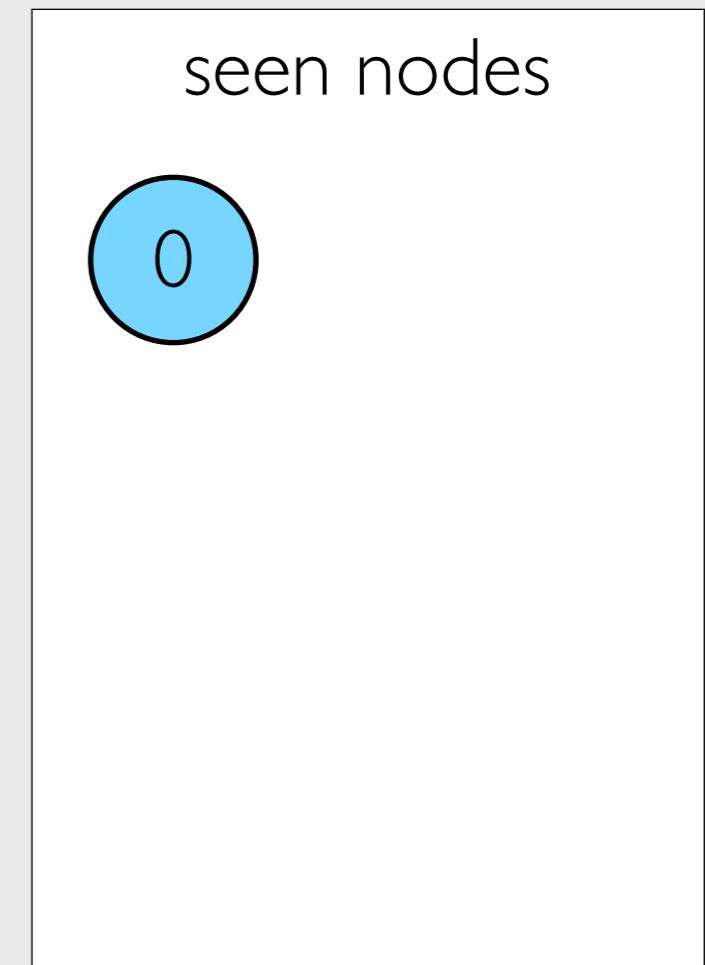
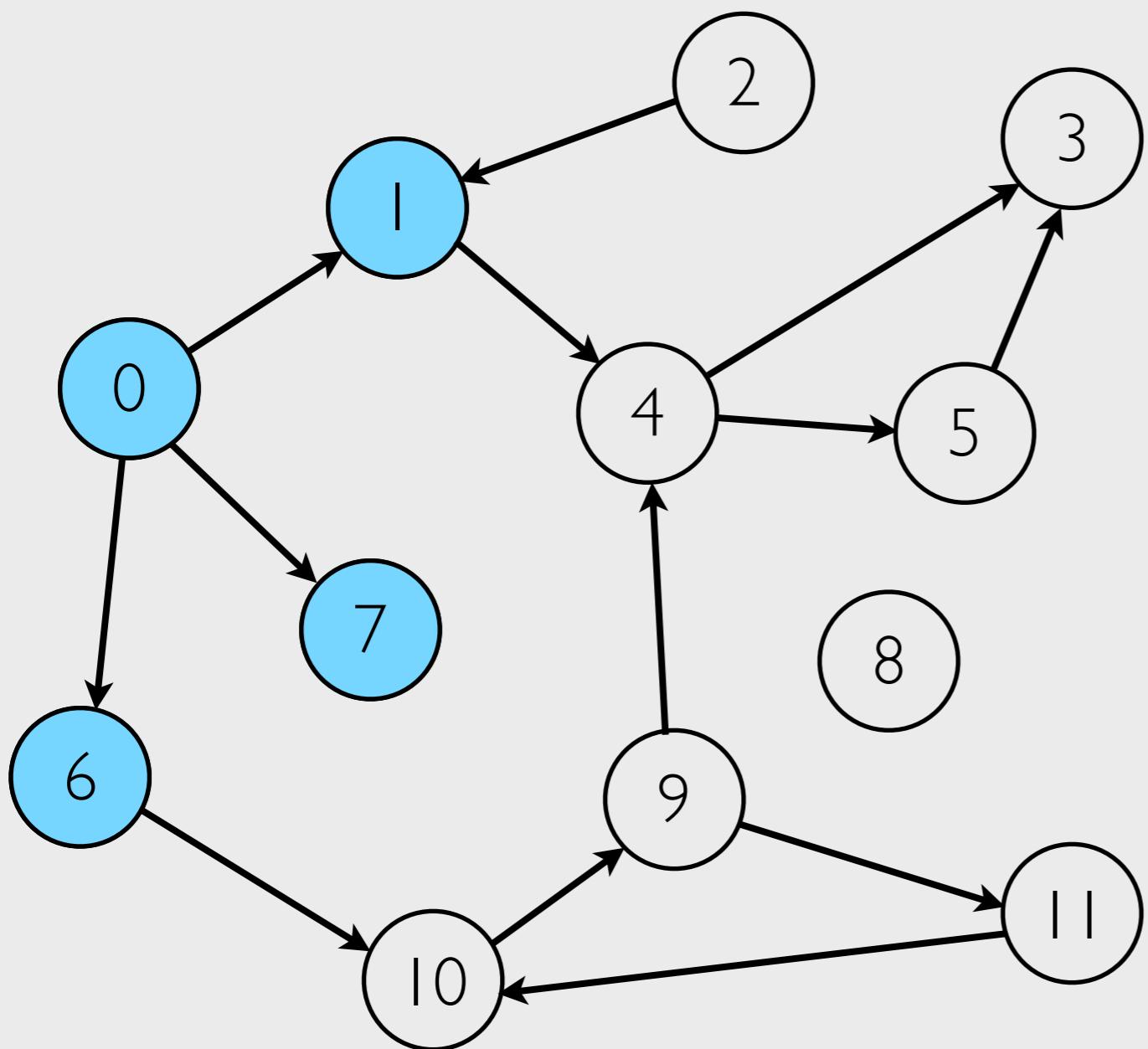


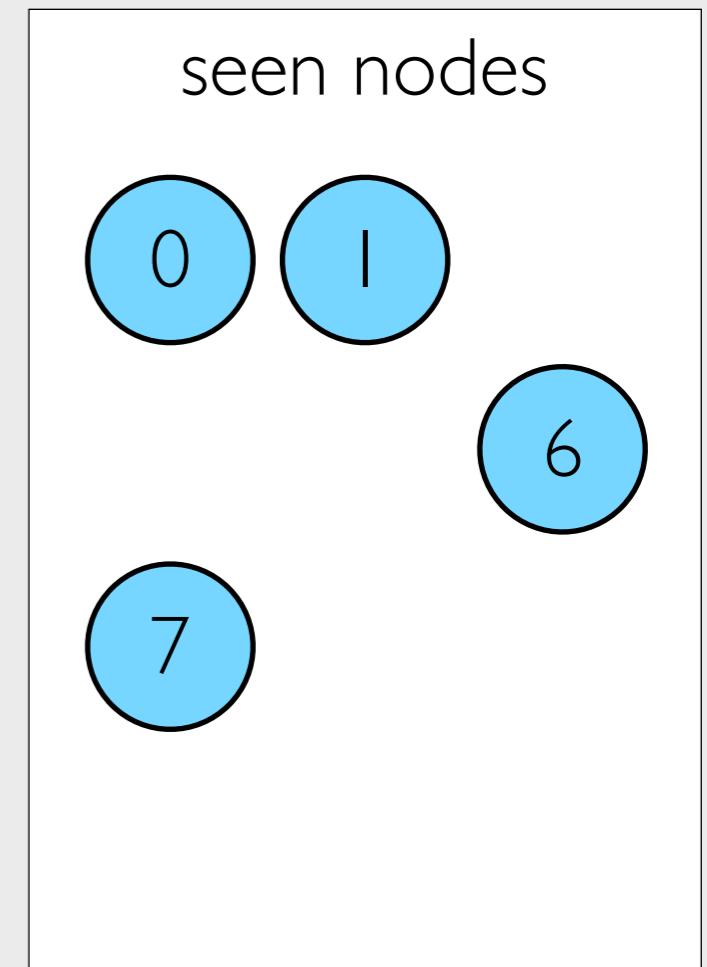
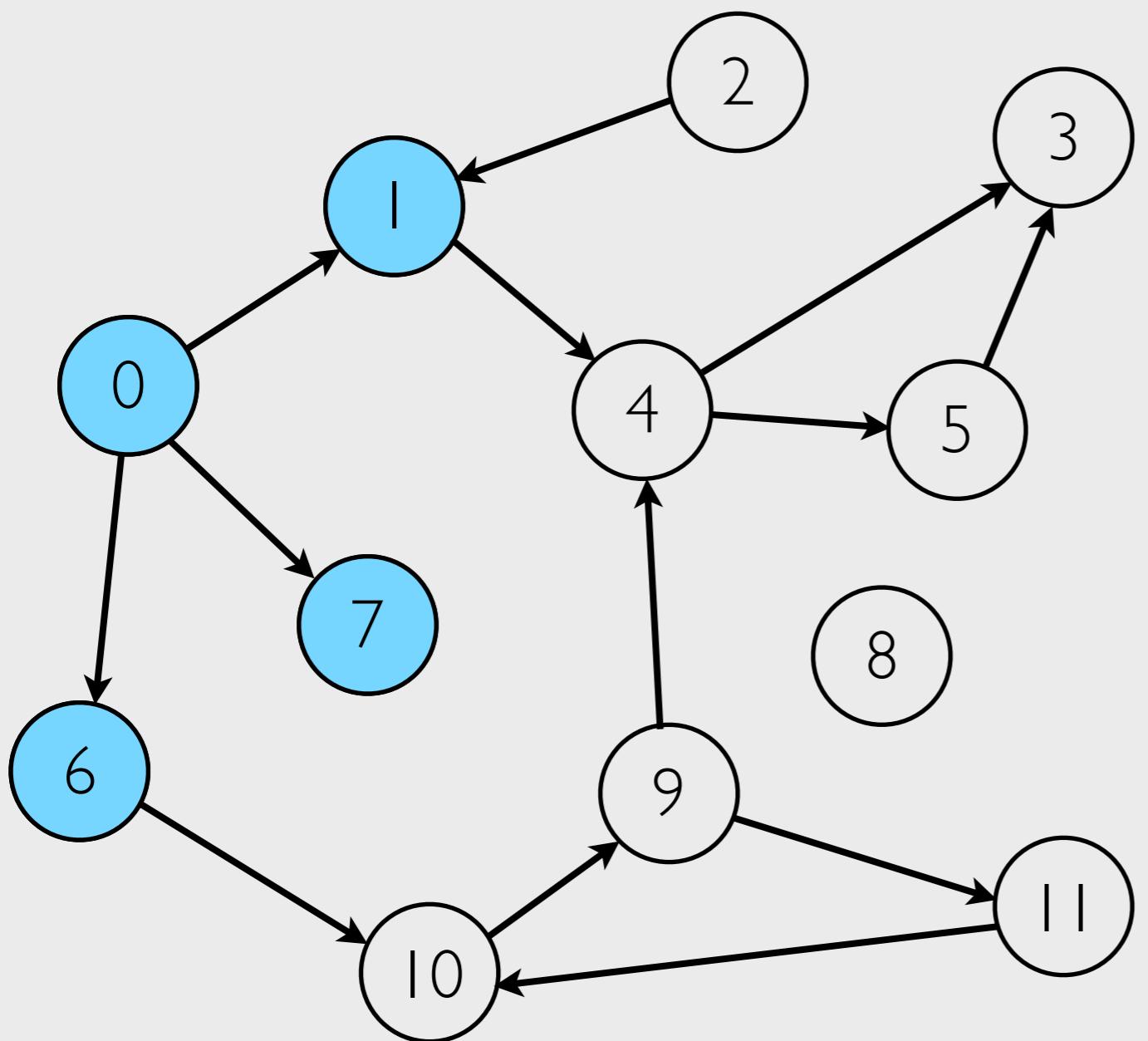
seen nodes

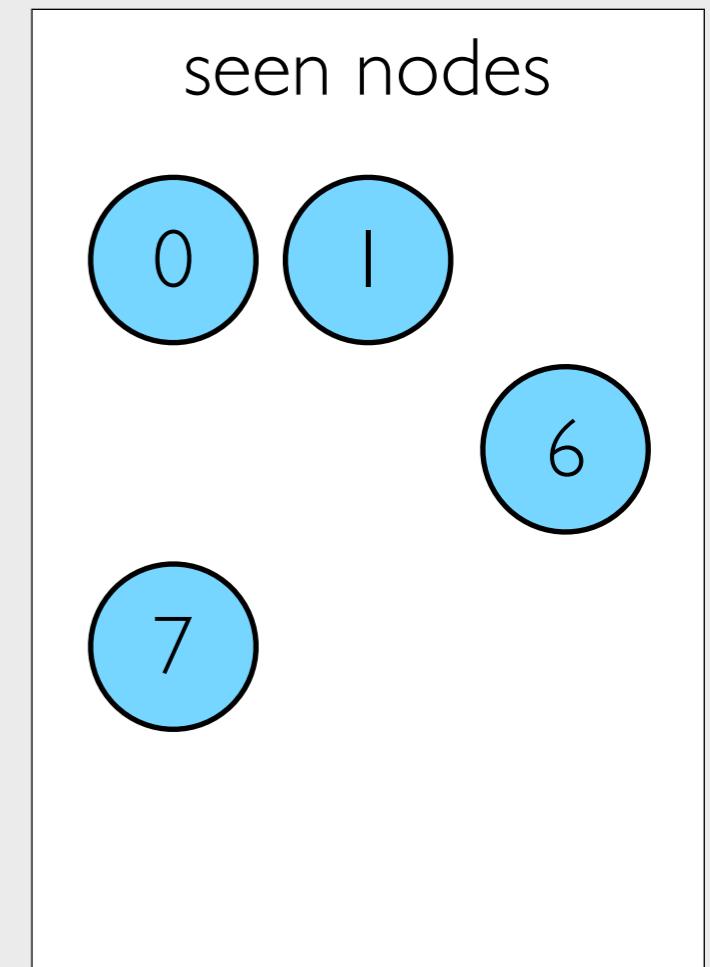
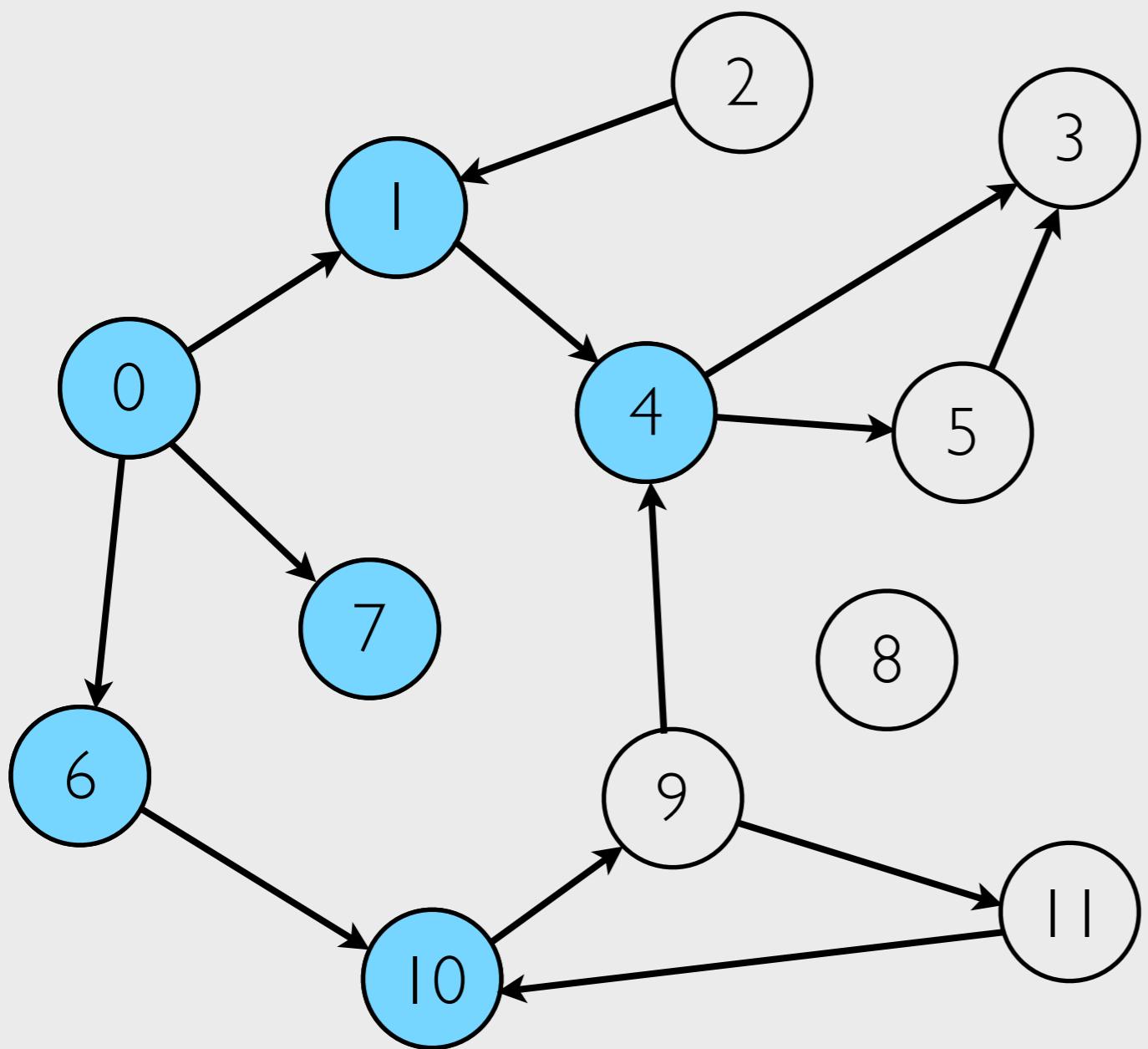


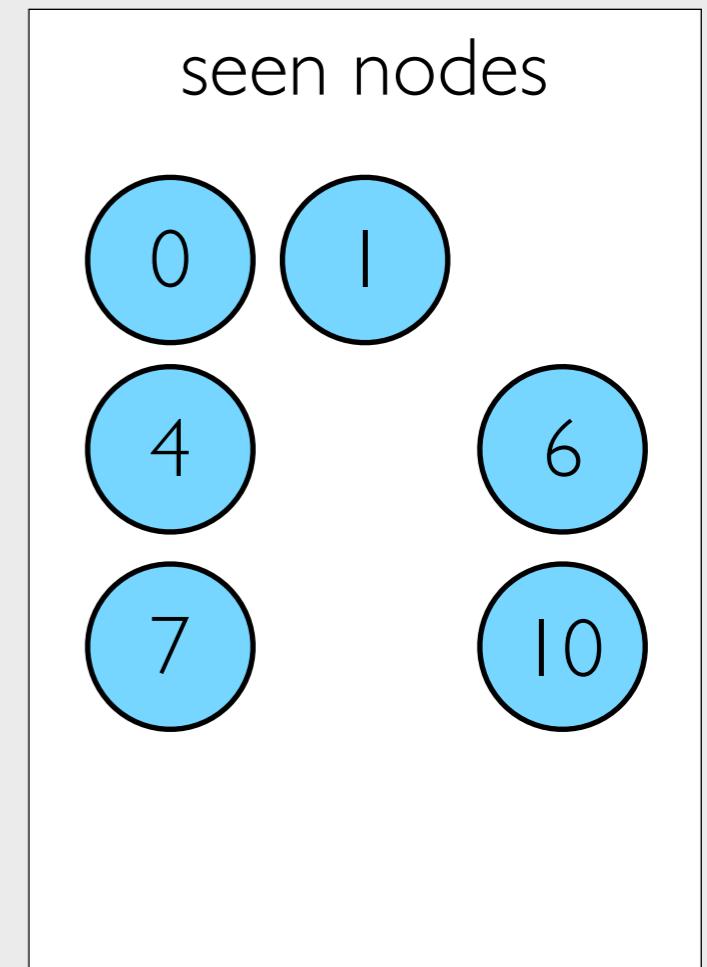
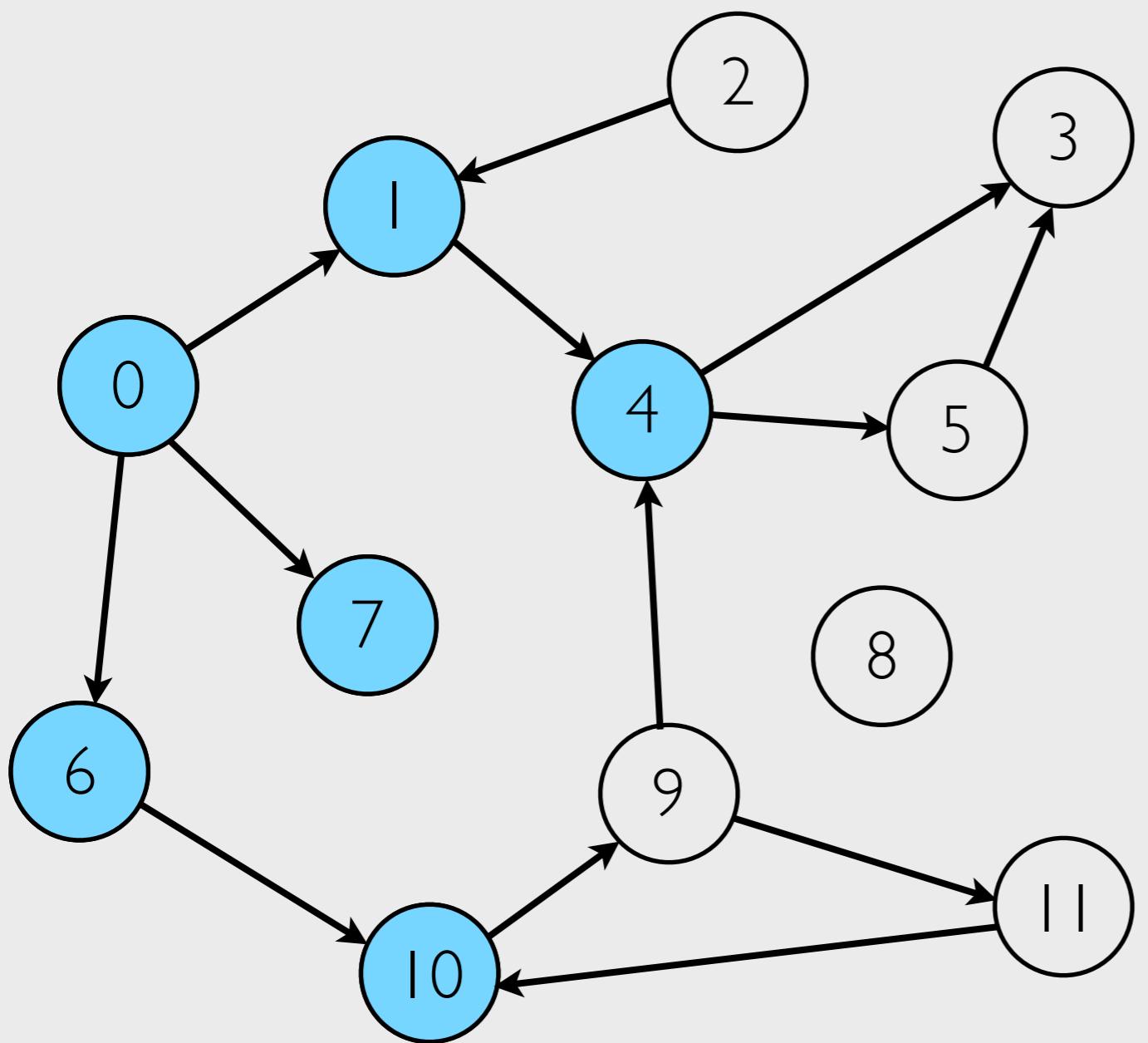
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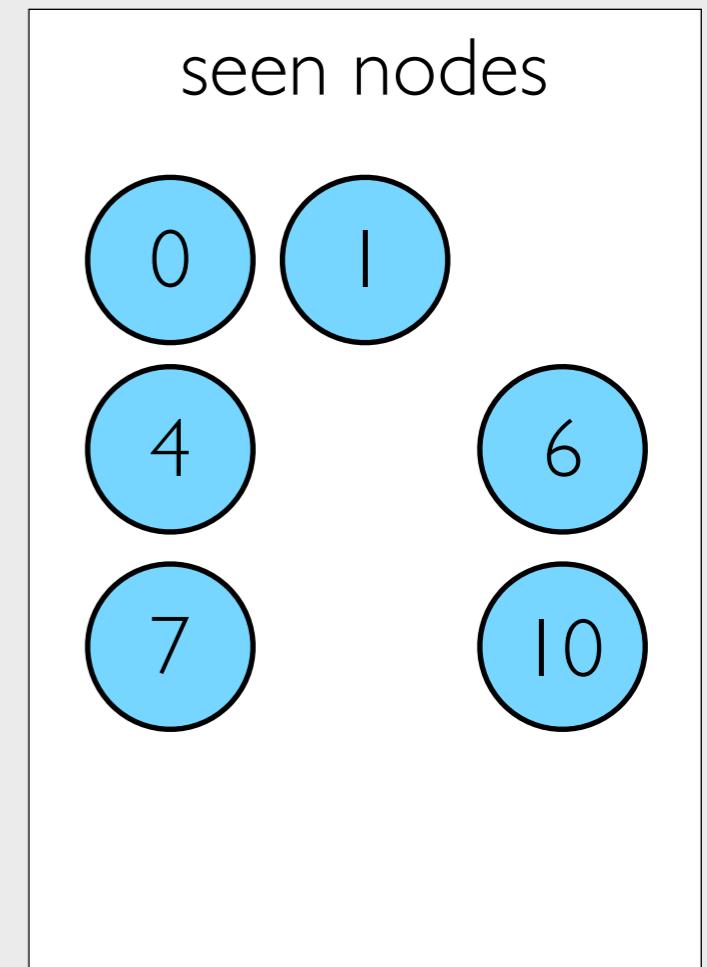
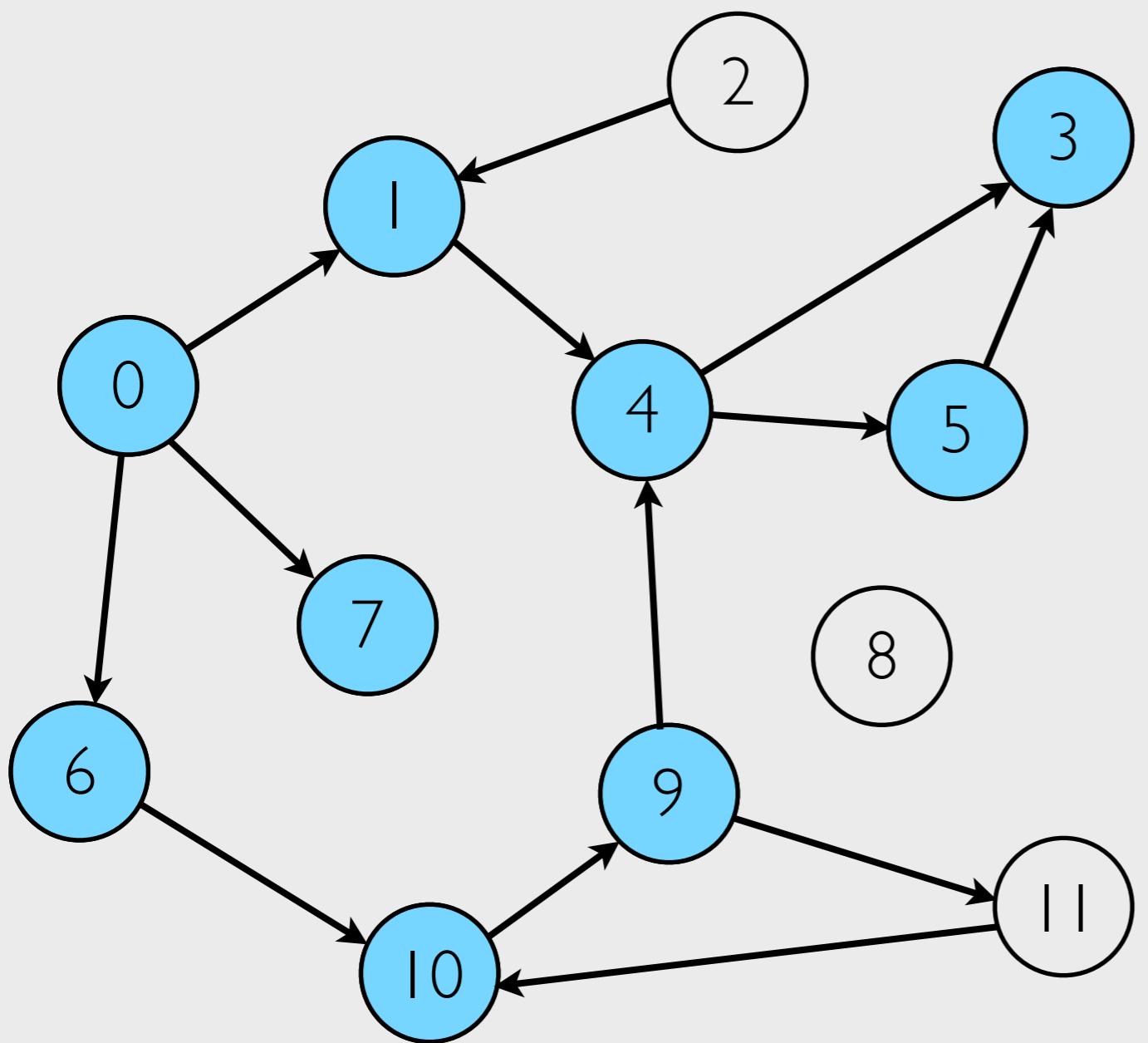


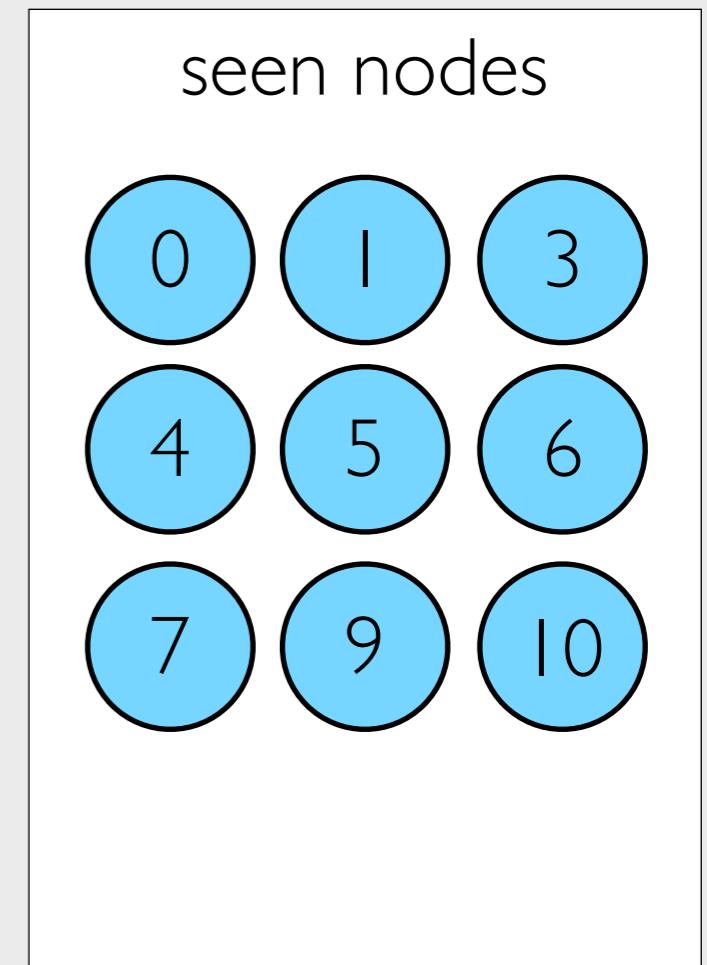
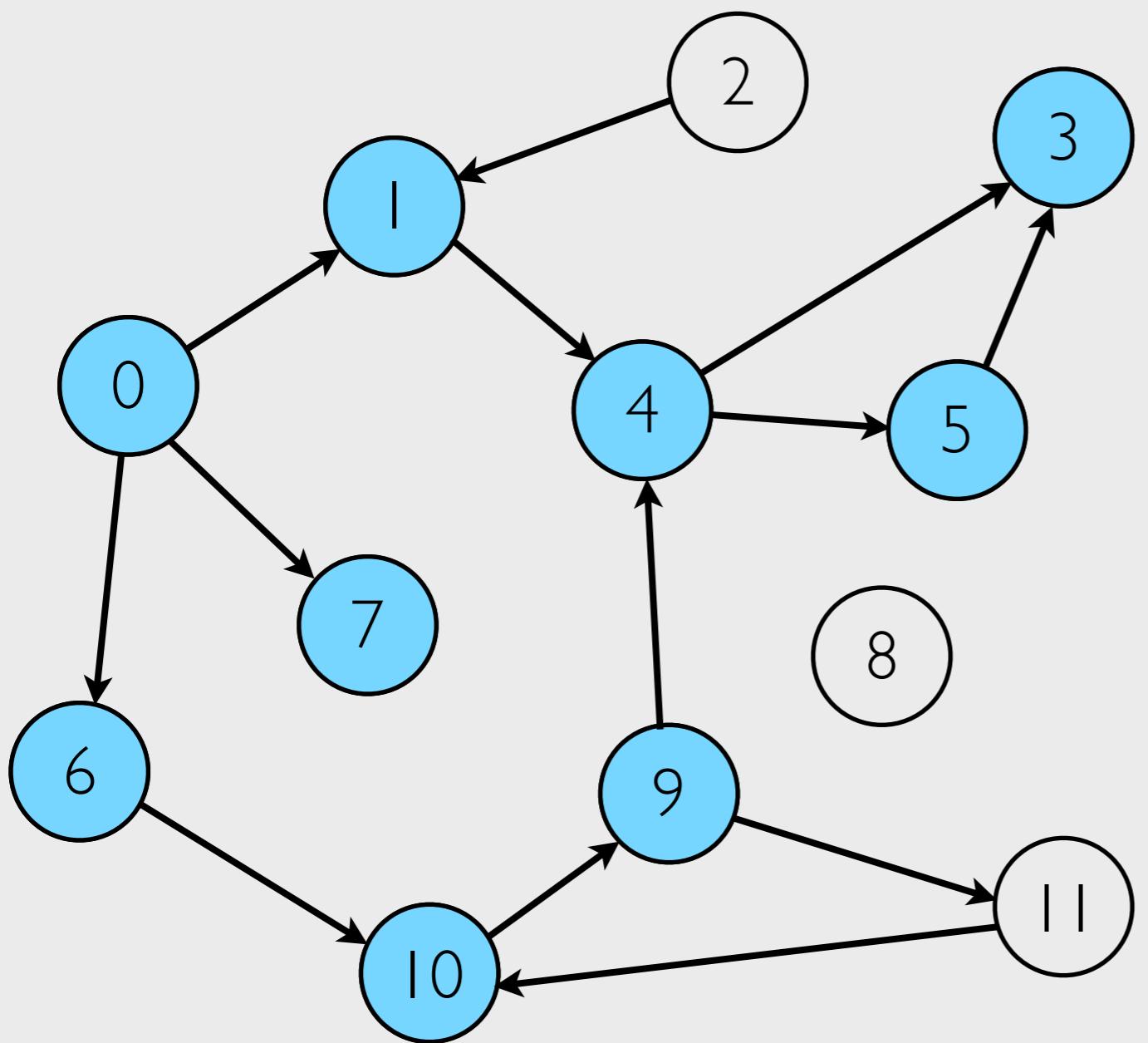


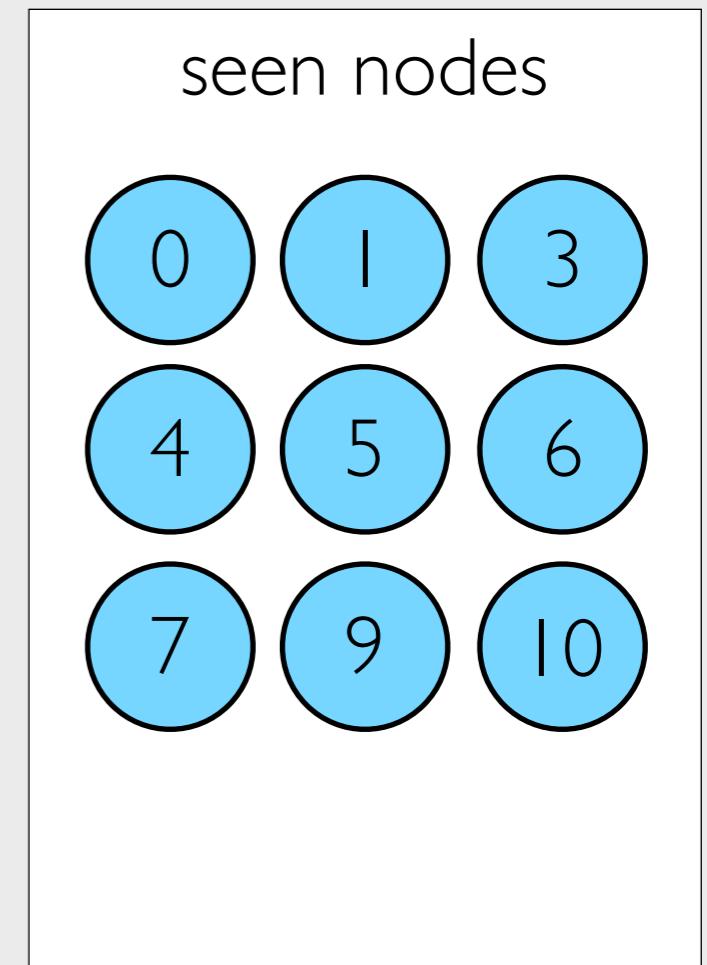
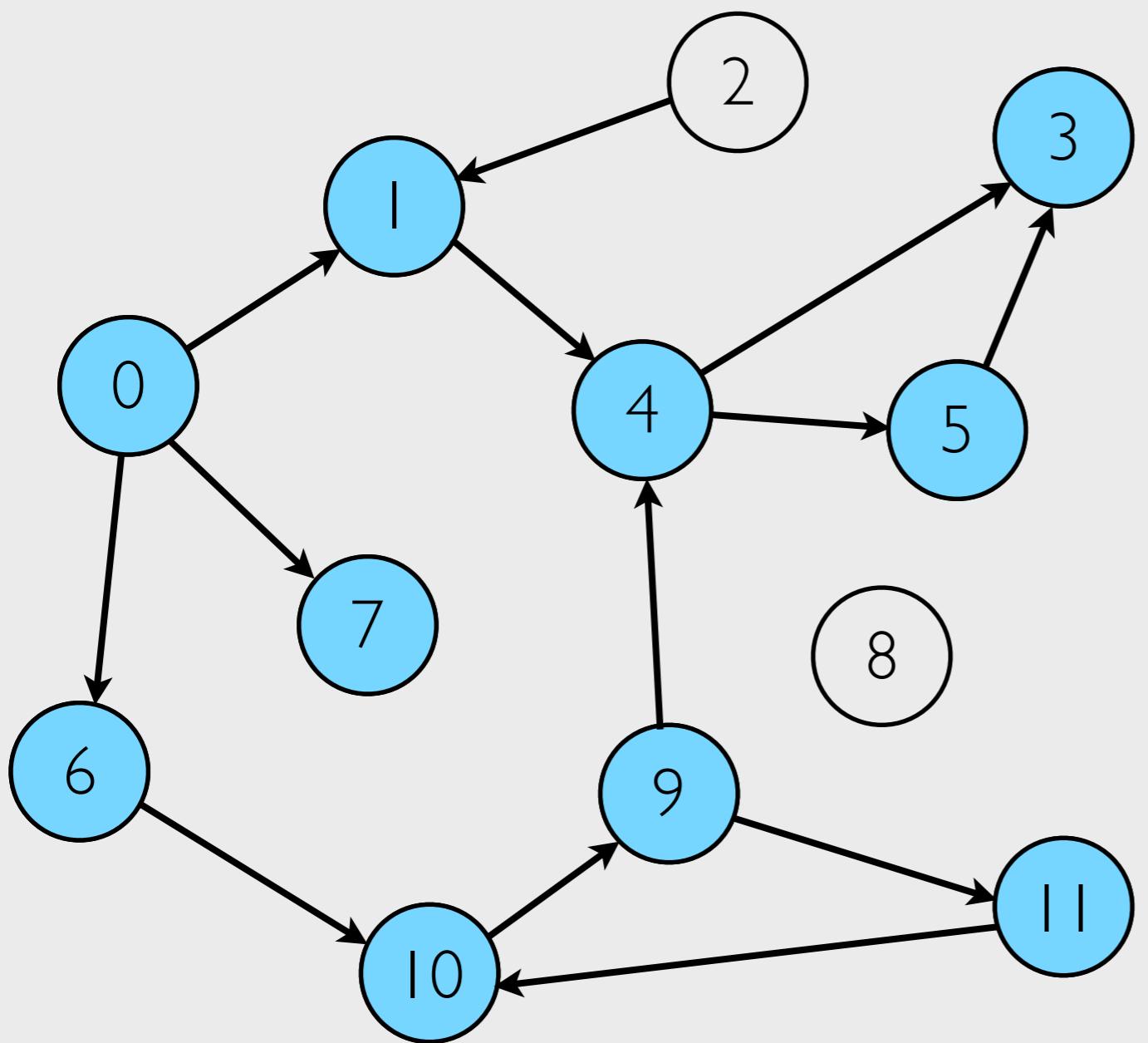


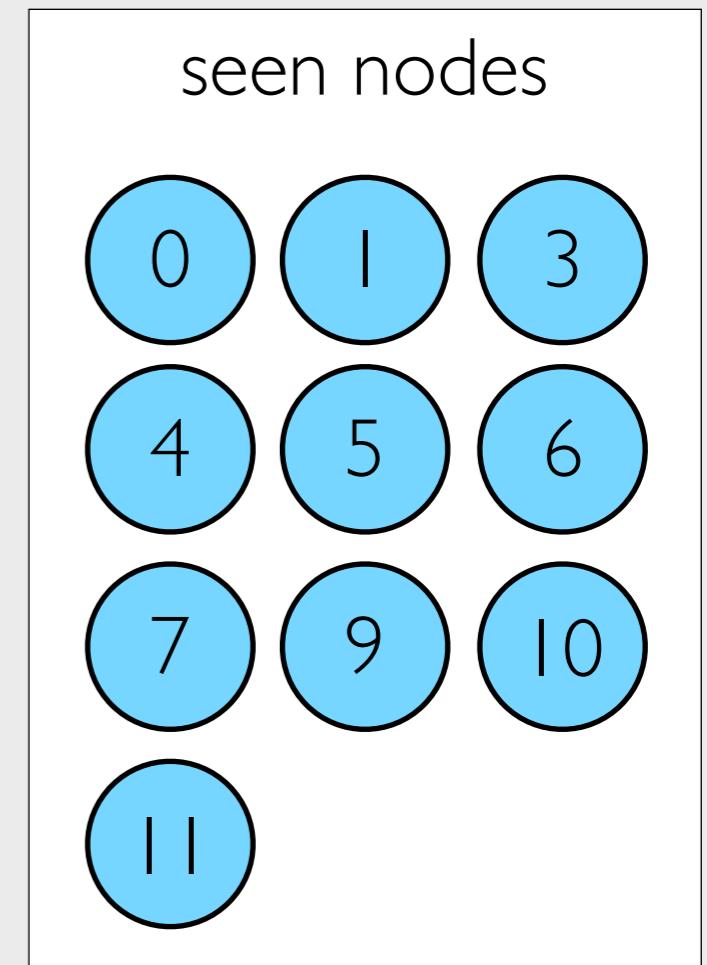
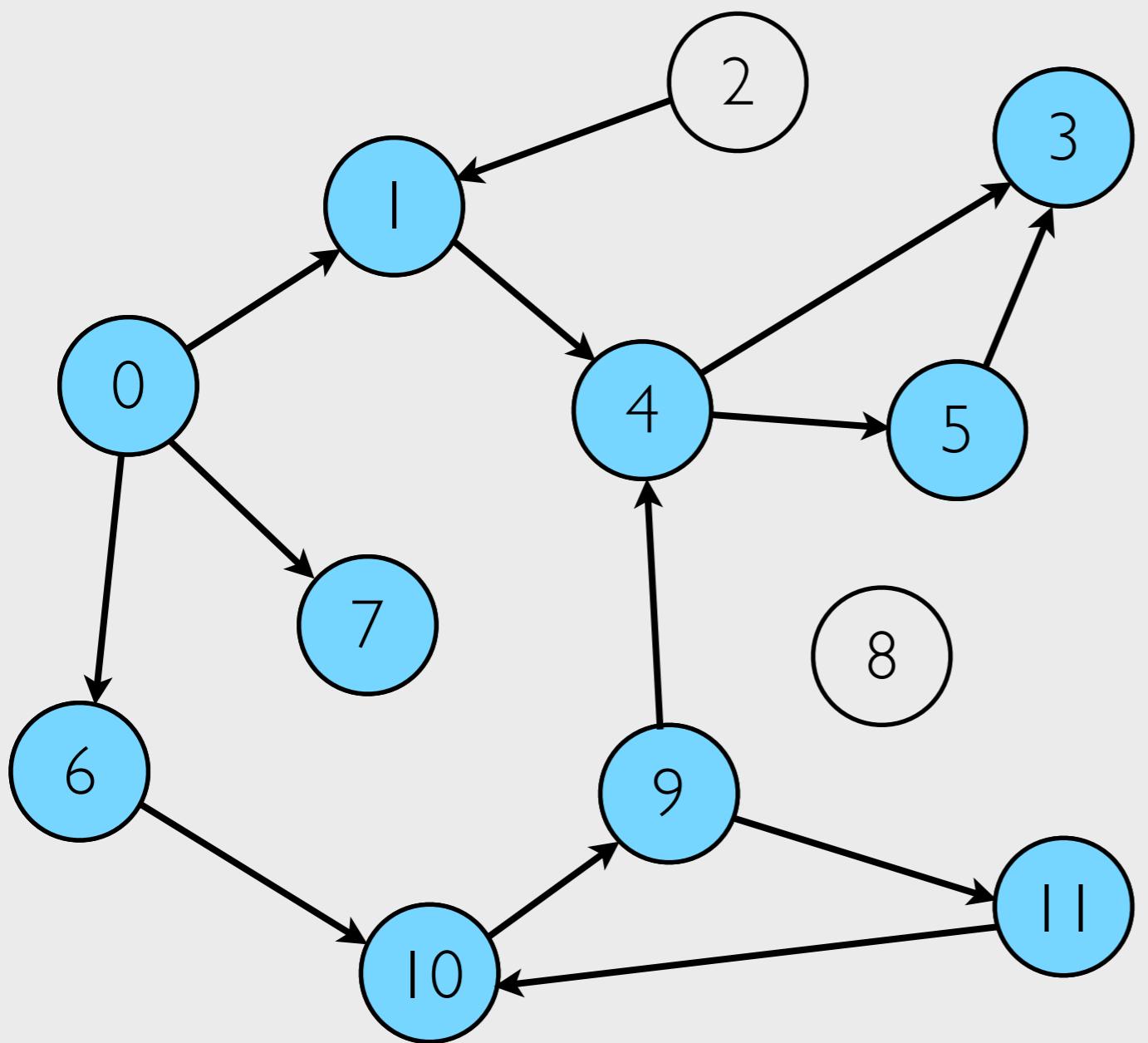


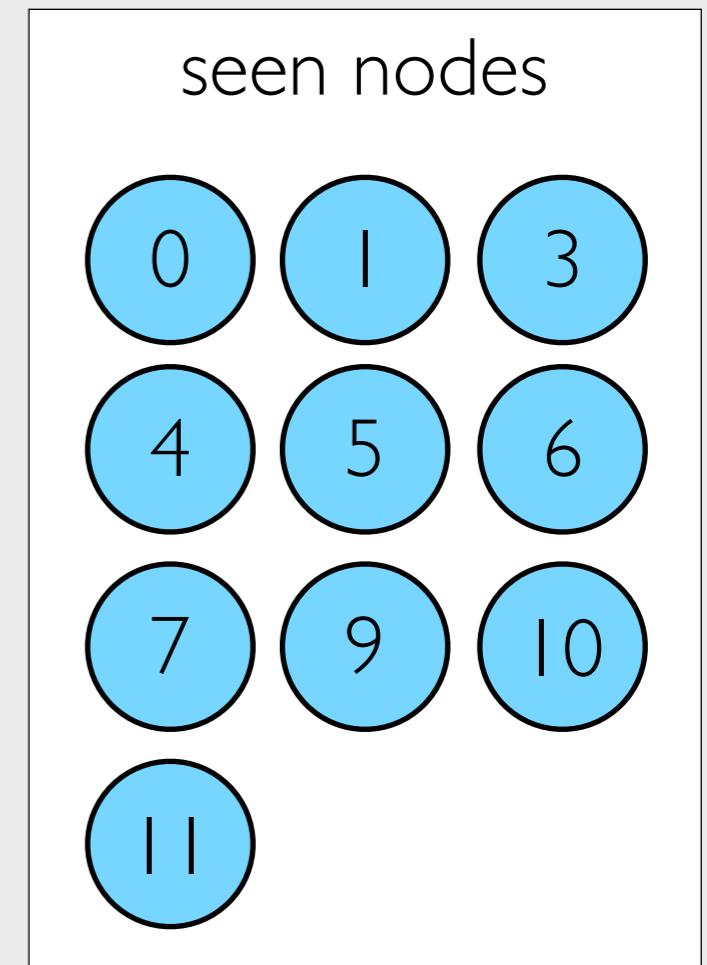
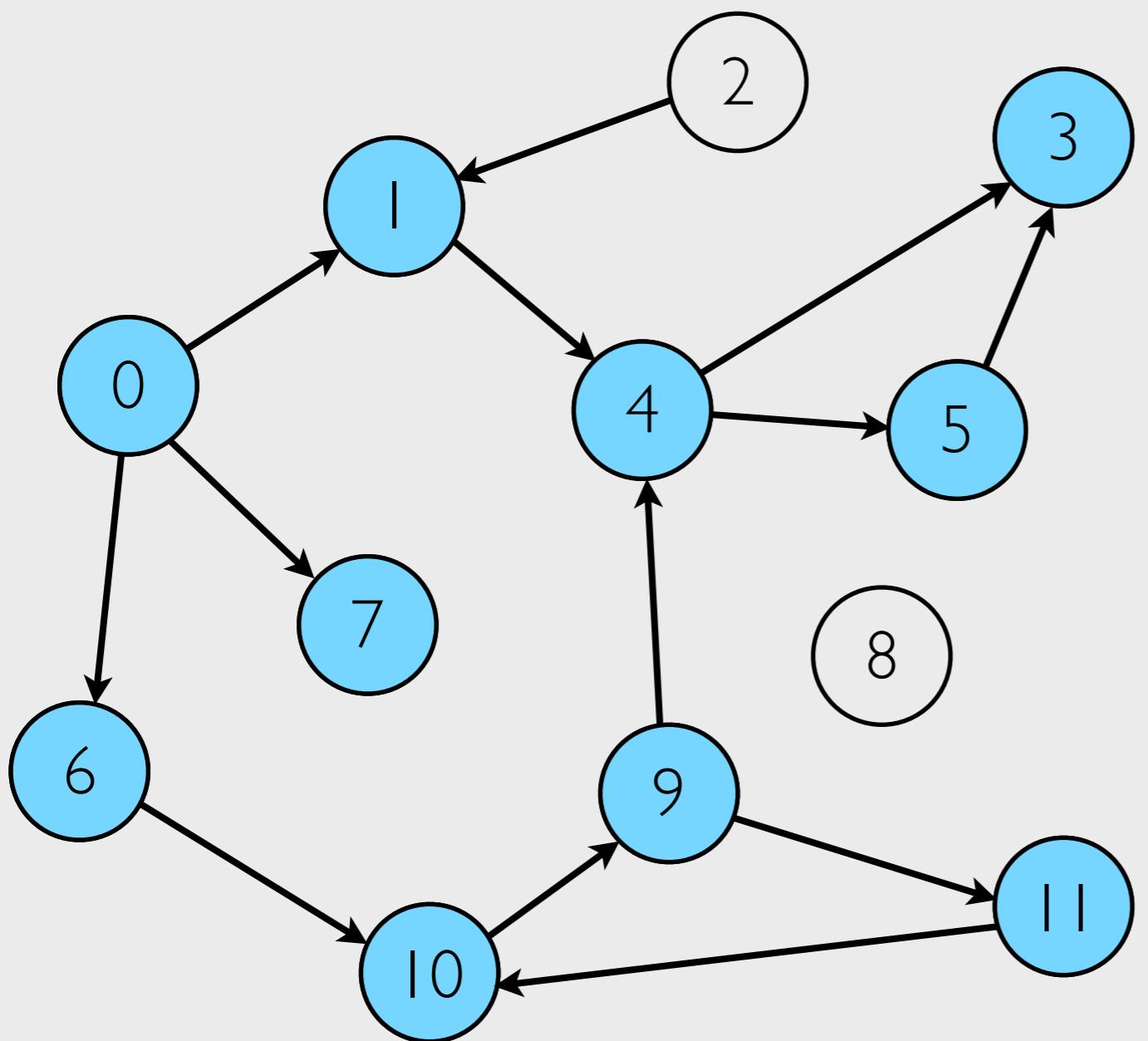


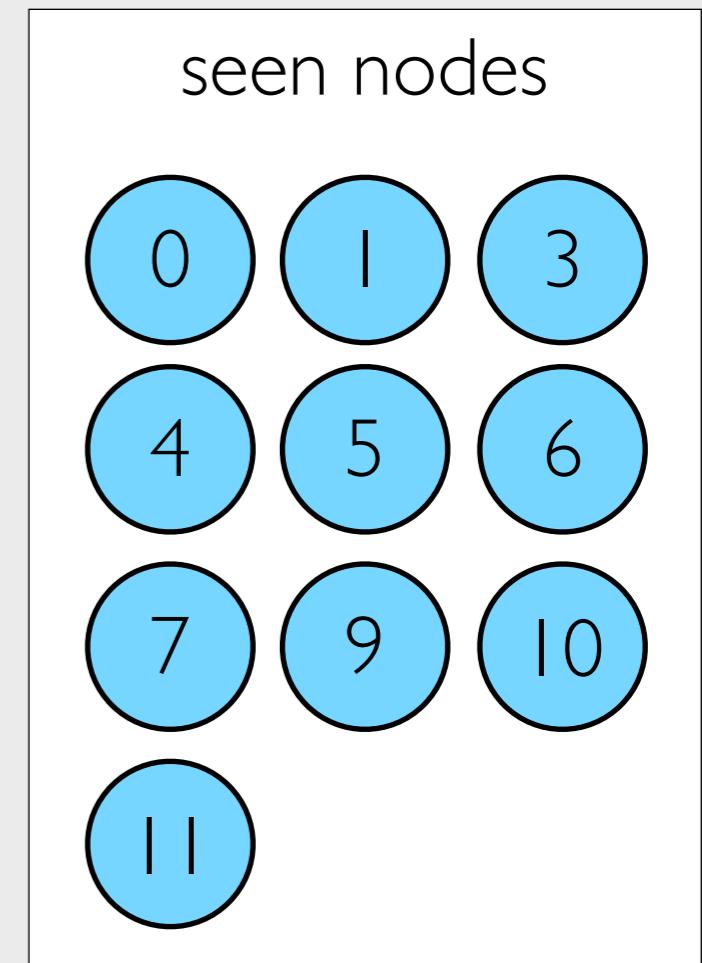
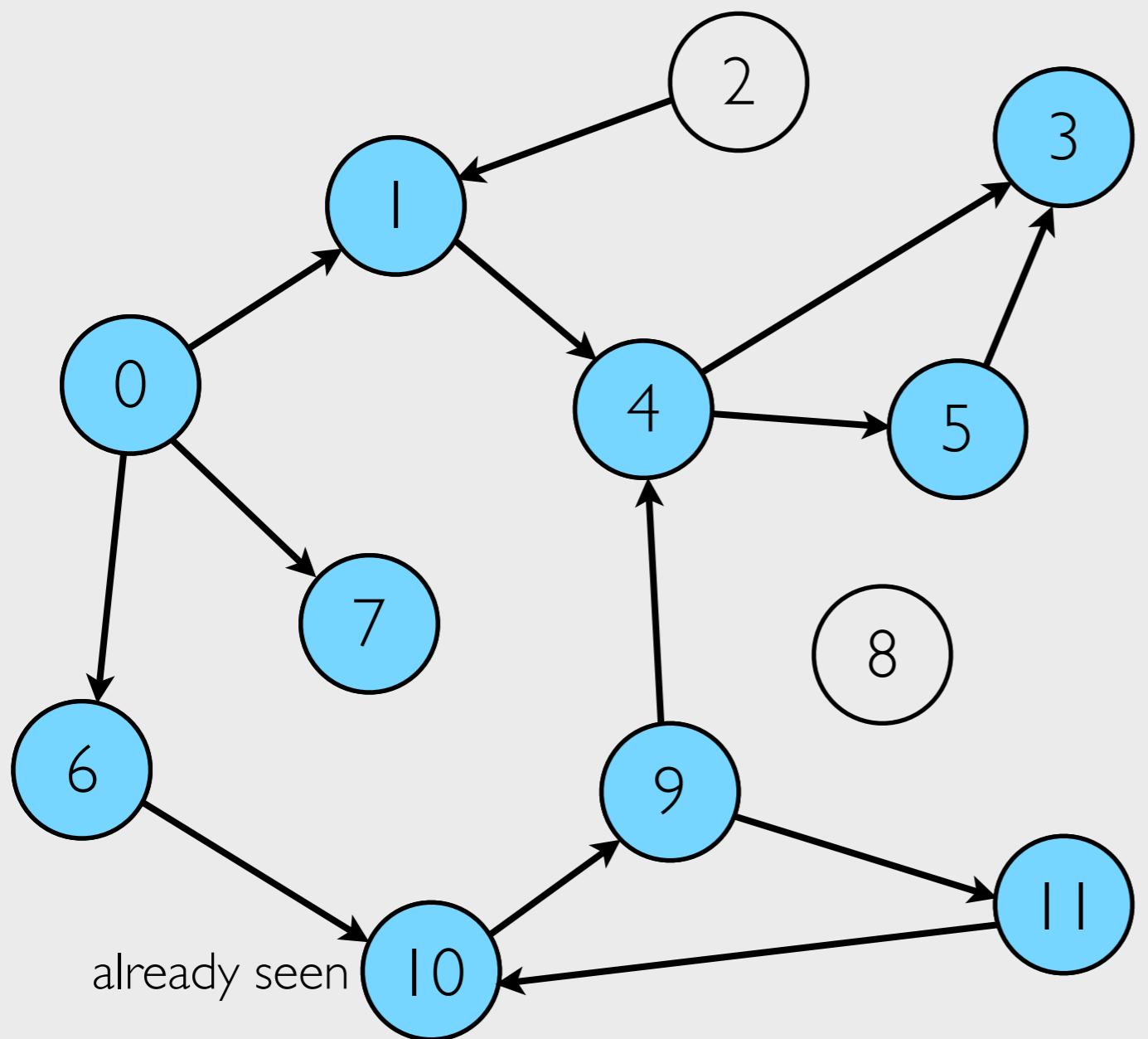


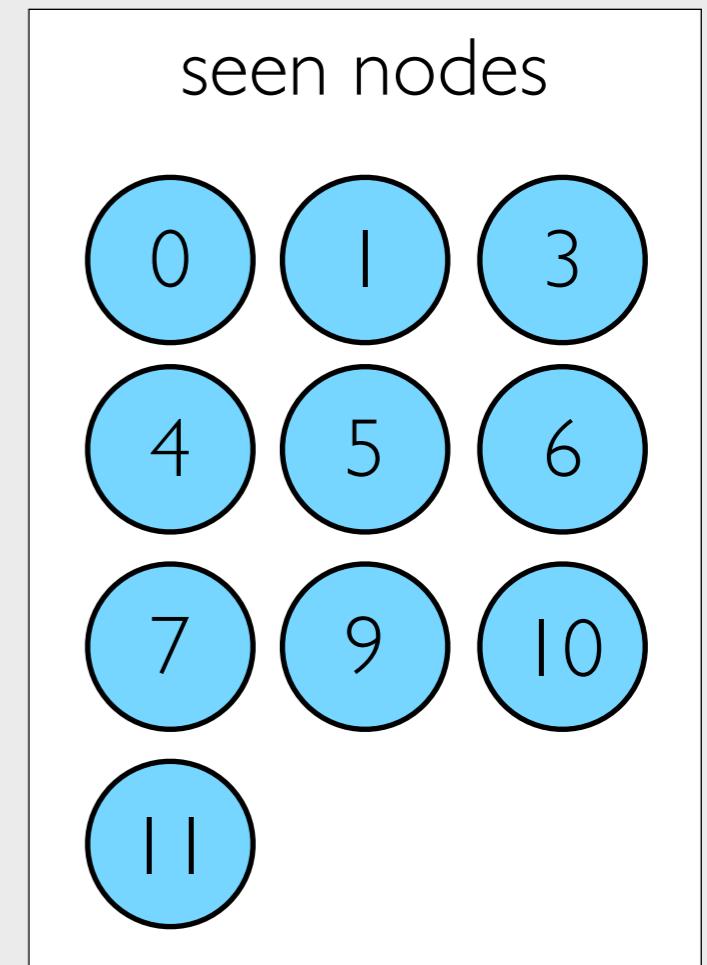
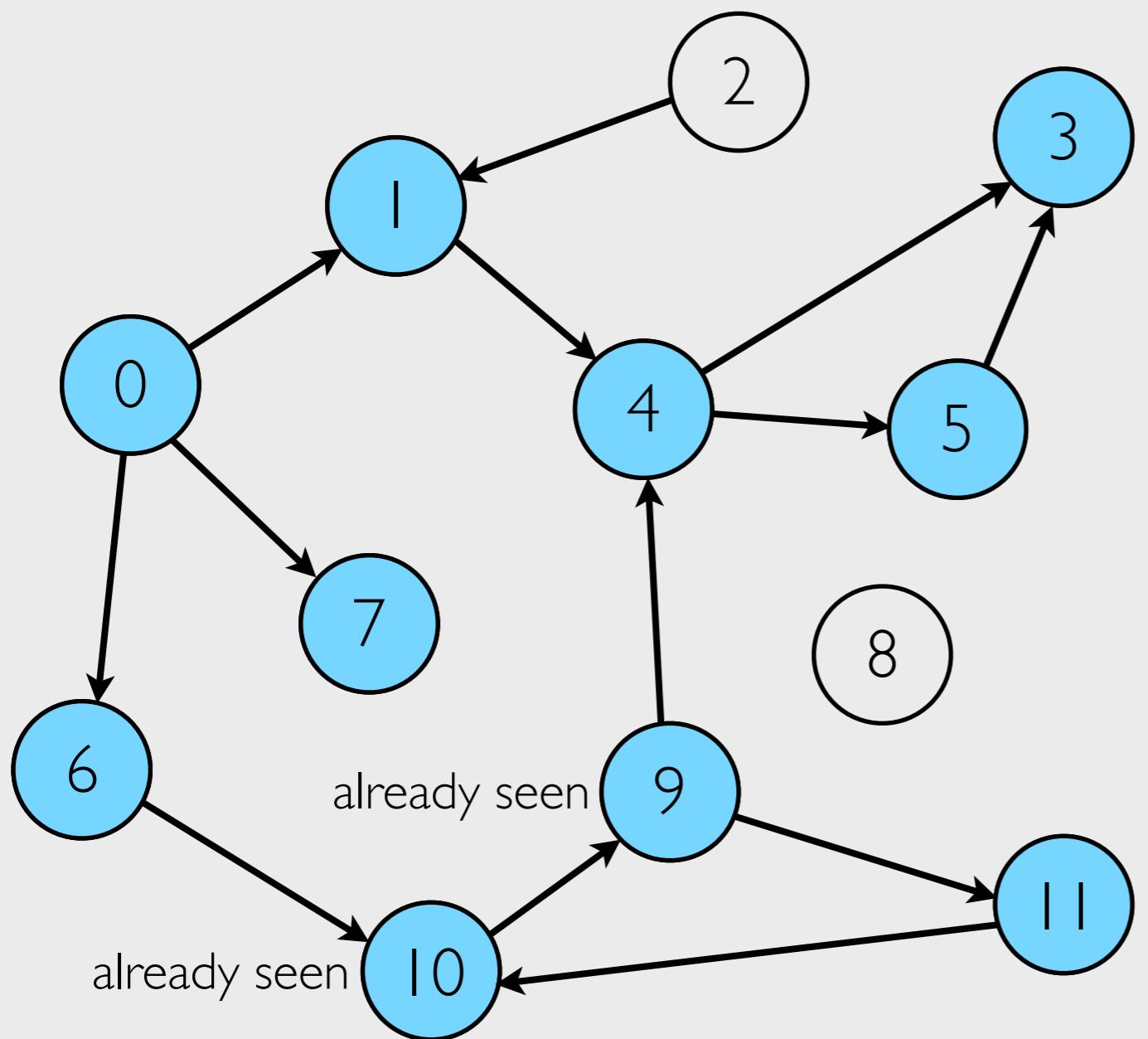


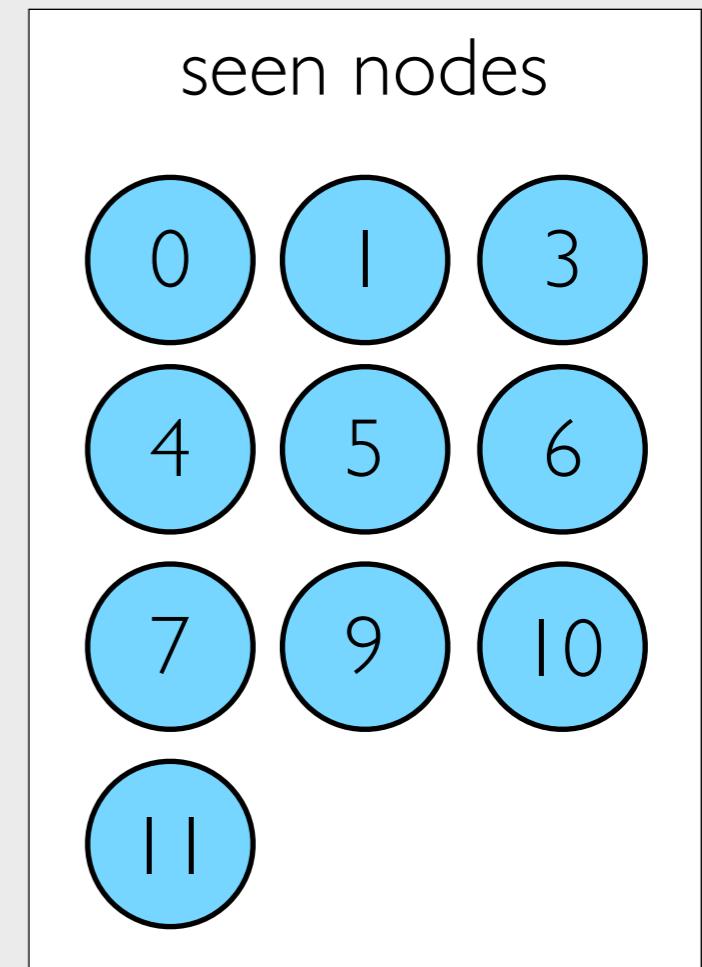
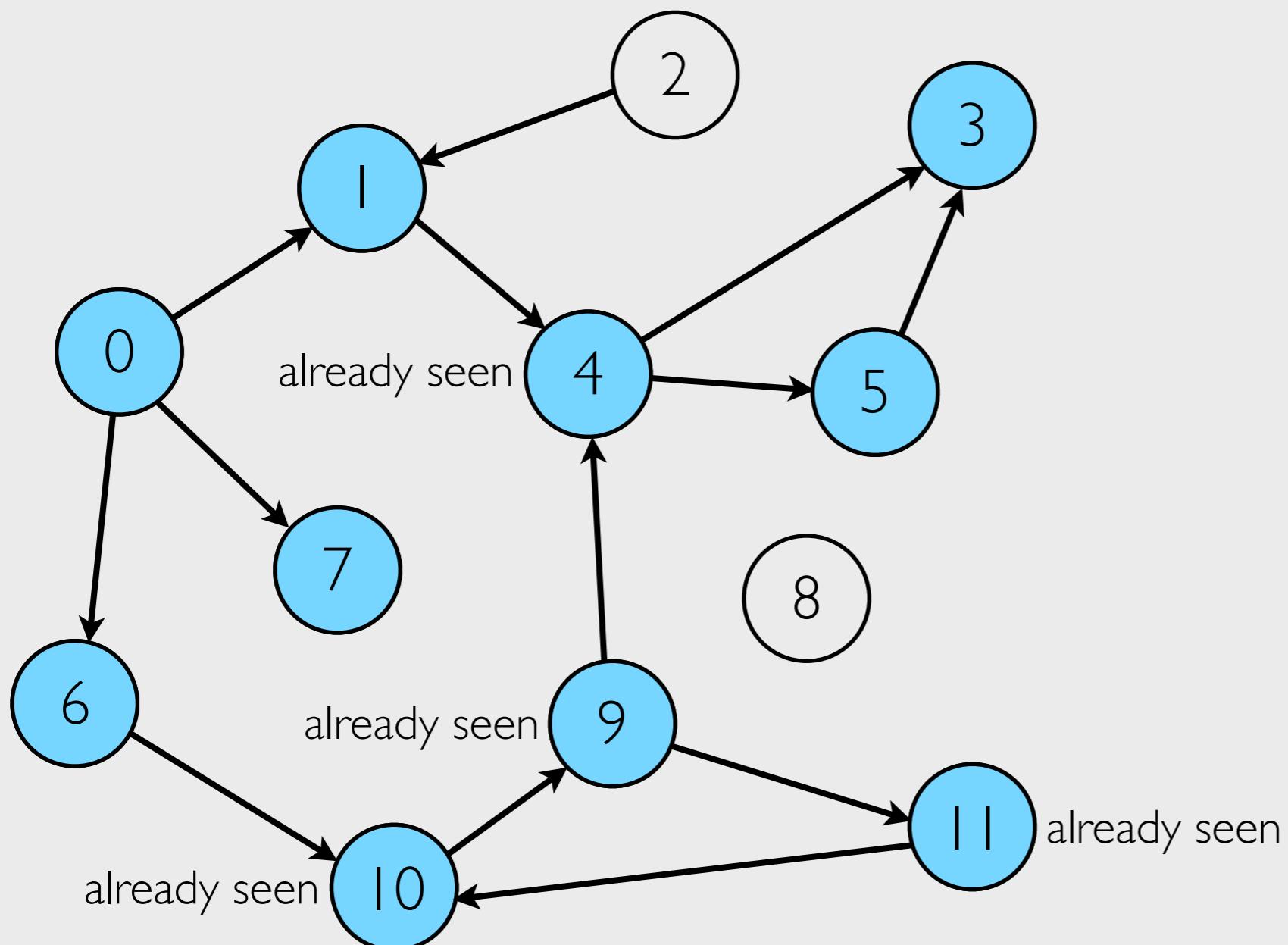


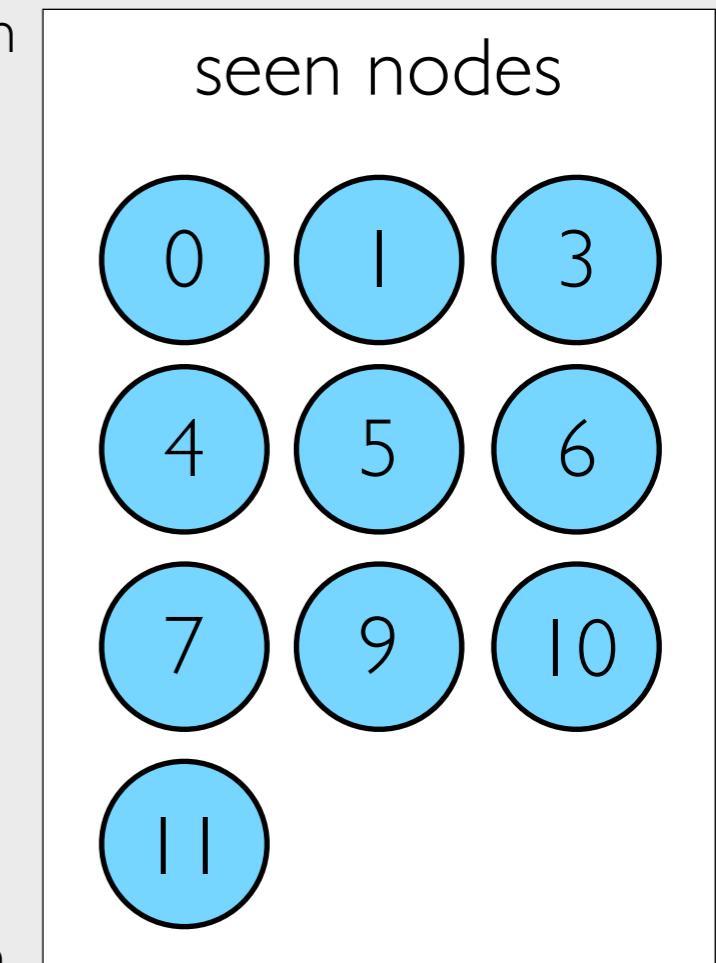
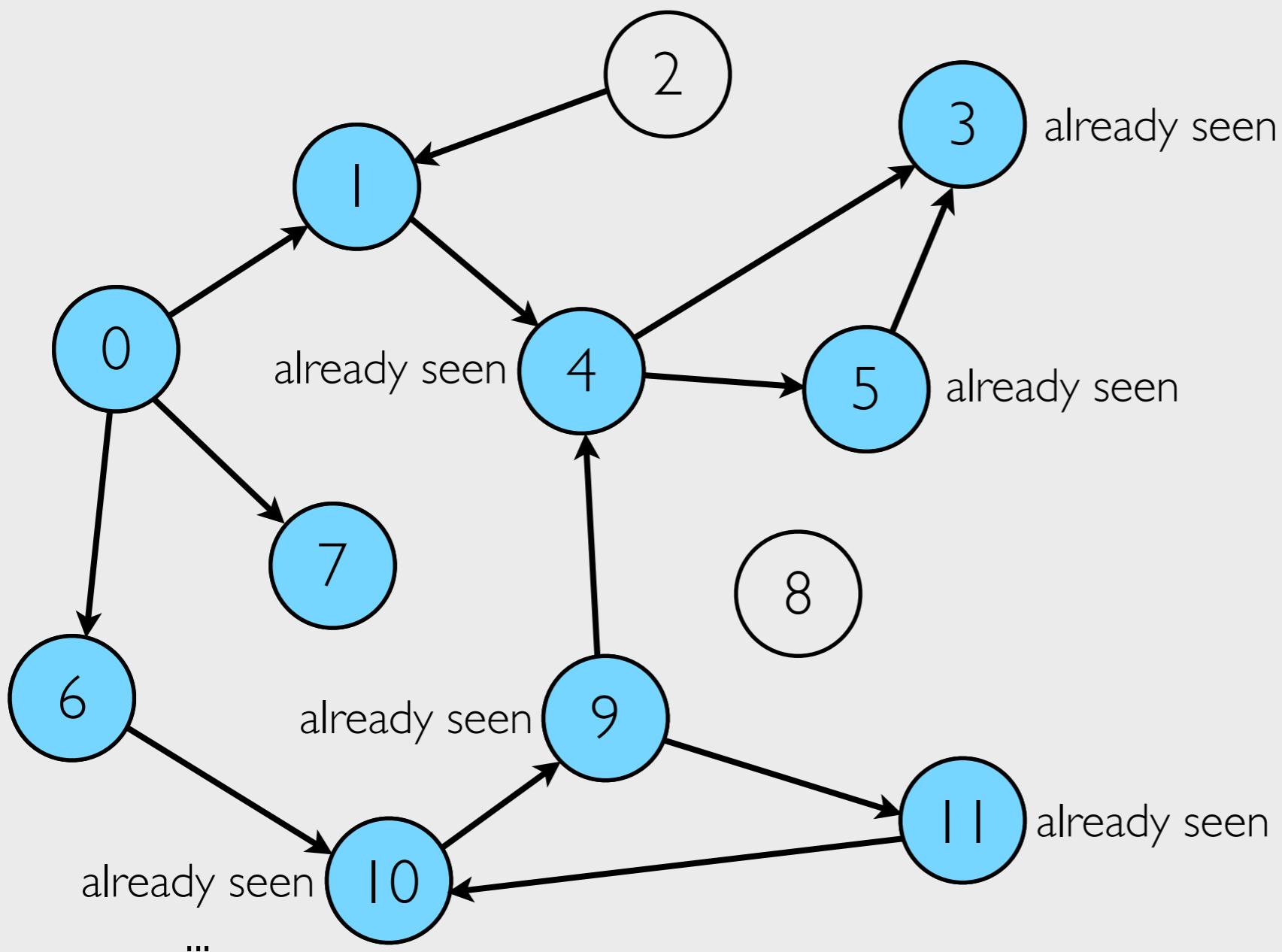


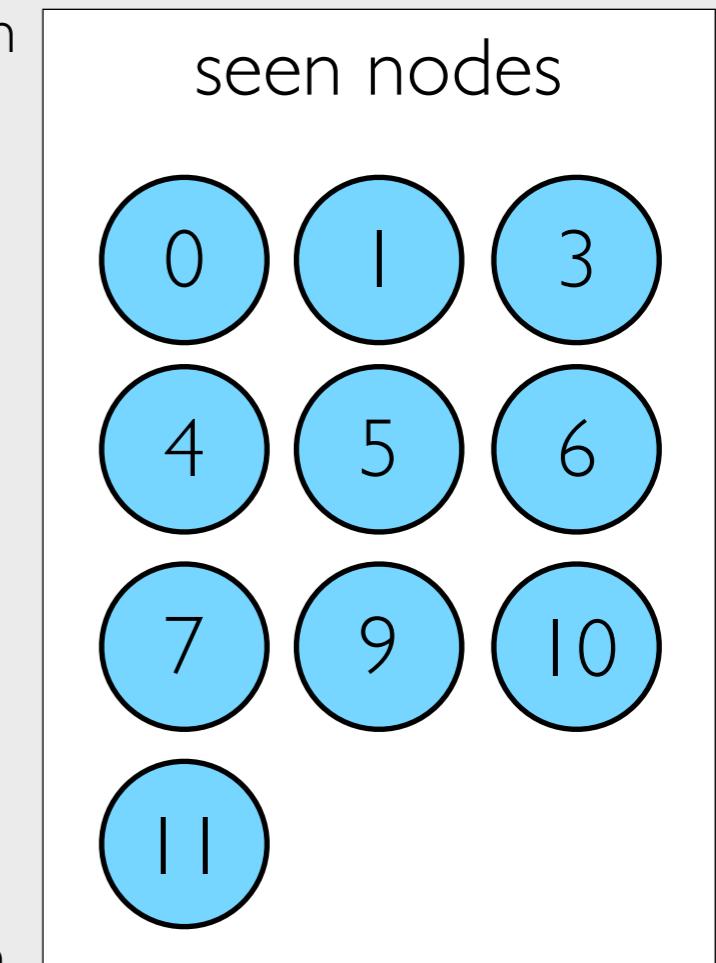
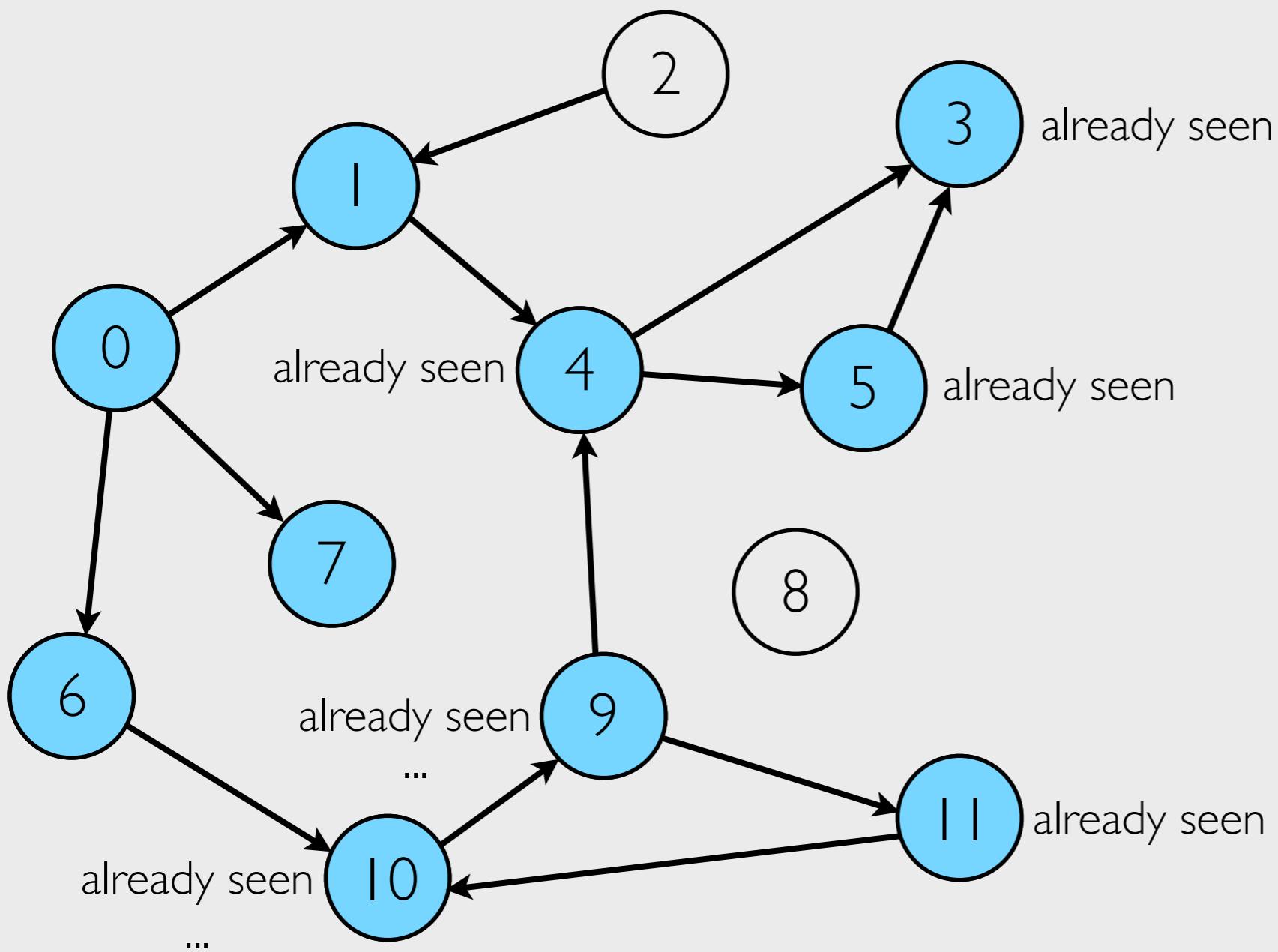


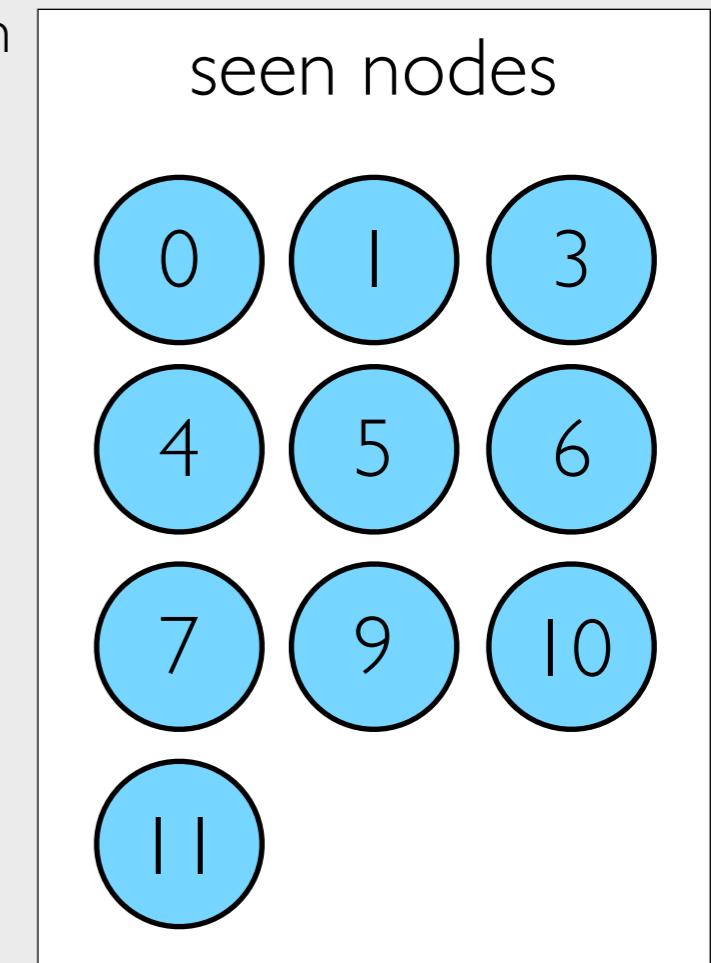
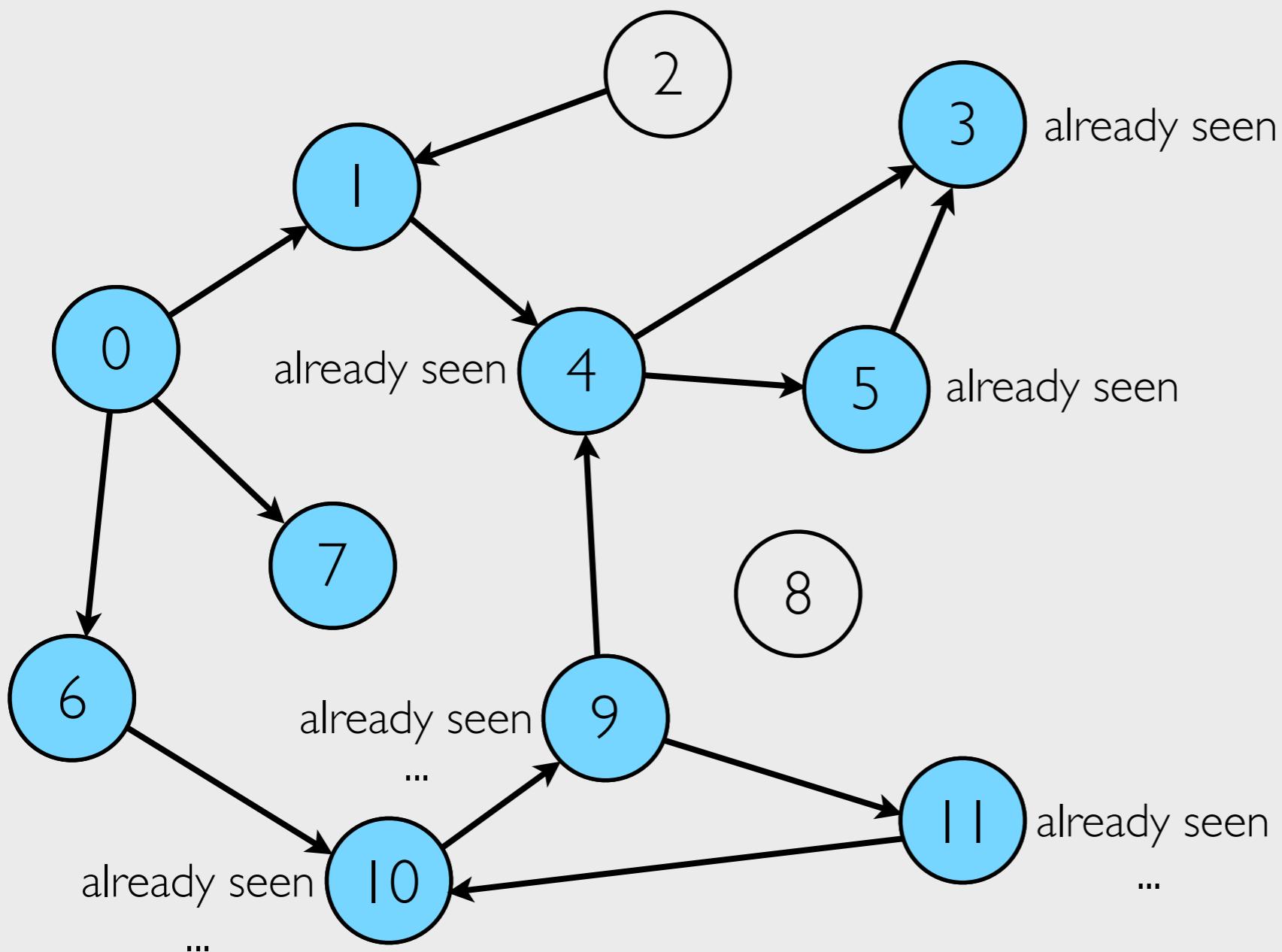




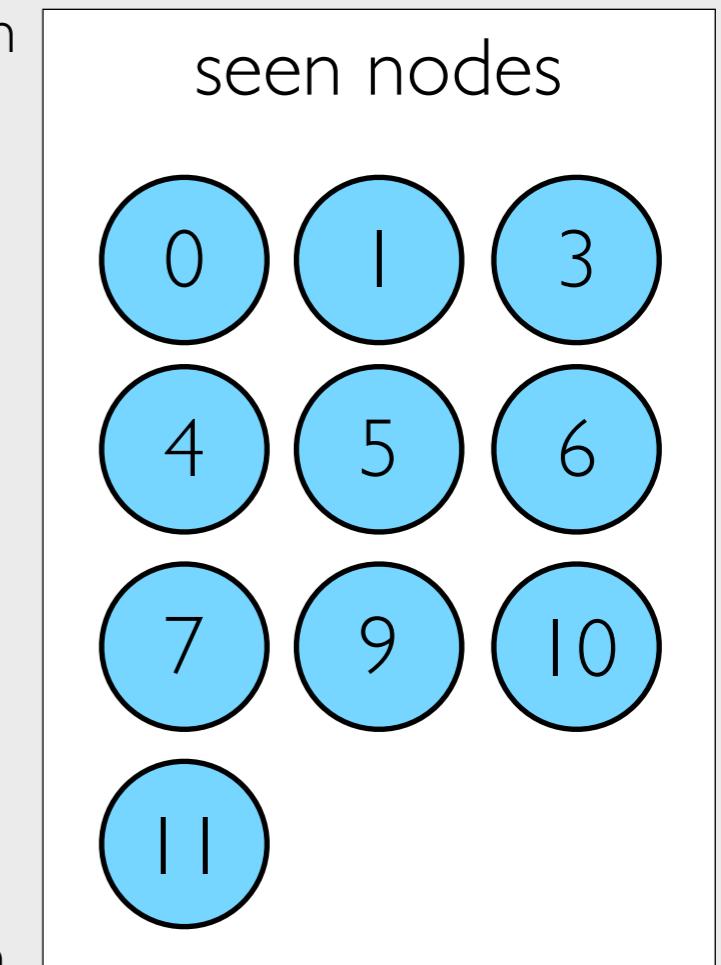
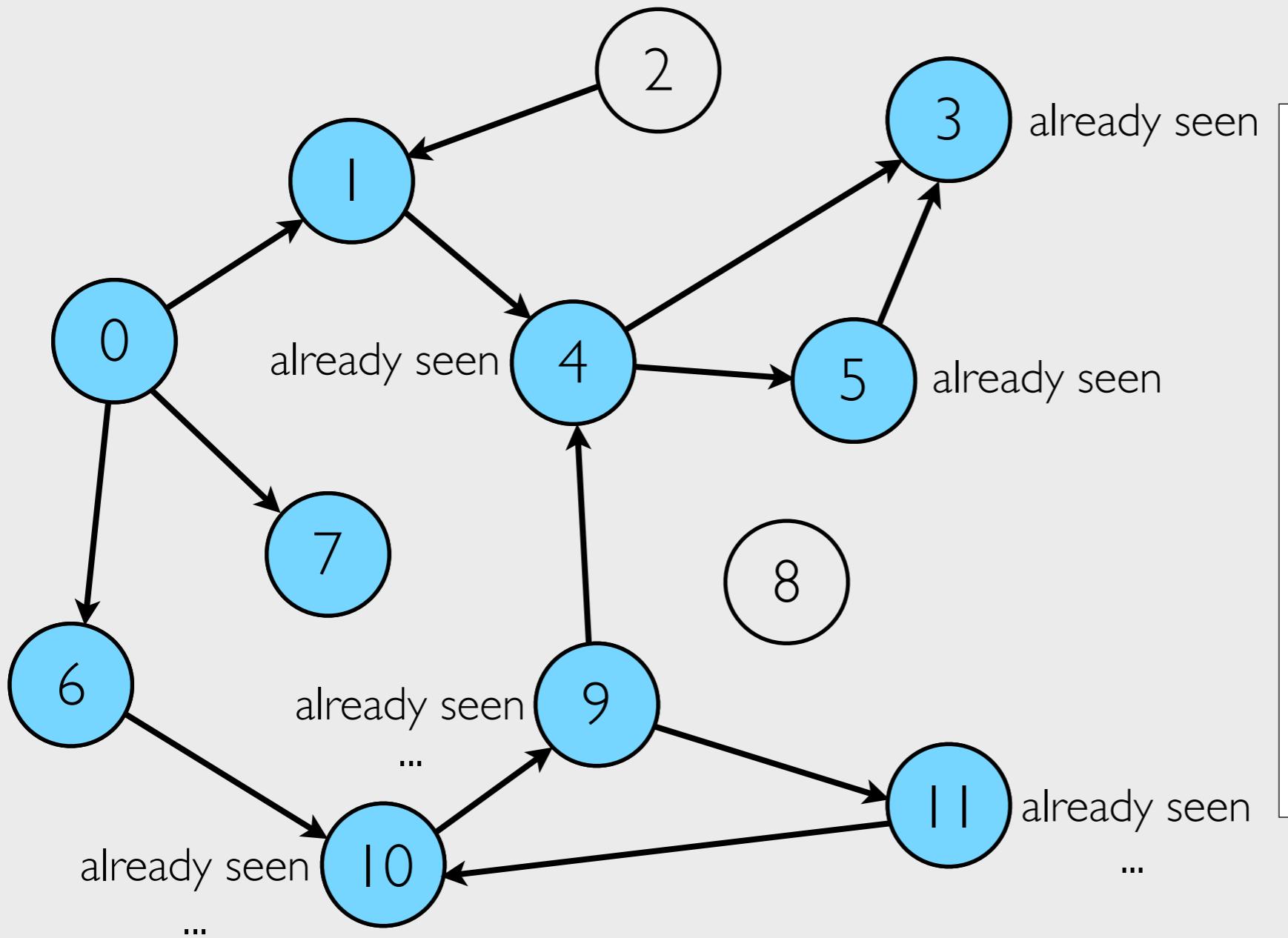






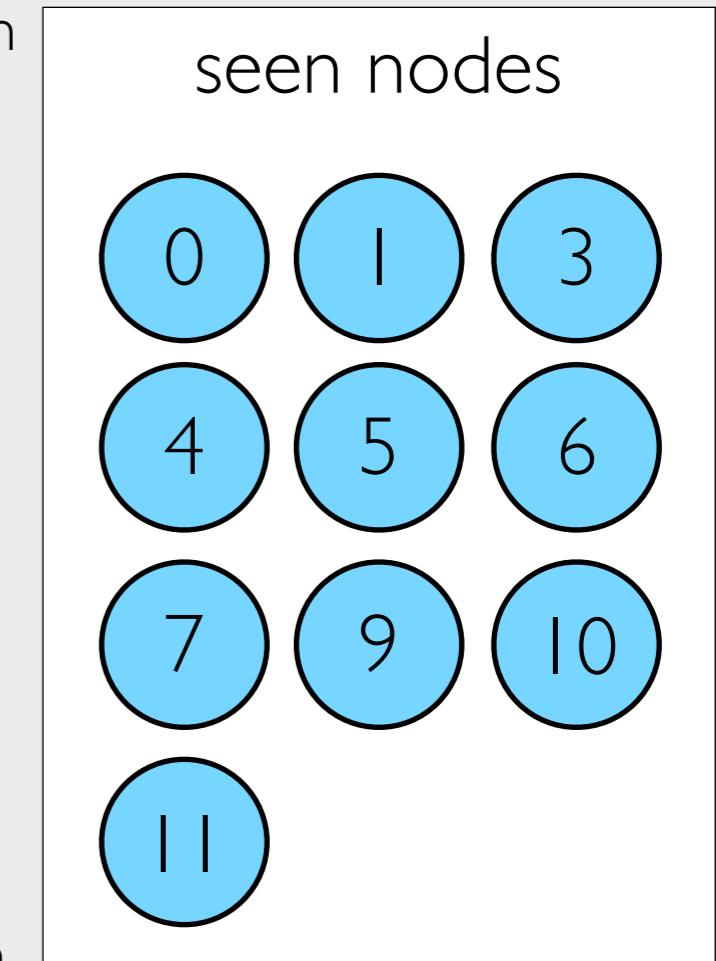
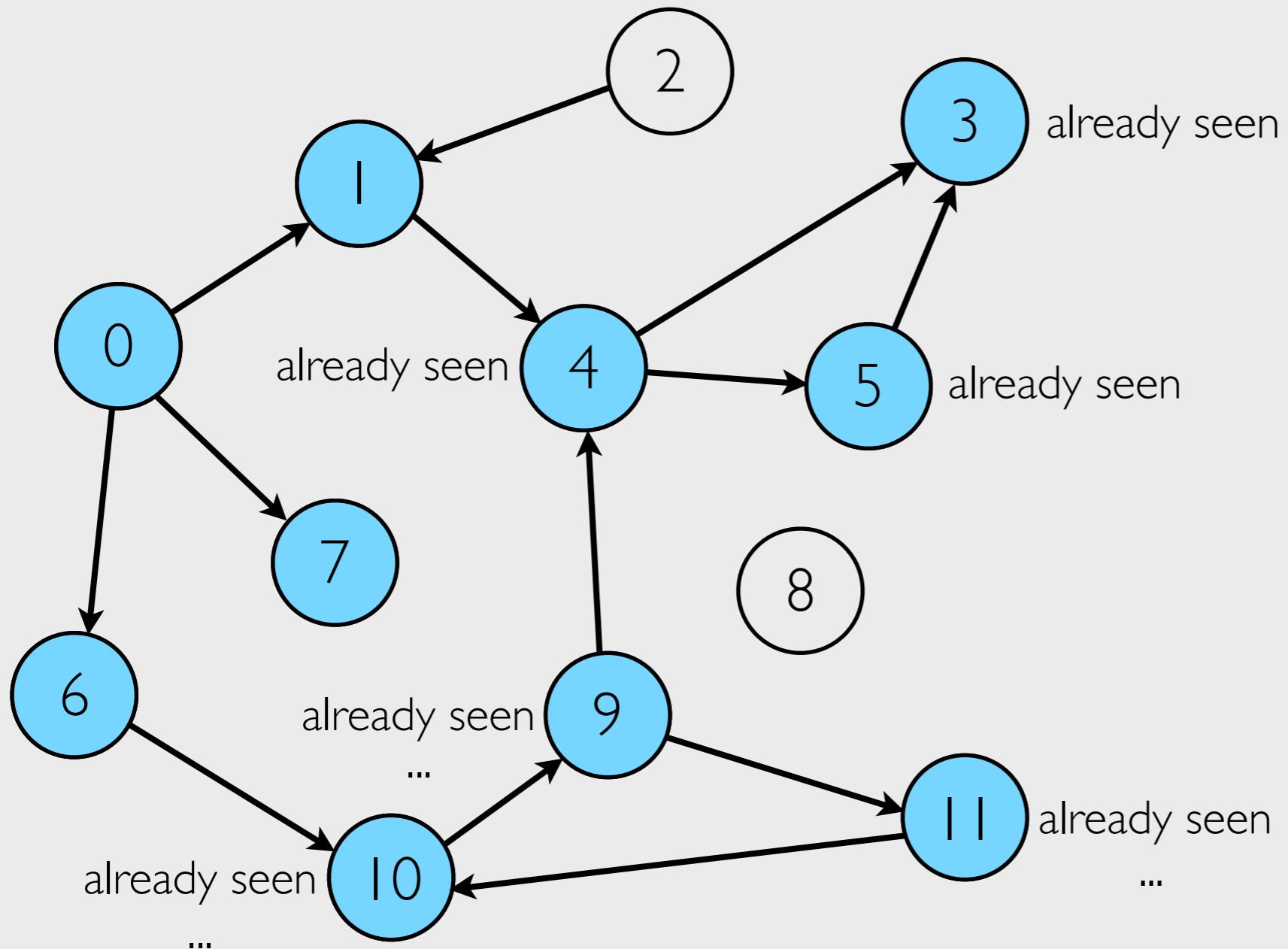


Events are updates that change an LVar's state



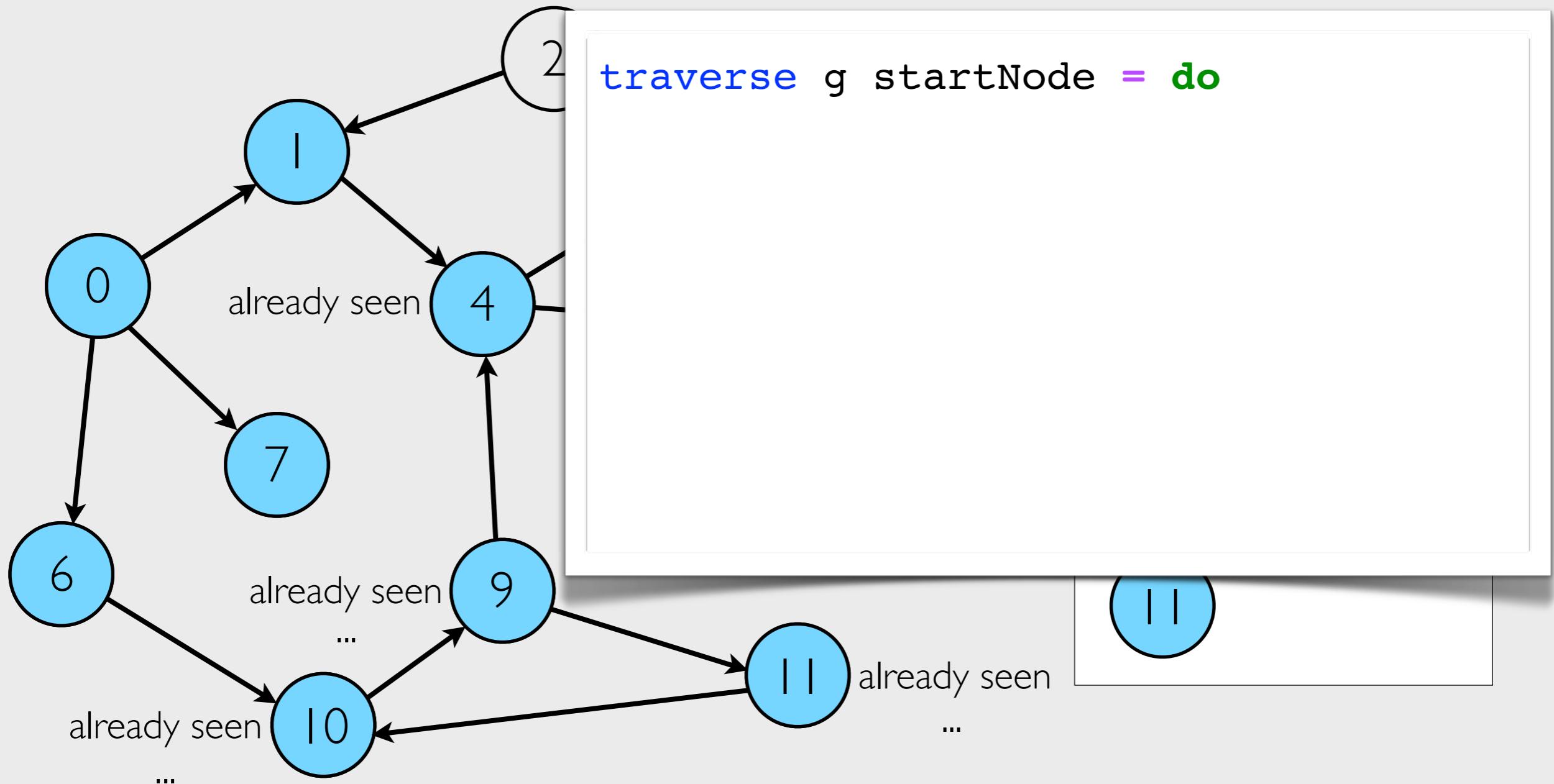
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Event handlers listen for events and launch callbacks in response



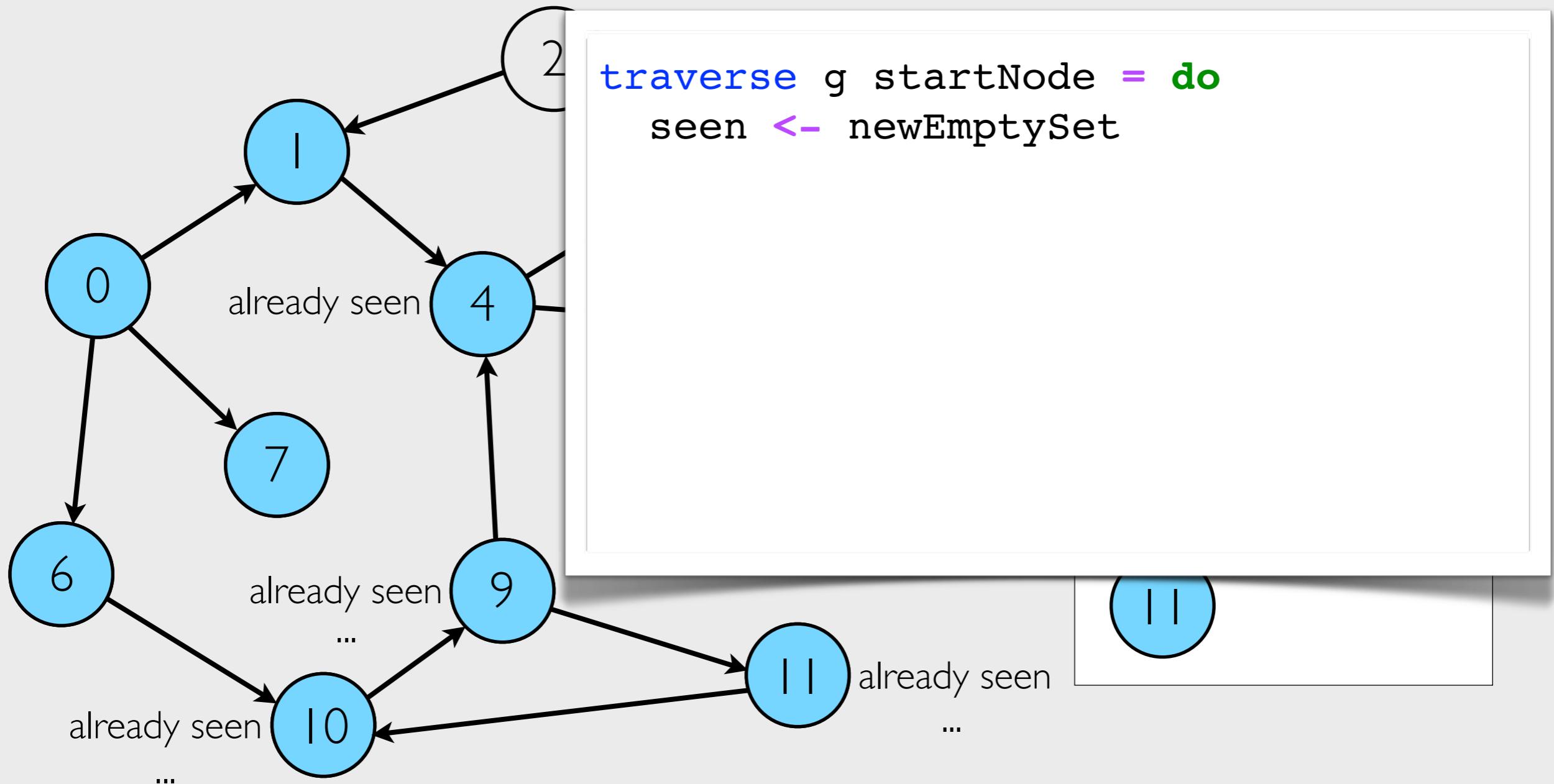
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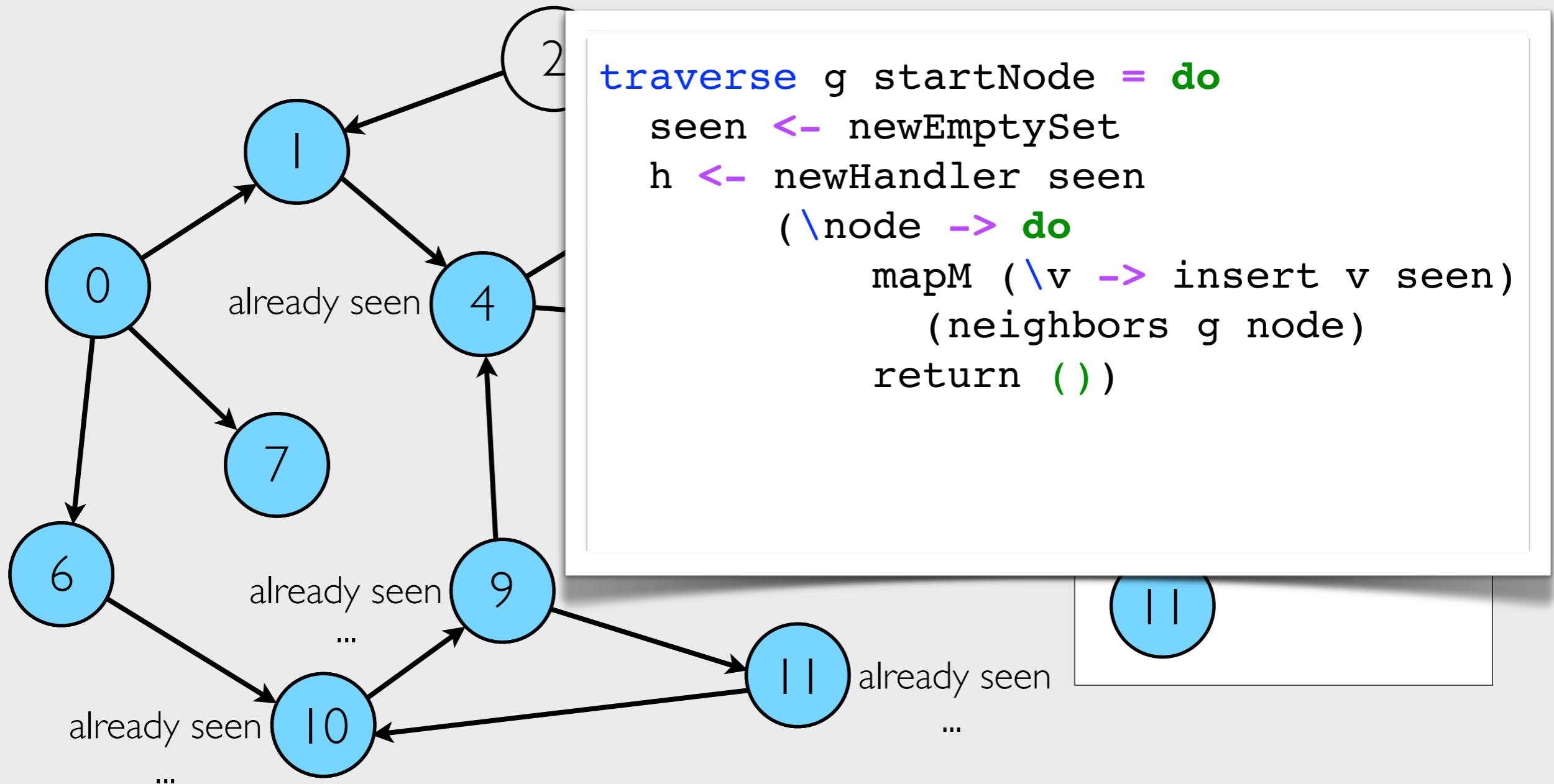
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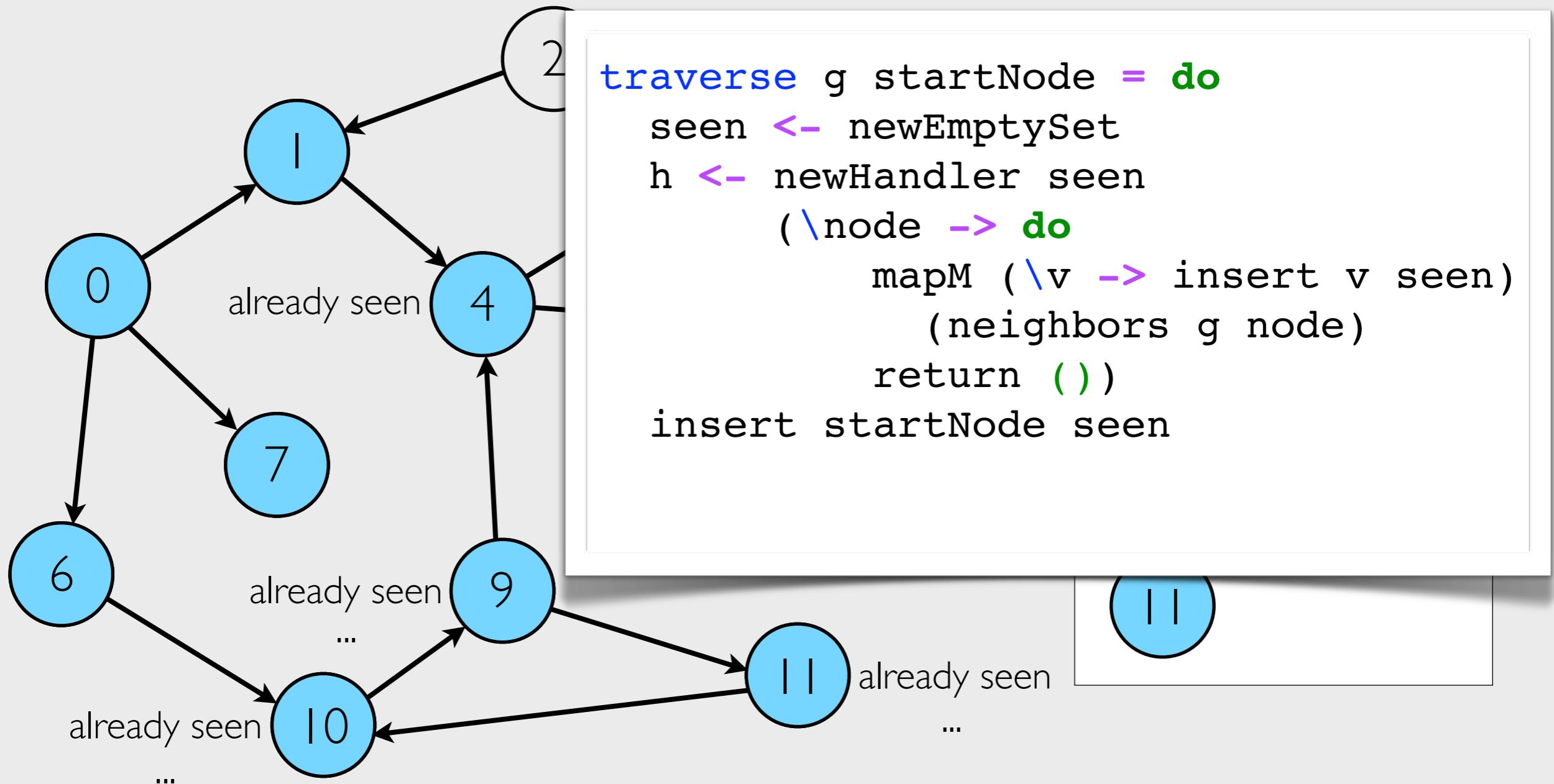
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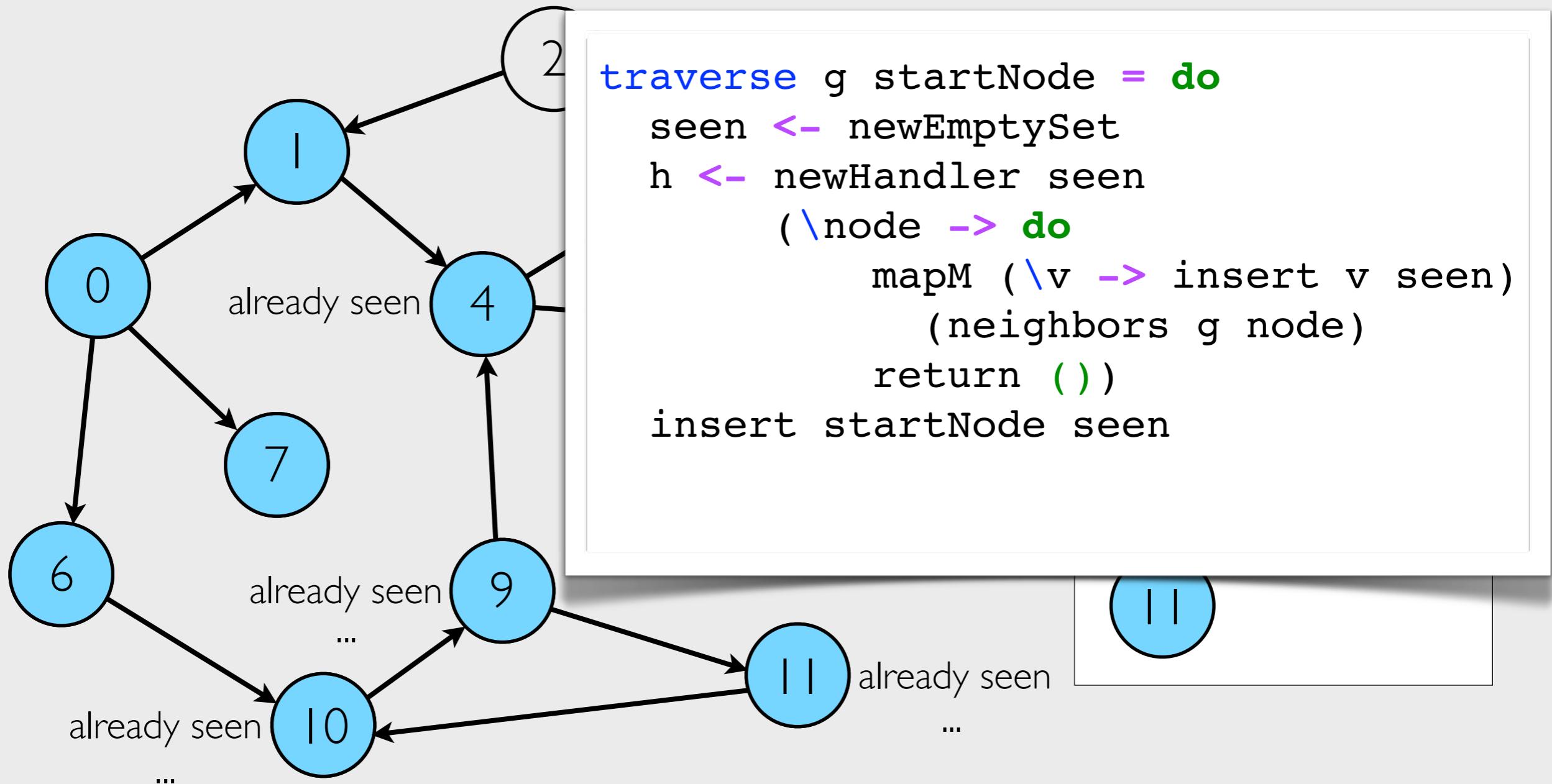
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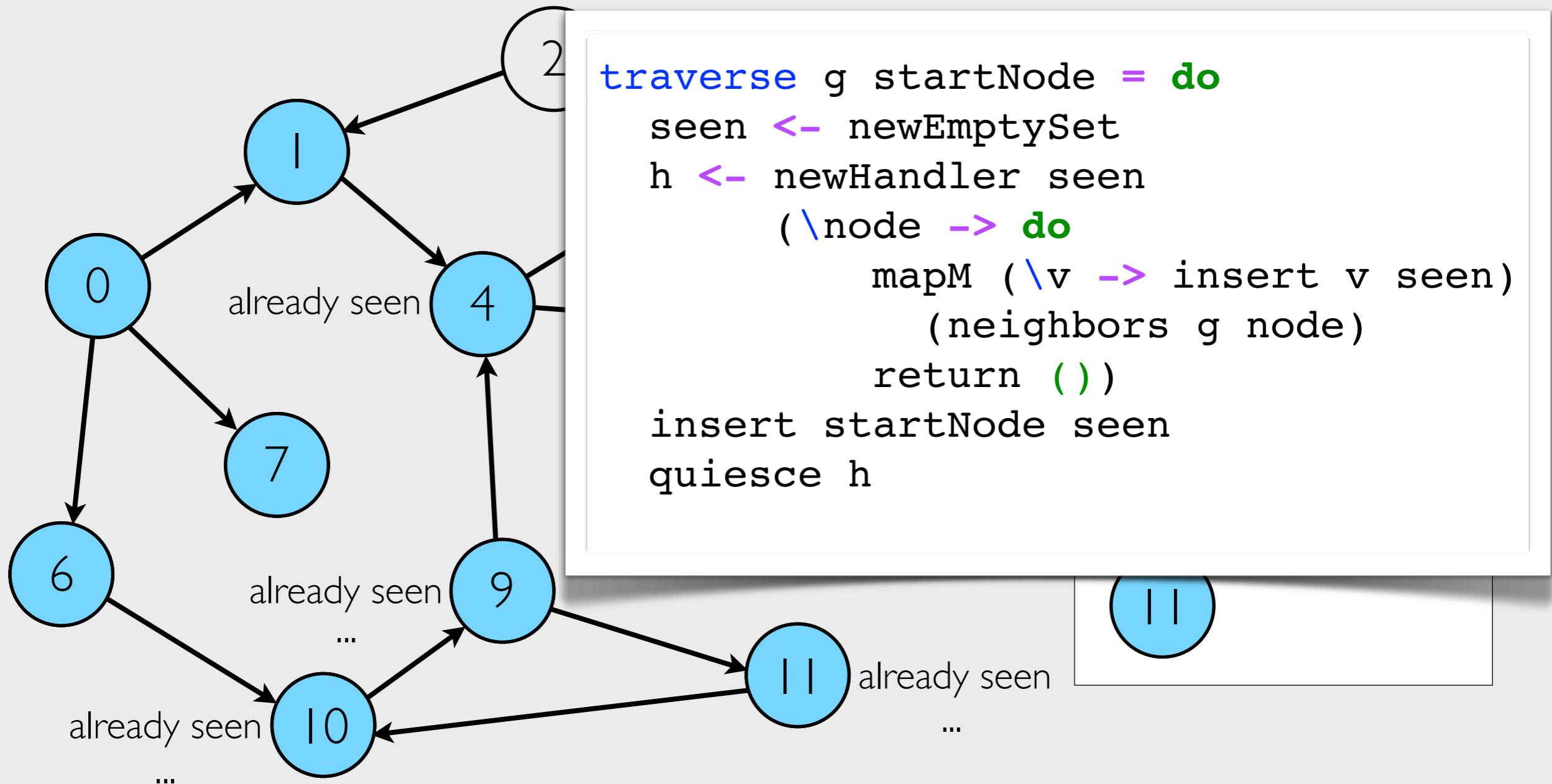
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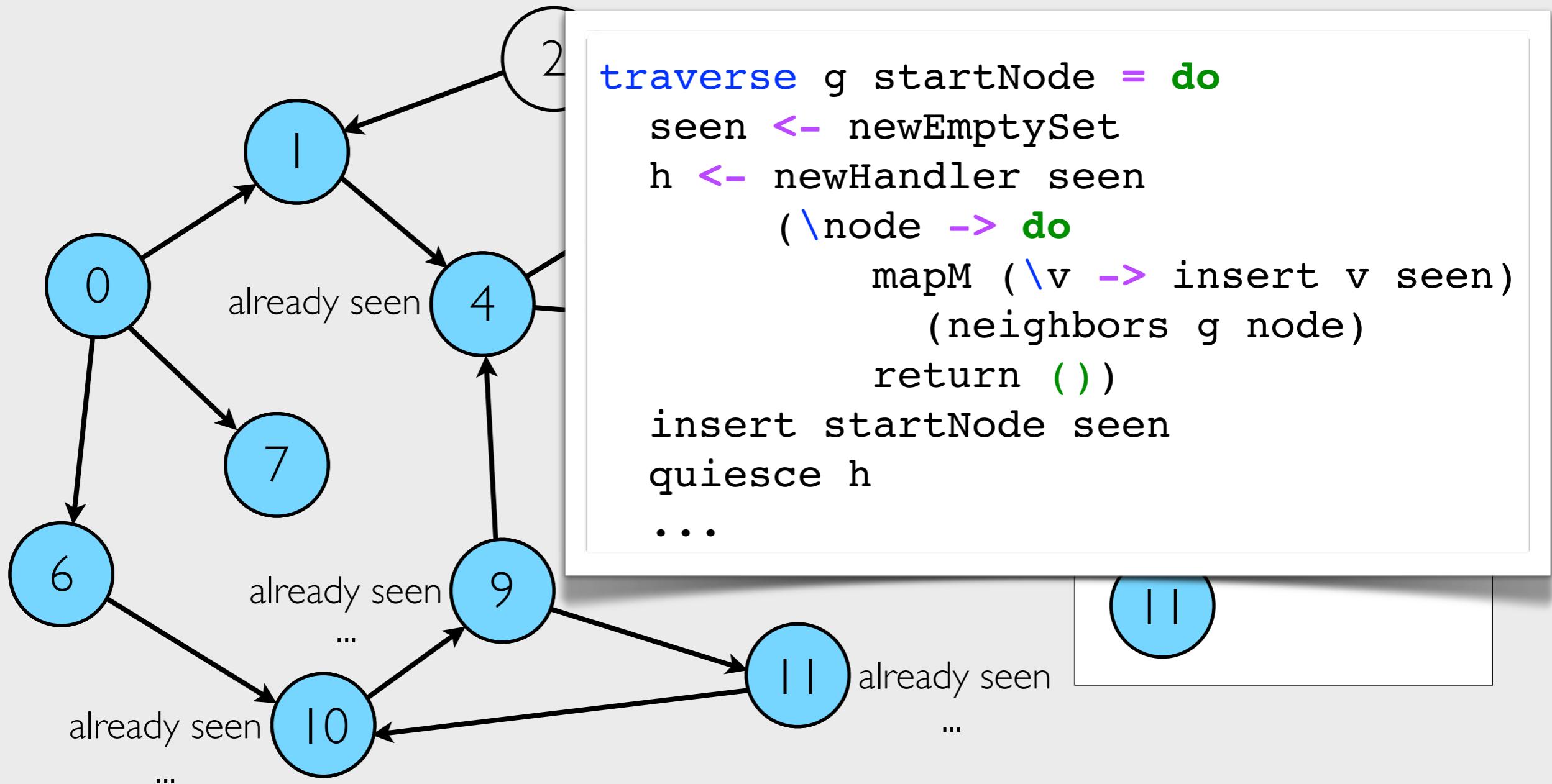
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freeze: exact non-blocking read

```
traverse g startNode = do
    seen <- newEmptySet
    h <- newHandler seen
    (\node -> do
        mapM (\v -> insert v seen)
            (neighbors g node)
        return ())
    insert startNode seen
    quiesce h
    ...
```

freeze: exact non-blocking read

Attempts to write to a frozen LVar raise a write-after-freeze exception

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Theorem 1 (Quasi-Determinism). If $\sigma \longrightarrow^* \sigma'$ and $\sigma \longrightarrow^* \sigma''$, **do**
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1. $\sigma' = \sigma''$ up to a permutation on locations π , or
2. $\sigma' = \text{error}$ or $\sigma'' = \text{error}$.

[POPL '14] insert v seen)

(neglecting node)

return ()

insert startNode seen

quiesce h

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[(Book,1),(Shoes,1)]

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~~[(B,1)]~~

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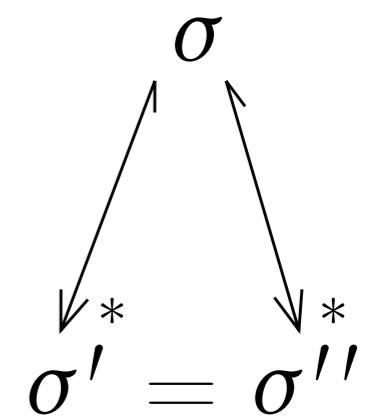
[(S,1)]

aka “ $LVars$ ”

Lattice-based data structures
are a general and practical unifying abstraction
for deterministic and quasi-deterministic
parallel and distributed programming.



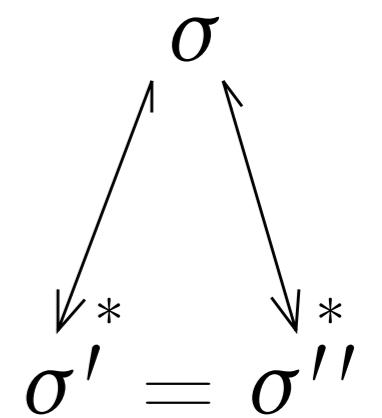
Determinism



do

```
fork (incr1 counter)
fork (incr42 counter)
get counter
```

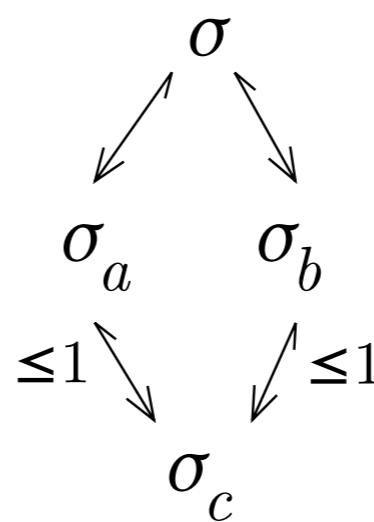
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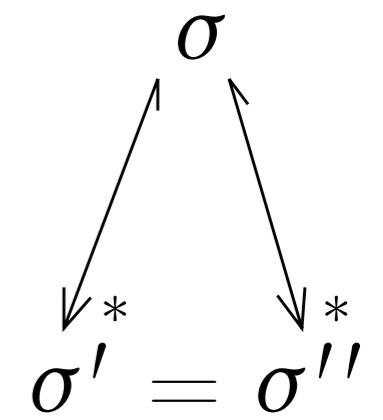
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Strong
Local
Confluence



Determinism



do

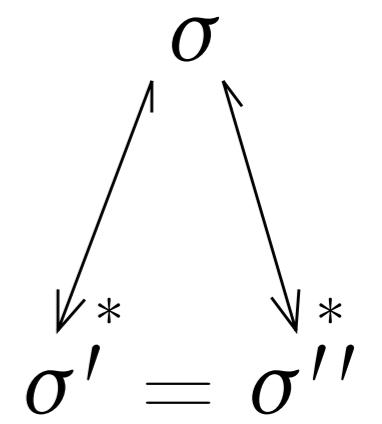
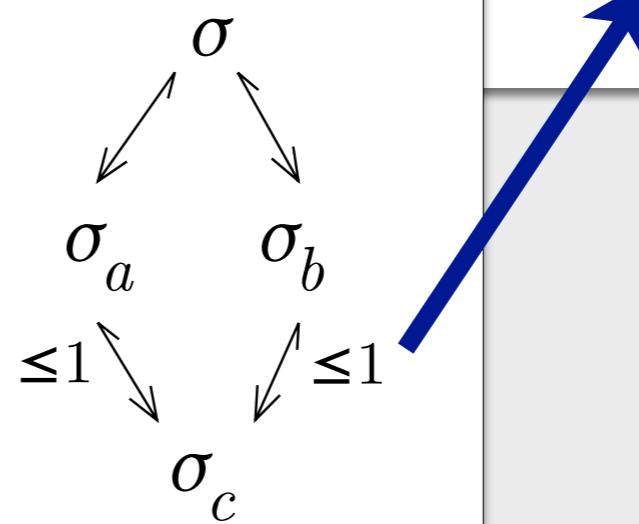
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Independence

$$\frac{\langle S; e \rangle \hookrightarrow \langle S'; e' \rangle}{\langle S \sqcup_S S''; e \rangle \hookrightarrow \langle S' \sqcup_S S''; e' \rangle}$$

Strong
Local
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Determinism



Frame rule

$$\frac{\{p\} \ c \ \{q\}}{\{p * r\} \ c \ \{q * r\}}$$

[O'Hearn *et al.*, 2001]

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LVish

a Haskell library for parallel programming with LVars



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LVar operations run in **Par** computations



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Lightweight threads



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Lightweight threads

Par computations indexed by effect level

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p :: HasPut e =>
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runParThenFreeze expresses
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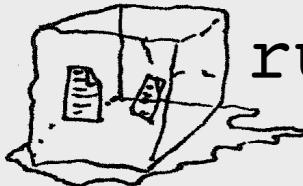
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hackage.haskell.org/package/lvish



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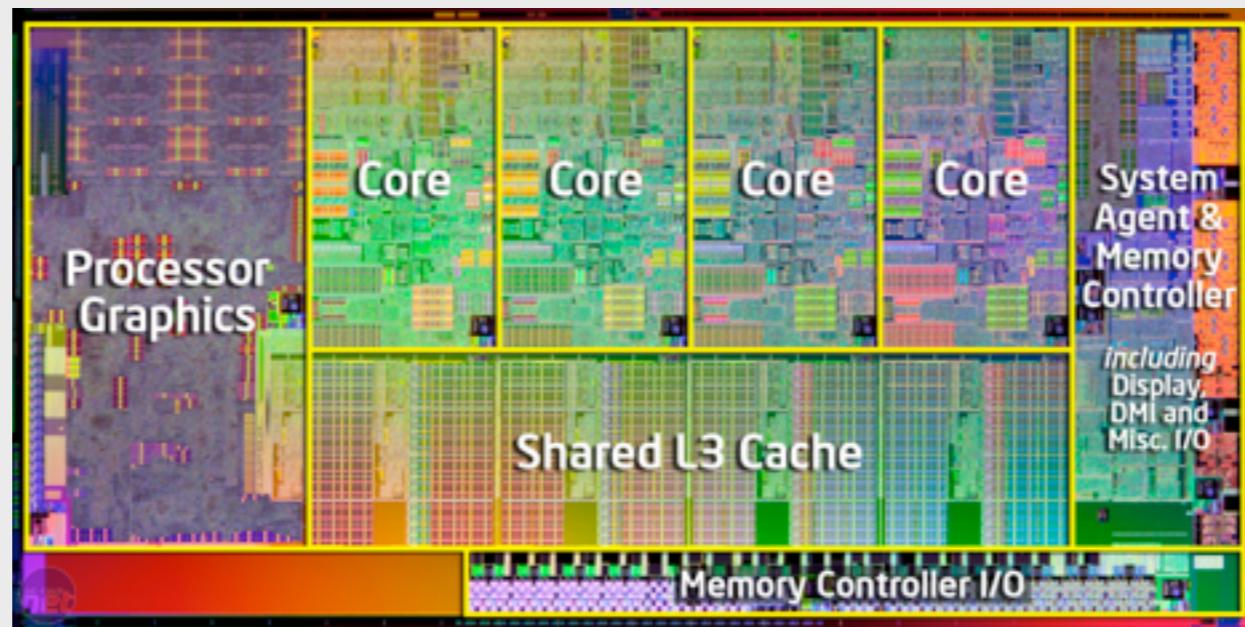
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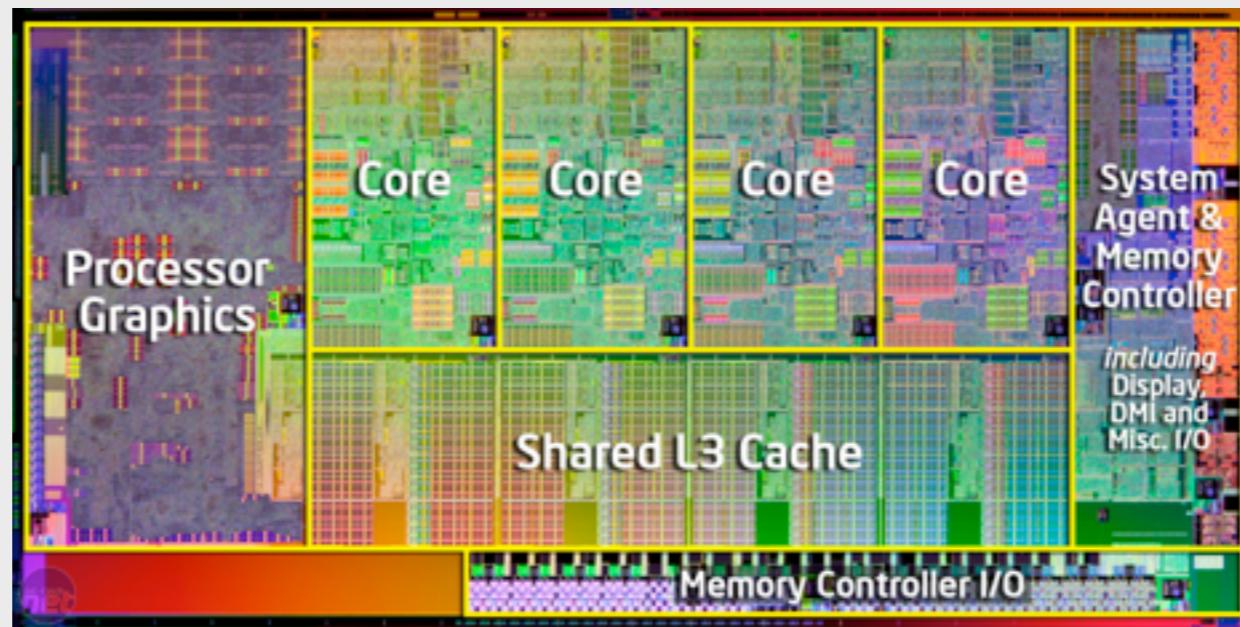
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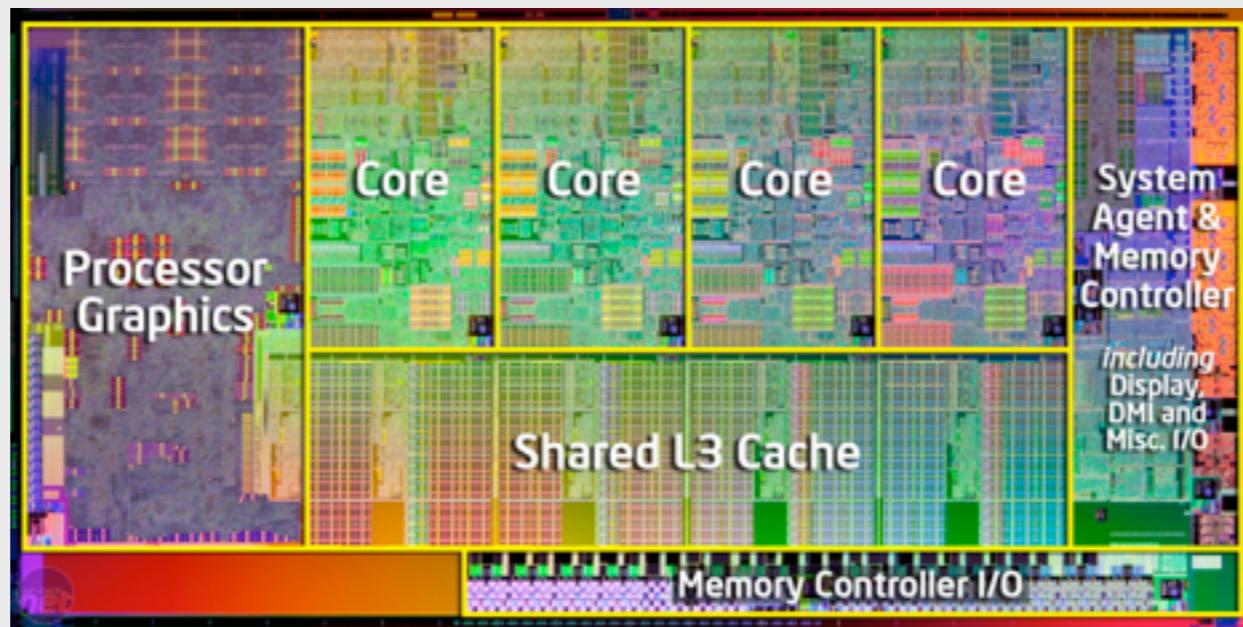
github.com/iu-parfunc/lvars



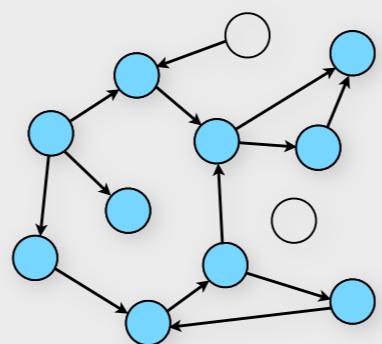
Deterministic Parallel Programming



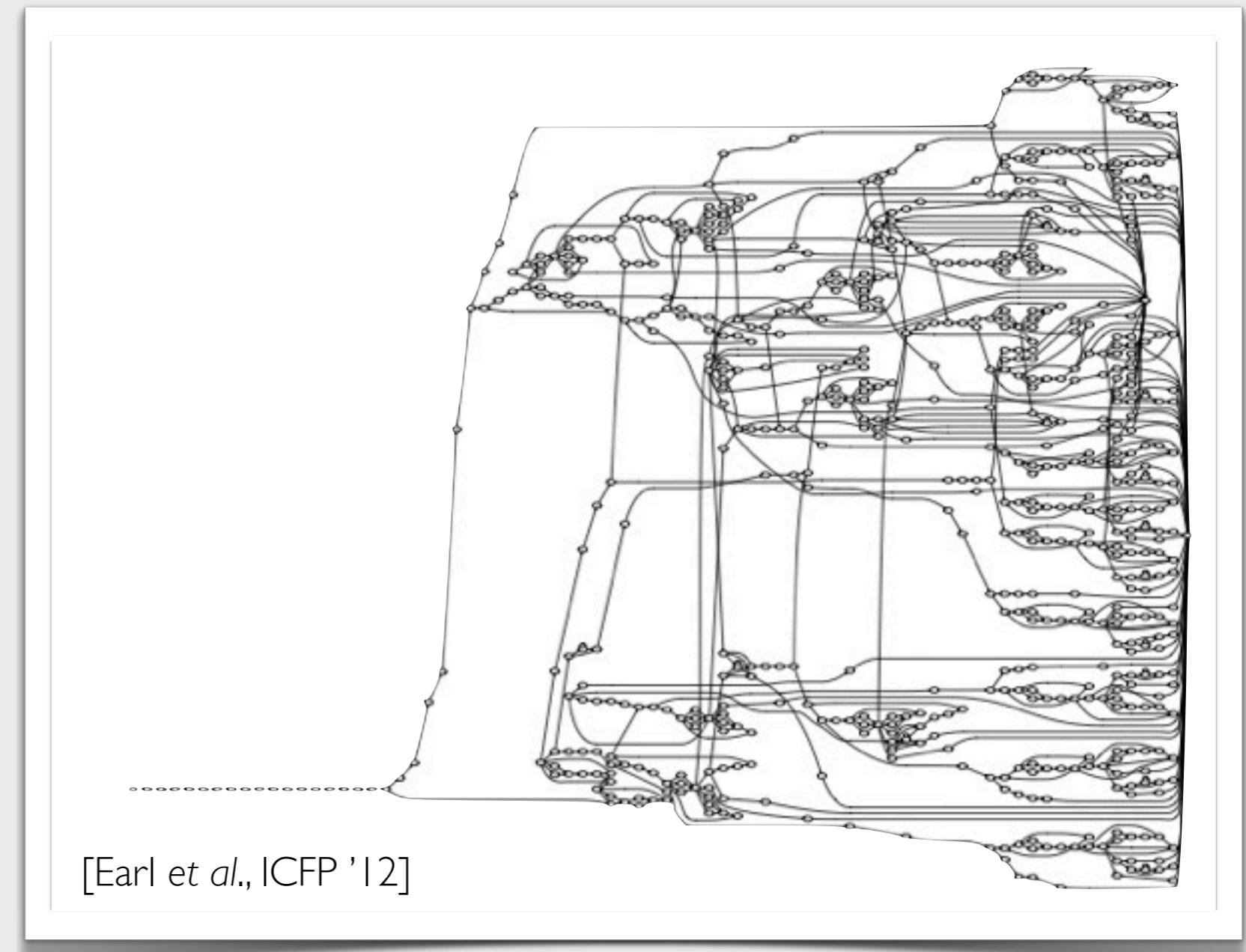
(observably)
Deterministic Parallel Programming



(observably) (irregular)
Deterministic Parallel Programming

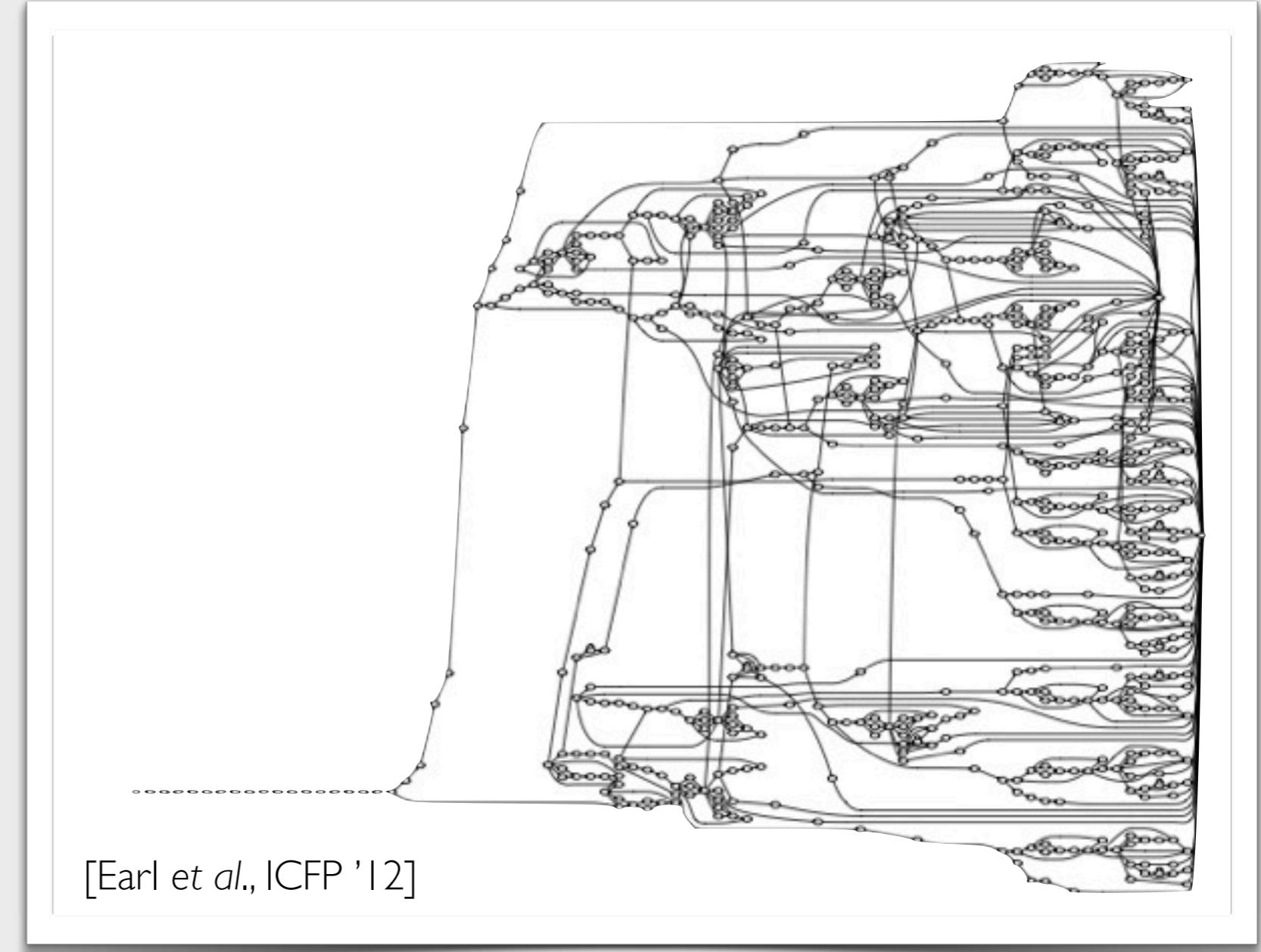


Case study: k-CFA static analysis parallelized with LVish [POPL '14]



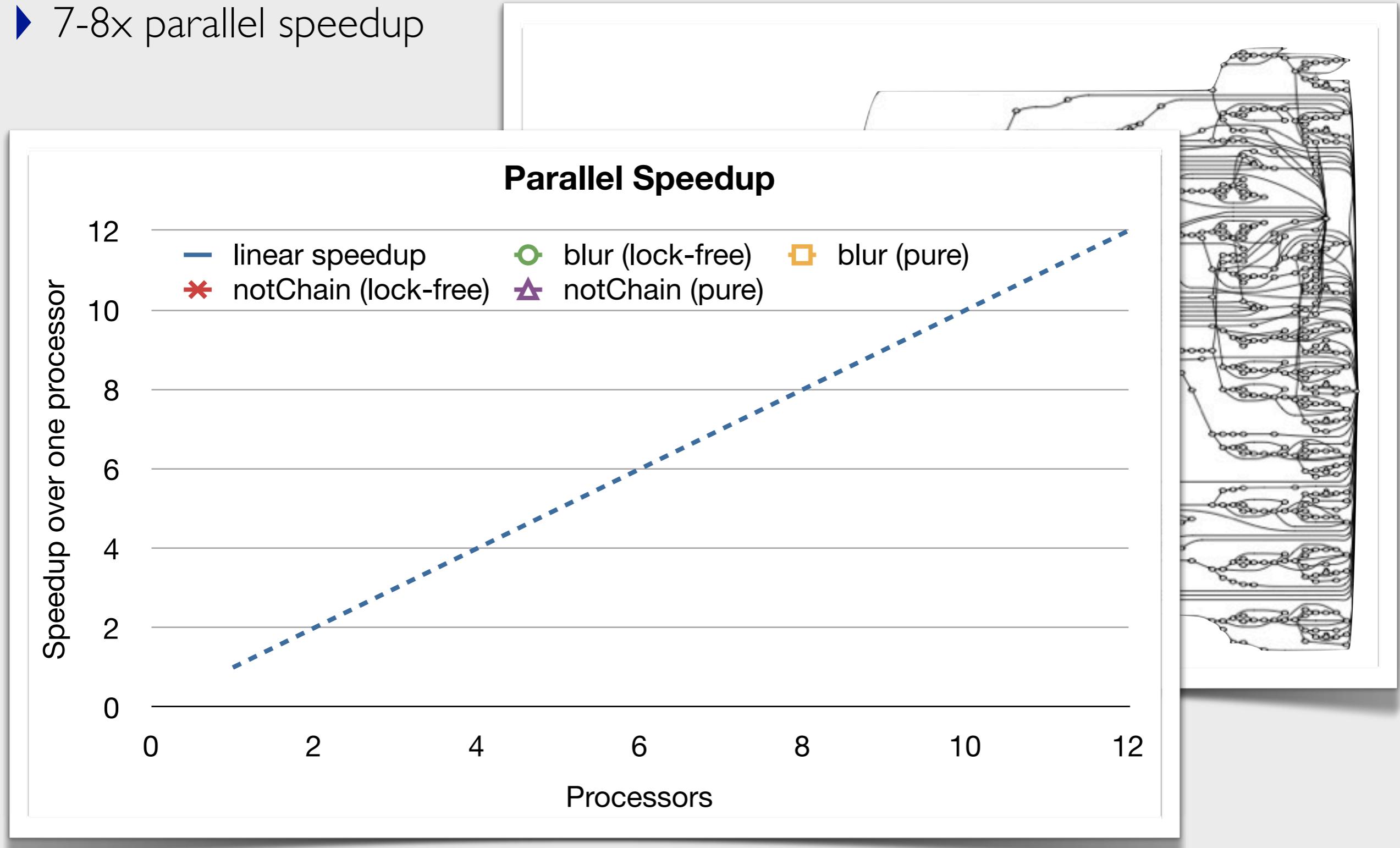
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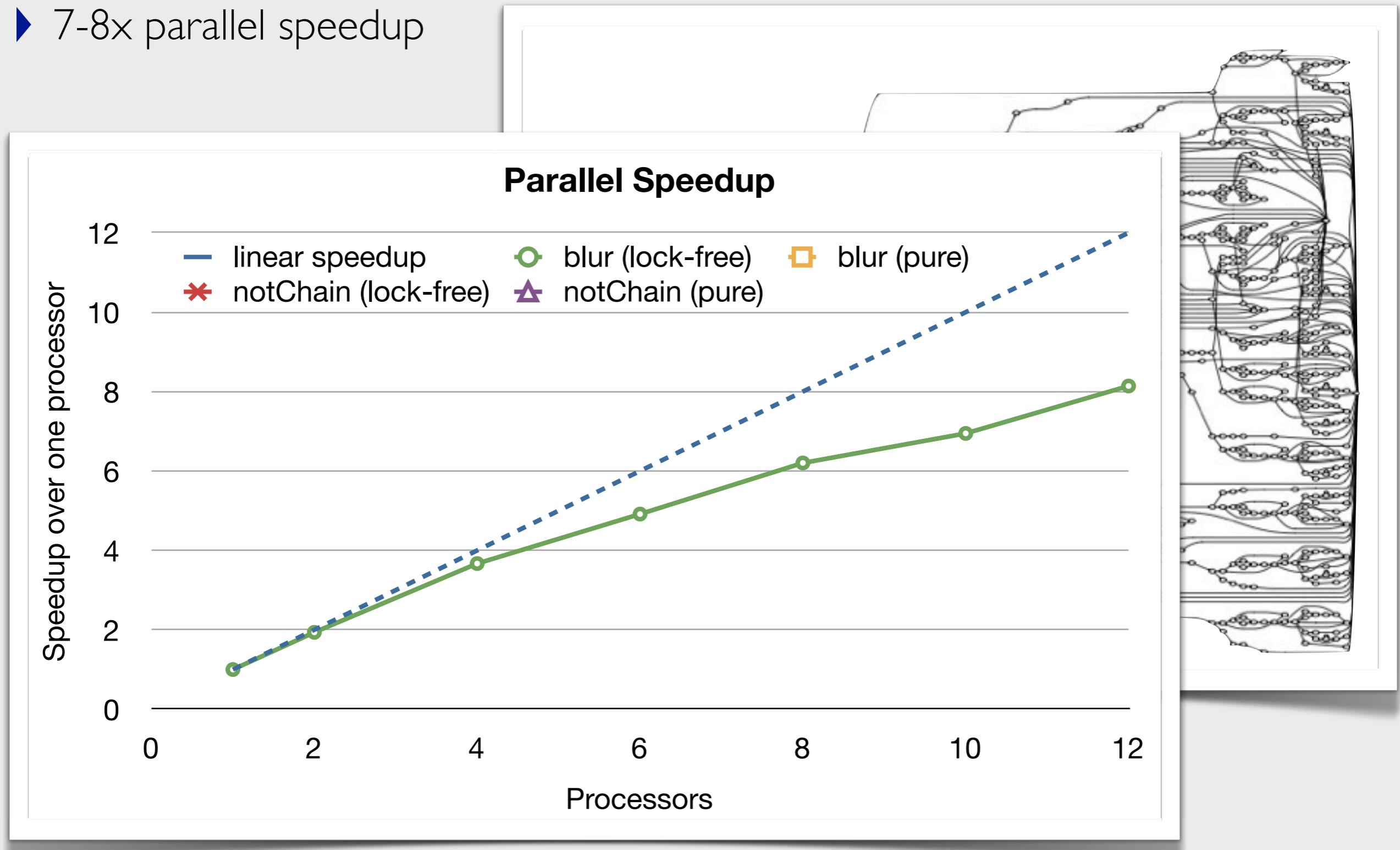
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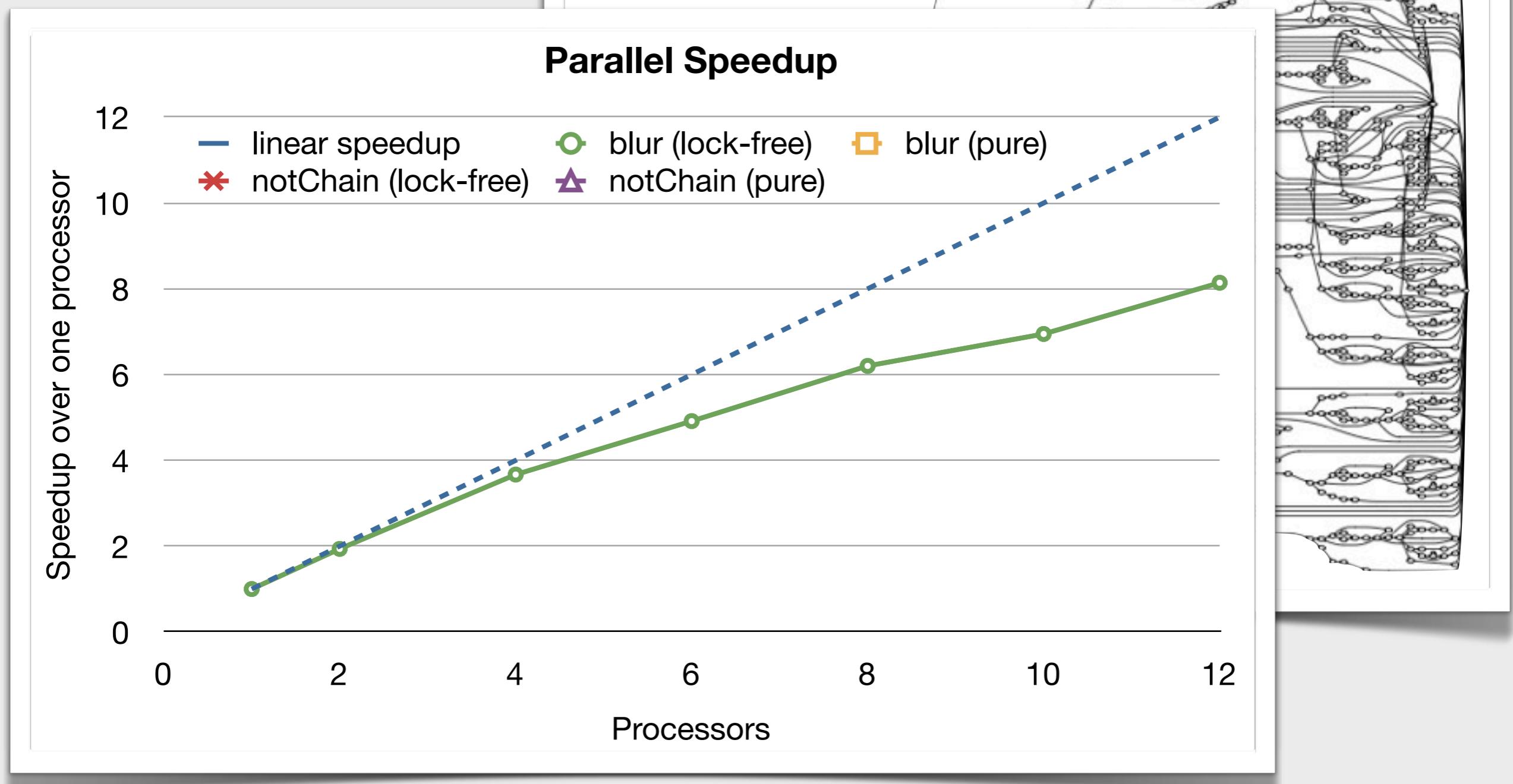
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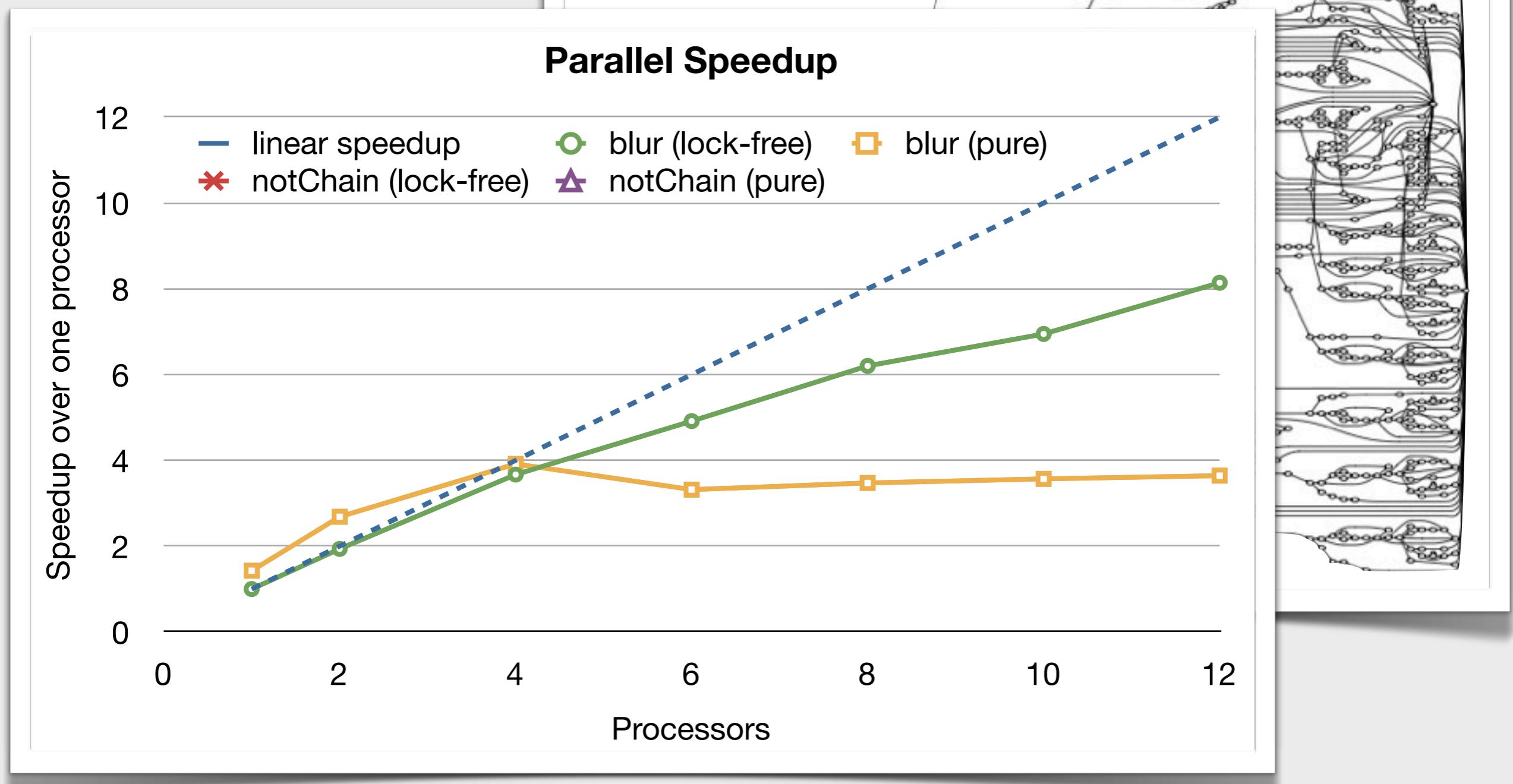
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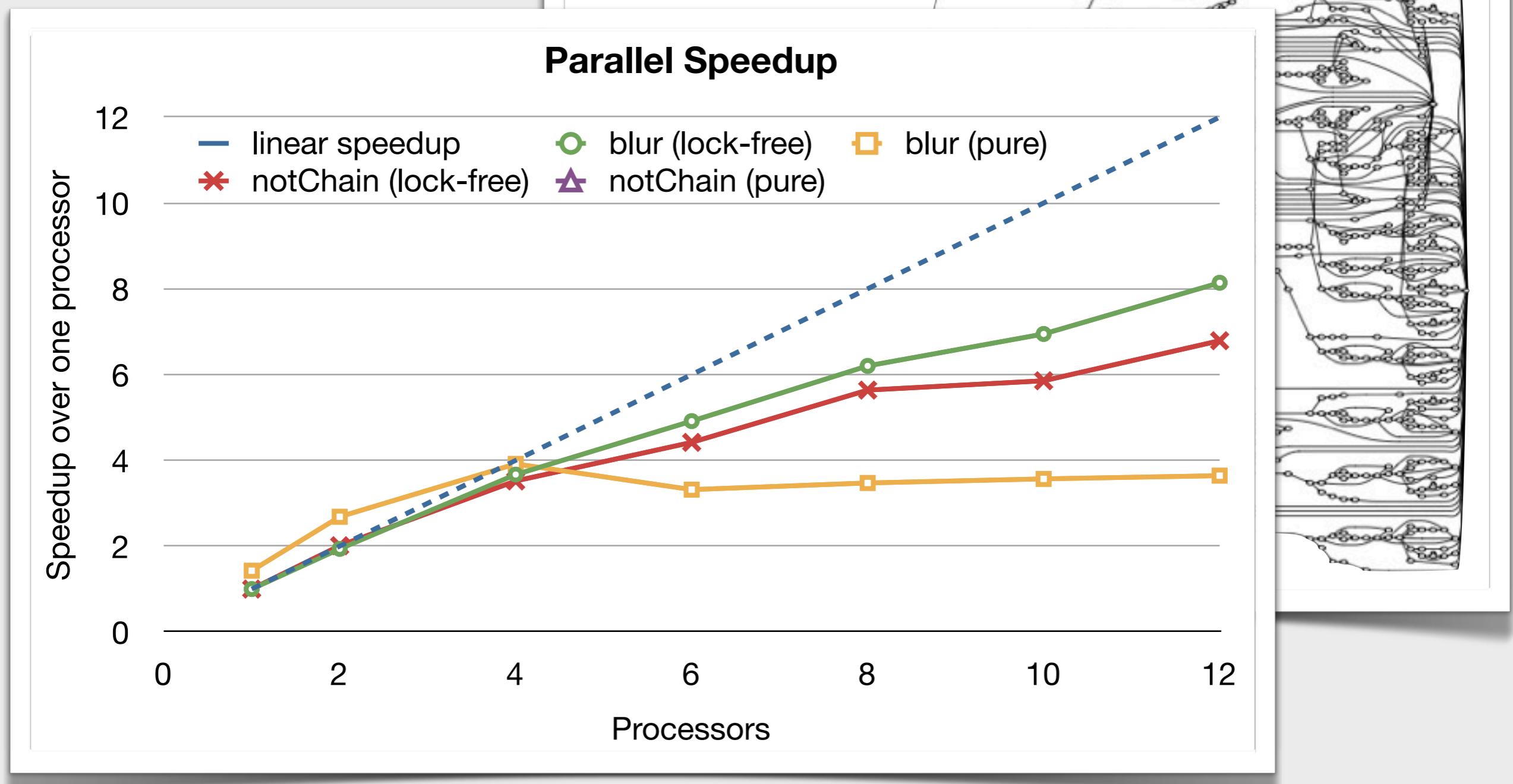
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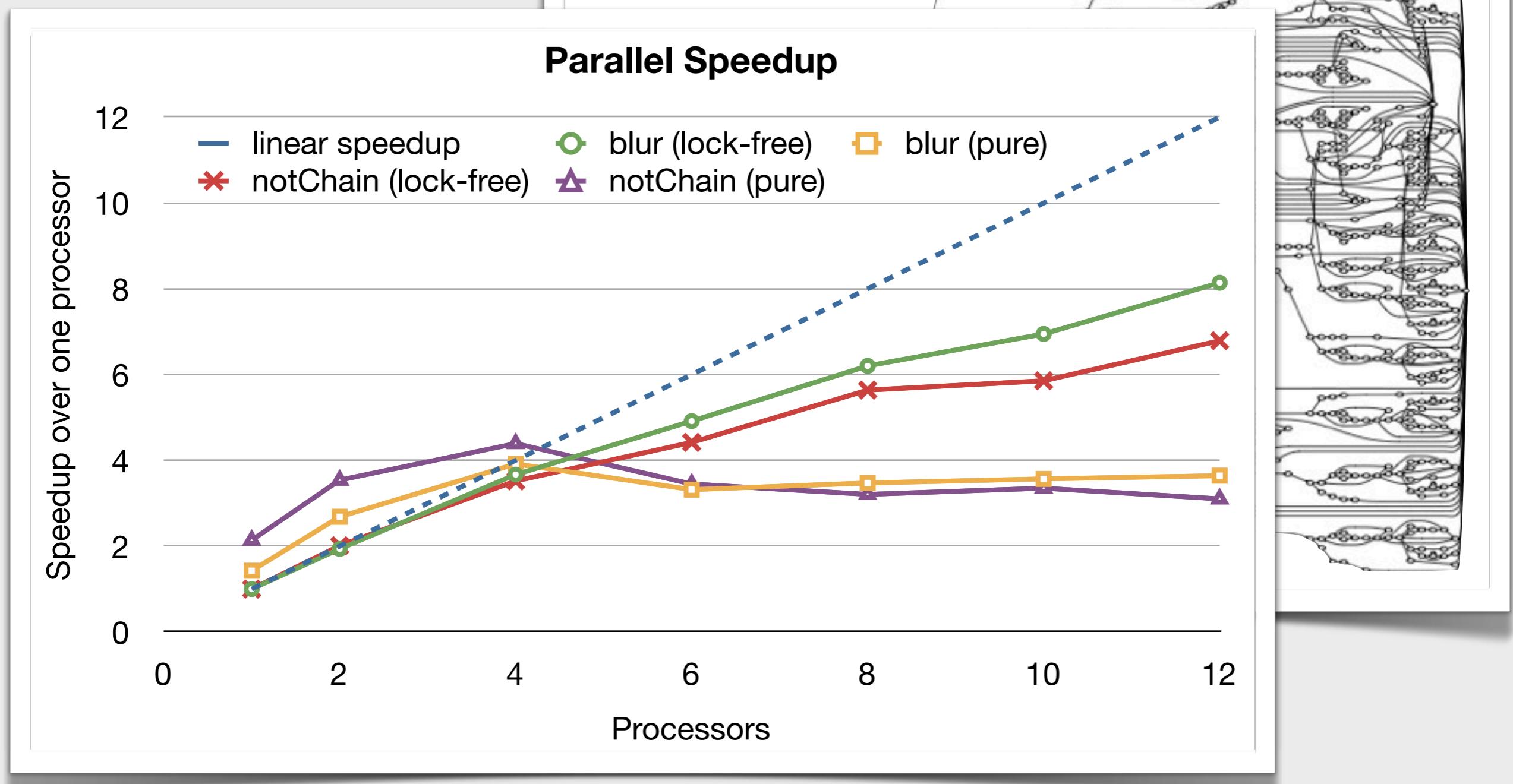
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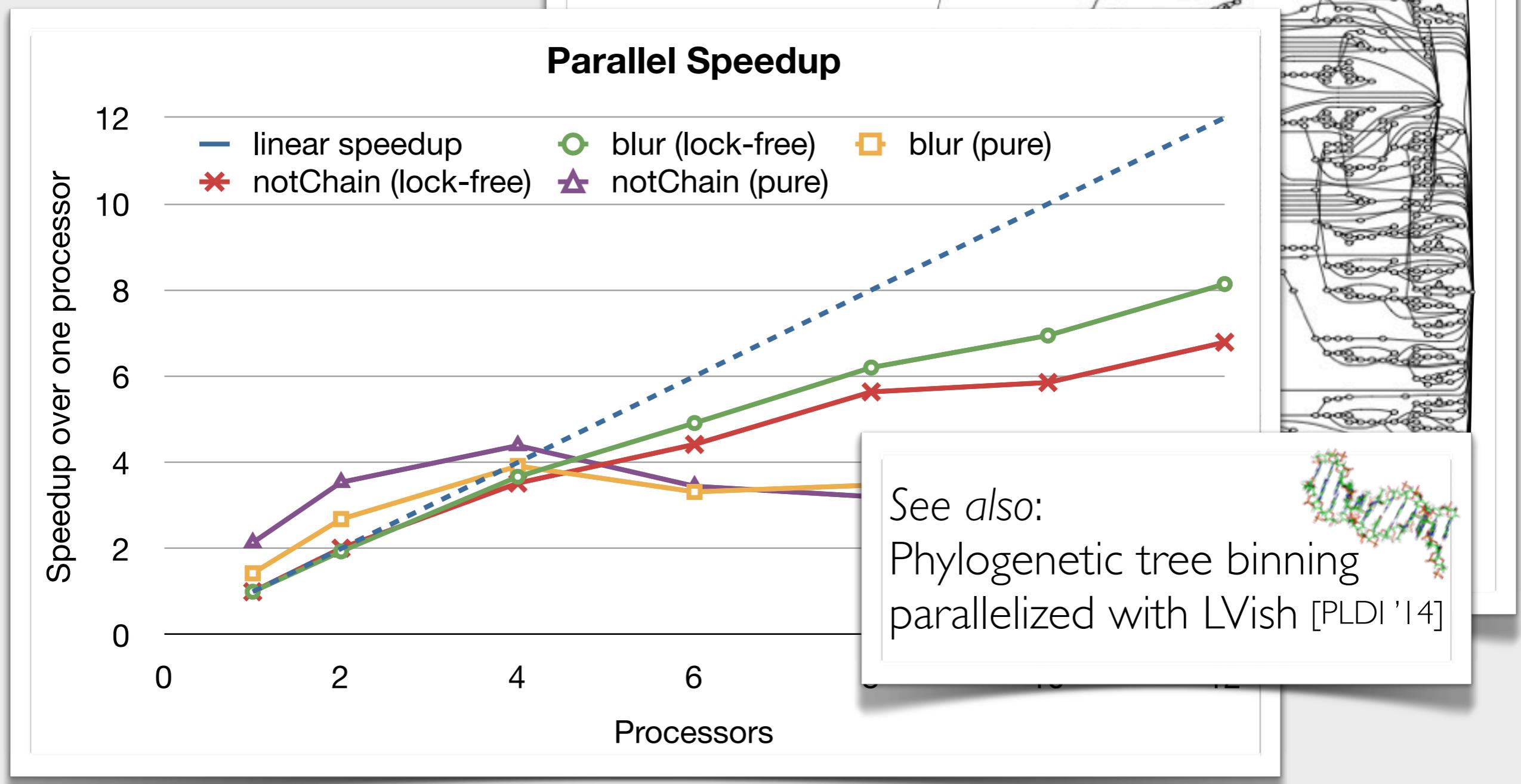
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Case study: k-CFA static analysis parallelized with LVish [POPL '14]

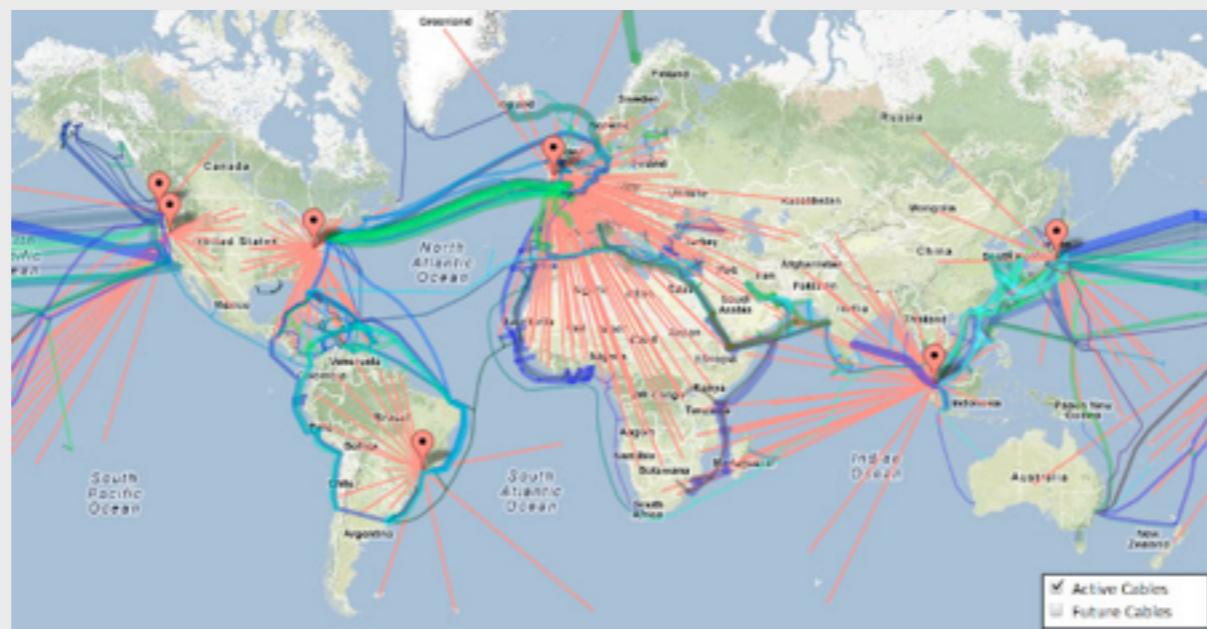
- ▶ up to 25x speedup, even on one core, from not having to copy data!
- ▶ 7-8x parallel speedup
- ▶ Lock-free structures help



aka “ $LVars$ ”

Lattice-based data structures
are a general and practical unifying abstraction
for deterministic and quasi-deterministic
parallel and distributed programming.



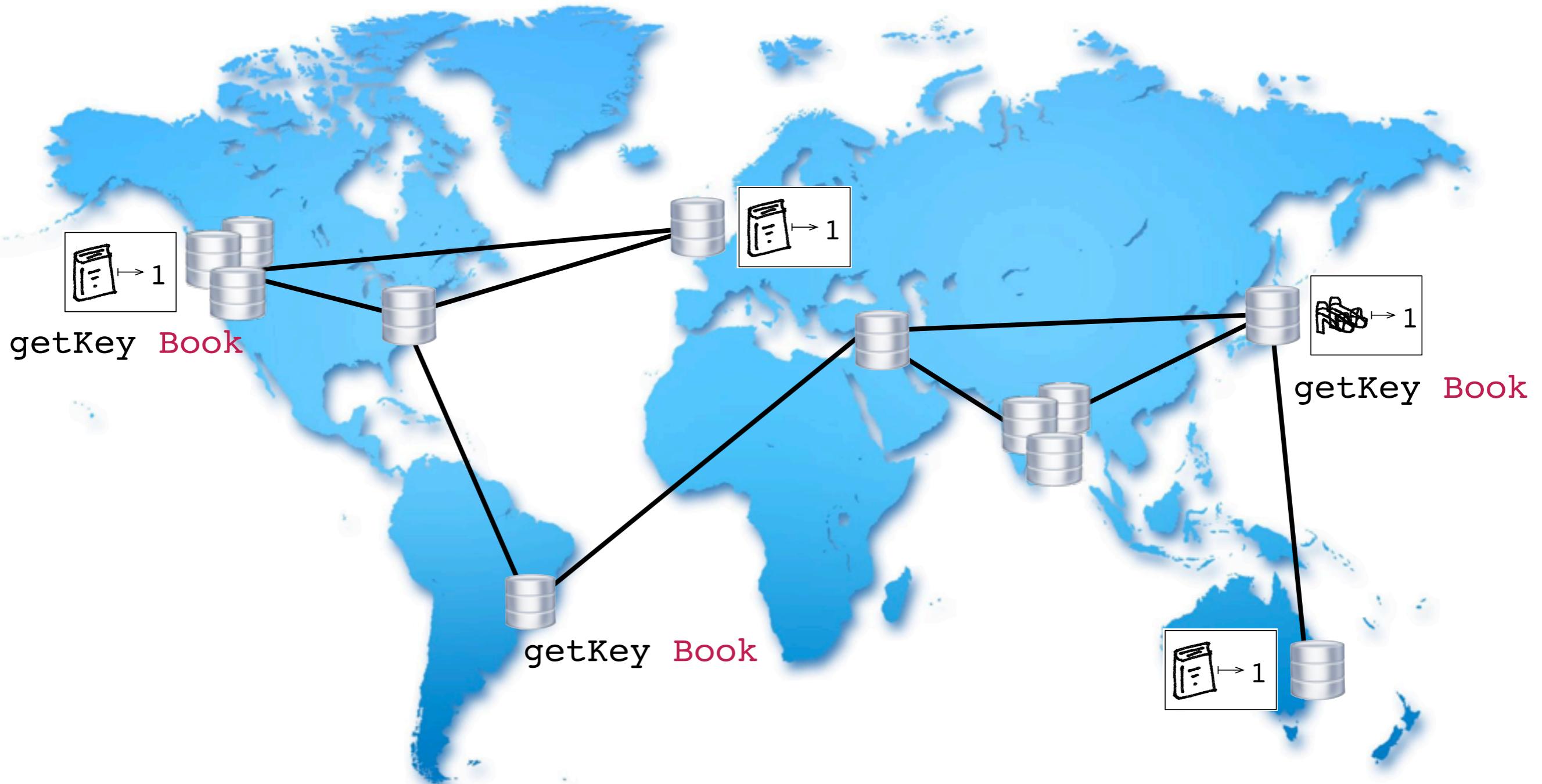


Distributed systems











Eventual consistency.

“if updates stop arriving,
replicas will eventually agree”



Eventual consistency...but how?

“if updates stop arriving,
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Dynamo: Amazon's Highly Available Key-value Store

Giuseppe DeCandia, Deniz Hastorun, Madan Jampani, Gunavardhan Kakulapati,
Avinash Lakshman, Alex Pilchin, Swaminathan Sivasubramanian, Peter Vosshall
and Werner Vogels

Amazon.com

ABSTRACT

Reliability at massive scale is one of the biggest challenges we face at Amazon.com, one of the largest e-commerce operations in the world; even the slightest outage has significant financial consequences and impacts customer trust. The Amazon.com platform, which provides services for many web sites worldwide, is implemented on top of an infrastructure of tens of thousands of servers and network components located in many datacenters around the world. At this scale, small and large components fail continuously and the way persistent state is managed in the face of these failures drives the reliability and scalability of the software systems.

This paper presents the design and implementation of Dynamo, a highly available key-value storage system that some of Amazon's core services use to provide an "always-on" experience. To achieve this level of availability, Dynamo sacrifices consistency under certain failure scenarios. It makes extensive use of object versioning and application-assisted conflict resolution in a manner that provides a novel interface for developers to use.

Categories and Subject Descriptors

D.4.2 [Operating Systems]: Storage Management; D.4.5 [Operating Systems]: Reliability; D.4.2 [Operating Systems]: Performance;

General Terms

Algorithms, Management, Measurement, Performance, Design, Reliability.

1. INTRODUCTION

Amazon runs a world-wide e-commerce platform that serves tens of millions customers at peak times using tens of thousands of servers located in many data centers around the world. There are strict operational requirements on Amazon's platform in terms of performance, reliability and efficiency, and to support continuous growth the platform needs to be highly scalable. Reliability is one of the most important requirements because even the slightest outage has significant financial consequences and impacts customer trust. In addition, to support continuous growth, the platform needs to be highly scalable.

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One of the lessons our organization has learned from operating Amazon's platform is that the reliability and scalability of a system is dependent on how its application state is managed. Amazon uses a highly decentralized, loosely coupled, service oriented architecture consisting of hundreds of services. In this environment there is a particular need for storage technologies that are always available. For example, customers should be able to view and add items to their shopping cart even if disks are failing, network routes are flapping, or data centers are being destroyed by tornados. Therefore, the service responsible for managing shopping carts requires that it can always write to and read from its data store, and that its data needs to be available across multiple data centers.

Dealing with failures in an infrastructure comprised of millions of components is our standard mode of operation; there are always a small but significant number of server and network components that are failing at any given time. As such Amazon's software systems need to be constructed in a manner that treats failure handling as the normal case without impacting availability or performance.

To meet the reliability and scaling needs, Amazon has developed a number of storage technologies, of which the Amazon Simple Storage Service (also available outside of Amazon and known as Amazon S3), is probably the best known. This paper presents the design and implementation of Dynamo, another highly available and scalable distributed data store built for Amazon's platform. Dynamo is used to manage the state of services that have very high reliability requirements and need tight control over the tradeoffs between availability, consistency, cost-effectiveness and performance. Amazon's platform has a very diverse set of applications with different storage requirements. A select set of applications require a storage technology that is flexible enough to let application designers configure their data store appropriately based on these tradeoffs to achieve high availability and guaranteed performance in the most cost effective manner.

There are many services on Amazon's platform that only need primary-key access to a data store. For many services, such as those that provide best seller lists, shopping carts, customer preferences, session management, sales rank, and product catalog, the common pattern of using a relational database would lead to inefficiencies and limit scale and availability. Dynamo provides a simple primary-key only interface to meet the requirements of these applications.

Dynamo uses a synthesis of well known techniques to achieve scalability and availability: Data is partitioned and replicated using consistent hashing [10], and consistency is facilitated by object versioning [12]. The consistency among replicas during updates is maintained by a quorum-like technique and a decentralized replica synchronization protocol. Dynamo employs

[DeCandia et al., SOSP '07]

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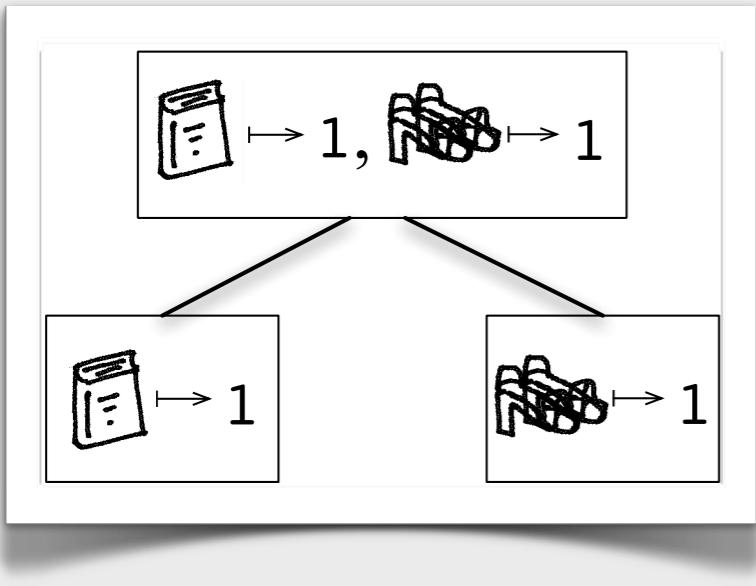
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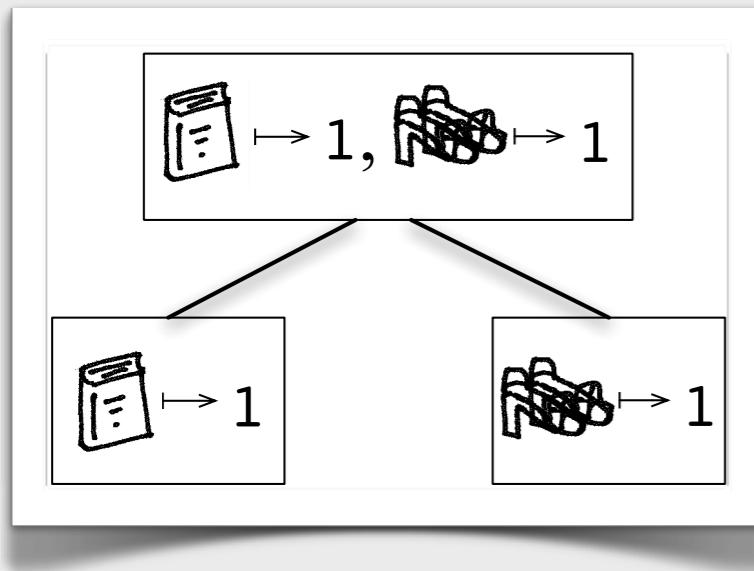
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[DeCandia et al., SOSP '07]

Convergent replicated data types (CvRDTs)

[Shapiro et al., 2011]



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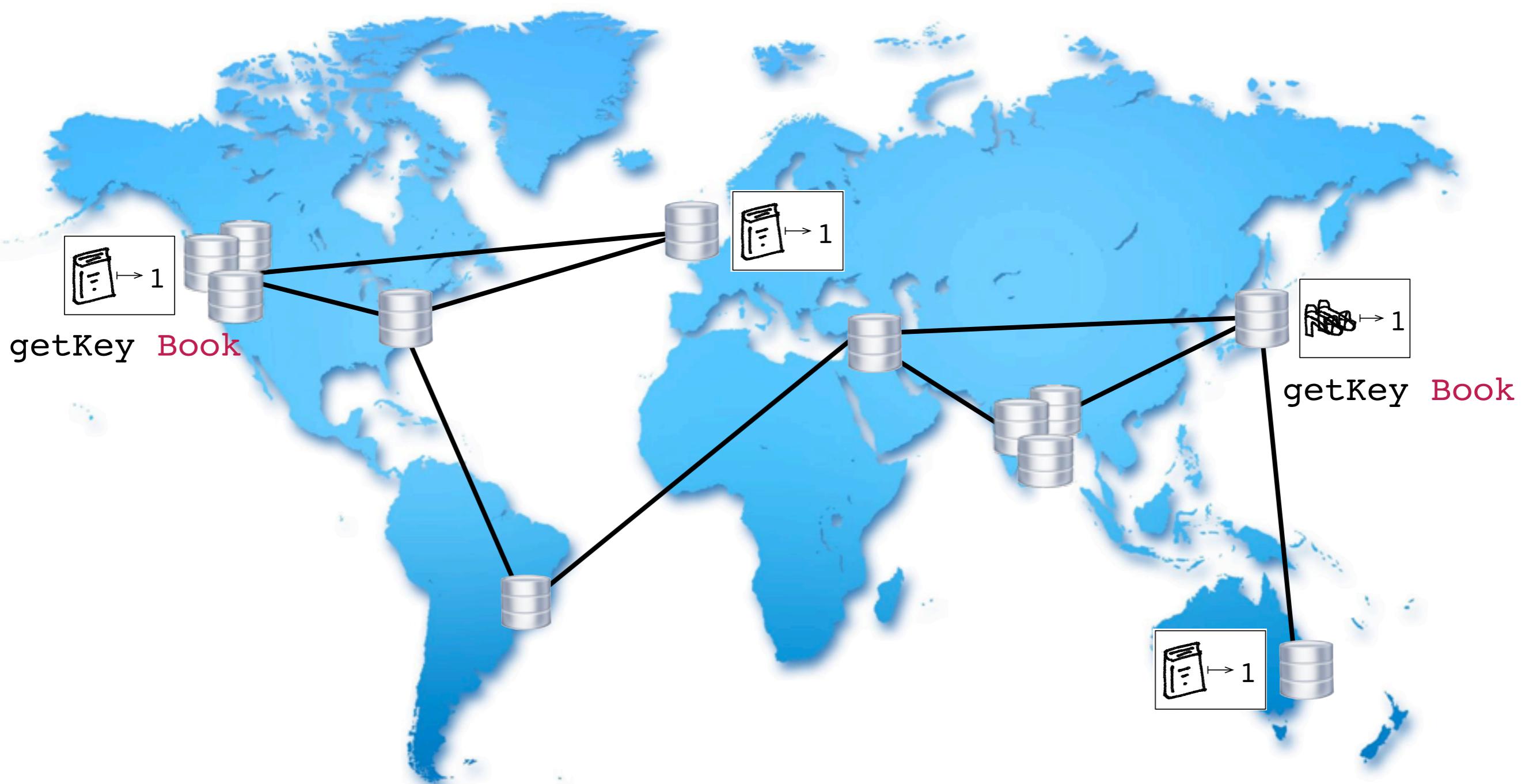
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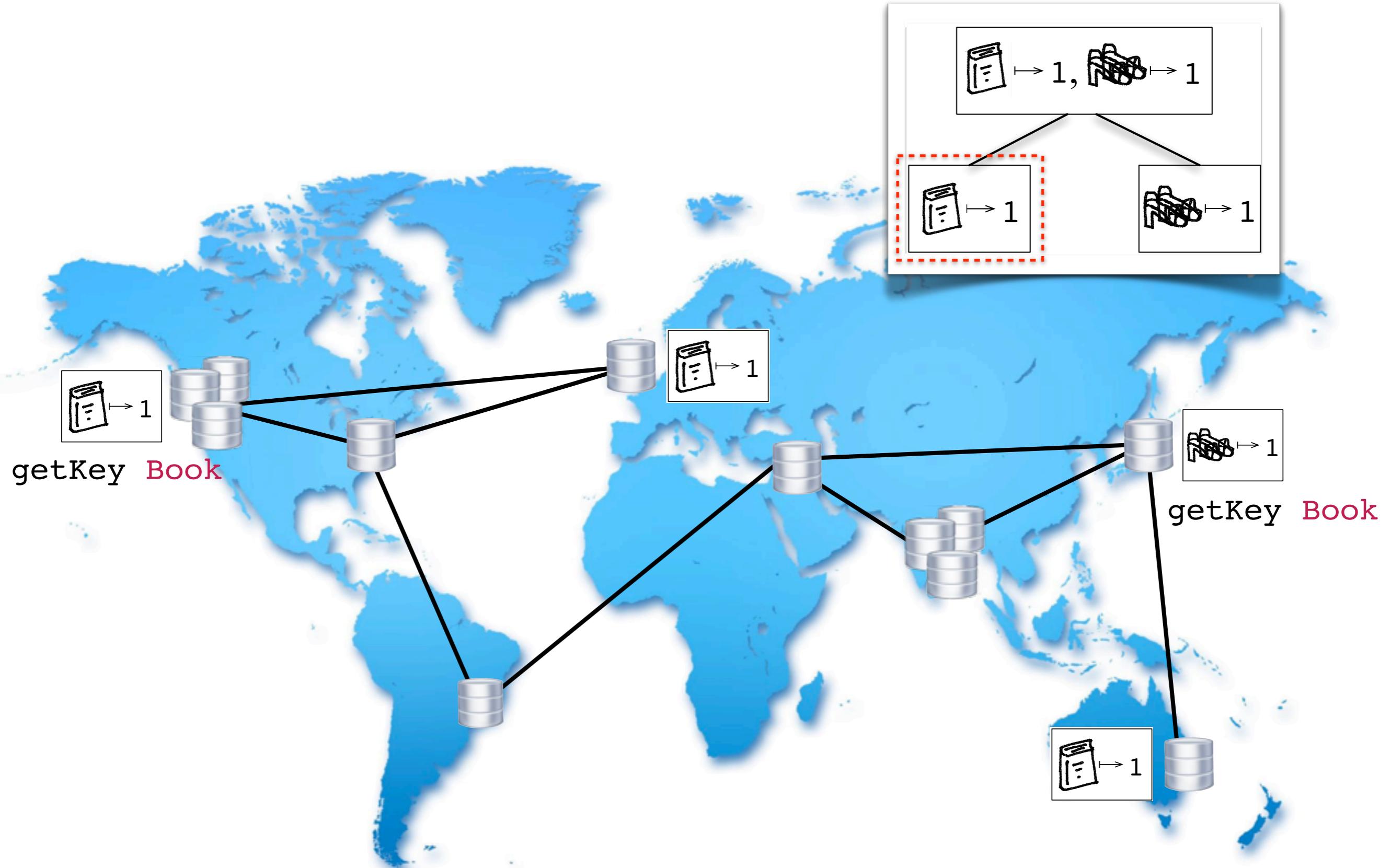
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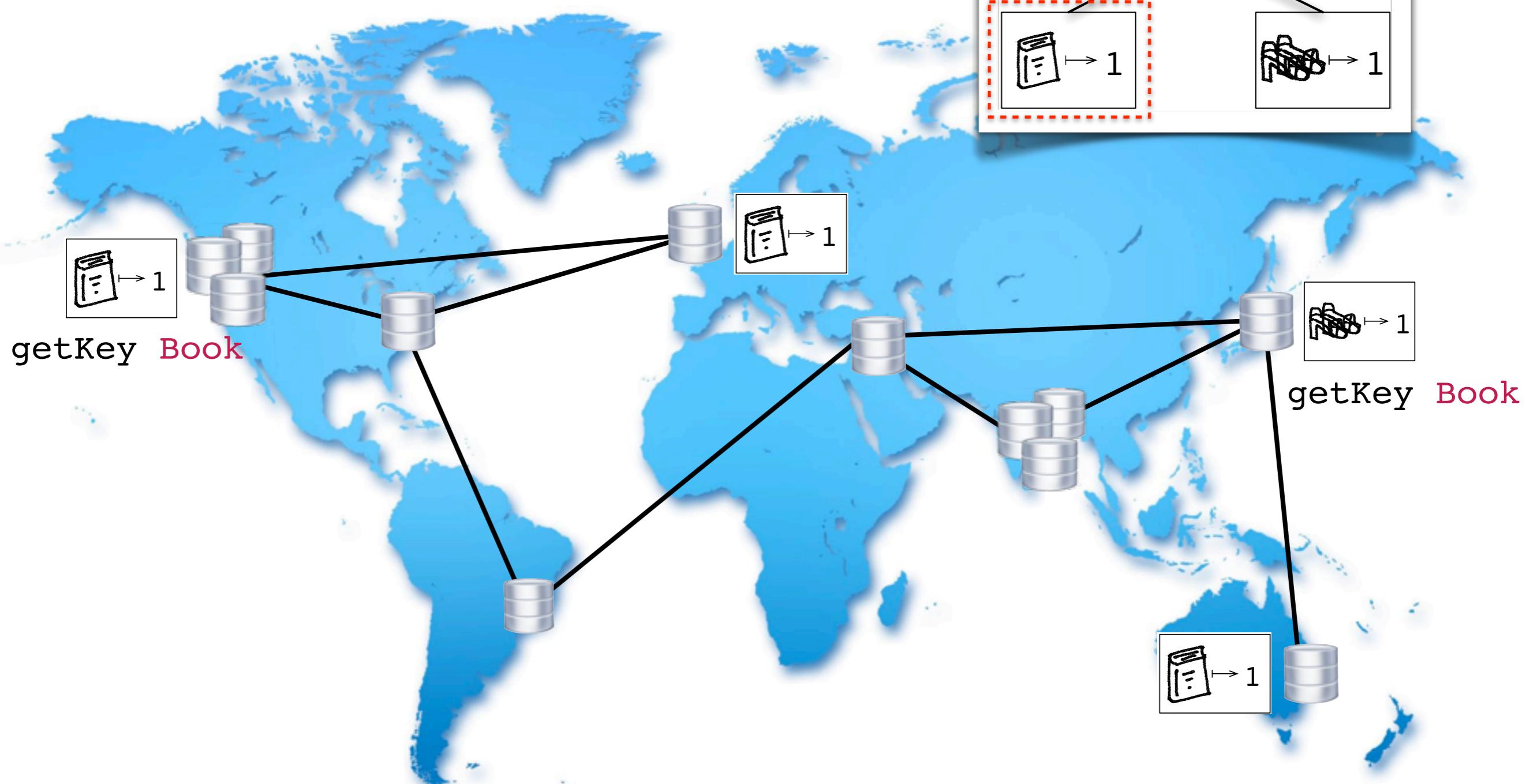
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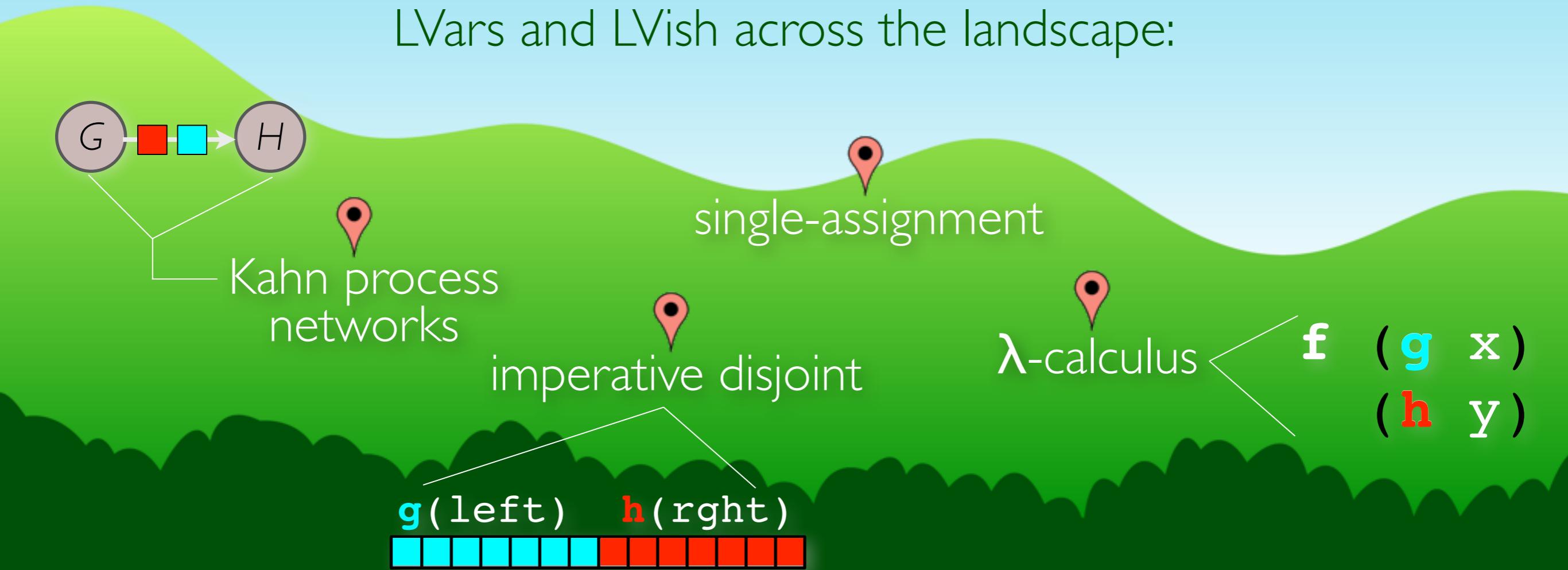




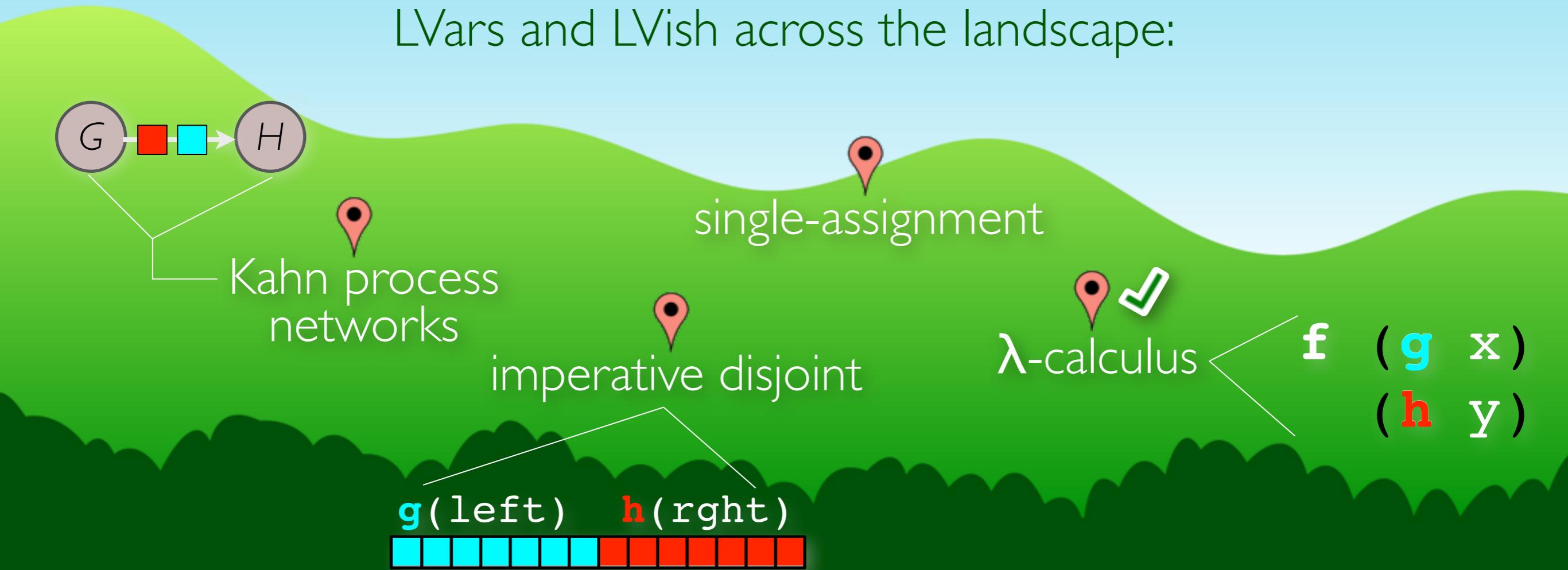
Our contribution:
deterministic threshold queries of CvRDTs



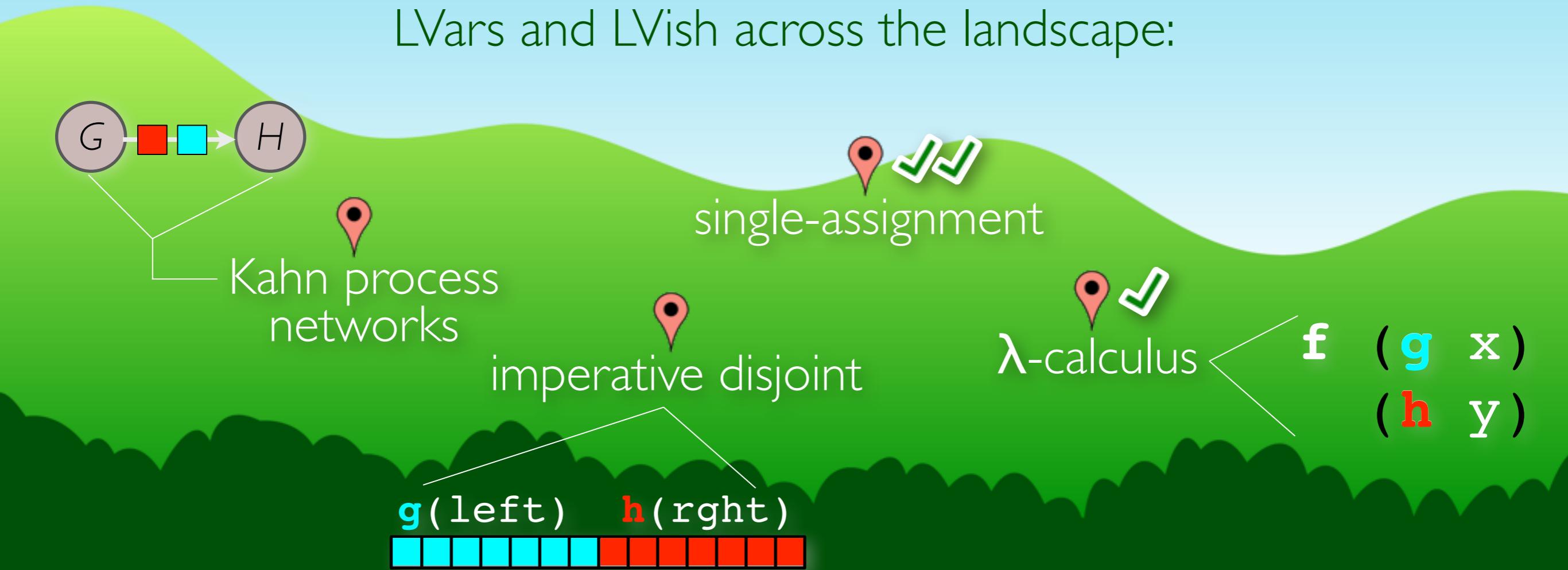
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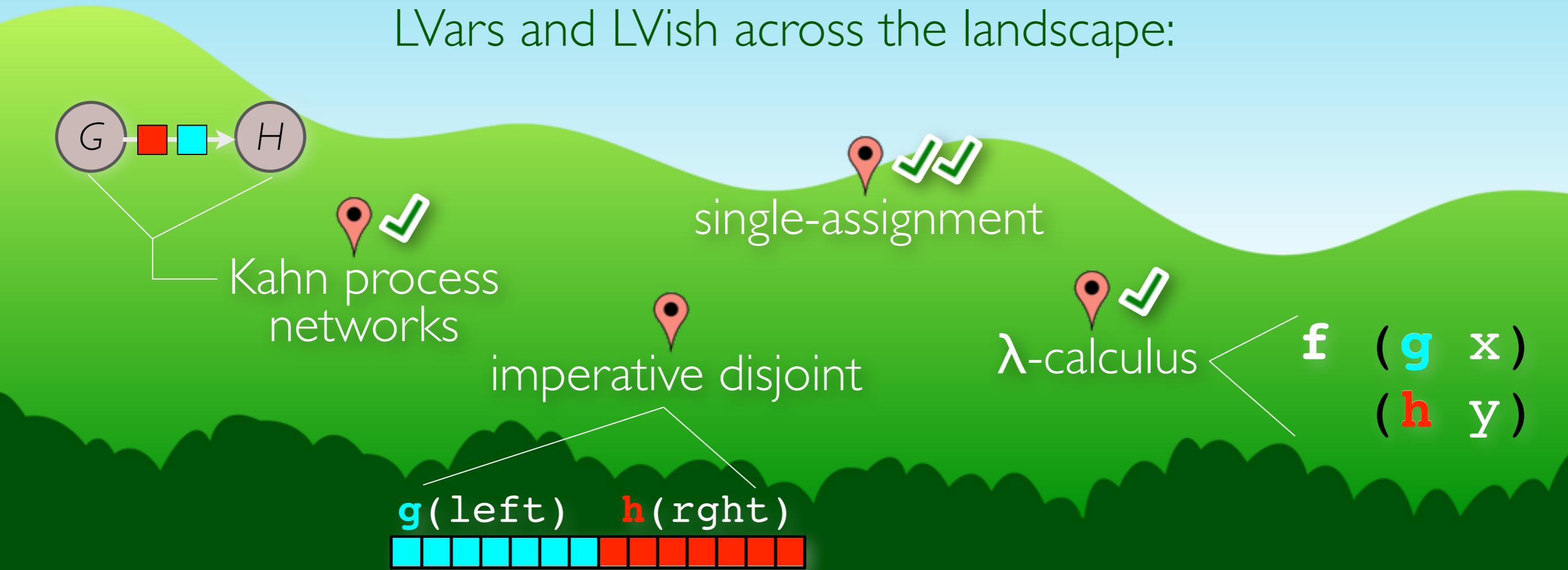
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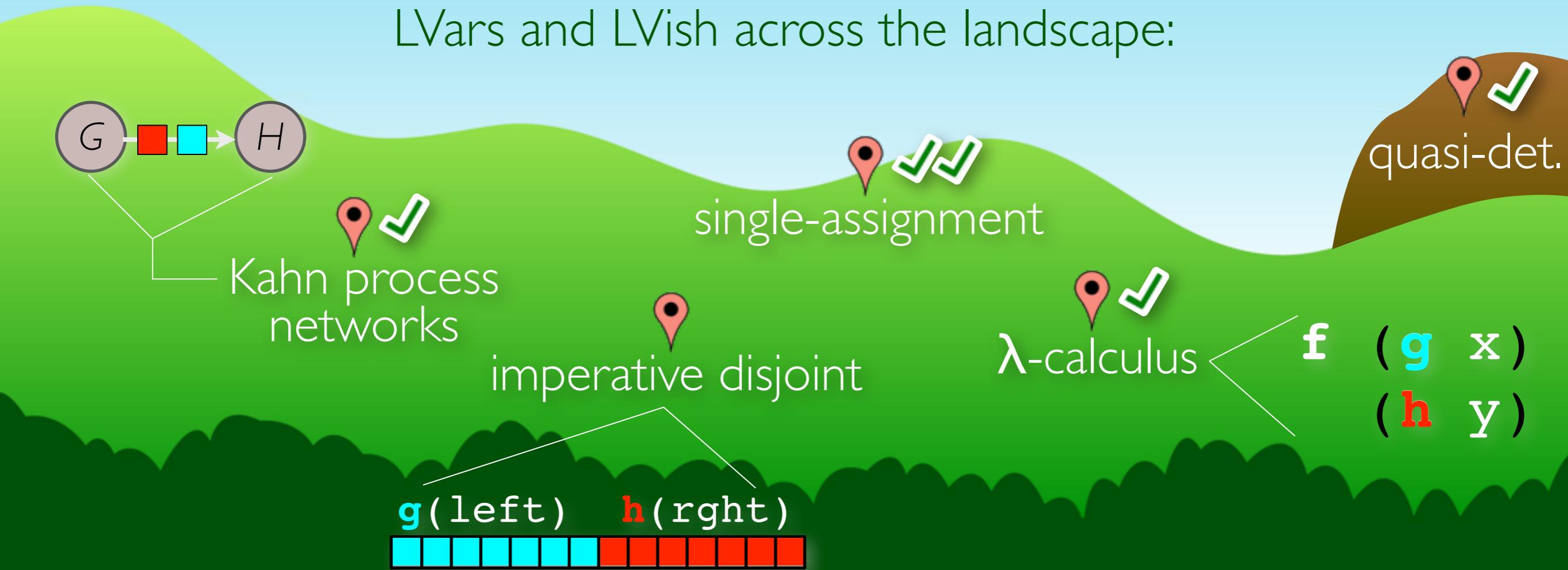
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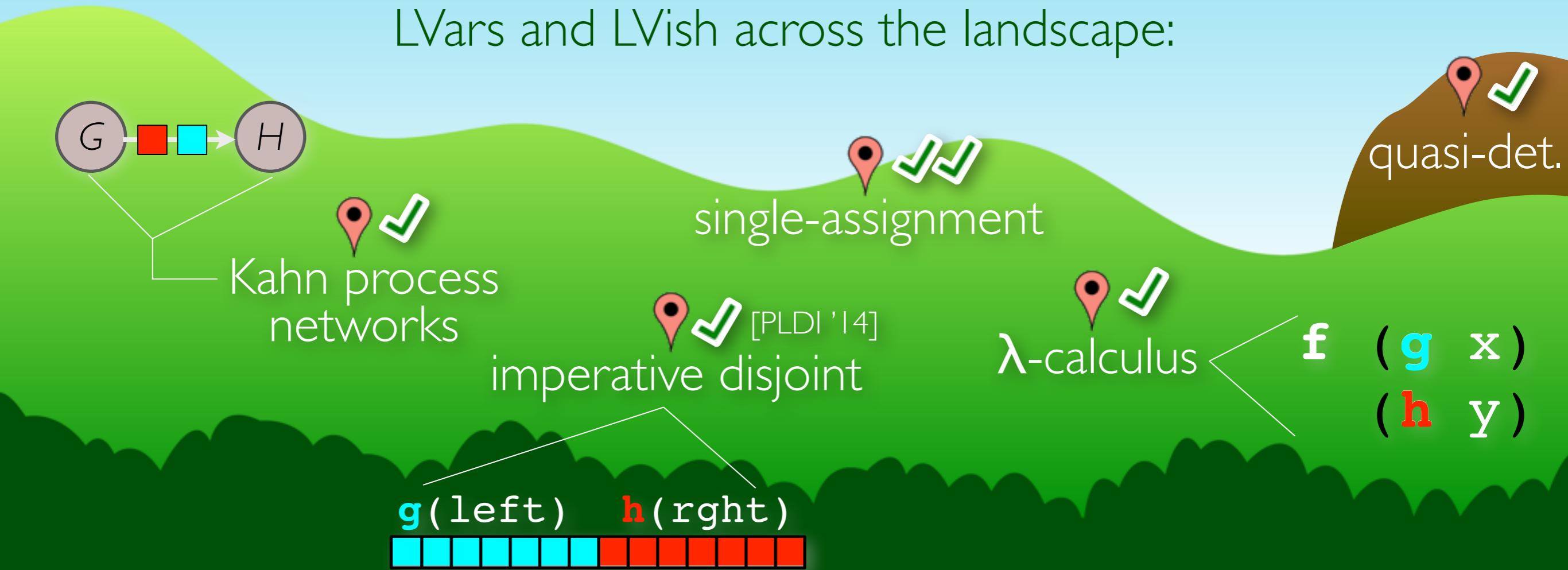
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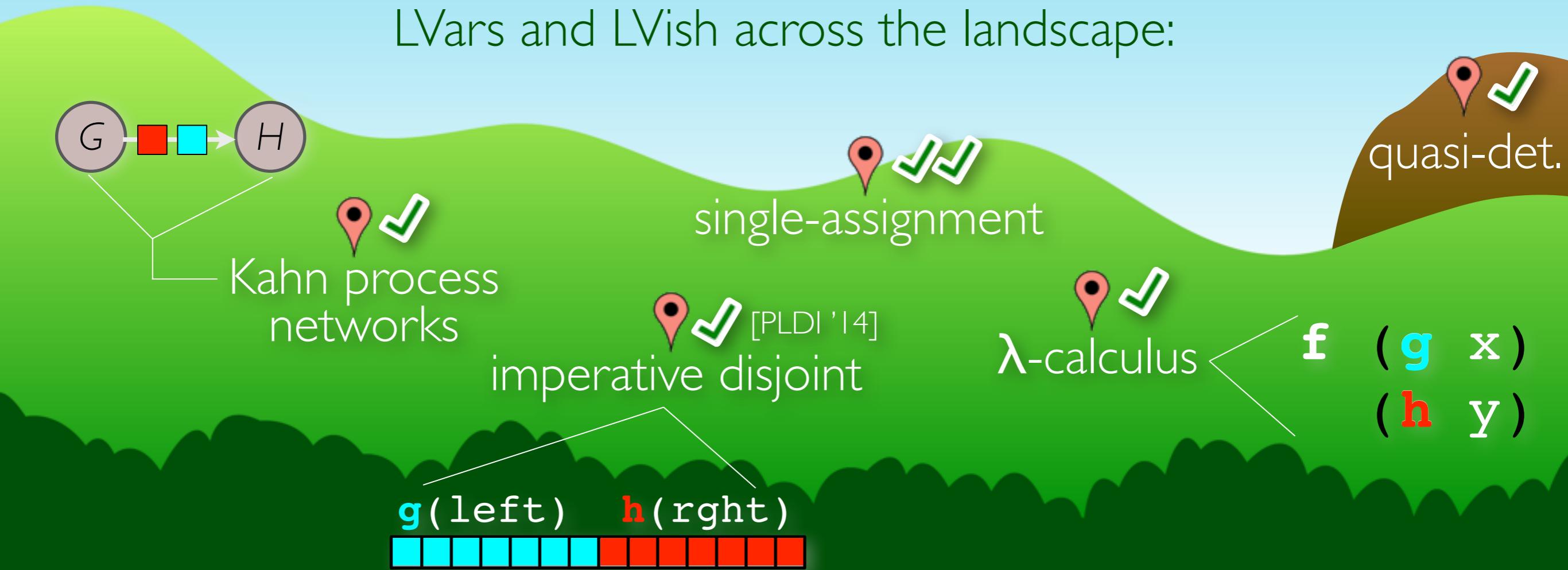
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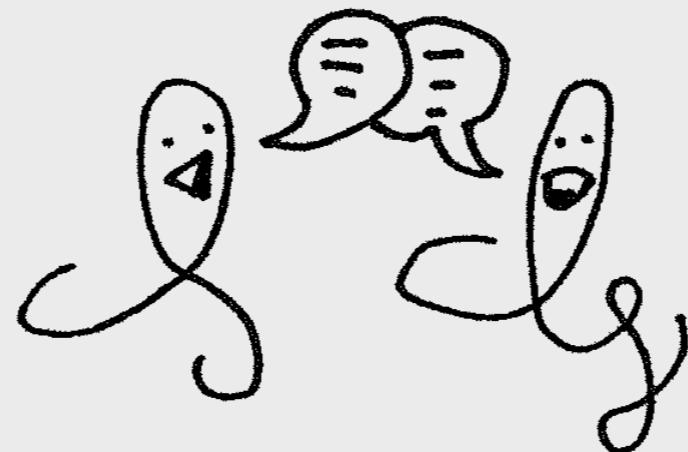


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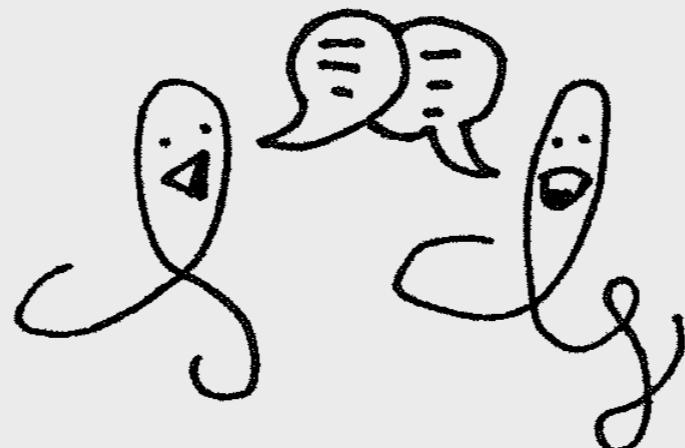
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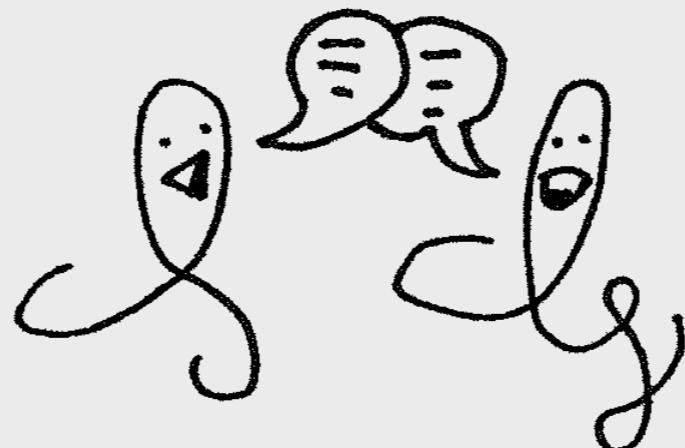
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Thank you!