

# 1 Activation functions in neural networks

## 1.1 Sigmoid $f(x) = \frac{1}{1+e^{-x}}$

### Description

- squashes numbers to range  $[0, 1]$   
high values near 1, high negative values near 0
- has a nice interpretation of saturating the "firing rate" of a neuron

### Problems

- saturated neurons "kill" the gradient  
high positive and high negative values generate  $\sim 0$  gradients (flat slope)
- sigmoid outputs are not zero-centered (inefficient gradient updates)
- the exponential function is computationally expensive

## 1.2 Tanh $f(x) = \tanh(x)$

### Description

- squashes numbers to range  $[-1, 1]$   
high values near 1, high negative values near -1
- outputs are zero-centered

### Problems

- saturated neurons "kill" the gradient

## 1.3 ReLU (REctified Linear Unit) $f(x) = \max(0, x)$

### Description

- does not saturate in the positive region
- very computationally efficient
- converges much faster than sigmoid/tanh in practice

### Problems

- not zero-centered output
- saturated neurons in the negative region
- dead ReLUs will never activate and therefore will never update

## 1.4 Leaky ReLU $f(x) = \max(0.1x, x)$

### Description

- does not saturate
- computationally efficient
- converges faster than sigmoid/tanh in practice
- will not die