Regularization in neural networks

Definition

A process of introducing additional information in order to solve an ill-posed problem or to prevent overfitting. It penalizes the loss function by adding a multiple of an L1 (Lasso) or an L2 (Ridge) norm of your weights vector w.

Why

Solve the overfitting problem.

Formulation

Cost function over *m* training examples

$$\frac{1}{m}L(\widehat{y}^{(i)},y^{(i)}) + \lambda * R(w)$$

Hyperparameters

• λ : the regularization parameter

Variations

L1 regulatization

Adds the absolute values of the model's coefficients as the penalty term.

$$R(w) = \frac{1}{m} \sum_{l=1}^{L} |w^{[l]}|$$

L2 regulatization

Adds the squared magnitude of the model's coefficients as the penalty term.

$$R(w) \!=\! \frac{1}{2m} \sum_{l=1}^{L} \lVert w^{[l]} \rVert^2 \!=\! \frac{1}{2m} \sum_{l=1}^{L} \sum_{i=i}^{n^{[l-1]}} \sum_{j=1}^{n^{[l]}} (w_{ij}^{[l]})^2$$

New formula for weight update

$$W^{[l]}\!=\!W^{[l]}-\alpha*dW^{[l]}\!=\!W^{[l]}-\alpha*(amount\:from\:backprob\:+\tfrac{\lambda}{m}W^{[l]})$$

Elastic net (L1 + L2)

Adds both L1 and L2 penalities.

$$R(w)\!=\!\sum_{l=1}^L\!\!\sum_{i=1}^{n^{[l-1]}}\!\!\sum_{j=1}^{n^{[l]}}\!\!\left(\beta*(w_{i,j}^{[l]})^2+|w_{i,j}^{[l]}|\right)$$