Special Pythagorean Triplet

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1 Euclid's formula

Euclid's formula is a formula for generating Pythagorean triples given an arbitrary pair of integers (m) and (n) with (m > n > 0). The formula states that the integers

$$a = m^2 - n^2$$
, $b = 2mn$, $c = m^2 + n^2$

form a Pythagorean triple.

2 Calculations

$$a + b + c = 1000$$

$$m^{2} - n^{2} + 2mn + m^{2} + n^{2} = 1000$$

$$2m^{2} + 2mn = 1000$$

$$m^{2} + mn = 500$$

$$m(m + n) = 500$$

We know $23^2 = 529$, therefore $m \le 22$ and if m = 22 and n = 1, the lowest value that n can assume, we have:

$$m(m+n) = 22(22+1)$$

= 22×23
= 506

Therefore, $m \le 21$.