

Formal Semantic

1. [12 points] Translate the following sentences into quantified formulas of first-order logic:

a. Angus likes someone and someone likes Julia.

$$\exists x \text{ likes}(\text{Angus}, x) \wedge \text{likes}(x, \text{Julia})$$

b. Nobody smiles at Pat.

$$\neg (\exists x \text{ smiles-at}(x, \text{Pat}))$$

c. Nobody coughed or sneezed

$$\neg (\exists x \text{ coughed}(x) \vee \text{sneezed}(x))$$

2. [12 points] Translate the following *verb phrases* using λ -abstracts and quantified formulas of first-order logic:

a. feed Cyril and give a compliment to Angus

$$\lambda x \text{ act}(x, \text{feed}), \text{feeder}(x), \text{fed}(\text{Cyril}) \wedge \lambda y \text{ act}(y, \text{compliment}), \text{complimentor}(y), \text{complimented}(\text{Angus})$$

b. be loved by everyone

$$\lambda x \forall y \text{ act}(x, \text{be-loved}), \text{being-loved}(x), \text{lover}(y)$$

c. be loved by everyone and detested by no-one

$$\lambda x \forall y \text{ act}(x, \text{be-loved}), \text{being-loved}(x), \text{lover}(y) \wedge \neg (\exists y \text{ act}(x, \text{be-detested}), \text{being-detested}(x), \text{detester}(y))$$

3. [6 points] Let $g = \text{chase}$ and $h = \lambda x. \forall y. (\text{dog}(y) \Rightarrow \text{chase}(x, y))$.
If $h = f(g)$, write down a λ -abstract for f .

$$f = \lambda x. \lambda w. \forall y. (\text{dog}(y) \Rightarrow w(x, y))$$

4. [7 points] Let
 $g = \text{give}$ and $h = \lambda z. \lambda x. \exists y. (\text{present}(y) \wedge \text{give}(x, y, z))$
 $h = \lambda z. \lambda x. \exists y. (\text{present}(y) \wedge \text{give}(x, y, z))$.
 If $h = f(g)$, write down a λ -abstract for f

$$f = \lambda z. \lambda x. \lambda w. \exists y. (\text{Present}(y) \wedge w(x, y, z))$$