# Deep Learning to Scale up Time Series Traffic Prediction

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Abstract—The transport literature is dense regarding shortterm traffic predictions, up to the scale of 1 hour, yet less dense for long-term traffic predictions. The transport literature is also sparse when it comes to city-scale traffic predictions, mainly because of low data availability. The main question we try to answer in this work is to which extent the approaches used for short-term prediction at a link level can be scaled up for long-term prediction at a city scale. We investigate a city-scale traffic dataset with 14 weeks of speed observations collected every 15 minutes over 1098 segments in the hypercenter of Los Angeles, California. We look at a variety of state-of-the-art machine learning and deep learning predictors for link-based predictions, and investigate ways to make such predictors scale up for larger areas, with brute force, clustering, and model design approaches. In particular we propose a novel deep learning spatio-temporal predictor inspired from recent works on recommender systems. We discuss the potential of including spatio-temporal features into the predictors, and conclude that modelling such features can be helpful for long-term predictions, while simpler predictors achieve very satisfactory performance for link-based and short-term forecasting. The trade-off is discussed not only in terms of prediction accuracy vs prediction horizon but also in terms of training time and model sizing.

Keywords: time series, traffic prediction, graph convolutional neural networks, feedforward neural networks, recurrent neural networks, autoregressive models.

#### I. Introduction

Traffic prediction in urban transport networks is a central task for the real-time operation of transportation systems, such as route planning, route guidance, on-demand mobility services Simonetto et al. (2019). In principle this task can be achieved with the help of an increasing large volume of observed traffic data that can be made available through, e.g., on-road sensors, GPS data, cameras, social media Zhu et al. (2019). In reality, the access to such data is limited as big traffic data sets are generally owned by specific companies and deemed as proprietary information and a valuable source of business.

Despite the limited availability of such data sets, there has been a constant interest in the transport and intelligent systems literature to develop forecasting methods for the prediction of traffic conditions, mainly traffic speeds. Traffic prediction is inherently a challenging problem, because of the high non-linearity of traffic variables, the sparsity of data Abadi et al. (2014), Abadi et al. (2015), Hofleitner et al. (2012), the spatio-temporal dependencies, the short vs long term dynamical effects, and the computational challenges of its application to large-scale networks. In order to be suitable

for practical implementation, predictions should be obtained in a reasonably fastand accurate manner, and the models used to make such predictions should scale up with the size of the geographic area under consideration.

Short-term time series traffic forecasting has been shown to be well handled via autoregressive models, in particular the univariate (seasonal) autoregressive integrated moving average (SARIMA) class of models Box et al. (2015). Such models are able to capture the strong autocorrelations in the evolution of speeds, as well as the cyclic patterns of traffic over time, and typically outperform pure linear regression, historical average, and non-parametric regression Smith et al. (2002), for predictions of no more than 1 hour. This class of models can be extended to the consideration of spatial dependencies with the vector autoregressive (VAR) and vector autoregressive with moving average (VARMA) models and their use may result in an improvement in the accuracy of the predictions Chandra & Al-Deek (2009). Possible improvements to accuracy can be found via multivariate approaches, although they might be computationally demanding Ghosh et al. (2009), Stathopoulos & Karlaftis (2003). Gradient boosting has also been adopted for shortterm traffic predictions Zhang & Haghani (2015), demonstrating to require modest data preprocessing, to fit complex nonlinear relationship, and to provide interpretable results.

The advent of deep learning techniques and their easy API access through the many wrappers to TensorFlow have led researchers into systematically contemplating them as plausible solution to the spatio-temporal traffic forecasting problem. Lv et al. (2015) proposed a stacked autoencoder model to consider the spatial and temporal correlations of traffic flow inherently. Spatio-temporal predictors can be enhanced with attention functions Do et al. (2019), or ensembled in convolutional models Liu et al. (2020). Short-term traffic flow prediction is performed in Polson & Sokolov (2017) on a 21-loop network via a multi-layer perception models. Spatio-temporal relations are captured by solving a prediction selection problem. The long term dependency of traffic predictions has also been taken into account in the Long Short-Term Memory Neural Network model Ma et al. (2015), Vinayakumar et al. (2017). Integrating spatial and exogenous dependencies of traffic predictions into LSTM architectures is an active research topic Ke et al. (2017).

In the deep learning applications, particularly speech, video, and image processing, the use of convolutional units has been shown to achieve remarkable results in terms of accuracy and scalability LeCun et al. (1995). Therefore, there is

a growing interest in applying convolutions to consume data with a clear grid-structured topology. In the Residual Neural Network framework of Zhang et al. (2017), the convolutional units model the spatial properties of the crowd flows. An emerging deep learning architecture is the Graph Convolutional Neural Network (GCNN) Bruna et al. (2014). GCNNs extend the Convolutional Neural Network architecture to cope with spatial features on graphs. A spectral construction of GCNN, which builds upon the properties of convolutions in the Fourier domain is applied to traffic forecasting in Yu et al. (2018). The model is effectively applied to networks with up 1,026 stations of speed measurement for predictions in a 45 minutes horizon. Zhang et al. (2019) proposed the use of wavelet decomposition to capture multiple time-frequency properties in a similar GCNN-based spatio-temporal model, that beat state-of-the art results on a dataset for short term traffic prediction. An effort to make the convolutional approach more scalable appears in Kipf & Welling (2016), and was applied successfully to traffic prediction in Zhao et al. (2019). The GCNN combined with gated recurrent units achieved remarkable results in terms of robustness and accuracy for predictions with up to 1 hour ahead. Finally, the GCNN of Ying et al. (2018), though not related to traffic forecasting, is of interest because of the large size of the network under test: by applying localized graph convolution, recommender systems with 7.5 billion training examples are built.

In this work we test several known time-series predictors for long-term forecasting, including contextual average model, autoregressive models, decision tree models, multi-layered perceptrons, and long short-term memory networks. The accuracy of the various predictors is evaluated at the link level and the relevance of the deep learning techniques is highlighted. We discuss a number of possibilities to scale up the deep learning techniques to the network level, where performance is sometimes achieved at the expense of accuracy. Finally, a spatio-temporal deep learning predictor relying on graph convolutional neural network architecture is proposed, achieving a satisfactory accuracy/performance trade-off.

The contributions of our approaches with respect to the current literature are: (i) we run a first comparative benchmarking study of traffic prediction models on a large-scale road network; (ii) we focus on the long term traffic prediction task, e.g. up to 3 hours ahead, and show the competitiveness of deep learning algorithms at the link level; (iii) we investigate how deep learning can be used to scale up traffic predictions at the network level; (iv) we show that an integrated Graph Convolutional Network architecture may serve as a compromise for city-scale traffic prediction.

# II. THE DATASET

## A. The dataset

The data set was made available to us through The Weather Company, an IBM business. We do not have agreement to share the data, however we believe that the findings presented in this work are valuable to the research community, as traffic data sets become increasingly available (see, e.g., the repository World traffic data (2019)). For the purpose of this work we selected a geographic area of Los Angeles inner city using the bounding box defined by the 4 latitude and longitude coordinates: north 34.047252, south 34.000675, east -118.244915, west -118.338785. This bounding box includes 1220 road segments, belonging to local roads, arterial roads, and highways. We gathered 14 weeks of speed observations data from Sunday 22 July 2018 00:00 to Saturday 28 October 2018 23:45. The speed observations come for all the segments at a frequency of 15 min, but there are some processing delays leading to uneven frequencies. Such speed observations are computed by averaging speeds of the vehicles transiting via a given segment over a window of 15 minutes. Speed observations are reported in km/h throughout the paper.

## B. Processing methodology

The data set requires some preprocessing prior to its utilization. We should mention that we proceed with the following steps: (i) removal of default average speeds used as instantaneous speeds; (ii) linear interpolation for missing speeds; (iii) time step regularization with linear interpolation to deal with shifted timestamps; (iv) optional low-pass filter to deal with high-frequency noise in the data set.

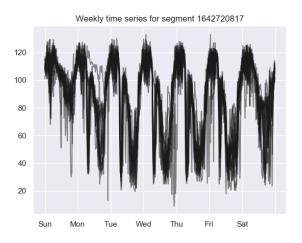


Fig. 1. Cumulative weekly time series for the 14 weeks of data, segment 1642720817. Speed values are given in km/h.

Note also that, if used, the low-pass filter needs to be carefully chosen, i.e. so as to remove high frequency but not to smooth out congestion transition regimes and therefore not to alter the physics of traffic speeds evolution. Figure 1 shows the cumulative weekly time series of the corrected speed observations. Since human mobility is a highly predictable phenomenon, up to 93% following the work of Song et al. (2010), it is interesting to look at the weekly patterns observed across the 14 weeks of the data set. The figure clearly shows the existence of predictable patterns in the data

set for the same selected segment. We must remark that such patterns are not always that obvious across segments. Finally, only the segments with missing values that account for less than 20% of the time series were considered. Starting from 1220 segments in the Los Angeles selected bounding box, this boils down to 1098 segments with enough observations.

## C. Stationarity and periodicity

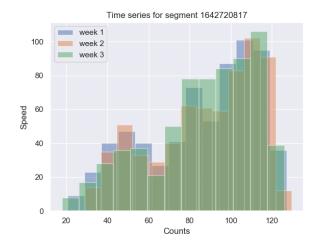
A first analysis prior to applying autoregressive models consists in looking at the time series observations, particularly at their stationarity and periodicity properties. The stationarity aims at saying if a preprocessing step is required before using autoregressive models, e.g. the integrated part of the class of seasonal autoregressive integrated moving average models Box et al. (2015). A common way of investigating the stationarity of the time series is to look at speed distributions across weeks. Here, as expected for the speed traffic variable, in Figure 2 (top) we see little variation of such distributions. The periodicity can be used for feature selection in feed-forward neural networks, or as a necessary preliminary step to applying seasonal autoregressive integrated moving average models Box et al. (2015). The autocorrelation plot Figure 2 (bottom) is of great use, and unsurprisingly exhibits strong positive correlations for periods of 24 hours and negative correlations for periods of 12 hours. This preliminary time series analysis is representative of all the segments in the considered bounding box, and will be used in the discussions of the next sections.

### III. TIME SERIES TRAFFIC PREDICTION

Time series forecasting consists in predicting the most likely measurements in a given time horizon of  $1, \ldots, h$  time steps given the previous available m observations. We write  $\mathbf{x}_t \in \mathbb{R}^N$  the vector of measurements of all N links at a given time  $t, \mathbf{x}_t = [x_{1,t}, \ldots, x_{N,t}]^T$ . The links are connected through the graph of the road network denoted  $\mathcal{G} = (\mathcal{N}, \mathcal{L}, \mathcal{W})$ , with  $\mathcal{N}$  the set of all nodes,  $\mathcal{L}$  the set of all links indexed by  $1, \ldots, N$ .

The univariate forecasting problem for link  $i \in \mathcal{L}$  consists in finding the estimates  $\hat{x}_{i,t+1}, \ldots, \hat{x}_{i,t+h}$  maximising the probability  $p(x_{i,t+1}, \ldots, x_{i,t+h} | x_{i,t-m+1}, \ldots, x_{i,t})$ , whereas the multivariate forecasting problem searches for the estimates  $\hat{\mathbf{x}}_{t+1}, \ldots, \hat{\mathbf{x}}_{t+h}$  maximising the probability  $p(\mathbf{x}_{t+1}, \ldots, \mathbf{x}_{t+h} | \mathbf{x}_{t-m+1}, \ldots, \mathbf{x}_t)$ .

We will see that for each selected algorithm, for obvious scalability reasons, we do not feed all the available m observations to make predictions, hence input feature selection is an important part of the algorithm configuration Kwak & Choi (2002), and we shall rely partly on domain knowledge for this.



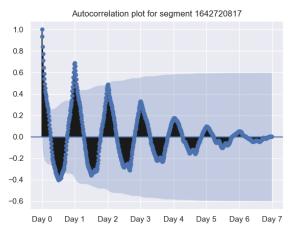


Fig. 2. Distributions of speeds for the first 3 weeks of the data set, segment 1642720817 (top). Autocorrelation plot for the first week of the data set, segment 1642720817 (bottom). Speed values are given in km/h.

## A. Clustering time-series

We explore time-series clustering as a potential prior step to the design of forecasting models. Note that the incorporation of clusters into the predictors will be done in ad-hoc or integrated way depending on the predictor itself. Note we do not perform spatio-temporal clustering despite recent works advocating for its promises Lopez et al. (2017), Pascale et al. (2015), as we aim to perform a regression task and not a classification one. Instead, we explore time series clustering for model sizing, as well as to investigate how it can help refining the prediction accuracy, particularly in the case of spatio-temporal predictors.

Specifically, for clustering we consider the standardized observations on the validation week for all 1098 links of the LA area and use a wavelet decomposition technique. We applied the Daubechies 6 wavelet to the time series to obtain the features of each link, which are the relative contributions of maximum resolution level J introduced in Antoniadis et al. (2013). In detail, given the wavelet coefficients  $\mathbf{d}_j = \{d_{j,0}, \dots, d_{j,2^j-1}\}_{j=0,\dots,J-1}$  of time series z,

the relative contributions of the scale j to the global energy of z via wavelet decomposition are

$$\operatorname{rel}_{j} = \frac{\|\mathbf{d}_{\mathbf{j}}\|^{2}}{\sum_{j=0}^{J-1} \|\mathbf{d}_{\mathbf{j}}\|^{2}} \quad j = 0, \dots, J-1.$$

The 3 features with lowest frequency are retained, as Antoniadis et al. (2013) shown them to be the most informative ones. Finally, we use a K-means clustering with input given by the features selected, in order to determine the clusters of links. The optimal number K=9 of clusters is detected by examining the elbow curve and silhouette scores obtained for a number of clusters up to 50.

## B. Baseline time-series predictors

We now present state-of-the-art predictors and how we used them in the context of this work. Note that the list of baseline predictors we consider here is not meant to be exhaustive, as other univariate models such as tree-based ensemble methods Zhang & Haghani (2015), generative additive models Dominici et al. (2002) could be used. Note that the list of baseline predictors we consider here is not meant to be exhaustive, but significant enough. In this section, t-d will denote the time step of the same time t the day before, and t-w the time step of the same time the week before.

1) Contextual average model: this model is the simplest possible, and consists in computing the plain average over the history of data points. With  $N_w$  being the number of weeks for which we have link-based historical data, we have  $\forall i \in \mathcal{L}$ ,

$$x_{i,t+k} = \frac{\sum_{j=1}^{N_w} x_{i,t-j\cdot w+k}}{N_w}, \quad k = 1, \dots, h.$$

2) Autoregressive models: for the literature on autoregressive models for time series forecasting the interested reader can refer to the book of Box et al. (2015).

In this work we consider the univariate autoregressive integrated moving average ARIMA-(p,d,q) model which is defined as a cascade of two models:

$$y_{i,t} = (1 - L)^{d} x_{i,t},$$

$$\left(1 - \sum_{j=1}^{p} \phi_{i} L^{j}\right) y_{i,t} = \left(1 + \sum_{j=1}^{q} \theta_{i} L^{j}\right) \epsilon_{i,t},$$

with L being the lag operator, i.e.  $L^j y_{i,t} = y_{i,t-j}$ , and  $\epsilon_{i,t}$  are the residuals assumed to be i.i.d. and sampled from a normal distribution with zero mean and standard deviation  $\sigma$ . The seasonal variant of the ARIMA model is written SARIMA- $(p,d,q) \times (P,D,Q)_S$ , with S the lag of the seasonality, typically of 7 days in the traffic prediction case. We can remark that such models are mostly used for short term forecasting, i.e. 1 step ahead forecasting, as the variance of the forecast error increases with the time horizon h. Note also that a multivariate extension of these models is the vector autoregression VAR-(p) model which

describes the evolution of stacked endogeneous variables. As this approach suffers scalability issues and its endogeneous assumption is not valid for the small city regions for which it scales, we leave it aside in this work.

- 3) Support Vector Regression: support-vector machines (SVM) have been introduced for binary classification, but received considerable attention for regression tasks Smola & Schölkopf (2004). The goal of support vector regression (SVR) is to find a function  $f(x) = w \cdot \Phi(x) + b$  that can approximate the relationship between features  $x_i \in \mathbb{R}^n$  with label  $y_i \in \mathbb{R}$ , on training points  $i = 1, \ldots, l$ . The non linear transformation  $\Phi$  maps  $R^n$  to a higher dimensional space. SVR is achieved by minimizing the regression risk  $C\sum_{i=1}^{l} (\Gamma(f(x_i) y_i)) + 1/2||w||^2$ , with C hyperparameter, and  $\Gamma$  cost function. Kernel functions are typically used to solve the optimization problem. We have followed Wu et al. (2004) to apply SVR to the traffic speed prediction.
- 4) Gradient boosting (GB): we look into ensemble models and more precisely into boosting algorithms, as a way to get a better performance and get a better bias. In boosting, weak learners are trained on sampled parts of the dataset and combined in an iterative way so as to get a strong learner. In this work, we selected gradient boosting Friedman (2001) where we use  $[1, \ldots, M]$  sampled datasets.  $\forall i \in [1, \ldots, M]$ , we compute the loss function  $L^i(y_j, F^i(\mathbf{x}_j))$  typically of the least square form  $\sum_{j=1}^n (y_j F^i(\mathbf{x}_j))^2$ , and we fit an estimator  $H^i$ , typically a shallow regression tree, to the gradient of the loss function  $\partial L^i/\partial \mathbf{x}_j$ . Then the predicted estimator becomes  $F^m(\mathbf{x}) = F^0(\mathbf{x}) + \rho \sum_{i=1}^m H^i(\mathbf{x})$ , where  $F^0(\mathbf{x})$  is an initial guess and  $\rho$  is the learning rate.
- 5) Deep Learning time-series predictors: we work with the windowed Multi-Layer Perceptron (MLP) and the Long Short Term Memory (LSTM) neural networks. Such models have proven to be relevant for time series forecasting, and a consensus is that recurrent networks should be tried if the simpler windowed feed-forward neural networks fails Gers et al. (2002). In fact, when the time series prediction task does not require RNNs, it is because all relevant information about the immediate future is contained in appropriately selected time windows.
- a) Link-based windowed MLP: the idea is to feed in the relevant input features only to the feed-forward network that will in turn learn complex dependencies with such features. Let  $w_n$  the selected time window for the previous hours,  $w_d$  the selected time window for the day before, and  $w_w$  the selected time window for the week before. Hence the vector of relevant speed observations is the stacked vector made of the weekly window  $X_{w,i,t} = \begin{bmatrix} x_{i,t-w-w_w+1}, \dots, x_{i,t-w+w_w} \end{bmatrix}^T$ , the daily window  $X_{d,i,t} = \begin{bmatrix} x_{i,t-d-w_d+1}, \dots, x_{i,t-d+w_d} \end{bmatrix}^T$ , and the previous observations window  $X_{n,i,t} = \begin{bmatrix} x_{i,t-w_n+1}, \dots, x_{i,t} \end{bmatrix}^T$ . In our case, we also consider a vector of contextual features  $C_t$ . In principle we have 2 contextual features, namely time of the day, day of the week, that we feed into the network under

a cyclical form. This is done to help the network condition the weights on the context.

Hence, the vector of input features  $I_{i,t}$  at a given time t is written  $I_{i,t} = [X_{w,t}^T, X_{d,t}^T, X_{n,t}^T, C_t^T]^T$ . This input passes through the network, layer by layer, until it arrives at the outputs of dimension h. For instance, with a vector of input features in  $\mathbb{R}^{d_0}$ , with  $d_0 = w_n + 2w_d + 2w_w + 3$ , the output of the first layer will be  $O_{1,i,t} = f_{1,\theta_1}(I_{i,t}) = f(W_1 \cdot I_t + b_1)$ , with  $W_1 \in \mathbb{R}^{d_0 \times d_1}$  and  $b_1 \in \mathbb{R}^{d_1}$  the weights and biases to be learned, and with  $f_1$  being the activation function. The final output  $O_{L,i,t}$  is of dimension h, with L is the number of layers in the feed-forward network. The training will aim to provide the vector of parameter estimates  $\hat{\theta}_1, \ldots, \hat{\theta}_L$ , and then the learned model can be scored to provide the best estimate,  $\forall i \in \mathcal{L}$ ,

$$\langle \hat{x}_{i,t+1}, \dots, \hat{x}_{i,t+h} \rangle = f_{L,\hat{\theta}_L} \circ \dots \circ f_{1,\hat{\theta}_1}(I_{i,t}).$$

b) Link-based LSTM: although recurrent neural networks are the natural way of modelling time series, they inevitably suffer from the gradient vanishing problem Hochreiter et al. (2001) when it comes to learning long-term dependencies. In practice, this can be avoided with LSTM networks Hochreiter & Schmidhuber (1997) which essentially introduces a cell state that keeps relevant information flowing along the network. For the given input feature  $I_{i,t}$ , an example of forward pass through a LSTM layer is written:

$$\begin{split} f_t &= \sigma_g(W_f I_{i,t} + U_f h_{t-1} + b_f), \\ i_t &= \sigma_g(W_i I_{i,t} + U_i h_{t-1} + b_i), \\ o_t &= \sigma_g(W_o I_{i,t} + U_o h_{t-1} + b_o), \\ c_t &= f_t * c_{t-1} + i_t * \sigma_h(W_c I_{i,t} + U_c h_{t-1} + b_c), \\ h_t &= o_t * \sigma_h(c_t), \end{split}$$

where \* is the Hadamard product,  $\sigma_g$  and  $\sigma_c$  are the sigmoid and hyperbolic tangent function,  $h_t$  is the vector of hidden states that can in turn be fed into a dense layer to obtain the vector of outputs of dimension h. Note that in this work, only link-based LTSM models are considered given their already large computational training time. Note also that we do not consider the promising attention-based RNN, see e.g. Do et al. (2019).

# C. Scalable Deep Learning time-series predictors

In this section, we propose a few Deep Learning architectures, in an attempt to move away from the link-based models presented so far, towards spatio-temporal models. From a practical perspective, this means fewer models to train and maintain, while there is the hope of a better performance given that we train on spatial dependencies.

1) Cluster-based MLP (C-MLP): we make use of the time series clustering of Section III-A by learning a model for each cluster k in the set of clusters C. Denoting  $L_k$  the set of links in the cluster k, we treat the relevant speed observations of each link in  $L_k$  as additional data points to

learn the unique model for k. Then after having estimated  $\hat{\theta}_1, \dots, \hat{\theta}_L$  for the given number of layers L, then the learned model can be scored in a univariate fashion to provide the best estimate, and we have  $\forall i \in \mathcal{L}_k$ ,

$$\langle \hat{x}_{i,t+1}, \dots, \hat{x}_{i,t+h} \rangle = f_{L,\hat{\theta}_L} \circ \dots \circ f_{1,\hat{\theta}_1}(I_{i,t}).$$

- 2) Area-based brute force MLP (B-MLP): a naive approach for MLP architectures consists in augmenting the input feature space by the number of links in the network, hence we have,  $\langle \hat{\mathbf{x}}_{t+1}, \dots, \hat{\mathbf{x}}_{t+h} \rangle = f_{L,\hat{\theta}_L} \circ \dots \circ f_{1,\hat{\theta}_1}(I_t)$ , where the stacked input feature vector is now written  $I_t = \begin{bmatrix} I_{1,t}^T, \dots, I_{N,t}^T \end{bmatrix}^T$ . Note that this approach does not increase the number of parameters comparing to the link-based MLP model as the set of weights is applied by the framework to all stacked feature vectors. This is the advantage of this method as the model size stays the same, which leads to the same scoring time per link.
- 3) Spatio-temporal deep learning predictor: the brute force MLP and cluster-based MLP offer relatively okay scalability at the expense of accuracy, as for the B-MLP a brute-force average model is in fact learned per link, and as for the C-MLP inter cluster dependencies are not modelled and spatial information, if considered, is embedded into temporal information. In order to circumvent such problems, here we introduce a scalable deep learning predictor that make use of spatio-temporal convolutions in the road network graph.

The architecture we present is novel, however we should remark here that it gets its inspiration from the hyper large-scale use of GCNN for web-scale recommender systems Ying et al. (2018), and from the use of a MLP-derived CNN architecture for city-wide crowd prediction Zhang et al. (2017). Because we are more interested into scalability and accuracy than proper mathematical derivation, we step away from the elegant graph convolutional works that use graph Laplacians to define convolutional operators in the Fourier domain, e.g. as proposed initially in Defferrard et al. (2016) as well as in the context of traffic predictions Zhao et al. (2019). In fact, making use of such a convolutional operator requires computing the eigenvalues and eigenvectors of the Graph Laplacian which is simply not scalable for networks with thousands of nodes. The work of Kipf & Welling (2016) proposes a first-order approximation, which only requires to know the adjacency and degree matrices of the graph. Their defined convolutional operator has 2 main differences with our proposed operator: first, due to the presence of the adjacency matrix in the operator, each layer acts upon its neighbours only, hence with a two-layer model the output of a node can only be affected by nodes in a 2-hop neighborhood, and that means many layers are needed to capture long spatial dependencies; and second, the operator does not capture distances between links.

In the architecture we propose, the input features combine the road network graph structure with the relevant traffic observations, as per the MLP link-based model. For a given link l, we consider the k nearest incoming links,  $(l_1^i, \dots, l_k^i)$ ,

and k nearest out-going links,  $(l_1^o, \cdots, l_k^o)$ , where  $k \in \mathbb{N}^*$  (here k = 5). The distance function d used here is defined as follows. For two links l, with center node O, and l', with center node O', the distance d(l, l') between l and l' is defined as the length of the shortest directed path connecting nodes O and O'.

Based on the selection of k nearest incoming links and k nearest outgoing links, we build an input tensor as illustrated in Figure 3. For the sake of clarity, in this Figure, we only show the input tensor for the previous observations window  $X_{n,i,t} = \left[x_{i,t-w_n+1},\ldots,x_{i,t}\right]^T$ . We remind that  $w_n$  is the length of the selected time window for the previous hours, and here  $x_t(l)$ , equivalently to  $x_{l,t}$ , denotes the speed observed for link l, at time step t.

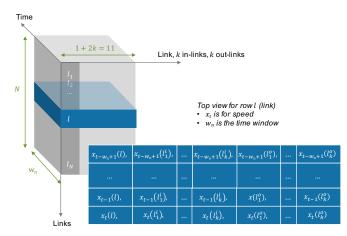


Fig. 3. GCNN Input Tensor.

With this input tensor we can then proceed with 2D and 3D convolutions. The 2D convolutions have a Kernel size of  $(2k+1) \times I$ , the 3D convolutions of  $1 \times (2k+1) \times I$ , where I is an integer which size varies across convolutional layers. The weights of the 2D convolutions are different across channels (links) whereas for 3D convolutions they are shared across links. Differently to a typical convolutional layer, no pooling is performed. In fact, we want to perform a regression task and the input tensor is shrunk until we get to a matrix of dimensions  $N \times h$  . Starting from the input feature tensor of dimension  $N \times (2k+1) \times W$ , with  $W = w_n + w_d + w_w$ , after one convolution, we get a tensor of dimension  $N \times 1 \times (W - I + 1)$ . After the standard ReLU activation unit there is a customized concatenation phase that reconstructs the tensor of dimension a tensor of dimension  $N \times (2k+1) \times (W-I+1)$  based on the graph topology. This customized phase enables the propagation in time and space of the speed observations. Note the weights are learned over the full vector whih is composed of the link together its neighbours, differently to Ying et al. (2018) where an aggregation step is introduced with a dense layer that is used to combine the representation of the link with the representation of its neighbours, and that we tried this feature without observing significant differences in the test set accuracy. Note that the first convolutional layers are done separetely on the three input tensors consisting of  $X_{n,t}$ ,  $X_{d,t}$ , and  $X_{w,t}$ , before being concatenated (in the time dimension) together. This means that the number of convolutions will be indicated e.g. as 2+5, meaning 2 separate convolutions +5 common convolutions. Finally, after a given number of operations (convolution + ReLU+ concatenation), the tensor is augmented with the contextual features (time of the day, day of the week) and fed into a final dense layer.

## IV. COMPUTATIONAL RESULTS

## A. Experimental methodology

We have 14 weeks of data from 2018-07-22 00:00 to 2018-10-27 23:45. We propose the following evaluation methodology of the predictors. We split the data in train, validation and test datasets: 12 weeks training until 2018-10-13 23:45, 1 week validating from 2018-10-14 00:00 until 2018-10-20 23:45, and 1 week testing from 2018-10-21 00:00 until 2018-10-27 23:45. The validation dataset is used for hyperparameters tuning of all predictors via grid search.

For the link-based predictors, we present the Root Mean Square Error (RMSE) results over a time horizon of 3 hours (h=12) for 50 considered links, randomly sampled from the 1098 links under consideration. Such evaluation is done with the processed dataset as per Section II.

For the area-based predictors, we present the average of the RSME results over a time horizon of 3 hours (h=12) for the previously sampled links. Note that the predictor is trained for the 1098 links but only evaluated on the 50 sampled links, for the sake of clarity of the comparison. Again, such evaluation is done with the processed dataset as per Section II.

Note that the RMSE $_h$  is defined as

$$\text{RMSE}_{h} = \sqrt{\frac{\sum_{i=1}^{L} \sum_{t=1}^{N} (\hat{x}_{i,t}^{h} - x_{i,t}^{h})^{2}}{NL}},$$

with L=50 being the number of sampled links, and N being the total number of tested timestamps within the testing week, i.e. with N=672. We compute RMSE for each time step h, thus  $\hat{x}_{i,t}$  and  $x_{i,t}$  take values for the corresponding h. We remark that the product NL is high and that focusing on such a long testing period will have a smoothing effect on the RMSE results, as some methods compare relatively similarly for long time periods, and as some links are more predictable than others. We choose to display those results as we aim to provide an objective accuracy metrics over a long enough time period (a week), as opposed to a metrics targeting more specific time periods.

We summarize here the hyperpameters determined for each predictor:

• For the autoregressive models, the simple AR model with no integrated or moving average term was selected with 28 previous observations following the methodology in Box et al. (2015).

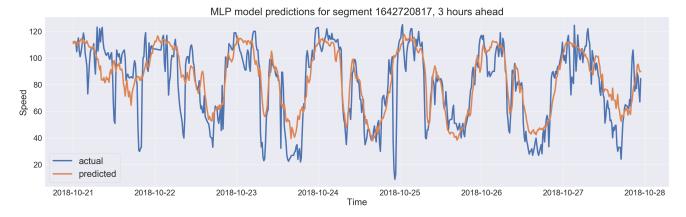


Fig. 4. MLP test results, segment 1642720817. Speed values are given in km/h.

- SVR implementation is based on the approach described in Wu et al. (2004) with the window size of 16 and the RBF kernel instead of a linear one.
- GB has been implemented in XGBoost considering techniques from Zhang & Haghani (2015), with maximum depth of a tree of 5, 200 trees to fit, 16 previous observations considered in the feature set, and the training has been performed with a learning rate of 0.1.
- For LSTM (described in Hochreiter & Schmidhuber (1997)) 24 previous observations have been considered in the feature set, and an architecture with 2 layers and 192 hidden states has been trained with mini-batches of size 50, learning rate 0.002 and 40 epochs.
- For the link-based MLP predictor, (inspired by Zhang et al. (2017)) the feature set contains observations in the previous w<sub>n</sub> = 6 hours (24 observations in a sample), in the time window of w<sub>d</sub> = 2 hours of the day before (16 observations), and in w<sub>w</sub> = 1 hour in the week before (8 observations). The number of layers has been set to 5, and the training is conducted with batch size of 150, learning rate of 0.0005, and weight decay factor of 0.0002. The number of epochs is optimized for each link via early stopping, and is consistently lower than 200. For the brute-force approach, the number of layers was increased to 10.
- For the cluster-based MLP, the feature set contains observations in the previous  $w_n=4$  hours (24 observations in a sample), in the time window of  $w_d=2$  hours of the day before (16 observations), and in  $w_w=2$  hour in the week before (8 observations). The training has been done on 80 epochs and a batch size of 100 for all clusters, on the same MLP architecture of the link-based predictors.
- For the GCNN, due to the higher computational time, we use the same feature set as the link-based MLP algorithm, which contains observations in the previous  $w_n=6$  hours, in the time window of  $w_d=2$  hours of the day before, and in  $w_w=1$  hour in the week before. The number of convolutional layers was determined

to be 5 + 4, with the first convolution being 2D and the rest 3D, and the Kernel parameter values I slowly decreasing from 5 to 2 with strides of 1. The training was done on 70 epochs with a batch size of 150.

As an example, on Figure 4 we show predictions produced by the MLP model for the chosen segment on the test data set. This figure represents traffic speed predictions made at a time of three hours ahead of the recent observations. Obviously, the MLP model was able to capture weekly patterns and provide reasonable predictions on a long term perspective.

## B. Trade-off: prediction accuracy vs prediction horizon

Table I summarizes the results, and the lowest RMSE reported among all predictors is marked in bold. The baseline indicates the contextual average model. All predictors are more accurate than the baseline in the first 4 time steps. GB and MLP are consistently better than the baseline, especially in the first 3 time steps, where GB achieves an RMSE reduction of more than 10%, and MLP of more than 20%. AR reports a 2.15% increase of RMSE in step 5, and the deviation to the baseline increases for longer term predictions, reaching a 14.90% increase at the last time steps. Despite SVR achieves results comparable to the best of the neural networks on the first step, the overall growth of RMSE is still high and at the end of the time horizon the results are comparable to the baseline while at the last two time steps RMSE values are higher than the baseline (less than 1%). B-MLP and C-MLP are more accurate than baseline for short-term predictions, while they report a greater RMSE after the 6-th time step. C-MLP is consistently more accurate than AR in all time steps, apart from the first one, where C-MLP is 2.14% less accurate. The difference between the RMSE of C-MLP and MLP reaches maximum value of 17.21% on the last time step. Interestingly the GCNN model reports the lowest RMSE for predictions on 2 hours ahead and the following ones. LSTM provides the best predictions for step 7 (along with GCNN), and performs slightly worse than GCNN for the

Method	$RMSE_h$											
Method	1	2	3	4	5	6	7	8	9	10	11	12
Baseline	8.37	8.38	8.38	8.38	8.38	8.38	8.38	8.38	8.38	8.38	8.38	8.39
AR	5.59	7.15	7.82	8.26	8.56	8.78	8.96	9.14	9.29	9.42	9.54	9.64
SVR	5.60	7.05	7.61	7.91	8.06	8.15	8.21	8.28	8.33	8.36	8.39	8.41
GB	5.42	6.85	7.39	7.61	7.76	7.83	7.90	7.92	7.93	7.96	7.98	8.00
MLP	5.58	6.82	7.27	7.50	7.63	7.71	7.79	7.86	7.91	7.97	8.03	8.08
LSTM	5.60	6.87	7.31	7.53	7.67	7.73	7.77	7.82	7.85	7.86	7.88	7.90
B-MLP	6.86	7.45	7.77	8.02	8.25	8.45	8.66	8.87	9.08	9.26	9.43	9.57
C-MLP	5.71	7.09	7.62	7.96	8.24	8.45	8.66	8.86	9.04	9.21	9.35	9.47
GCNN	5.72	7.08	7.41	7.57	7.68	7.74	7.77	7.80	7.82	7.85	7.87	7.87

TABLE I: RMSE $_h$  reported for each prediction method and time step  $h=1,\ldots,12$ , on the raw dataset. The baseline predictors reported are: SVR (Wu et al. 2004), GB Zhang & Haghani (2015), AR Box et al. (2015), MLP (inspired by Zhang et al. (2017)), LSTM Hochreiter & Schmidhuber (1997).

longer term prediction. This shows that long-term predictions are more accurate when spatio-temporal dependencies are considered by GCNN. Similarly, LSTM perform better than link-based and cluster-based spatial predictors for long-term predictions, and our interpretation is that it can capture more complex temporal dependencies caused by e.g. spatial dependencies.

## C. Trade-offs: training time, model sizing, recommendations

This Section looks at the operational cost of selecting a given model e.g. in a production system. Table II summarizes training times, model sizes and number of links covered the models. We remind that N is the total number of links in the network, h the length of the prediction window. Hyperparametrization is not included in the training times, but we should keep in mind that the hyperparametrization effort grows with the number of models. Training times and model sizes are specified per model while the models spans different number of links. The AR model provides the best training time and smallest model size, however without surprise the prediction accuracy becomes worse than the baseline after 4 steps only. The SVR model training time is still very short, compared to the neural networkbased models. The drawback of SVR is the number of models needed (1 model per link and per prediction horizon), together with the large storage space needed. The GB model training time is 1.8 larger comparing to SVR but still quite short. The model suffers from the same drawbacks as SVR but to a less extent The GB model produces the best results on the very first step. The LSTM model training time is more than 6 times greater than the MLP one, and the model size is 47 larger than MLP. This is a high computational cost to pay, however the LSTM provides low RMSEs for longterm predictions. We experimented the spatial models for scalability reasons (1 or C models for the whole network), however B-MLP, C-MLP, are heavy in training and are not able to produce better accuracy results than the other predictors, excepted for the GCNN model. Their advantage lies in the decreased number of models, hence reduced hyperparametrization effort.

From a practical perspective, the MLP model may be the best trade-off considering training time, model size and overall prediction accuracy in the prediction horizon of 3 hours. Figure 4 shows that the accuracy at 3 hours, for a representative link, is still satisfactory despite other models providing slightly better accuracy. But a single MLP model still covers only one link which may be an inconvenience to maintain, when the road network grows to 1M+ links (which corresponds to the Greater Los Angeles Area). The GCNN model may naturally be the second choice in this case, as the model size is only 40 times larger than the MLP one, however GCNN can capture spatio-temporal dependencies of the whole study area, and reports the best results for long-term prediction. The drawback of the GCNN approach resides in data preparation and in the requirement of the road network as input.

Predictors	Training time	Size	# of models
SVR	28.8	8236	O(Nh)
GB	51.9	4751	O(Nh)
AR	30.2	9	O(N)
MLP	315.4	17	O(N)
LSTM	1892.6	800	O(N)
C-MLP	36147.6	10	O(C)
B-MLP	5352.2	38	O(1)
GCNN	18892.4	652	O(1)

TABLE II: The training times reported are the average training time per model in seconds. The model size reported is the average model size and is expressed in Kb.

## V. CONCLUSIONS

The implementation of transport and intelligent systems services calls for accurate and fast predictors that are able to scale to a city-level and be reliable for long trip. While short-term traffic predictions have been extensively studied with approaches such as autoregressive models, decision trees, feedforward and recurrent neural networks, in this paper we have looked into longer term predictions for a large urban area of interest. We have provided an evaluation of several literature machine learning and deep learning predictors for link-based prediction in an area with 1098 links in Los Angeles, California. We have proposed ways to make such predictors scale with brute-force, clustering, and model design methods. The conclusion are three-fold: (i) for short-term prediction and when scalability is not a concern, deep learning techniques do not appear to be particularly useful; (ii) when scalability is a concern, deep learning techniques may be used as they enable to deal with fewer models without deteriorating accuracy significantly; (iii) for long-term prediction and/or when scalability is a concern, deep learning techniques may be proven to be particularly useful. We should stress that these conclusions are valid for the dataset investigated, and may be less valid across different datasets. In our analysis, the MLP predictors provide a good trade-off between training time, model size, and accuracy. The LTSM predictors, as well

as the GCNN predictor we introduced, proved to be the most accurate predictors for prediction horizons higher than 2 hours ahead. Future work will include the adoption of other ensemble methods and different clustering methods to improve accuracy, while keeping overall performance in mind. The integration of LSTM and GCNN, which provided the best prediction results for long-term prediction, should also be investigated, also from a scalability perspective.

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