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2 Abstract

We trained a computational model (the Chunk Based Learner; CBL) on a longitudinal

4 corpus of child-caregiver interactions to test whether one proposed statistical learning

mechanism—backward transitional probability (BTP)—is able to predict children's speech

6 productions with stable accuracy throughout the first few years of development. We

predicted that the model less accurately generates children's speech productions as they grow

<sup>8</sup> older because children gradually begin to generate speech using abstracted forms rather than

specific "chunks" from their speech environment. To test this idea, we trained the model on

both recently encountered and cumulative speech input from a longitudinal child language

corpus. We then assessed whether the model could accurately reconstruct children's speech.

12 Controlling for utterance length and the presence of duplicate chunks, we found no evidence

that the CBL becomes less accurate in its ability to reconstruct children's speech with age.

Our findings suggest that BTP is an age-invariant learning mechanism.

15 Keywords: statistical learning, language learning, abstraction, developmental trajectory,

age-invariance, CHILDES, children

17 Word count: 6056

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Modeling the influence of language input statistics on children's speech production

During the first few years of life children learn the basic building blocks of the 19 language(s) around them. One way they do so is via statistical learning (SL), the process of 20 extracting regularities present in the language environment. Over the past few decades, SL 21 has become a major topic in the field of first language acquisition, ranging in application from speech segmentation (Jusczyk & Aslin, 1995; J. R. Saffran, Aslin, & Newport, 1996) 23 and phonotactic learning (Chambers, Onishi, & Fisher, 2003) to producing irregulars (Arnon & Clark, 2011), discovering multi-word structures (Bannard, Lieven, & Tomasello, 2009; Chang, Lieven, & Tomasello, 2006; Frost, Monaghan, & Christiansen, 2019), and much more (see J. R. Saffran and Kirkham (2018) for a recent review). By its nature, work in this domain is heavily concerned with at least two major topics: (1) the information available in children's language environments (the "input") from which they can pick up on patterns, 29 and (2) the precise mechanisms by which children convert these "raw" environmental statistics into internalized knowledge about language. A third issue is whether and how 31 children's SL behavior changes as they develop (Shufaniya & Arnon, 2018). The current 32 paper taps into each of these three issues: we train a computational model on a longitudinal 33 corpus of child-caregiver interactions to test whether one proposed SL mechanism—backward transitional probability (BTP)—is able to predict children's speech 35 productions with stable accuracy as they get older.

# 37 SL over development

The ability to detect and store patterns in the environment begins in infancy (e.g., S. P. Johnson et al., 2009; Kidd, Junge, Spokes, Morrison, & Cutler, 2018; J. R. Saffran et al., 1996; Teinonen, Fellman, Näätänen, Alku, & Huotilainen, 2009), continues into adulthood (e.g., Christopher M Conway, Bauernschmidt, Huang, & Pisoni, 2010; Frost & Monaghan, 2016; J. R. Saffran, Johnson, Aslin, & Newport, 1999), and crosses a range of modalities

(Christopher M. Conway & Christiansen, 2005; Emberson, Conway, & Christiansen, 2011; Monroy, Gerson, & Hunnius, 2017). However, it is still a matter of debate whether SL is an age-invariant skill or not (Arciuli & Simpson, 2011; Raviv & Arnon, 2018; J. R. Saffran, 45 Newport, Aslin, Tunick, & Barrueco, 1997; Shufaniya & Arnon, 2018). Recent work that investigates SL abilities in 5–12-year-old children suggests that, while both visual and 47 auditory SL improve with age for non-linguistic stimuli, performance stays the same across childhood for linguistic stimuli (Raviv & Arnon, 2018; Shufaniya & Arnon, 2018). From this finding, the authors conclude that SL for language might be age-invariant. On the other hand, infant SL abilities do appear to shift within the first year, both for linguistic (Kidd et al., 2018) and non-linguistic (S. P. Johnson et al., 2009) stimuli. For example, while 11-month-olds can detect and generalize over regularities in a sequence, 8-month-olds are only capable of detecting the regularities, and neither group succeeds yet at learning visual non-adjacent dependencies (see also Bulf, Johnson, & Valenza, 2011, and @slone2015infants; S. P. Johnson et al., 2009).

These changes in SL ability during infancy and early childhood may relate to changes in other fundamental cognitive skills. For example, SL-relevant brain regions, such as the pre-frontal cortex, continue maturing through childhood (Casey, Giedd, & Thomas, 2000; Diamond, 2002; Rodríguez-Fornells, Cunillera, Mestres-Missé, & Diego-Balaguer, 2009; Uylings, 2006), which may change how children attend to the linguistic information around them as they get older. Similarly, infants' long-term memory continuously improves between ages 0;2 and 1;6 (Bauer, 2005; Wojcik, 2013). Therefore, the manner in which they store linguistic regularities in long-term memory may also shift during this period. Relatedly, working memory and speed of processing change continuously throughout early childhood (Gathercole, Pickering, Ambridge, & Wearing, 2004; Kail, 1991), implying that there could be a developmental change in the rate and scale at which children can process chunks of information from the unfolding speech signal.

Continued exposure to linguistic input itself can also be an impetus for change in SL 69 ability—a view supported by multiple, theoretically distinct, approaches to early syntactic 70 learning. For example, Yang (2016) proposes that children gather detailed, exemplar-based 71 statistical evidence until it is more cognitively efficient for them to make a categorical abstract generalization. He proposes that, at that point, the learner instantiates a rule to 73 account for patterns in the data. Usage-based theories of early language development instead propose that children first learn small concrete linguistic sequences from their input that are made up of specific words or word combinations (e.g., "dog" and "I wanna"; or multi-word combinations, "where's the ..."; Tomasello (2008)). Then, over time, children are proposed 77 to form abstract schemas centered on lexical items (see also Bannard et al. (2009) and Chang et al. (2006)). This representational shift, from probabilistic and lexical to abstract and syntactic, is used to account for how children can eventually create utterances that they have never heard before. Crucially, the representational shift implies a change in the way children apply the original SL mechanism(s) to incoming linguistic information (see also Lany & Gómez, 2008). 83

Change in SL ability following further linguistic experience is also predicted in models
that do not assume abstraction. In chunk-based models of language learning (Arnon,
McCauley, & Christiansen, 2017; M. H. Christiansen & Arnon, 2017; M. H. Christiansen &
Chater, 2016; Misyak, Goldstein, & Christiansen, 2012; StClair, Monaghan, & Christiansen,
2010), children use statistical dependencies in the language input (e.g., between words or
syllables) to store chunks of co-occurring forms. Dependencies between the chunks
themselves can also be tracked with continued exposure and chunk storage (see, e.g., Jost
& Christiansen, 2016). In this case, the development of a detailed chunk
inventory can gradually change overt SL performance. Fundamentally, however,
this apparent change in SL still comes through the use of the original underlying
mechanisms (Misyak et al., 2012); there is no qualitative change in how the system
processes data, and the mechanisms for processing, storing, and deploying information

96 stay the same.

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We investigated the possibility of developmental change in SL using computational 97 modeling, which enables us to define and test the goodness-of-fit for any given learning mechanism on a dataset of natural speech. We chose to use a longitudinal child language 99 dataset, in which the same children were tracked across the developmental period of interest 100 for early speech production (1:0-4:0). By choosing data in this age range, we could test 101 whether use of a learning mechanism changed for each child across the studied developmental 102 time points. We tested for developmental change in the use of a single proposed statistical 103 learning mechanism: backward transitional probability (McCauley & Christiansen, 2011; 104 Onnis & Thiessen, 2013; Pelucchi, Hay, & Saffran, 2009; Perruchet & Desaulty, 2008). 105

## 106 BTP and the Chunk-Based Learner

Our model is based on McCauley and Christiansen's (2011, 2014a) Chunk-Based
Learner (CBL) model, which uses one measure—backward transitional probability—to
detect statistical dependencies in the speech stream. BTP for a given pair of words is defined
as the occurrence probability of the previous word  $(w_{-1})$  given the current word  $(w_0)$ . It can
be estimated for each word in a sentence in order to reveal peaks and dips in transitional
likelihood, which reflect places where words are likely (peaks) or unlikely (dips) to co-occur.

The CBL model divides utterances into chunks, splitting the utterances whenever the
BTP between two words drops below the running average BTP. In the example in Figure 1,
the CBL might decide to split the sentence ("did you look at the doggy") into three chunks
"did you", "look at", and "the doggy", and store all three in its memory. As it sees more
sentences, it would continue to add new chunks and track how often they co-occurred.

The CBL was developed to model children's early speech production and comprehension without appealing to abstract grammatical categories. Specifically, it was

# # did you | look at | the doggy

(BTP) 0.96 0.88 0.34 0.92 0.23 0.87

Figure 1. Example of a sentence with BTP between consecutive words. Chunks are split at points of low BTP (indicated by the vertical lines). "#" denotes a start-of-sentence marker.

designed as an implementation of the hypothesis that children detect and store multi-word chunks using BTP, and also use the stored chunks to parse speech and produce new utterances (see also Arnon and Snider (2010) and Bannard and Matthews (2008)). The model's ability to simulate learning can be measured by first training it on what children hear and then having the model reproduce what children say from the chunks that it learned.

We chose to build on the CBL model because it has successfully accounted for 125 production data in multiple corpora, including **child language** datasets. For example: (a) 126 it parsed text better than a shallow parser in three different languages (English, German and 127 French) when using individual words rather than word classes, (b) it was able to recreate up 128 to 60% of child utterance productions in 13 different languages, and (c) it closely replicated 129 data from an artificial grammar learning study (McCauley & Christiansen, 2011; Saffran, 130 2002). The model has also been able to replicate experimental data on children's multi-word 131 utterance repetitions (Bannard & Matthews, 2008), over-regularization of irregular plural 132 nouns (Arnon & Clark, 2011), and L2-learner speech (see also McCauley & Christiansen, 133 2014b, 2017). In sum, the CBL model appears to robustly predict the word-chunk patterns in children's speech when given information about what they hear in their input. We 135 extend this work by testing how the model performs with longitudinal data; it 136 is not yet known how well it functions as a predictor of what children can say

as they become more linguistically sophisticated.

## 139 Testing for change with age

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Following McCauley and colleagues (2011, 2014a, 2019) we tested the CBL model's ability to learn language by checking how well it can reconstruct children's utterances from the chunks discovered in their caregivers' speech. As we are interested in developmental change over the first three years of speech production, we analyzed the model's reconstruction ability with two measures:

- "Uncorrected": The binary (success/fail) reconstruction score originally used by McCauley and colleagues (2011, 2014a, 2019).
- "Corrected": A length-and-repetition-controlled reconstruction score that accounts for the fact that longer utterances have more opportunities for error reconstruction, and for the fact that some child utterances contain repetitions of **chunks**(s), making multiple reconstructions match the original utterance.

If BTP is an age-invariant mechanism, it should apply equally well to shorter

utterances and longer utterances; the latter of which are more often produced as children get

older. We therefore tested for age invariance both with the original binary ("uncorrected")

reconstruction score and a new ("corrected") score we proposed to account for utterance

length and word repetitions. If we find age-invariance, even while controlling for utterance

length and word repetitions, it would strongly suggest that the mechanism is stable over the

first three years of speech production and not simply influenced by other factors, e.g.,

utterance length. If not, it would suggest that use of the mechanism, in fact, changes with

age (Bannard et al., 2009; Tomasello, 2005; Yang, 2016).

## 160 Predictions

With these previous findings as a starting point, we investigated whether the CBL could account for child speech production with equal precision over the first four years of life.

Taking for granted that children eventually develop abstract representations

(Tomasello, 2008; as in, e.g., Yang, 2016), we predicted that:

- The CBL would less accurately generate children's speech productions as they grew older; given the assumption that children gradually learn to abstract over the specific "chunks" they encounter (Bannard et al., 2009; Tomasello, 2005; Yang, 2016) and, therefore, their speech should less often directly mirror their linguistic input at later ages. This finding would indicate that the immediate influence of children's language input statistics on their speech production decreases across development.
  - Children will be more likely to use words that are not documented in the caregiver speech as they get older. These words could originate from other sources, such as peer speech or non-recorded caregiver speech (Hoff, 2010; Hoff-Ginsberg & Krueger, 1991; Mannle, Barton, & Tomasello, 1992; B. C. Roy, Frank, & Roy, 2009).
  - Younger children's utterances would be reconstructed well on the basis of recently heard speech alone, whereas older children's utterances would be best constructed when considering a longer period of their historical input. Our reasoning was that older children's increased memory capacity (Bauer, 2005; Gathercole et al., 2004; Wojcik, 2013) allows them to draw on older input more easily in producing speech. If so, the findings would suggest that memory plays a critical role in the use of the same learning mechanism with age.

In sum, we expected to find that the CBL's ability to reconstruct children's speech decreases in-line with a concomitant increase in children's linguistic sophistication; an effect driven by children's use of more abstracted representations, words from other speech sources,

and their increased ability to use historical input.

186 Methods

## 87 Model

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The CBL model (McCauley & Christiansen, 2011) is an incremental, online computational model of language acquisition, that explores the possibility that infants and children parse their input into (multi-word) chunks during the process of acquiring language.

The model takes transcribed speech as input and divides the transcribed utterances 191 into multi-word chunks. Each utterance begins with a start cue (denoted "#"). The exact 192 placement of a chunk boundary within an utterance is determined by two factors: (1) the 193 backward transitional probability (BTP) between consecutive words in the utterance, and (2) 194 the inventory of already-discovered chunks. All newly discovered chunks are saved into the 195 inventory, alongside the BTPs associated with each chunk. The only information that the 196 model tracks and stores are the discovered chunks, the BTPs between words, and the BTPs 197 between discovered chunks. For example, the model might parse the utterances "I see the doggy" and "did you look at the doggy?" into five different chunks, namely "I", "see", "the doggy", "did you", and "look at" based on the BTPs between these words compared to the 200 average BTP found in the corpus so far. 201

## 202 Child utterance reconstruction task

Once the model has been trained on adult utterances, and thereby has discovered
chunks in the adults' speech, we can test whether it closely matches the linguistic structures
produced by the children in the same caregiver-child corpus. Following McCauley and
Christiansen (2011), we use a child utterance reconstruction task to test whether the chunk

statistics present in the adults' utterances are also present in the child's utterances. The 207 model reconstructs the child utterances from the chunks and their related BTPs from the 208 adult's utterances at the same age point. This reconstruction process, which is slightly 209 different from McCauley and Christiansen's (2011) process, is done in two steps 210 (see Figure 2). First, a child utterance is converted into an unordered bag-of-chunks 211 containing chunks discovered in the adults' speech, in line with the bag-of-words approach 212 proposed in Chang, Lieven, and Tomasello (2008). Whenever the model encounters a word 213 in the child utterance that is not present in the adult-based chunk inventory, it stops 214 processing that utterance. For instance, in the toy example in Figure 2, the child utterance 215 "look at the doggy" would be **broken down into a** set of **known** chunks which were 216 discovered in the adults' speech (e.g., "look at" and "the doggy", as in the step 2 217 speech bubble). If the utterance were "look at the doggy there", and the model had not already added a chunk for the word "there" during training, then the word is 219 unknown to the model and the utterance cannot be reconstructed; therefore the utterance would be rejected from further processing. However, in the case 221 that the utterance can be broken down into known chunks, the model then tries 222 to reconstruct the utterance by shuffling the chunks detected and reordering 223 them based on their known transitional probailities: the model begins with the 224 utterance start cue and then follows that initial cue with the chunk that has the 225 highest transitional probability following the start cue, which is followed by the 226 remaining chunk that has the highest transitional probability following the 227 previous chunk, and again and again, until the set of chunks for that utterance 228 is exhausted. So, the set of chunks "look at" and "the doggy" would be ordered depending 229 on which chunk had the highest BTP with respect to the utterance start cue ("look at"),

<sup>&</sup>lt;sup>1</sup>McCauley and Christiansen (2011) handle these cases differently. Our CBL implementation is identical to theirs up to this point. Therefore we also provide sentence reconstruction scores using their original method in the Supplementary Materials.

followed by the chunk with the highest BTP with respect to "look at" ("the doggy").

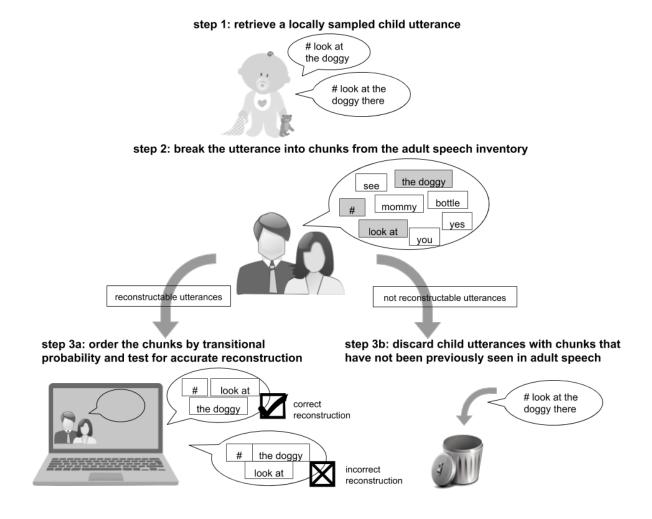


Figure 2. Example of a reconstruction attempt of two child utterances by a toy model. The model is able to reconstruct the first utterance, but it cannot do so with the second utterance, which contains a word ("there") that it has not previously seen.

# Materials and Procedure

As input to the model we used transcripts of 1–2-hour recordings of at-home interaction between six North American children and their caregivers who were recorded approximately every two weeks between ages 1;0 and 4;0 (the Providence corpus; Demuth, Culbertson, and Alter (2006)). We pre-processed the transcripts, which were formatted using

CHAT conventions (MacWhinney, 2000), such that the input to the model only contained plain text orthographic transcriptions of what was said.<sup>2</sup> We split the transcripts into two separate files, one with all the caregivers' utterances and one with all the child's utterances.

Our pre-processing also added a "#" prefix to the start of each utterance.

The transcripts were sampled at approximate 6-month intervals between ages 1;0 and 241 4:0. We used two different sampling methods: a local data sampling method and a 242 cumulative data sampling method. With the local data sampling method we selected data 243 within a two-month interval around each age point. For example, for age point 1;6 we 244 selected transcripts in which the child was between 1:5.0 and 1:6.31 years of age. This 245 method led to ~800–4000 caregiver utterances at each age point. By design, the local 246 sampling method focuses the model's training solely on recent linguistic input so that, when it tries to reconstruct children's utterances, the result is a test of how closely their current 248 speech environment can account for what they say. We sample around target age 249 points and not *up-until* target age points because, while the Providence corpus 250 is relatively densely sampled, recording sessions weren't frequent enough to guarantee a representative picture of each child's input in the month preceding 252 each of the target age points. For this reason, we decided that training the 253 model on input proximal to the tested age was a better method for getting a 254 broad, but age-specific model of adult speech for each child at each age point. 255

In contrast, the cumulative sampling method focuses the model's training on all
previously heard linguistic input so that, when it tries to reconstruct children's utterances,
the result is a test of how closely their current *and* previous speech environments can
account for what they say. For the cumulative sample we selected data for each age point by

<sup>&</sup>lt;sup>2</sup>All punctuation marks, grammatical notes, omitted word annotations, shortenings, and assimilations were removed from the utterances, such that only the text representing the spoken words of the utterance remained.

taking all the available transcripts up to that age point. For example, for age 1;6 we selected all transcripts in which the child was 1;6 or younger. This method led to ~800–60,000 caregiver utterances across the different age points, with the number of caregiver utterances increasing (i.e., accumulating) with child age. As a consequence, the cumulative sample always contained more caregiver utterances than the local sample, except at age 1;0, the first sampled age point.

While we used two different sampling methods for training the model on adult data, all child utterances used for the reconstruction task were retrieved using the local sampling method for that particular age point. In other words, we only reconstructed the child utterances local to each tested age, regardless of the training strategy.

# 270 Analysis

We modeled two primary scores related to utterance reconstruction: the uncorrected 271 (binary: success/fail) reconstruction score used by McCauley and colleagues (2011, 2014a, 272 2019) and the corrected reconstruction score we introduce in the current paper. The 273 uncorrected reconstruction score (1: success, 0: fail) was computed for all child utterances 274 that could be decomposed into previously seen chunks (see step 3a in Figure 2). The 275 corrected reconstruction score (defined below) was computed for the same set of utterances. 276 We additionally included a third analysis: the likelihood that an utterance contains 277 previously unseen words which, by our version of the CBL, cannot be reconstructed (see step 278 3b in Figure Figure 2). 279

We used mixed-effects regression to analyze the effect of child age on both of the
reconstruction scores and whether utterances contained previously unseen words. All
mixed-effects models included child age as a fixed effect and by-child random intercepts with
random slopes of child age. The mixed-effects model of utterances with previously unseen

words also included the number of words in the utterance, as explained below. By default, 284 child age was modeled in years (1-4) so that the intercept reflects a developmental trajectory 285 beginning at age 0. However, for the model of corrected reconstruction accuracy, 286 we wanted to know if the CBL's accuracy score would exceed chance 287 performance on average, i.e., at the average age in our longitudinal dataset 288 (age 2;6). To test this, we centered age on zero in the statistical (ages 1;0, 1;6, 280 2;0, 2;6, 3;0, 3;6, and 4;0 are re-coded as -1;5, -1, -0.5, 0, 0.5, 1, and 1.5) such 290 that the default model output from the lme4 statistical package (Bates, 291 Mächler, Bolker, & Walker, 2015) would reflect the estimated difference from 292 chance at the middle point of our age range (i.e., age 2;6). 293

All analyses were conducted using the lme4 package (Bates et al., 2015) and all figures
were generated with the ggplot2 package in R (R Core Team, 2014; Wickham, 2009). All
code used to create the model and analyze its output is available at
https://osf.io/ca8ts/?view\_only=daaa1bcc71654842b0d70efe785a26b9. Before turning to the
main results we briefly describe the corrected reconstruction score and the analysis of
previously unseen words in more detail.

# 300 Corrected reconstruction accuracy

The corrected, length-and-repetition-controlled reconstruction score is a function of
three factors: (a) whether the model successfully reconstructed the child utterance or not,
(b) the number of chunks used to reconstruct the utterance, and (c) the number of duplicate
chunks involved in the reconstruction. By taking the number of chunks into account, this
reconstruction score compensates for the fact that successful reconstruction is less likely for
longer utterances. When an utterance contains duplicate chunks, the exact ordering of those
duplicate chunks does not influence the correctness of the reconstruction. For example, if the
utterance "I wanna, I wanna" is decomposed into the two chunks "I wanna" and "I wanna",

it does not matter which of the two "I wanna" chunks is placed first when calculating the
reconstruction accuracy of the utterance. Thus, utterances containing duplicate chunks are
more likely to be reconstructed by chance alone than utterances with the same number of
chunks with no duplicates. Note that here we detecting duplicate *chunks* in the
utterance rather than duplicate *words*. At this post-training stage, the model
is only able to parse the utterance into chunks; that is the relevant unit over
which duplication may affect reconstruction accuracy.

An utterance that is decomposed into N unique chunks can be reconstructed in N!different orders. Hence, the probability of obtaining the correct order of N unique chunks
merely by chance equals 1/N!. When we take into account that chunks can be repeated
within an utterance, chance level equals  $(n_1!n_2! \dots n_k!)/N!$  where N is the total number of
chunks in the utterance, and  $n_1, \dots, n_k$  are the number of times a chunk is repeated for each
of the k unique chunks found in the utterance.

When probability of reconstruction was lower, we scored a correctly reconstructed 322 utterance higher. We assigned a score of  $-\log(chance)$  for each correct reconstruction and 323  $\log(1-chance)$  for each incorrectly reconstructed utterance. In layman's terms, this means 324 that successfully reconstructed utterances were scored positively, but were weighed relative 325 to the number of chunks and the number of repetitions they had, such that reconstructions of long utterances were given higher scores than reconstructions of short utterances. Along the same lines, incorrectly reconstructed utterances were scored negatively and were also weighed relative to the number of chunks they had, such that incorrect reconstructions of 329 long utterances were given higher (i.e., less negative) scores than incorrect reconstructions of 330 short utterances. 331

To illustrate the corrected scoring method, let's compare two three-chunk utterances, one of which contains a duplicate chunk: "I wanna I wanna see" (chunks: "I wanna", "I wanna", "see") and "I wanna see that" (chunks: "I wanna", "see", "that"). For the first

utterance, chance level equals  $(2! \times 1!)/(3!)$ : The numerator is determined by the number of 335 times each unique chunk is used, so because "I wanna" occurs two times and "see" occurs 336 once, that is  $2! \times 1!$ . The denominator is determined by the factorial of total number of 337 chunks (here:  $3! = 3 \times 2 \times 1$ ). The resulting chance level is then 2/6. For the second 338 utterance, chance level equals  $(1! \times 1! \times 1!)/(3!)$ : The numerator is equal to  $1! \times 1! \times 1!$  here 339 because all chunks occur only once in the utterance. The denominator is the same as for the 340 first utterance as the total number of chunks in the utterance is the same. Here, the 341 resulting chance level is 1/6. If the utterances are reconstructed correctly, the score is computed by  $-\log(chance)$ . So, the first utterance would get a positive score of 343  $-\log(chance) = -\log(2/6) \approx 1.098$  and the second utterance would get a higher positive score of  $-\log(chance) = -\log(1/6) \approx 1.791$  for increased reconstruction difficulty. If the utterances are reconstructed incorrectly, the score is computed by  $\log(1 - chance)$ . Thus, the first utterance would get a negative score of  $\log(1-chance) = \log(1-(2/6)) \approx -0.405$ and the second utterance would get a less negative score of  $\log(1 - chance) = \log(1 - (1/6)) \approx -0.182.$ 

#### 50 Previously unseen words

Our third analysis focused on whether or not each child utterance contained words that
were not previously seen, that is, not present in the trained adult-speech chunk inventory.
Each utterance was coded for unseen words with a binary value (1: at least one unseen word,
0: no unseen words). Longer utterances are more likely to contain unseen words:
an utterance with N words has a probability of 1-((1-p)<sup>N</sup>) of containing at least
one unseen word. We are interested in the likelihood of utterance with unseen
words beyond these effects of sentence length. We therefore include utterance
length as a control predictor in the regression.

Results

## 50 Uncorrected reconstruction accuracy

The uncorrected score of accurate utterance reconstruction (McCauley & Christiansen, 361 2011, 2014a) showed that model's average percentage of correctly reconstructed utterances across children and age points was similar for the locally and cumulatively sampled speech (local: mean = 65.4%, range across children = 59.9%–70.3%; cumulative: mean = 59.9%, 364 range across children = 53.1%–68.2%). This is similar to, or slightly higher than, results reported by McCauley and Christiansen (2011) who found an average percentage of correctly reconstructed utterances of 59.8% over 13 typologically different languages with a mean age 367 range of 1;8–3;6 years. Additionally, McCauley and Christiansen (2019) reported an average 368 reconstruction percentage of 55.3% for 160 single-child corpora of 29 typologically different 360 languages, including a performance of 58.5% for 43 English single-child corpora with a mean 370 age range of 1;11-3;10. 371

In our statistical models of the uncorrected reconstruction accuracy<sup>3</sup>, we first analyzed the CBL model's performance when it was trained on locally sampled caregiver speech. The number of correctly reconstructed utterances decreased with age (b = -0.805, SE = 0.180, p < 0.001); over time the BTP statistics present in the caregivers' speech were less reflected in the child's own speech (Figure 3, left panel).

We then tested the model's performance when it was trained with a cumulative sample of caregiver speech, rather than just a local sample. As before, the number of correctly reconstructed utterances decreased with child age (b = -0.821, SE = 0.146, p < 0.001; Figure 3, right panel). These results indicate age-variance for the SL mechanism; its utility for modeling children's utterances changes with age.

 $<sup>^{3}</sup>$ accuracy  $\sim$  age + (age|child), family = binomial(link = "logit").

Importantly, however, the length of the child utterances varied quite a lot (range = 382 1-44 words long; mean = 2.8, median = 2), and some of them contained repetitions of 383 chunks (e.g., "I wanna, I wanna"), both of which influence the baseline likelihood of accurate 384 reconstruction. Utterances from older children tended to contain more words than utterances 385 from younger children (Figure 4, left panel). As a consequence, on average, utterances from 386 older children are systematically less likely to be correctly reconstructed by chance, 387 contributing to the decrease in the CBL's overall performance with age. Additionally, the 388 percentage of child utterances that contained duplicate chunks decreased over time (Figure 4, 389 right panel). Utterances with duplicate chunks had a higher baseline probability of being 390 accurately reconstructed by the model. So again, on average, utterances from older children 391 were systematically more difficult, contributing to the age-related decrease in uncorrected 392 reconstruction scores.

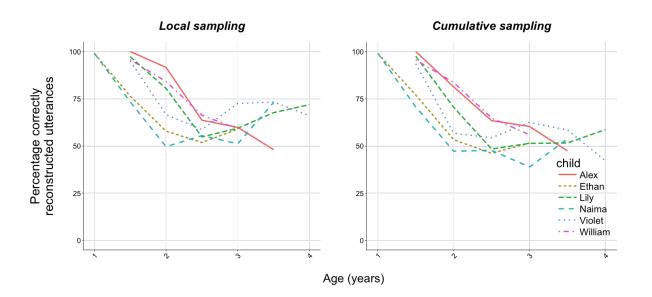


Figure 3. Percentage of correctly reconstructed utterances across the age range, using local (left) and cumulative (right) sampling.

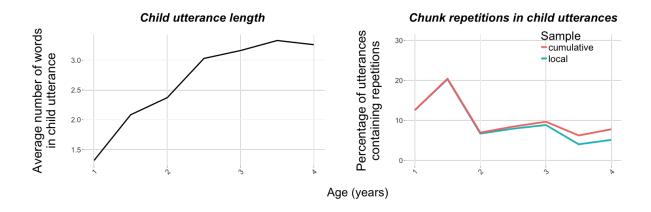


Figure 4. Children's utterances increased in length (number of words) with age (left) while simultaneously decreasing in the number of duplicate chunks used (right).

# 94 Corrected reconstruction accuracy

Next, we used our corrected reconstruction score to assess the model's reconstruction 395 accuracy while controlling for utterance length and the use of duplicate chunks. The score 396 weighs whether each utterance was accurately reconstructed against its chance level of reconstruction, depending on the total number of chunks and number of duplicate chunks it 398 contains. The model's average reconstruction score across children and age points was 399 similar for the locally and cumulatively sampled speech (local: mean = 0.10, SE = 0.01; 400 cumulative: mean = 0.06, SE = 0.01). Note again that one aim of this analysis was to test 401 whether the corrected reconstruction score was above chance—here represented by a score of 402 zero—so in the statistical models we centered child age on zero so that the estimation would 403 reflect the difference from zero for the average age in our sample (2;6).<sup>4</sup> 404

Again, we first analyzed the model's performance when it was trained on locally sampled caregiver speech. We found a significant positive intercept (b=0.11, SE=0.02, t=5.064) and no significant change across age (b=0.030, SE=0.018, t=1.681); the BTP statistics from the caregivers' speech were

 $<sup>^{4}</sup>$ accuracy  $\sim$  age + (age|child).

consistently reflected in the child's own speech (Figure 5, left panel).

As before, we created a parallel set of analyses to test the model's performance when it was trained with a cumulative sample of caregiver speech. We again found a significant positive intercept (b = 0.06, SE = 0.010, t = 6.238) and that accuracy did not change significantly across age (b = 0.02, SE = 0.013, t = 1.590; Figure 5, right panel).

In sum, contrary to the uncorrected reconstruction accuracy analysis, these corrected reconstruction score results indicate age-invariance for the SL mechanism. In addition, the model performed significantly above chance level in both the local and cumulative sampling contexts.

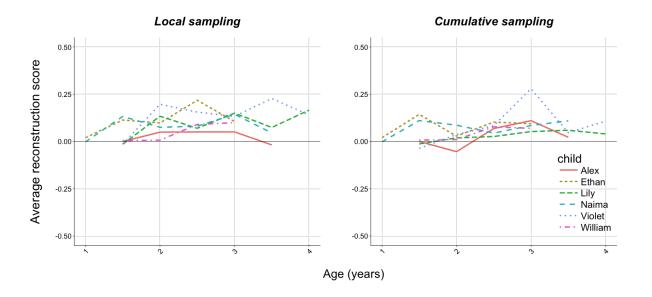


Figure 5. Corrected reconstruction scores across the age range, using local (left) and cumulative (right) sampling.

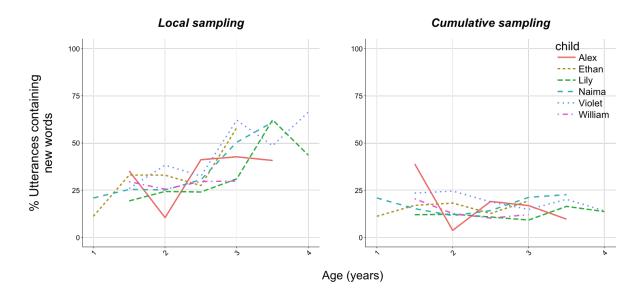


Figure 6. Number of utterances with previously unseen words across the age range, using local (left) and cumulative (right) sampling.

#### 418 Children's use of unseen words

Finally, we modeled whether an utterance had a previously unseen word or not (1: at 419 least one unseen word, 0: no unseen words). Using local sampling the number of child 420 utterances that contained one or more previously unseen words increased with age 421 (b = 0.364, SE = 0.093, p < 0.001; Figure 6, left panel). Unsurprisingly, longer utterances 422 were also significantly more likely to have previously unseen words in them 423 (b = 0.170, SE = 0.005, p < 0.001). By taking a longer history of linguistic input into 424 account (i.e., by using cumulative sampling), we expected to see a smaller increase in 425 previously unseen words with age. That is, an unseen chunk in the local sampling 426 could become a seen chunk in the cumulative sampling. We indeed found that utterances containing previously unseen words became less likely with age (b = -0.139, SE = 0.068, p < 0.05; Figure 6, right panel). Also, as before, previously unseen words were more likely to occur in longer utterances (b = 0.105, SE = 0.006, p < 0.001).  $^{5}$ has\_unseen\_words ~ age + (age|child) + num\_words\_in\_utt, family = binomial(link = "logit")

431 Discussion

Our primary research question (as raised by, e.g., Arciuli & Simpson, 2011; Raviv & 432 Arnon, 2018; J. R. Saffran et al., 1997; Shufaniya & Arnon, 2018) was whether the CBL 433 would change in its ability to predict children's speech productions throughout 434 development. We tested the model using both the original measure of accuracy as well as a 435 new measure that takes into account utterance length and duplicate chunks in the utterance, 436 which can make accurate reconstruction less likely (length) or more likely (duplicates). Using this corrected measure, we found that there was no significant change in the use of BTP with age. Notably, the CBL was able to construct utterances at above-chance levels despite these changes with age. Overall, and against our predictions in the Introduction, the current findings support the view that BTP is an age-invariant learning mechanism for speech production. In fact, the positive, but non-significant coefficients for the effect of age 442 on corrected reconstruction accuracy indicate that, the CBL is, at least, not getting worse at 443 reconstructing children's utterances with age. Also, the divergence in findings between the corrected and uncorrected accuracy scores illustrates how effects 445 of length and chunk/word duplication can critically shift baseline performance 446 during reconstruction; these features of natural speech should be controlled for 447 in future work.

## 449 Different words at different ages

We also analyzed the number of utterances with previously unseen words in them,
arguing that older children's increased memory capacity (Bauer, 2005; Gathercole et al.,
2004; Wojcik, 2013) would possibly allow them to draw upon older input more easily in
producing speech. Indeed, we found an increase in the number of utterances containing
previously unseen words with age in the local sample but a decrease when taking their longer
linguistic history into account. The change in word usage we find here could be partly due to

a change in linguistic input not captured in the transcripts. The corpus we used is relatively 456 dense: multi-hour at-home recordings made approximately every two weeks for 2–3 years. 457 However, this corpus still only contained a small fraction of what each child heard during the 458 represented periods of time (i.e., 2 hours of ~200 waking hours in a fortnight). Non-recorded 459 caregiver speech may contribute an increasing amount of lexical diversity. Consider, for 460 example, that input from peers containing different lexical items could have increased as 461 children became old enough to independently socialize with other children or attend daycare 462 or preschool (Hoff, 2010; Hoff-Ginsberg & Krueger, 1991; Mannle et al., 1992), which may 463 help to account for the increased presence of words not found in the caregiver's speech. This 464 problem is difficult to address directly since, even with cutting-edge tools and significant 465 supporting resources, it is still nearly impossible to collect and transcribe a child's complete language environment (Casillas & Cristia, under review; B. C. Roy et al., 2009). This effect could instead be simulated in future work by feeding speech from other children or adults into the model to mimic speech from peers and other caregivers. That said, our results showed that the likelihood of previously unseen words actually decreased with age for the cumulative sample, suggesting that the "missing" words are present in caregiver speech, just 471 not always in the recently recorded input.

Additionally, an improvement in memory capacity with age provides a potential 473 explanation for the current findings. Throughout childhood, including the first few years, 474 SL-relevant cortical regions continue maturing (Casey et al., 2000; Diamond, 2002; 475 Rodríguez-Fornells et al., 2009; Uylings, 2006) with concurrent increases in long-term 476 memory (Bauer, 2005; Wojcik, 2013), working memory, and speed of processing (Gathercole et al., 2004; Kail, 1991). By ages three and four, the children in the current study may have 478 been able to much more reliably draw upon information they were exposed to in the more distant past. If so, we would expect no significant increase in the use of previously unheard words as children get older with the cumulative sampling method—consistent with what we 481 found here (Figure 6, right panel). This pattern of results indicates that children's

developing memory could play an important role in the way they use environmental input statistics over age.

# 85 Abstraction and complex utterances

Our findings are not consistent with a representational shift toward abstraction during 486 the early language learning process. For instance, if children schematized their constructions 487 or switching to rule-based representations (Bannard et al., 2009; Tomasello, 2005; Yang, 488 2016), we would expect a decrease in reconstruction accuracy over time, given that the CBL's 480 reconstructions are limited to the immediate statistics of the child's language environment. 490 In contrast, we saw that the model's ability to reconstruct child utterances from caregivers' 491 speech was age-invariant when taking into account utterance length and chunk duplicates. These results do fall in line with SL theories proposing that the mechanisms for processing, 493 storing, and deploying information stay the constant over age, even though SL behavior on 494 the surface might seen to change over time (e.g., Misyak et al., 2012). 495

As the CBL model only employs a single, simple mechanism for creating and tracking linguistic units, it is impressive that it performs at above-chance levels when accounting for children's speech productions in the first few years. If the mechanism is truly age-invariant, it should be able to handle both young children's speech and adults' speech; here we see that it handles the developing linguistic inventory of children ages 1;0 to 4;0, during which time children's utterances come much more sophisticated and much closer to adult-like form.

Going beyond the scope of this paper, a next step would be to explore how the CBL could be modified to augment its performance, particularly on more complex utterances. For example, the CBL model does not include the use of semantics when dividing the caregivers' speech into chunks or when reconstructing the child utterances. However, the meaning of what both caregivers and child are trying to convey plays a fundamental role in selecting

words from the lexicon and in constructing utterances—they are interacting, and not just 507 producing speech. The same set of words, ordered in different ways, can have entirely 508 different meanings (e.g., "the dog bites the man" vs. "the man bites the dog"). Additionally, 509 the CBL currently works on text-only transcriptions of conversations, but speech prosody 510 could potentially critically change how children detect chunks. Prosodic structures within an 511 utterance highlight syntactic structures and help to distinguish between pragmatic 512 intentions, for example, distinguishing between questions, imperatives, and statements (e.g., 513 Bernard & Gervain, 2012; Speer & Ito, 2009). Ideally, the CBL model would also be tested 514 on a (more) complete corpus of what children hear in the first few years to further 515 investigate the origins of the "previously unseen" words in children's utterances; though we 516 appreciate that densely sampled and transcribed collections of audio recordings are 517 extremely costly to create (Casillas & Cristia, under review; B. C. Roy et al., 2009).

519 Conclusion

In this study, we investigated whether the CBL model—a computational learner using 520 one SL mechanism (BTP)—could account for children's speech production with equal 521 accuracy across ages 1;0 to 4;0 given information about their speech input. The model's 522 ability to reconstruct children's utterances remained stable with age when controlling for 523 utterance length and duplicate chunks, both when taking into account recent and cumulative 524 linguistic experience. These findings suggest that this particular mechanism for segmenting 525 and tracking chunks of speech may be age-invariant (Raviv & Arnon, 2018; Shufaniya & Arnon, 2018). A rich and growing literature on SL in development has demonstrated that similar mechanisms can account for much of children's early language behaviors; knowing 528 whether the use of these mechanisms changes as children get older is a crucial piece of this 529 puzzle. To explore this topic further, future work will have to address additional cues to 530 linguistic structure and meaning, the density of data needed to get reliable input estimates, 531

533

and the interaction of SL with other developing skills that also impact language learning.

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