

<sup>1</sup> Supplementary materials: Modeling the influence of language input statistics on children's  
<sup>2</sup> speech production

## Abstract

*Keywords:* statistical learning, language learning, abstraction, developmental trajectory,  
age-invariance, CHILDES, children

7 Supplementary materials: Modeling the influence of language input statistics on children's  
8 speech production

9 **Full model output of main text analyses**

10 Below readers will find the full statistical model output for each of the six  
11 models reported in the main text (that is, one for local input and one for  
12 cumulative input for each of the three analyses: uncorrected likelihood of  
13 accurate reconstruction, corrected reconstruction accuracy, and likelihood of  
14 unseen words).

Table 1

*\*\*Full model output for the analysis of uncorrected reconstruction accuracy using local speech input. \*\**

effect	group	term	estimate	std.error	statistic	p.value
fixed	NA	(Intercept)	2.59	0.50	5.19	0.00
fixed	NA	age	-0.81	0.18	-4.44	0.00
ran_pars	child	sd__(Intercept)	1.36	NA	NA	NA
ran_pars	child	sd__age	0.49	NA	NA	NA
ran_pars	child	cor__(Intercept).age	-0.97	NA	NA	NA

## Results using the original McCauley and Christiansen (2011) reconstruction method

While our implementation of the CBL learner is identical to McCauley and Christiansen’s, our implementation of the *reconstruction task* diverges slightly from theirs: we discard utterances with unknown words and instead provide a second analysis focused on the number of these “un-reconstructable” utterances across age. Our reasoning for discarding utterances with unknown words was that there is no obvious way to give them a valid default transition matrix with other existing chunks. In contrast, McCauley and Christiansen (2011) built a new chunk for each unknown word when reconstructing utterances. This chunk with the unknown word was then assigned a BTP equal to zero with respect to any other chunk in the utterance it originated from. In what follows, we present results using McCauley and Christiansen’s (2011) original reconstruction task method. Because their reconstruction task attempts to reconstruct all utterances, we do not also provide analyses of the number of utterances containing unknown words.

Table 2

*\*\*Full model output for the analysis of uncorrected reconstruction accuracy using cumulative speech input.\*\**

effect	group	term	estimate	std.error	statistic	p.value
fixed	NA	(Intercept)	2.40	0.39	6.09	0.00
fixed	NA	age	-0.82	0.14	-5.83	0.00
ran_pars	child	sd__(Intercept)	1.18	NA	NA	NA
ran_pars	child	sd__age	0.41	NA	NA	NA
ran_pars	child	cor__(Intercept).age	-0.96	NA	NA	NA

Table 3

*\*\*Full model output for the analysis of corrected reconstruction accuracy using local speech input.\*\**

effect	group	term	estimate	std.error	statistic	p.value
fixed	NA	(Intercept)	0.11	0.02	5.06	NA
fixed	NA	recentered_age	0.03	0.02	1.68	NA
ran_pars	child	sd__(Intercept)	0.05	NA	NA	NA
ran_pars	child	sd__recentered_age	0.04	NA	NA	NA
ran_pars	child	cor__(Intercept).recentered_age	0.63	NA	NA	NA
ran_pars	Residual	sd__Observation	0.63	NA	NA	NA

Table 4

*\*\*Full model output for the analysis of corrected reconstruction accuracy using cumulative speech input.\*\**

effect	group	term	estimate	std.error	statistic	p.value
fixed	NA	(Intercept)	0.06	0.01	6.24	NA
fixed	NA	recentered_age	0.02	0.01	1.59	NA
ran_pars	child	sd__(Intercept)	0.02	NA	NA	NA
ran_pars	child	sd__recentered_age	0.03	NA	NA	NA
ran_pars	child	cor__(Intercept).recentered_age	-0.71	NA	NA	NA
ran_pars	Residual	sd__Observation	0.59	NA	NA	NA

Table 5

*\*\*Full model output for the analysis of likelihood that a word in the child's speech was seen during training.\*\**

effect	group	term	estimate	std.error	statistic	p.value
fixed	NA	(Intercept)	3.13	0.33	9.64	0.00
fixed	NA	age	-0.55	0.11	-5.00	0.00
ran_pars	child	sd__(Intercept)	0.74	NA	NA	NA
ran_pars	child	sd__age	0.25	NA	NA	NA
ran_pars	child	cor__(Intercept).age	-0.94	NA	NA	NA

Table 6

*\*\*Full model output for the analysis of number of utterances with previously unheard words using cumulative speech input.\*\**

effect	group	term	estimate	std.error	statistic	p.value
fixed	NA	(Intercept)	2.85	0.36	7.82	0.00
fixed	NA	age	-0.02	0.12	-0.18	0.86
ran_pars	child	sd__(Intercept)	0.78	NA	NA	NA
ran_pars	child	sd__age	0.25	NA	NA	NA
ran_pars	child	cor__(Intercept).age	-0.96	NA	NA	NA

We analyzed the effect of child age on the model’s reconstruction abilities for the child utterances with a mixed-effects model, including age as a fixed effect and a by-child random intercept with random slopes of age.

First, we used the binary (1: reconstructed correctly, 0: not reconstructed correctly) measure from McCauley & Christiansen (2011, 2014). The model’s average percentage of correctly reconstructed utterances across children and age points was similar for the locally and cumulatively sampled speech (local: mean = 61.3 %, range across children = 51.6%–69.6%; cumulative: mean = 59.4%, range across children = 50.8%–68.4%). The number of correctly reconstructed utterances decreased with age, regardless of the sampling methods (local:  $b = -0.939$ ,  $SE = 0.174$ ,  $p < 0.001$ ; cumulative:  $b = -0.848$ ,  $SE = 0.138$ ,  $p < 0.001$ ; see Figure 1).

Second, we used our corrected, length-and-repetition-controlled reconstruction score. The model’s average reconstruction score across children and age points was similar for the locally and cumulatively sampled speech (local: mean = 0.12,  $SE = 0.01$ ; cumulative: mean = 0.08,  $SE = 0.01$ ). As in the main text, we centered age in the model so that we could investigate whether reconstruction was greater than chance level at the average age in our

sample (2;6 years). Using both sampling methods, we found a significantly positive intercept  
 (local sampling:  $b = 0.130, SE = 0.016, t = 7.911$ ; cumulative sampling:  
 $b = 0.0789, SE = 0.012, t = 6.426$ ), and the model’s reconstruction score increased over age,  
 significantly in the case of the cumulative sampling method (local sampling:  
 $b = 0.029, SE = 0.016, t = 1.854$ ; cumulative sampling:  $b = 0.031, SE = 0.013, t = 2.333$ );  
 see Figure 2). These results show that the model performed at above-chance levels, and  
 indicates age-invariance with the corrected reconstruction score.

Importantly, these results are highly similar to those from our implementation of the  
 CBL model in the main text, which does not attempt to reconstruct utterances with  
 previously unseen words. These findings suggest that the CBL is not significantly impacted  
 in its ability to reconstruct children’s utterances in the first four years, regardless of the  
 minor algorithmic differences in how new words are treated between the original and current  
 CBL models.

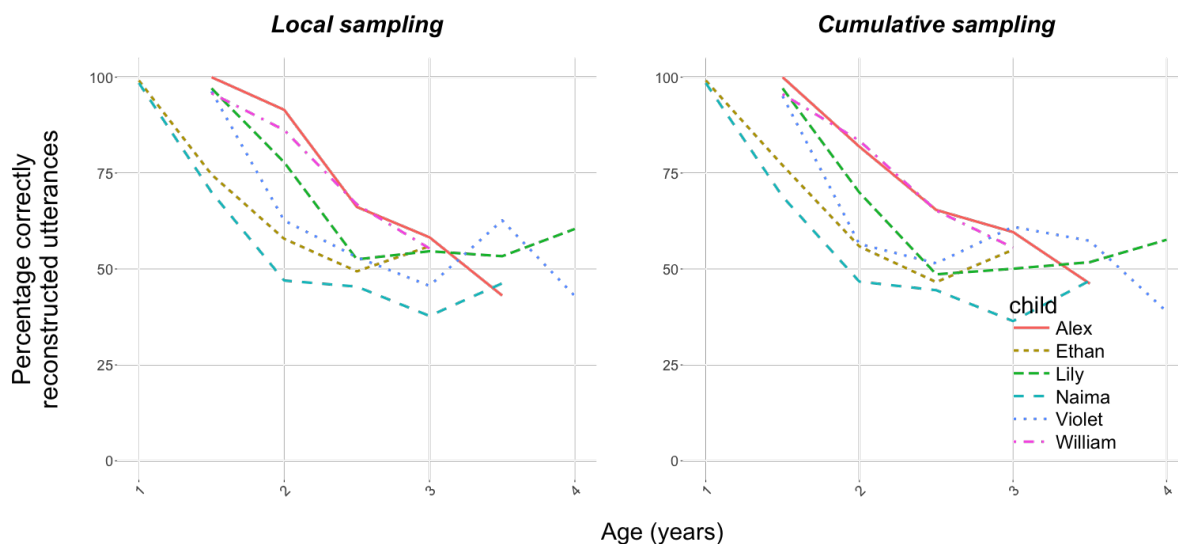


Figure 1. Uncorrected reconstruction scores across the analyzed age range for local (left) and cumulative (right) sampling while using McCauley and Christiansen’s method for handling new words.



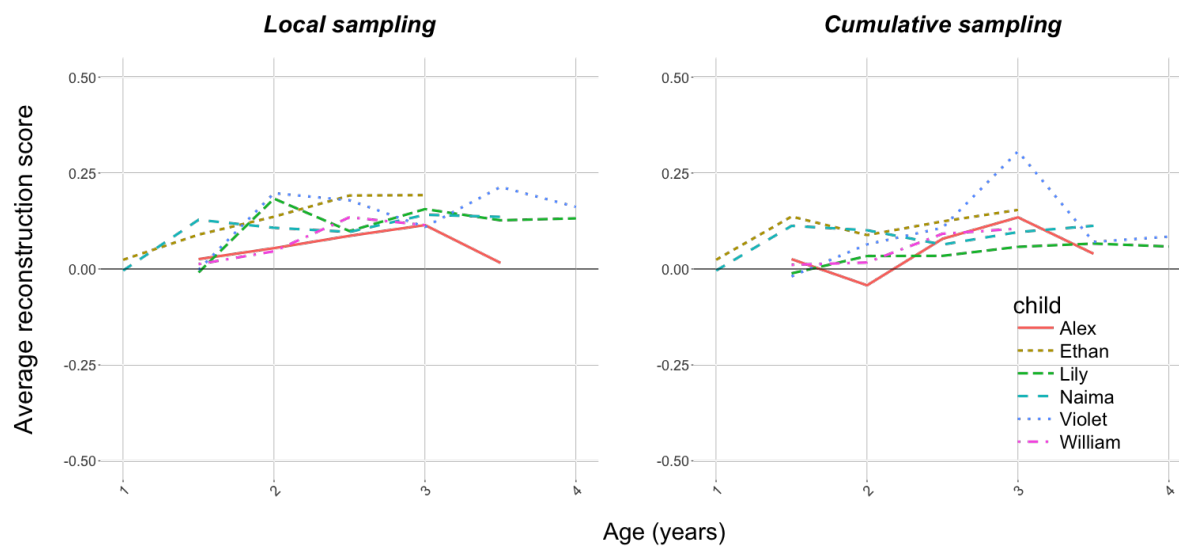


Figure 2. Corrected reconstruction scores across the analyzed age range for local (left) and cumulative (right) sampling while using McCauley and Christiansen’s method for handling new words.

## References

- McCauley, S. M., & Christiansen, M. H. (2011). Learning simple statistics for language comprehension and production: The CAPPUCCINO model. *Proceedings of the 33rd Annual Meeting of the Cognitive Science Society*, 1619–1624.
- McCauley, S. M., & Christiansen, M. H. (2014). Acquiring formulaic language: A computational model. *The Mental Lexicon*, 9(3), 419–436.