Graph theory package for Giac/Xcas

User manual

Luka Marohnić

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1 Introduction

This document contains an overview of the graph theory commands built in the Giac/Xcas software, including the syntax, the detailed description and practical examples for each command.

The commands are divided into the following six sections: *Constructing graphs*, *Modifying graphs*, *Import and export*, *Graph properties*, *Traversing graphs* and *Visualizing graphs*.

2 Constructing graphs

2.1 Creating graphs from scratch: graph, digraph

The command graph accepts between one and three mandatory arguments, each of them being one of the following structural elements of the resulting graph:

- the number or list of vertices (a vertex may be any atomic object, such as an integer, a symbol or a string); it must be the first argument if used,
- the set of edges (each edge is a list containing two vertices), a permutation, a trail of edges or a sequence of trails; it can be either the first or the second argument if used,
- the adjacency or weight matrix.

Additionally, some of the following options may be appended to the sequence of arguments:

- directed = true or false,
- weighted = true or false,
- color = an integer or a list of integers representing color(s) of the vertices,
- coordinates = a list of vertex 2D or 3D coordinates.

The graph command may also be called by passing a string, representing the name of a special graph, as its only argument. In that case the corresponding graph will be constructed and returned. The supported graphs and their names are listed below.

• Clebsch graph: clebsch

• Coxeter graph: coxeter

• Desargues graph: desargues

• Dodecahedron graph: dodecahedron

• Dürer graph: durer

• Dyck graph: dyck

• Grinberg graph: grinberg

• Grotzsch graph: grotzsch

• Harries graph: harries

• Harries-Wong graph: harries-wong

• Heawood graph: heawood

• Herschel graph: herschel

• Icosahedron graph: icosahedron

• Levi graph: levi

• Ljubljana graph: ljubljana

• McGee graph: mcgee

• Möbius-Kantor graph: mobius-kantor

• Nauru graph: nauru

• Octahedron graph: octahedron

• Pappus graph: pappus

• Petersen graph: petersen

• Robertson graph: robertson

• Soccer ball graph: soccerball

• Tetrahedron graph: tehtrahedron

The digraph command is used for creating directed graphs, although it is also possible with the graph command by specifying the option directed=true. Actually, calling digraph is the same as calling graph with that option appended to the sequence of arguments. However, creating special graphs is not supported by digraph since they are all undirected. Edges in directed graphs are called *arcs*. Edges and arcs are different structures: an edge is represented by a two-element set containing its endpoints, while an arc is represented by the ordered pairs of its endpoints.

The following series of examples demostrates the various possibilities when using graph and digraph commands.

Creating vertices. A graph consisting only of vertices and no edges can be created simply by providing the number of vertices or the list of vertex labels. Input:

Output:

an undirected unweighted graph with 5 vertices and 0 edges

Input:

Output:

an undirected unweighted graph with 3 vertices and 0 $\,$ edges

Creating single edges and arcs. Edges/arcs must be specified inside a set so that it can be distinguished from a (adjacency or weight) matrix. If only a set of edges/arcs is specified, the vertices needed to establish these will be created automatically. Note that, when constructing a directed graph, the order of the vertices in an arc matters; in undirected graphs it is not meaningful. Input:

Output:

an undirected unweighted graph with 3 vertices and 3 edges

Edge weights may also be specified.

Input:

Output:

an undirected weighted graph with 3 vertices and 3 edges

If the graph contains isolated vertices (not connected to any other vertex) or a particular order of vertices is desired, the list of vertices has to be specified first. Input:

Output:

an undirected unweighted graph with 4 vertices and 3 edges

Creating paths and trails. A directed graph can also be created from a list of n vertices and a permutation of order n. The resulting graph consists of a single directed path with the vertices ordered according to the permutation. Input:

Output:

a directed unweighted graph with 4 vertices and 3 arcs

Alternatively, one may specify edges as a trail.

Input:

Output:

a directed unweighted graph with 4 vertices and 3 arcs

Using trails is also possible when creating undirected graphs. Also, some vertices in a trail may be repeated, which is not allowed in a path. Input:

Output:

an undirected unweighted graph with 4 vertices and 3 edges

There is also the possibility of specifying several trails in a sequence, which is useful for designing more complex graphs.

Input:

graph
$$(trail(1,2,3,4,2),trail(3,5,6,7,5,4))$$

Output:

an undirected unweighted graph with 7 vertices and 9 edges

Specifying adjacency or weight matrix. A graph can be created from a single square matrix $A = [a_{ij}]_n$ of order n. If it contains only ones and zeros and has zeros on its diagonal, it is assumed to be the adjacency matrix for the desired graph. Otherwise, if an element outside the set $\{0,1\}$ is encountered, it is assumed that the matrix of edge weights is passed as input, causing the resulting graph to be weighted accordingly. In each case, exactly n vertices will be created and i-th and j-th vertex will be connected iff $a_{ij} \neq 0$. If the matrix is symmetric, the resulting graph will be undirected, otherwise it will be directed. Input:

```
graph([[0,1,1,0],[1,0,0,1],[1,0,0,0],[0,1,0,0]])
```

Output:

an undirected unweighted graph with 4 vertices and 3 edges

Input:

```
graph([[0,1.0,2.3,0],[4,0,0,3.1],[0,0,0,0],[0,0,0,0]])
```

Output:

a directed weighted graph with 4 vertices and 4 arcs

List of vertex labels can be specified before the matrix.

Input:

```
graph([a,b,c,d],[[0,1,1,0],[1,0,0,1],[1,0,0,0],[0,1,0,0]])
```

Output:

an undirected unweighted graph with 4 vertices and 3 edges

When creating a weighted graph, one can first specify the list of n vertices and the set of edges, followed by a square matrix A of order n. Then for every edge $\{i,j\}$ or arc (i,j) the element a_{ij} of A is assigned as its weight. Other elements of A are ignored.

Input:

Output:

a directed weighted graph with 3 vertices and 3 arcs

When a special graph is desired, one just needs to pass its name to the graph command. An undirected unweighted graph will be returned.

Input:

Output:

an undirected unweighted graph with 10 vertices and 15 $$\operatorname{\text{\rm edges}}$$

2.2 Promoting to directed and/or weighted graphs: make_directed, make_weighted

The command make_directed is called with one or two arguments, an undirected graph G(V,E) and optionally a square matrix of order |V|. Every edge $\{i,j\} \in E$ is replaced with the pair of arcs (i,j) and (j,i). If matrix A is specified, a_{ij} and a_{ji} are assigned as weights of these arcs, respectively. Thus a directed (and possibly weighted) graph is created and returned. Input:

```
make_directed(cycle_graph(4))
```

Output:

a directed unweighted graph with 4 vertices and 8 arcs $\ensuremath{\operatorname{Input}}$:

Output:

a directed weighted graph with 4 vertices and 8 arcs

The command <code>make_weighted</code> accepts one or two arguments, an unweighted graph G(V,E) and optionally a square matrix A of order |V|. If the matrix specification is omitted, a square matrix of ones is assumed. Then a copy of G is returned where each edge/arc $(i,j) \in E$ gets a_{ij} assigned as its weight. If G is an undirected graph, it is assumed that A is symmetric.

Input:

make_weighted(graph(
$$\{[1,2],[2,3],[3,1]\}\}$$
), [[0,2,3],[2,0,1],[3,1,0]])

Output:

an undirected weighted graph with 3 vertices and 3 edges

2.3 Cycle graphs: cycle graph

The command cycle_graph accepts a positive integer n or a list of distinct vertices as its only argument and returns a graph consisting of a single cycle through the specified vertices in the given order. If n is specified it is assumed to be the desired number of vertices, in which case they will be created and labeled with the first n integers (starting from 0 in Xcas mode and from 1 in Maple mode). Input:

Output:

an undirected unweighted graph with 5 vertices and 5 edges

Input:

Output:

an undirected unweighted graph with 5 vertices and 5 edges

2.4 Path graphs: path_graph

The command path_graph accepts a positive integer n or a list of distinct vertices as its only argument and returns a graph consisting of a single path through the specified vertices in the given order. If n is specified it is assumed to be the desired number of vertices, in which case they will be created and labeled with the first n integers (starting from 0 in Xcas mode and from 1 in Maple mode). Input:

Output:

an undirected unweighted graph with 5 vertices and 4 edges

Input:

Output:

an undirected unweighted graph with 5 vertices and 4 edges

2.5 Trail of edges: trail

The command trail is called with a sequence of vertices as arguments. The symbolic expression representing the trail of edges through the specified vertices is returned, which is recognizable by graph and digraph commands. Note that a trail may cross itself (some vertices may be repeated in the given sequence). Input:

$$T:=trail(1,2,3,4,2); graph(T)$$

Output:

trail(1,2,3,4,2), an undirected unweighted graph with 4 vertices and 4 edges

2.6 Complete graphs: complete_graph, complete_binary_tree, complete_kary_tree

The command complete_graph creates complete (multipartite) graphs. It can be called with a single argument, a positive integer n or a list of distinct vertices, in which case the complete graph with the specified vertices will be returned. If integer n is specified, it is assumed that it is the desired number of vertices and they will be created and labeled with the first n integers (starting from 0 in Xcas mode and from 1 in Maple mode). Alternatively, a sequence of positive integers n_1, n_2, \ldots, n_k may be passed as arguments, in which case the complete multipartite graph with partitions of size n_1, n_2, \ldots, n_k will be returned. Input:

complete_graph(5)

Output:

an undirected unweighted graph with 5 vertices and 10 edges

Input:

complete_graph([a,b,c])

Output:

an undirected unweighted graph with 3 vertices and 3 edges

Input:

complete_graph(2,3)

Output:

an undirected unweighted graph with 5 vertices and 6 edges

The command complete_binary_tree accepts a single positive integer n as its argument and constructs a complete binary tree of depth n. Input:

complete_binary_tree(2)

Output:

an undirected unweighted graph with 7 vertices and 6 edges

The command complete_kary_tree accepts two positive integers k and n as its arguments and constructs a complete k-ary tree of depth n. For example, to get a ternary tree with two levels, input:

complete_kary_tree(3,2)

Output:

an undirected unweighted graph with 13 vertices and 12 edges

2.7 Creating graph from a graphic sequence: is_graphic_sequence, sequence_graph

The command is_graphic_sequence accepts a list L of positive integers as its only argument and returns true if there exists a graph G(V,E) with degree sequence $\{\deg v:v\in V\}$ equal to L, else it returns false. The algorithm is based on Erdős-Gallai theorem and has the complexity $O(|L|^2)$. Input:

Output:

true

The command sequence_graph accepts a list L of positive integers as its only argument. If the list represents a graphic sequence, the corresponding graph is constructed by using Havel–Hakimi algorithm with complexity $O(|L|^2 \log |L|)$. If the argument is not a graphic sequence, an error is returned. Input:

Output:

an undirected unweighted graph with 8 vertices and 15 edges

2.8 Interval graphs: interval_graph

The command interval_graph takes as its argument a sequence or list of realline intervals and returns an undirected unweighted graph with these intervals as vertices (the string representations of the intervals are used as labels), each two of them being connected with an edge if and only if the corresponding intervals intersect.

Input:

```
interval_graph(0..8, 1..pi, exp(1)..20, 7..18, 11..14, 17..24, 23..25)
```

Output:

an undirected unweighted graph with 7 vertices and 10 edges

2.9 Star graphs: star_graph

The command $star_graph$ accepts a positive integer n as its only argument and returns the star graph with n+1 vertices, which is equal to the complete bipartite graph $complete_graph(1, n)$ i.e. a n-ary tree with one level. Input:

Output:

an undirected unweighted graph with 6 vertices and 5 edges

2.10 Wheel graphs: wheel_graph

The command wheel_graph accepts a positive integer n as its only argument and returns the wheel graph with n+1 vertices. Input:

Output:

an undirected unweighted graph with 6 vertices and 10 edges

2.11 Web graphs: web graph

The command web_graph accepts two positive integers a and b as its arguments and returns the web graph with parameters a and b, namely the Cartesian product of cycle_graph(a) and path_graph(b).

Input:

$$web_graph(7,3)$$

Output:

an undirected unweighted graph with 21 vertices and 35 edges

2.12 Prism graphs: prism_graph

The command $prism_graph$ accepts a positive integer n as its only argument and returns the prism graph with parameter n, namely $web_graph(n, 2)$. Input:

Output:

an undirected unweighted graph with 10 vertices and 15 $$\operatorname{\text{\rm edges}}$$

2.13 Antiprism graphs: antiprism_graph

The command antiprism_graph accepts a positive integer n as its only argument and returns the antiprism graph with parameter n, which is constructed from two concentric cycles of n vertices by joining each vertex of the inner to two adjacent nodes of the outer cycle.

Input:

Output:

an undirected unweighted graph with 10 vertices and 20 edges

2.14 Grid graphs: grid_graph, torus_grid_graph

The command <code>grid_graph</code> accepts two positive integers m and n as its arguments and returns the m by n grid on $m \cdot n$ vertices, namely the Cartesian product of <code>path_graph(m)</code> and <code>path_graph(n)</code>. Input:

Output:

an undirected unweighted graph with 15 vertices and 22 edges

The command <code>grid_graph</code> accepts two positive integers m and n as its arguments and returns the m by n torus grid on $m \cdot n$ vertices, namely the Cartesian product of <code>cycle_graph(m)</code> and <code>cycle_graph(n)</code>. Input:

Output:

an undirected unweighted graph with 15 vertices and 30 edges

2.15 Kneser graphs: kneser_graph, odd_graph

The command kneser_graph accepts two positive integers $n \leq 20$ and k as its arguments and returns the Kneser graph with parameters n, k. It is obtained by setting all k-subsets of a set of n elements as vertices and connecting each two of them if and only if the corresponding sets are disjoint. The Kneser graphs can get exceedingly complex even for relatively small values of n and k: note that the number of vertices is equal to $\binom{n}{k}$. Input:

$$kneser_graph(5,2)$$

Output:

an undirected unweighted graph with 10 vertices and 15 edges

The command odd_graph accepts a positive integer $d \leq 8$ as its only argument and returns the Kneser graph with parameters $n=2\,d+1$ and k=d. Input :

Output:

an undirected unweighted graph with 10 vertices and 15 edges

2.16 Sierpiński graphs: sierpinski_graph

The command sierpinski_graph accepts two or three arguments. Calling the command with two positive integers n and k produces the Sierpiński graph S_k^n . In particular, for k=2 a path with 2^n vertices is returned, and for k=3 one obtains the Sierpiński sieve graph of order n. If the symbol triangle is passed as the optional third argument, a Sierpiński triangle graph ST_k^n is returned. It is obtained by contracting all non-clique edges from S_k^n .

Input:

sierpinski_graph(4,3)

Output:

an undirected unweighted graph with 81 vertices and 120 edges

Input:

sierpinski_graph(4,3,triangle)

Output:

an undirected unweighted graph with 42 vertices and 81 edges

2.17 Generalized Petersen graphs: petersen_graph

The command petersen_graph accepts one or two arguments: a positive integer n and optionally a positive integer k (which defaults to 2). The command returns generalized Petersen graph P(n,k) which is a connected cubic graph consisting of an inner star polygon n,k and an outer regular polygon n such that the corresponding vertices in inner and outer polygons are connected with edges. If k=1, the prism graph of order n is obtained.

For example, to obtain the dodecahedral graph P(10, 2) one may input:

petersen_graph(10)

Output:

an undirected unweighted graph with 20 vertices and 30 edges

To obtain Möbius-Kantor graph, input:

petersen_graph(8,3)

Output:

an undirected unweighted graph with 16 vertices and 24 edges

Note that Desargues, Dürer and Nauru graphs are also generalized Petersen graphs, respectively P(10,3), P(6,2) and P(12,5).

¹For the definition see the paper "A survey and classification of Sierpiński-type graphs" by Andreas M. Hinz et al.

2.18 Isomorphic copy of a graph: isomorphic_copy, permute_vertices, relabel_vertices

The three commands presented in this section are used to obtain isomorphic copies of an existing graph.

The command isomorphic_copy accepts two arguments, a graph G(V,E) and a permutation σ of order |V|, and returns the copy of graph G with vertices rearranged according to σ .

Input:

```
isomorphic_copy(path_graph(5), randperm(5))
```

Output:

an undirected unweighted graph with 5 vertices and 4 $\,$ edges

The command permute_vertices accepts two arguments, a graph G(V,E) and a list L of length |V| containing all vertices from V in a certain order, and returns a copy of G with vertices rearranged as specified by L. Input:

```
permute_vertices(path_graph([a,b,c,d]),[b,d,a,c])
```

Output:

an undirected unweighted graph with 4 vertices and 3 $\,$ edges

The command $relabel_vertices$ accepts two arguments, a graph G(V,E) and a list L of vertex labels, and returns the copy of G with vertices relabeled with labels from L.

Input:

```
relabel_vertices(path_graph(4),[a,b,c,d])
```

Output:

an undirected unweighted graph with 4 vertices and 3 $\,$ edges $\,$

2.19 Extracting subgraphs of a graph: subgraph, induced_subgraph

The command subgraph accepts two arguments, a graph G(V,E) and a list of edges $L \subset E$, and returns the subgraph of G formed by edges from L. Input:

```
subgraph (complete_graph (5), [[1,2], [2,3], [3,4], [4,1]])
```

Output:

an undirected unweighted graph with 4 vertices and 4 edges

The command induced_subgraph accepts two arguments, a graph G(V,E) and a list of vertices $L\subset V$, and returns the subgraph of G formed by all edges in E which have endpoints in L.

Input:

```
induced_subgraph(petersen_graph(5),[1,2,3,6,7,9])
```

Output:

an undirected unweighted graph with 6 vertices and 6 edges

2.20 Underlying graph: underlying_graph

The command underlying_graph accepts a graph G as its only argument and returns the underlying graph of G obtained by dropping the directions of arcs and weights of edges/arcs.

Input:

```
G:=digraph(%{[[1,2],6],[[2,3],4],[[3,1],5]%})
```

Output:

a directed weighted graph with 3 vertices and 3 ${\it arcs}$

Input:

```
underlying_graph(G)
```

Output:

an undirected unweighted graph with 3 vertices and 3 edges

2.21 Reversing the edge directions: reverse_graph

The command reverse_graph accepts a graph G(V,E) as its only argument and returns the reverse graph $G^T(V,E')$ of G where $E'=\{(j,i):(i,j)\in E\}$, i.e. returns the copy of G with the directions of all edges reversed. It is defined for both directed and undirected graphs, but gives meaningful results only for directed graphs. G^T is also called the $transpose\ graph$ of G because adjacency matrices of G and G^T are transposes of each other.

Input:

```
G:=digraph(6, %{[1,2],[2,3],[2,4],[4,5]%}):;
GT:=reverse_graph(G):; edges(GT)
```

Output:

```
Done, Done, [[2,1],[3,2],[4,2],[5,4]]
```

2.22 Graph complement: graph_complement

The command graph_complement accepts a graph G(V, E) as its only argument and returns the complement GC(V, EC) of G, where EC is the largest set containing only edges/arcs not present in G.

Input:

```
graph_complement(cycle_graph(5))
```

Output:

an undirected unweighted graph with 5 vertices and 5 edges

2.23 Union of graphs: graph_union, disjoint_union

The command graph_union accepts a sequence of graphs $G_k(V_k, E_k)$ for $k = 1, 2, \ldots, n$ as its argument and returns their union G(V, E), where $V = V_1 \cup V_2 \cup \cdots \cup V_k$ and $E = E_1 \cup E_2 \cup \cdots \cup E_k$. Input:

```
G1:=graph([1,2,3],%{[1,2],[2,3]%}):;
G2:=graph([1,2,3],%{[3,1],[2,3]%}):;
graph_union(G1,G2)
```

Output:

```
Done, Done, an undirected unweighted graph with 3 vertices and 3 edges
```

The command disjoint_union accepts a sequence of graphs $G_k(V_k, E_k)$ for $k=1,2,\ldots,n$ as its argument and returns their disjoint union G(V,E), obtained by labeling all vertices with strings "k:v" where $v\in V_k$ and all edges with strings "k:e" where $e\in E_k$ and calling the graph_union command subsequently. As all vertices and edges are labeled differently, it follows $|V|=\sum_{k=1}^n |V_k|$ and $|E|=\sum_{k=1}^n |E_k|$. Input:

```
disjoint_union(cycle_graph(3), path_graph(3))
```

Output:

an undirected unweighted graph with 6 vertices and 5 edges

2.24 Joining two graphs: graph_join

The command graph_join accepts two graphs G and H as its arguments and returns the graph which is obtained by connecting all the vertices of G to all vertices of H. The vertex labels in the resulting graph are strings of the form "1:u" and "2:v" where u is a vertex in G and v is a vertex in H. Input:

Output:

an undirected unweighted graph with 5 vertices and 7 edges

2.25 Graph power: graph_power

The command graph_power accepts two arguments, a graph G(V,E) and a positive integer k, and returns the k-th power G^k of G with vertices V such that $v,w,\in V$ are connected if and only if there exists a path of length at most k in G. The adjacency matrix A_k of G^k is obtained by adding powers of the adjacency matrix A of G together:

$$A_k = \sum_{i=1}^k A^k.$$

The above sum is obtained by assigning $A_k \leftarrow A$ and repeating k-1 times the instruction $A_k \leftarrow (A_k+I) A$, so exactly k matrix multiplications and k additions are required.

Input:

Output:

an undirected unweighted graph with 5 vertices and 7 edges

Input:

Output:

an undirected unweighted graph with 5 vertices and 9 edges

2.26 Reversing the edge directions: reverse_graph

The command reverse_graph accepts a graph G(V,E) as its only argument and returns the reverse graph $G^T(V,E')$ of G where $E'=\{(j,i):(i,j)\in E\}$, i.e. returns the copy of G with the directions of all edges reversed. It is defined for both directed and undirected graphs, but gives meaningful results only for directed graphs. G^T is also called the $transpose\ graph$ of G because adjacency matrices of G and G^T are transposes of each other.

Input:

```
G:=digraph(6, %{[1,2],[2,3],[2,4],[4,5]%}):;
    GT:=reverse_graph(G):; edges(GT)
```

Output:

2.27 Graph product: cartesian_product, tensor_product

The command cartesian_product accepts a sequence of graphs $G_k(V_k, E_k)$ for $k=1,2,\ldots,n$ as its argument and returns the Cartesian product $G_1\times G_2\times\cdots\times G_n$ of the input graphs. The Cartesian product $G(V,E)=G_1\times G_2$ is the graph with list of vertices $V=V_1\times V_2$, labeled with strings " v_1 : v_2 " where $v_1\in V_1$ and $v_2\in V_2$, such that (" u_1 : v_1 "," u_2 : v_2 ") is in E if and only if u_1 is adjacent to u_2 and $v_1=v_2$ or $v_1=v_2$ and $v_2=v_3$ and $v_3=v_3=v_4$. Input:

G1:=graph(trail(1,2,3,4,1,5)):; G2:=star_graph(3):;

Output:

Done, Done

Input:

cartesian_product(G1,G2)

Output:

an undirected unweighted graph with 20 vertices and 35 edges

The command tensor_product accepts a sequence of graphs $G_k(V_k, E_k)$ for $k=1,2,\ldots,n$ as its argument and returns the tensor product $G_1\times G_2\times \cdots \times G_n$ of the input graphs. The tensor product $G(V,E)=G_1\times G_2$ is the graph with list of vertices $V=V_1\times V_2$, labeled with strings " v_1 : v_2 " where $v_1\in V_1$ and $v_2\in V_2$, such that (" u_1 : v_1 "," u_2 : v_2 ") is in E if and only if u_1 is adjacent to u_2 and v_1 is adjacent to v_2 .

Input:

tensor_product (G1,G2)

Output:

an undirected unweighted graph with 20 vertices and 30 $\,$ edges $\,$

2.28 Seidel switch: seidel_switch

The command seidel_switch accepts two arguments, an undirected and unweighted graph G(V,E) and a list of vertices $L\subset V$, and returns the copy of G in which, for each vertex $v\in L$, its neighbors become its non-neighbors and vice versa.

Input:

seidel_switch(cycle_graph(5),[1,2])

Output:

an undirected unweighted graph with 5 vertices and 7 edges

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