

Example GIAC session



Here follows a sample session, which was started using $Insert {\rightarrow} Session {\rightarrow} Giac.$

Giac CAS for TeXmacs, released under the GPL license (3.0)

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Xcas (C-like) syntax mode

> f(x):=sin(x)+x

 $x \mapsto \sin x + x$

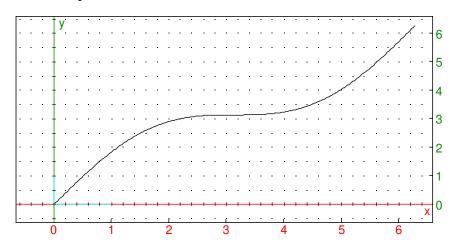
> diff(f(x),x)

 $\cos x + 1$

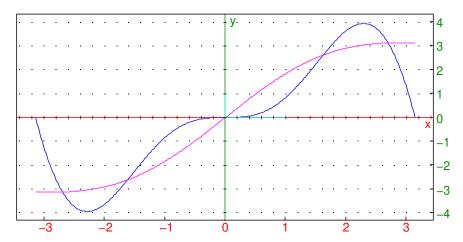
> integrate(f(x),x=0..pi)

$$\frac{\pi^2+2}{2}+1$$

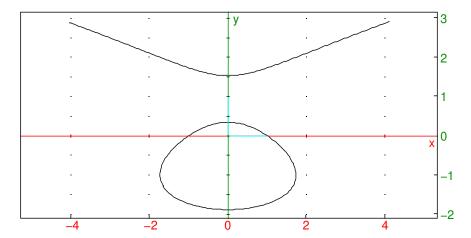
> plot(f(x),x=0..2*pi)



> plot([x^2*sin(x),f(x)],x=-pi..pi,color=[blue,magenta])



 $> implicitplot(x^2=y^3-3y+1,x=-4..4,y=-4..4)$



Mathematical and physical constants, including physical units, are typeset properly using the conventional notation whenever possible, as in the example below.

> e,i,pi,euler_gamma,inf,5_Angstrom,10_(m/s^2),_NA_,_REarth_,_hbar_

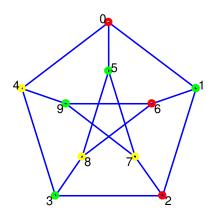
e, i,
$$\pi, \gamma, +\infty, 5$$
 Å, 10 $\frac{\mathrm{m}}{\mathrm{s}^2}, 1$ $N_{\!A}, 1$ $R_{\oplus}, 1$ \hbar

Graphs can be constructed, manipulated with and drawn.

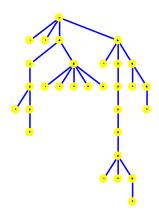
> G:=graph("petersen")

an undirected unweighted graph with 10 vertices and 15 edges

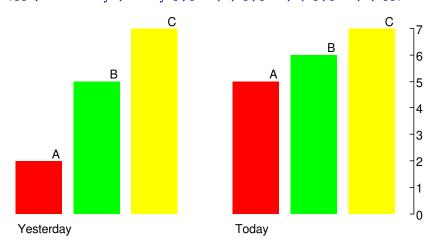
> draw_graph(highlight_vertex(G,vertices(G),greedy_color(G)))



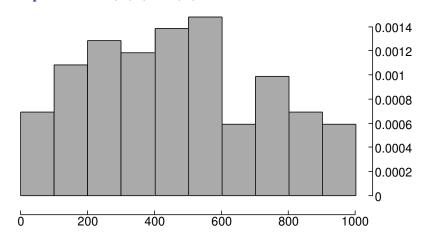
> draw_graph(random_tree(30),labels=false)



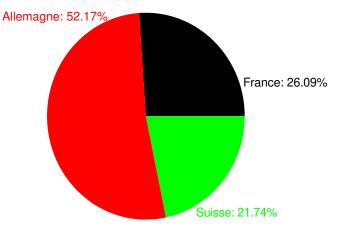
In the following examples it is demonstrated how to create bar plots, histograms and pie charts. > bar_plot([[2,"Yesterday","Today"],["A",2,5],["B",5,6],["C",7,7]])



> histogram(seq(rand(1000),k,0,100),0,100)

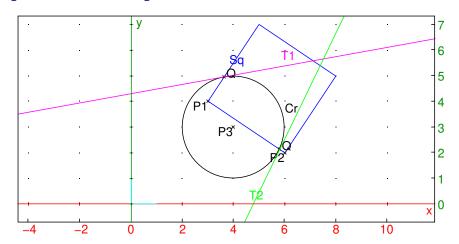


> camembert([["France",6],["Allemagne",12],["Suisse",5]])



A 2D geometry example:

> P1:=point(3,4); P2:=point(6,2); P3:=point(4,3); Sq:=square(P1,P2,color=blue);
Cr:=circle(P3,2); Q:=inter(Sq,Cr); T1:=tangent(Cr,Q[0],color=magenta);
T2:=tangent(Cr,Q[1],color=green)



The GIAC plugin has a good support for mathematical input mode. Besides the usual algebraic expressions, the following standard notations are supported:

- (partial) derivatives
- integrals, sums and products
- limits
- piecewise defined functions
- simplified notation for powers of trigonometric and other elementary functions (e.g. $\sin^2 x$)
- absolute values, floor, ceiling
- sets, lists, and matrices
- special functions
- complex conjugates, real and imaginary parts
- etc.

When entering derivatives, the function application symbol (entered by pressing Space) between the derivative operator and the argument is mandatory, as well as the parentheses around the argument. To hide the latter, one can enter invisible parentheses by pressing (Tab, which are treated as normal parentheses. Note that they are used around the argument of ln function in the expressions below (parentheses around function arguments are mandatory in GIAC).

$$> \frac{\mathrm{d}}{\mathrm{d}x} \left(x \ln x - \frac{1}{1-x} \right)$$

$$\ln x + 1 - \frac{1}{(1-x)^2}$$

$$> \frac{\mathrm{d}^2}{\mathrm{d}x^2} \left(x \ln x - \frac{1}{1-x} \right)$$

$$\frac{x^3 - 3\,x^2 + 5\,x - 1}{x^4 - 3\,x^3 + 3\,x^2 - x}$$

In the following example, the stationary points of the function f are computed.

$$> f := \text{unapply}\left(\frac{\ln x}{r} - \frac{r x}{x+1}, x\right)$$

$$x \mapsto \frac{\ln x}{r} - \frac{rx}{x+1}$$

> solve
$$\left(\frac{\mathrm{d}}{\mathrm{d}x}f(x) = 0, x\right)$$

$$\left[\frac{r^2 + r\sqrt{r^2 - 4} - 2}{2}, \frac{r^2 - r\sqrt{r^2 - 4} - 2}{2}\right]$$

Various notations for deriatives in differential equations are supported.

> dsolve
$$\left(\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} - y = 2\sin x, x, y\right)$$

$$c_0 e^x + c_1 e^{-x} - \sin x$$

> dsolve
$$(y'' - y = 2 \sin x \wedge y(0) = 0 \wedge y'(0) = 1, x, y)$$

$$e^x - e^{-x} - \sin x$$

$$>$$
 dsolve ($\ddot{x} = x, t, x$)

$$c_0 e^t + c_1 e^{-t}$$

> simplify (dsolve
$$(y^{(3)} = t + y, t, y)$$
)

$$c_0 e^t + c_1 \cos\left(\frac{1}{2}\sqrt{3}t\right) e^{-\frac{t}{2}} + c_2 e^{-\frac{t}{2}} \sin\left(\frac{1}{2}\sqrt{3}t\right) - t$$

Partial derivatives are supported as well.

$$> \text{collect}\left(\frac{\partial^3}{\partial x \, \partial y^2} \left(\frac{y \, \mathrm{e}^{-x}}{x^2 + y^2}\right)\right)$$

$$\frac{2\,y \left(3\,{x}^{4}+12\,{x}^{3}+2\,{x}^{2}\,{y}^{2}-12\,x\,{y}^{2}-{y}^{4}\right) {{\rm e}^{-x}}}{(\,{y}^{2}+{x}^{2})^{4}}$$

$$> \frac{\partial^2}{\partial x \, \partial y} g(x, x \, y)$$

$$x y g^{(2,2)}(x, x y) + x g^{(1,2)}(x, x y) + g^{(2)}(x, x y)$$

> addtable (fourier, y(x), Y(s), x, s)

1

>
$$T := \text{fourier}\left(y\left(x+1\right) - \frac{d^3}{dx^3}y\left(x\right), x, s\right)$$

$$(e^{is} + is^3) Y(s)$$

> eq:=euler_lagrange
$$(x^2 \cdot (y')^2 + 2y^2)$$

$$\frac{\mathrm{d}^{2}}{\mathrm{d}x^{2}}y\left(x\right) = \frac{-2\frac{\mathrm{d}}{\mathrm{d}x}y\left(x\right)x + 2y\left(x\right)}{x^{2}}$$

> dsolve (eq, x, y)

$$\frac{\left(-\frac{c_0}{3x^3}+c_1\right)x^3}{x^2}$$

Integrals, sums and products are entered in the usual way.

$$> \int \frac{1}{(x^2+9)^3} \, \mathrm{d}x$$

$$\frac{x^3 + 15 x}{216 (x^2 + 9)^2} + \frac{\arctan\left(\frac{x}{3}\right)}{648}$$

$$> \int_0^{\pi/4} \sqrt{\tan x} \, \mathrm{d}x$$

$$\frac{\pi\sqrt{2}-\sqrt{2}\ln\left(\sqrt{2}+2\right)+\sqrt{2}\ln\left(-\sqrt{2}+2\right)}{4}$$

$$> \int_{-\infty}^{+\infty} e^{-x^2} dx$$

$$\sqrt{\pi}$$

> assume $(\alpha > 0)$

 α

$$> \int_0^{+\infty} \ln\left(1 + \frac{\alpha^2}{x^2}\right) dx$$

 $\pi \alpha$

$$> \sum_{k=1}^{+\infty} \frac{1}{1+\pi^2 k^2}$$

$$\frac{1}{e^2 - 1}$$

$$> \prod_{k=1}^{10} \left(1 - \frac{1}{2k^2}\right)$$

$$\frac{103376401778279}{275188285440000}$$

Heaviside function and Dirac δ -distribution are associated with upright Greek symbols ϑ and δ , respectively.

$$> F := \text{fourier}\left(\frac{x}{x^2 - x + 1}, x, \omega\right)$$

$$\pi \left(i \vartheta \left(-\omega \right) e^{\frac{\omega \sqrt{3} - i\omega}{2}} - i \vartheta \left(\omega \right) e^{\frac{-\omega \sqrt{3} - i\omega}{2}} + e^{-\frac{1}{2} i\omega} e^{-\frac{3|\omega|e^{-\frac{\ln(3)}{2}} + \ln(3)}{2}} \right)$$

 $> F := \exp 2pow (lin (F))$

$$\pi\,i\,\vartheta\,(-\omega)\,e^{\frac{\omega\,\sqrt{3}-i\,\omega}{2}} - \pi\,i\,\vartheta\,(\omega)\,e^{-\frac{\omega\,\sqrt{3}+i\,\omega}{2}} + \pi\,e^{\frac{-i\,\omega\,\sqrt{3}-3\,|\omega|}{2\,\sqrt{3}}}\sqrt{3}^{-1}$$

> ifourier (F, ω, x)

$$\frac{x}{x^2 - x + 1}$$

> h :=fourier (1)

$$2\pi\delta(x)$$

> ifourier(h)

GIAC can determine domain of an univariate real function and solve inequalities.

$$\rightarrow$$
 domain $\left(\sqrt{3-\sqrt{2-\sqrt{1-x}}},x\right)$

$$x \geqslant -3 \land x \leqslant 1$$

> solve
$$(|2x^2 - 3| \le 5, x)$$

$$[x \geqslant -2 \land x \leqslant 2]$$

$$>$$
 solve $(x - |x - |x^2 - 3x - 2|| - 1 > 0, x)$

$$\left[\,x>\frac{\sqrt{13}+1}{2} \land x<\frac{\sqrt{13}+3}{2}, x>\frac{\sqrt{21}+3}{2} \land x<\frac{\sqrt{29}+5}{2}\,\right]$$

A partial fractions decomposition example:

> partfrac
$$\left(\frac{x^4 - 44x^3 + 22x^2 - 11x + 1}{x^5 + 3x^4 + x^3 - x^2 - 4}, x\right)$$

$$-\frac{31}{18 \left(x-1\right)}-\frac{479}{15 \left(x+2\right)^2}+\frac{1742}{225 \left(x+2\right)}+\frac{-251 \, x+107}{50 \left(x^2+1\right)}$$

Simplification and auto-simplification examples:

> simplify
$$\left(\sqrt{5+2\sqrt{6}} + \sqrt{9-2\sqrt{6}-4\sqrt{5-2\sqrt{6}}}\right)$$

$$2\sqrt{2}+2$$

$$>$$
 simplify $\left(\cot\left(\arctan\left(\frac{12}{13}\right) + a\cos\left(\frac{4}{5}\right)\right)\right)$

$$\frac{16}{87}$$

> trigsimplify
$$\left(1 - \frac{1}{4}\sin^2(2x) - \sin^2 y - \cos^4 x\right)$$

$$\sin^2 x - \sin^2 y$$

> trigsimplify
$$\left(\frac{\sum_{n=1}^{5} \sin{(n \, x)}}{\sum_{n=1}^{5} \cos{(n \, x)}}\right)$$

$$\tan(3x)$$

> assume (n, integer); additionally $(n \ge 0)$

$$\mathbb{Z}, n$$

$$> \Gamma(n+1)$$

n!

 $> \cos(n\pi)$

$$(-1)^n$$

Binomial coefficients are entered using the binom tag. > $\binom{49}{7}$

85900584

An expression with the wide bar accent is interpreted as the complex conjugate. Additionally, the usual notation for real and imaginary parts is supported.

> csolve
$$(z^2 \cdot \bar{z} = \Re(z) - 8i, z)$$

$$[-2i]$$

Substitution of parameters in an expression can be executed using the | symbol, obtained by pressing | Tab.

$$> \cos^2 y + y \sin x | x = \frac{\pi}{3}, y = \frac{\pi}{4}$$

$$\left(\frac{\sqrt{2}}{2}\right)^2 + \frac{\pi\sqrt{3}}{4\cdot 2}$$

The invisible addition symbol, entered with + Tab Tab Tab, translates to +. > $7\sqrt[3]{4}$

$$\frac{31}{4}$$

The invisible symbol, entered with _ Tab Tab, is interpreted as the underscore (_). It is useful for e.g. differentiating between e.g. x0 and x_0 , which are both typeset (and, in math input mode, entered) as x_0 . However, in the latter case the invisible symbol is appended to x, as in the example below. Since the subscript of a symbol is simply appended to the symbol for input in GIAC, the concatenation yields x_0 . The invisible symbol is also used for entering physical units, which begin with _, and physical constants, which begin and end with _ in GIAC.

$$>$$
 simplify $(x_0 - x_0)$

$$-x_0 + x_0$$

> mksa (12.3 km²)

 12300000.0 m^2

>mksa(c)

$$299792458.0~{\rm m\,s^{-1}}$$

Bold symbols may be used, which is useful for denoting matrices and vectors. Bold symbols are input as double symbol, e.g. G is GG in GIAC. Note that indices in GIAC are 0-based by default. For 1-based indices, switch to Maple mode.

> **A**:= matrix
$$(4, 4, (j, k) \mapsto k + j^{k+1})$$

$$\left(\begin{array}{cccc}
0 & 1 & 2 & 3 \\
1 & 2 & 3 & 4 \\
2 & 5 & 10 & 19 \\
3 & 10 & 29 & 84
\end{array}\right)$$

 $> \det(\mathbf{A})$

-24

> **A**⁻¹

$$\begin{pmatrix}
-\frac{17}{6} & -\frac{3}{2} & \frac{3}{2} & -\frac{1}{6} \\
\frac{17}{6} & \frac{23}{4} & -\frac{7}{2} & \frac{5}{12} \\
-\frac{7}{6} & -4 & \frac{5}{2} & -\frac{1}{3} \\
\frac{1}{6} & \frac{3}{4} & -\frac{1}{2} & \frac{1}{12}
\end{pmatrix}$$

$$> \mathbf{v} := [-1, 3, 7]$$

$$[-1, 3, 7]$$

The expression below is computed as ℓ^2 -norm of \mathbf{v} .

 $> \|\mathbf{v}\|$

 $\sqrt{59}$

If A is a matrix, then its element a_{ij} can be fetched using the common notation, as below. Note that the indices in the subscript must be enclosed within invisible parentheses and separated by (invisible) comma.

 $> {\bf A}_{32}$

29

> $\mathbf{v}_1 + \mathbf{v}_2$

10

Limits are entered like in the examples below. Note that the body of a limit must be parenthesed (use invisible parentheses when appropriate) and prepended by the function application symbol.

$$> \lim_{x \to 0} \frac{1 - \frac{1}{2}x^2 - \cos\left(\frac{x}{1 - x^2}\right)}{x^4}$$

 $\frac{23}{24}$

 $> \lim_{x \to 0^+} e^{-1/x}$

0

 $= \lim_{x \to 1^{-}} \sin(\pi x)^{1/\ln(1-x)}$

е

 $> \lim_{n \to +\infty} \left(\sqrt[3]{n^3 - 2n^2 + n - 1} - n \right)$

 $-\frac{2}{3}$

It can be shown that be shown that the series $\sum_{n=0}^{\infty} s(n)$, where s is defined below, converges to $\frac{1}{\pi}$ (J. M. Borwein et al., 1989). We prove the convergence using the criterion of D'Alembert and compute the number of significant digits in the approximation of π using the first 11 terms.

>
$$s(n) := {2n \choose n}^3 \frac{42n+5}{2^{12n+4}}$$

$$n \mapsto {2n \choose n}^3 \frac{42n+5}{2^{12n+4}}$$

$$\lim_{n \to +\infty} \frac{s(n+1)}{s(n)} < 1$$

true

$$> p := \left(\sum_{n=0}^{10} s(n)\right)^{-1}$$

 $\frac{332306998946228968225951765070086144}{105776603012651189498293061907704445}$

> simplify $(1 + \lfloor -\log_{10}(2|\pi - p|) \rfloor)$

The symbol ε stands for epsilon() in GIAC, which is by default set to 10^{-12} . > $125.483 \, \varepsilon$

$$1.25483\times 10^{-10}$$

Finite sequences, lists, and sets can be generated as in the examples below. The symbol | is entered by pressing | Tab Tab Tab Tab Tab.

> euler (k) | k = 1...20

$$1, 1, 2, 2, 4, 2, 6, 4, 6, 4, 10, 4, 12, 6, 8, 8, 16, 6, 18, 8\\$$

> [ithprime (j) | j = 1...20]

$$[2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71]$$

 $A := \{k^2 \mid k = 1...10\}$

$$\{1, 4, 9, 16, 25, 36, 49, 64, 81, 100\}$$

 $> B := \{1 + 8k \mid k = 1...10\}$

$$\{9, 17, 25, 33, 41, 49, 57, 65, 73, 81\}$$

 $> C := \{9, 18, 27\}$

$$\{9, 18, 27\}$$

Set operations are entered in the usual way.

 $> A \setminus B$

 $> (A \cap B) \cup C$

$$\{9, 25, 49, 81, 18, 27\}$$

Using the notation $a \in A$ we get the 1-based index of the element a in the set A, or 0 if $a \notin A$. $> 19 \in A, 57 \in B$

0, 7

The usual notation for composition of functions is supported.

 $> (\cos \circ \sin)(\pi)$

1

 $f := x \mapsto x^2 + 1; g := y \mapsto y - 1$

$$x \mapsto x^2 + 1, y \mapsto y - 1$$

 $> (f \circ g)(4)$

10

Conditionals are entered like in the examples below.

> 1 === 2

false

 $> 1 \neq 0$

true

>assume $(h \ge 0)$

h

> h < h + 1

true

 $> \sin(h) - h \leqslant 2$

true

Polynomials may be entered as lists of coefficients with double-struck brackets.

> p := [-1, 3, 2]; q := [2, 0, -2, 1]

$$[-1, 3, 2], [2, 0, -2, 1]$$

 $> p \cdot q$

$$[-2, 6, 6, -7, -1, 2]$$

> expand (poly2symb (p+q,x))

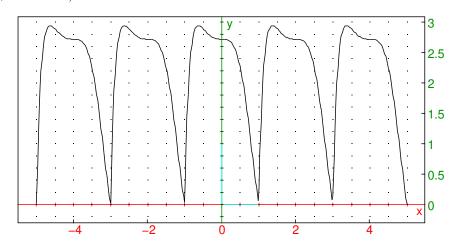
$$2x^3 - x^2 + x + 3$$

Periodic functions can be defined, as demonstrated below.

> $h := \text{periodic}((1-x^4)e^{1-x^3}, x = -1...1)$

$$\left(1 - \left(x - 2\left|\frac{x+1}{2}\right|\right)^4\right) e^{1 - \left(x - 2\left|\frac{x+1}{2}\right|\right)^3}$$

> plot (h, x = -5...5)

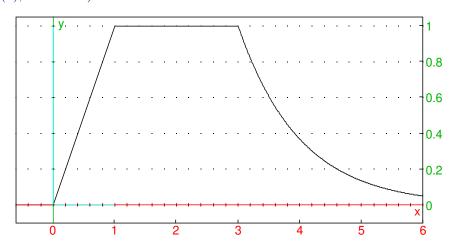


Piecewise functions are supported as well. Note that a textual "condition" (a text tag) is interpreted as "otherwise", no matter of its contents.

$$> f(x) := \begin{cases} 0, & x < 0 \\ x, & x < 1 \\ 1, & x < 3 \\ \mathrm{e}^{3-x}, & \text{in all other cases} \end{cases}$$

$$x \mapsto \begin{cases} 0, & x < 0 \\ x, & x < 1 \\ 1, & x < 3 \\ e^{3-x}, & \text{otherwise} \end{cases}$$

> plot (f(x), x = -1...6)



>