

$$12. y = f(x, c) = \text{pow\_constant}(x, c) = x^c$$

$$12.3 \quad dx = dy \cdot c x^{c-1}$$

$$13. y = f(c, \infty) = \text{constant\_pow}(c, \infty) = c^\infty$$

$$13.3 \quad dx = dy \cdot y \ln c$$

$$14. y = f(\infty) = \text{negate}(x) = -x$$

$$14.3 \quad dx = -dy$$

$$15. y = f(x) = \exp(x) = e^x$$

$$15.3 \quad dx = dy \cdot e^x = y dy$$

$$16. y = f(x) = \log(x) = \ln x$$

$$16.3 \quad dx = \frac{dy}{x}$$

$$17. y = f(x) = \log(p(x)) = \log((1+x)^{\frac{1}{n(x+1)}})$$

$$17.3 \quad dx = dy \cdot \frac{1}{x+1}$$

$$y = f(x, c) = \text{add\_constant}(x, c) = x + c$$

$$6.3 \quad dx = dy$$

$$7. y = f(x, c) = \text{sub\_constant}(x, c) = x - c$$

$$7.3 \quad dx = dy$$

$$8. y = f(c, x) = \text{constant\_sub}(c, x) = c - x$$

$$8.2 \quad y = x \cdot \text{new\_sets}(x) \cdot \text{fill}(c) \cdot \text{sub\_onto}(x)$$

$$8.3 \quad dx = -dy$$

$$9. y = f(x, k) = \text{mul\_constant}(x, k) = kx$$

$$9.3 \quad dx = k dy$$

$$10. y = f(\infty, k) = \text{div\_constant}(x, k) = \frac{\infty}{k}$$

$$10.3 \quad dx = \frac{dy}{k}$$

$$11. y = f(k, \infty) = \text{constant\_div}(k, \infty) = \frac{k}{\infty}$$

$$11.2 \quad y = x \cdot \text{new\_sets}(x) \cdot \text{fill}(k) \cdot \text{div}(x)$$

$$11.3 \quad dx = -\frac{k}{x^2} dy, \text{ here } dx := \frac{dL}{dx}$$

$$dy := \frac{dL}{dy}$$

$$\boxed{+ \dots +}$$

$$1. \text{ add: } z = f(x, y) = x + y$$

$$1.3 \quad dz \Rightarrow dx, dy, \text{ here } dz := \frac{dL}{dz}$$

$$(dx, dy) = (dz, dz)$$

$$2. z = f(x, y) = \text{sub}(x, y) = x - y$$

$$2.3 \quad (dx, dy) = (dz, -dz)$$

$$3. z = f(x, y) = \text{mul}(x, y) = xy$$

$$3.3 \quad (dx, dy) = (y dz, x dz)$$

$$4. z = f(x, y) = \text{div}(x, y) = \frac{x}{y}$$

$$4.3 \quad (dx, dy) = \left(\frac{dz}{y}, -\frac{x dz}{y^2}\right)$$

$$= \left(\frac{dz}{y}, -\frac{z dz}{y}\right)$$

$$y = f(x, p) = \text{pow}(x, p) = x^p$$

$$(dx, dp) = (dy \cdot p x^{p-1}, dy \cdot x^p \ln x)$$

$$= (dy \cdot p x^{\frac{y}{x}}, dy \cdot y \ln x)$$