

$$p \notin L,$$

$$\Rightarrow \text{distance}(p, L)$$

$$\text{solve: } \text{let } x_0 \in L, x_0 \in L^*$$

$$\text{here } L^* = \{x \mid dx + c = 0\}$$

$$c = -p \cdot d \in \mathbb{R}.$$

L^* is plane

$$\text{② } \text{distance}(p, L)$$

$$= \|x_0 - p\|$$

$$\text{③ } \text{let } dx + c = 0, x_0 \in L$$

$$\text{let } da + \lambda \|d\|^2 + c = 0$$

$$\text{let } \lambda = \frac{(p-a) \cdot d}{\|d\|^2}$$

$$\Rightarrow x_0 = a + \lambda d$$

$$\Rightarrow ds = \|x_0 - p\|$$

$$\text{④ } L(p)$$

$$= L(p - x_0) + L(x_0) - c$$

$$= L(p - x_0) - c$$

$$= L(-s_0 n) - c$$

$$= -s_0 \|n\|^2$$

$$\text{let } \|s_0\| n = \frac{L(p)}{\|n\|}$$

$$\text{⑤ } \text{let } ds = \|p - x_0\|$$

$$= \| -s_0 n \|$$

$$= \frac{L(p)}{\|n\|}$$

2. line L in \mathbb{R}^n ,

$$L = \{x \mid a + \lambda d = x\} \quad \forall \lambda \in \mathbb{R}$$

$$\boxed{\text{distance}(p, L)}$$

1. plane L in \mathbb{R}^n ,

$$L = \{x \mid nx + c = 0\}, p \notin L, c \in \mathbb{R},$$

$$\Rightarrow \text{distance}(p, L)$$

solve:

$$\text{① let } L(x) = nx + c,$$

$$\text{let } L^* = \{x \mid x = p + sn, \forall s \in \mathbb{R}\}$$

$$\text{② let } x_0 \in L^*, x_0 \in L$$

$$\Rightarrow \text{distance}(p, L) = \|p - x_0\|$$

$$\text{③ } \text{let } \exists s_0, \text{ s.t. } x_0 = p + s_0 n,$$

$$\text{let } x_0 \in L, \therefore L(x_0) = 0$$