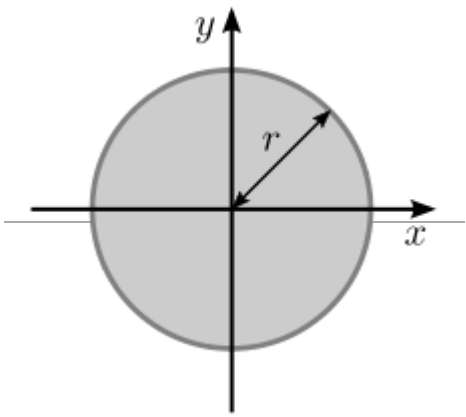
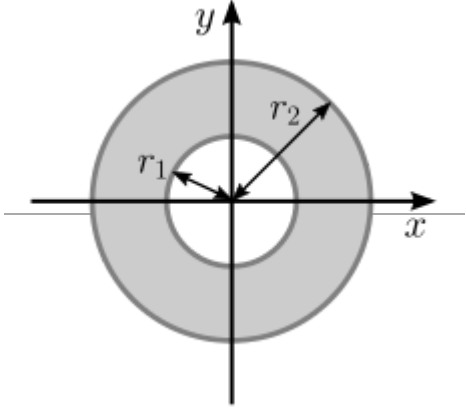
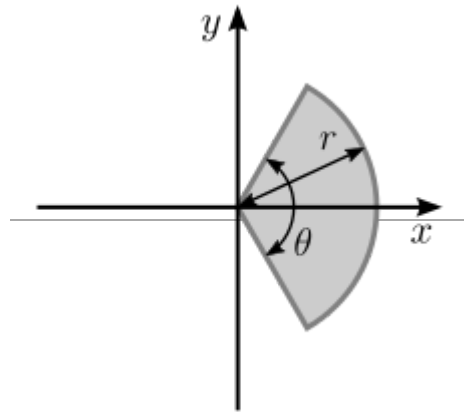
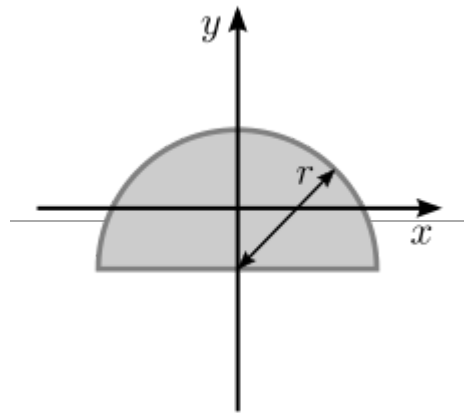


Description	Figure	Area moment of inertia	Comment
A filled circular area of radius r		$I_x = \frac{\pi}{4} r^4$ $I_y = \frac{\pi}{4} r^4$ $I_z = \frac{\pi}{2} r^4 \text{ [1]}$	I_z is the <u>Polar moment of inertia</u> .
An <u>annulus</u> of inner radius r_1 and outer radius r_2		$I_x = \frac{\pi}{4} (r_2^4 - r_1^4)$ $I_y = \frac{\pi}{4} (r_2^4 - r_1^4)$ $I_z = \frac{\pi}{2} (r_2^4 - r_1^4)$	For thin tubes, $r \equiv r_1 \approx r_2$ and $r_2 \equiv r_1 + t$. So, for a thin tube, $I_x = I_y \approx \pi r^3 t$. I_z is the <u>Polar moment of inertia</u> .
A filled circular sector of angle θ in radians and radius r with respect to an axis through the centroid of the sector and the center of the circle		$I_x = (\theta - \sin \theta) \frac{r^4}{8}$	This formula is valid only for $0 \leq \theta \leq \pi$



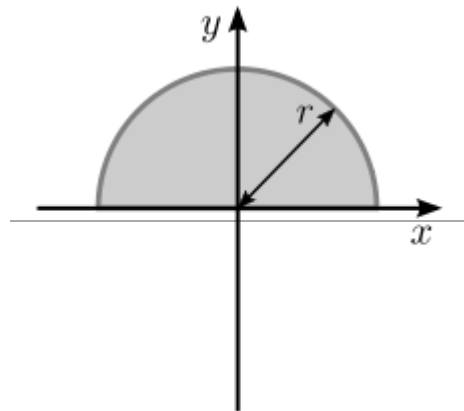
A filled semicircle with radius r with respect to a horizontal line passing through the centroid of the area



$$I_x = \left(\frac{\pi}{8} - \frac{8}{9\pi} \right) r^4 \approx 0.1098r^4$$

$$I_y = \frac{\pi r^4}{8} \quad [2]$$

A filled semicircle as above but with respect to an axis collinear with the base

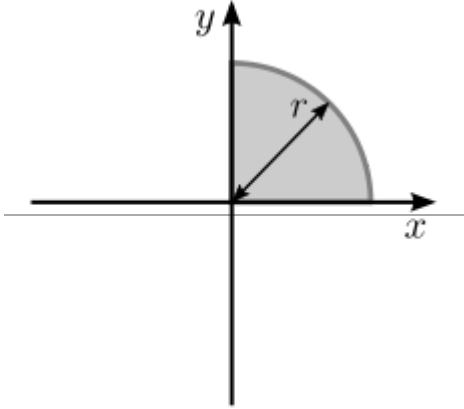
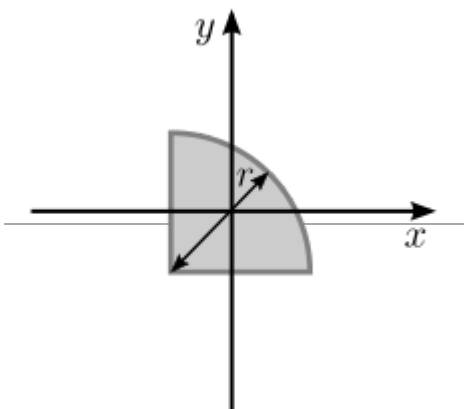
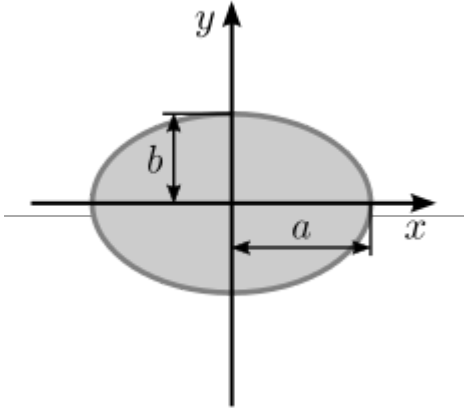


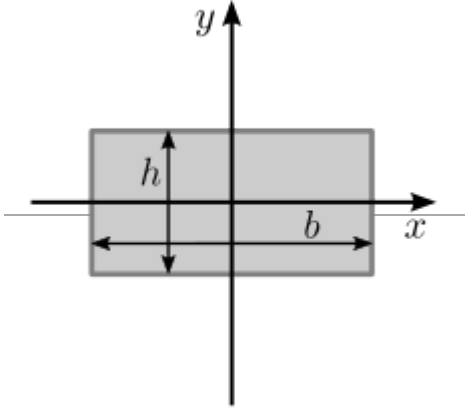
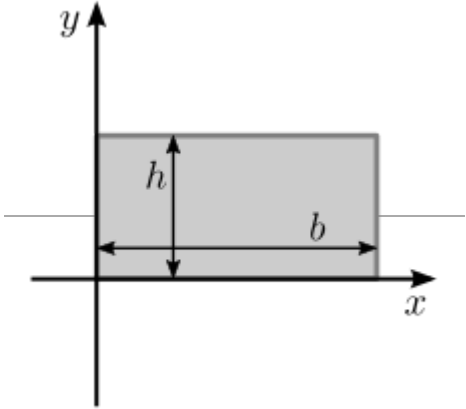
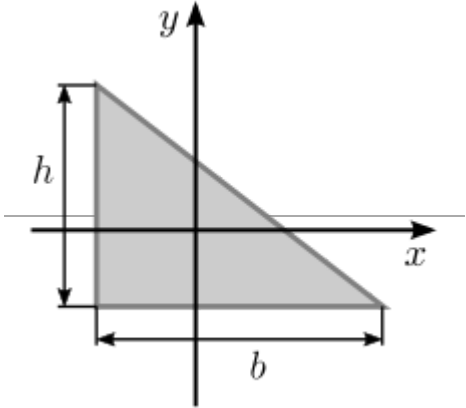
$$I_x = \frac{\pi r^4}{8}$$

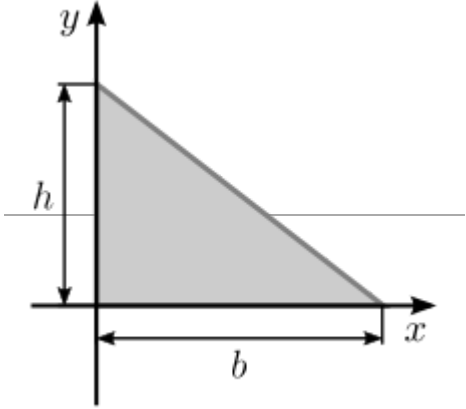
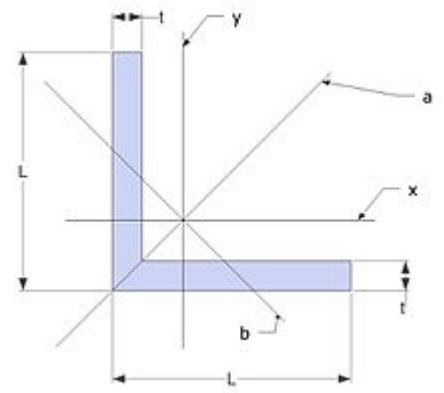
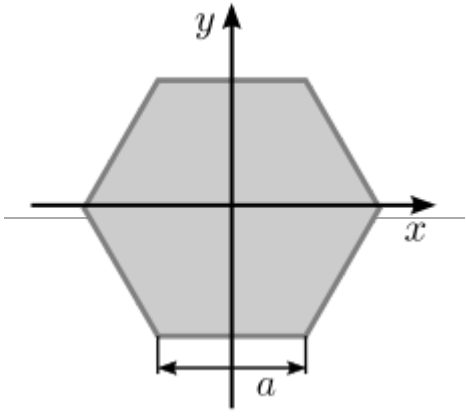
$$I_y = \frac{\pi r^4}{8} \quad [2]$$

I_x : This is a consequence of the parallel axis theorem and the fact that the distance between the x axes of the previous one and this one is $\frac{4r}{3\pi}$

A filled quarter circle with radius r with the

<p>axes passing through the bases</p>		$I_x = \frac{\pi r^4}{16}$ $I_y = \frac{\pi r^4}{16} \text{ [3]}$	
<p>A filled quarter circle with radius r with the axes passing through the centroid</p>		$I_x = \left(\frac{\pi}{16} - \frac{4}{9\pi} \right) r^4 \approx 0.0549r^4$ $I_y = \left(\frac{\pi}{16} - \frac{4}{9\pi} \right) r^4 \approx 0.0549r^4 \text{ [3]}$	<p>This is a consequence of the parallel axis theorem and the fact that the distance between these two axes is $\frac{4r}{3\pi}$</p>
<p>A filled ellipse whose radius along the x-axis is a and whose radius along the y-axis is b</p>		$I_x = \frac{\pi}{4} ab^3$ $I_y = \frac{\pi}{4} a^3 b$	
<p>A filled rectangular area with a base width of</p>			

b and height h		$I_x = \frac{bh^3}{12}$ $I_y = \frac{b^3h}{12} \text{ [4]}$	
A filled rectangular area as above but with respect to an axis collinear with the base		$I_x = \frac{bh^3}{3}$ $I_y = \frac{b^3h}{3} \text{ [4]}$	This is a result from the <u>parallel axis theorem</u>
A filled triangular area with a base width of b and height h with respect to an axis through the centroid		$I_x = \frac{bh^3}{36}$ $I_y = \frac{b^3h}{36} \text{ [5]}$	
A filled triangular area as above but with			This is a

<p>respect to an axis collinear with the base</p>		$I_x = \frac{bh^3}{12}$ $I_y = \frac{b^3h}{12} \text{ [5]}$	<p>consequence of the <u>parallel axis theorem</u></p>
<p>An equal legged angle, commonly found in engineering applications</p>		$I_x = I_y = \frac{t(5L^2 - 5Lt + t^2)(L^2 - Lt + t^2)}{12(2L - t)}$ $I_{(xy)} = \frac{L^2t(L - t)^2}{4(t - 2L)}$ $I_a = \frac{t(2L - t)(2L^2 - 2Lt + t^2)}{12}$ $I_b = \frac{t(2L^4 - 4L^3t + 8L^2t^2 - 6Lt^3 + t^4)}{12(2L - t)}$	<p>$I_{(xy)}$ is the often unused product of inertia, used to define inertia with a rotated axis</p>
<p>A filled <u>regular hexagon</u> with a side length of a</p>		$I_x = \frac{5\sqrt{3}}{16}a^4$ $I_y = \frac{5\sqrt{3}}{16}a^4$	<p>The result is valid for both a horizontal and a vertical axis through the centroid, and therefore is also valid for an axis with arbitrary direction that passes through the origin.</p>