


CH 17 

Grammar

used to describe a seq of symbols

↳ operations

- ↳ concat
- ↳ repetition
- ↳ union
- ↳ + repetition
- ↳ character classes

Regular Grammar

A *regular* grammar has a special property: by substituting every nonterminal (except the root one) with its righthand side, you can reduce it down to a single production for the root, with only terminals and operators on the right-hand side.

Our URL grammar was regular. By replacing nonterminals with their productions, it can be reduced to a single expression:

```
url ::= 'http://' ([a-z]+ '.' )+ [a-z]
+ ( ':' [0-9]+ )? '/'
```

The Markdown grammar is also regular:

```
markdown ::= ( [^_]* | '_' [^_]* '_' )*
```

But our HTML grammar can't be reduced completely. By substituting righthand sides for nonterminals, you can eventually reduce it to something like this:

```
html ::= ( [^<>]* | '<i>' html '</i>' ) *
```

...but the recursive use of `html` on the righthand side can't be eliminated, and can't be simply replaced by a repetition operator either. So the HTML grammar is not regular.

Context-Free Grammars

- a language that can be expressed using the pre-defined system of grammar
- context-free \leftrightarrow regular
- nested languages are context free but not regular