

# Bootstrapping the Universal Wave Function

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I assume quantum mechanics applies to the entire universe and solve the Schrödinger equation exactly, obtaining a unique closed-form wavefunction of the universe. Quantum information and quantum geometry emerge as one from the bootstrap. The geometry of quantum information is central to the problem of time in quantum cosmology, which is resolved by an emergent flat space holographic duality between a timeless theory in Euclidean 3-space without a spin-2 field, and a theory in  $3 + 1$  spacetime dimensions with a spin-2 field. Among the observable consequences is a spectacular prediction: black holes are dark energy composite objects, implying all black holes grow in mass proportional to the third power of the cosmological scale factor. Another consequence is the de Sitter limit has a dual solution: a dual vacuum stress-energy tensor with the dark matter equation of state.

## I. INTRODUCTION

The cosmos seems to have been born into a spatially flat and thermal state of low entropy [1], originating from a curvature singularity beyond the effective field theory (EFT) description of space, time, matter, and energy [2]. This grand puzzle demands new physics.

The quantum-first program—the idea that spacetime and quantum fields emerge from the wavefunction of the Universe—has recently been proposed by Carroll [3, 4]. *Everett's Principle of Quantum Universality* is radically conservative: assume the Schrödinger equation is valid on all scales and throw away the collapse postulate [5]. How can it be that the world of dynamical spacetime and quantum fields follows from a single unifying principle? Carroll and Singh approach this problem by trying to find the most useful factorization of Hilbert space into quasi-classical subsystems with only the Hamiltonian and an initial state [7]. Since no preferred factorization is assumed, there is no preferred basis other than the eigenstates of the Hamiltonian, which is fully specified by its eigenspectrum (and the initial state). In other words, they attempt to derive the world from nothing more than a set of energy eigenvalues by decomposing Hilbert space into the most "information-rich" tensor factors. As ingenious as their approach is, it comes with classical baggage: a classical global time coordinate is assumed.

In this paper, I report a minimalistic bootstrapping of Everett's principle and what I claim is the logical conclusion of Everettian quantum mechanics (QM). No relic classical baggage is assumed. The exact form of the wavefunction of the universe and some of its *observable consequences* are derived. To the author's knowledge, this is the first attempt to write down the quantum state of the universe that is not some semiclassical approximation like the Hartle-Hawking no-boundary proposal [8, 9], Vilenkin's tunneling proposal [10, 11], or numerous minisuperspace models, which all assume the Wheeler-DeWitt (WdW) equation as a starting point [12].

No assumptions of space, time, matter, or energy are made and put in by hand. In what is to follow, I argue a corollary of quantum universality is this: nature has no fundamental scale—the *form* of the laws of physics remains unchanged on all scales. From this elementary assumption, everything that follows is pure deduction.

## II. ON THE ORIGINS OF THE UNIVERSE

Quantum universality implies there is no Heisenberg cut between quantum and classical systems. The Everettian view is austere. The universe, on all scales, is quantum. If nature has no fundamental scale, the mass term  $M$  in the Schrödinger equation must multiply out, implying

$$\hat{H}\Psi = 0. \quad (1)$$

Neither time nor mass-energy is fundamental. This further implies the wavefunction of the universe is scale-invariant:  $\Psi \sim a^n$  where  $a$  is the cosmological scale factor, and  $n$  is an arbitrary integer. One can now solve for the potential  $V$  and write down the following timeless equation:

$$\left(-\frac{\partial^2}{\partial a^2} + \frac{n(n-1)}{a^2}\right)\Psi = 0. \quad (2)$$

Clearly,  $\Psi$  can not be normalized. The above equation is not quite consistent with the axioms of QM. But observe the following. The potential is the scalar curvature of an  $n$ -sphere with radius  $a$ , the kinetic term is the scalar curvature of an  $n$ -hyperbola, and the right-hand side of the equation is the scalar curvature of Euclidean  $n$ -space. From this simple conformal bootstrap, the fundamental space forms emerge. There is a scalar curvature singularity at  $V(a=0)$ . Still, since the Hamiltonian annihilates the universal quantum state, the scalar curvature singularity cancels with the kinetic term, yielding a zero-total energy universe that implies global spatial flatness, a prediction consistent with current observations [1].

There is no unitary evolution of  $\Psi$ . A problem indeed. The timeless equation occupies a liminal space between

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geometry and quantum mechanics. Can we bootstrap our way to a consistent instantiation of the timeless equation? Yes, we can—with symmetry. There is a trivial  $\mathbb{Z}_2$  action  $a \rightarrow -a$  and a non-trivial  $\mathbb{Z}_2$  action  $n \rightarrow -n$ . The former is a symmetry of the system; the latter is not. Suppose we demand the latter is a symmetry of the system. The action  $n \rightarrow -n$  gives the potential  $R_{n+1} = \frac{n(n+1)}{a^2}$  and is interpreted as the scalar curvature of an  $(n+1)$ -sphere. The potential then becomes,

$$V \sim \begin{pmatrix} R_n & 0 \\ 0 & R_{n+1} \end{pmatrix} \quad (3)$$

implying  $\Psi$  is promoted to a pair of complex numbers, i.e., a spinor. A complex 2-spinor solution, together with the consequence of conformal flatness, implies an underlying  $SU(n=2)$  symmetry, forcing the self-consistent equations of motion to take the unique form:

$$(D^2 + V)\Psi = 0 \quad (4)$$

where

$$D = i(\sigma^1 \partial_1 + \sigma^2 \partial_2 + \sigma^3 \partial_3) \quad (5)$$

is the Dirac-spin operator and the  $\sigma^i$  are the Pauli matrices. In the limit  $V \rightarrow 0$ , we have  $D^2\Psi = D\Psi = 0$ , i.e., the Dirac equation. So for large scale factors, solutions to  $\hat{H}\Psi = 0$  are effectively harmonic spinors and the underlying space is a Calabi-Yau (spin) manifold.

Naively, the components of  $\Psi$  correspond to the 2-sphere and 3-sphere, respectively. The Hopf fibration uniquely relates these spheres: one can always think of the 3-sphere as a  $U(1)$ -fiber over the 2-sphere [13]. But there is a caveat. We know the components of the spinor are not real-valued power laws. They are complex. This means the potential will take a slightly different form from eq. (3) with the spinor components encoding the *quantized* 3-sphere as a  $U(1)$ -fiber over the *quantized* 2-sphere. It is implicitly assumed the fibration between the quantum spheres is preserved and that the  $U(1)$  fiber is the complex phase that complexifies the power-law components of  $\Psi$ .

Let us take a moment to absorb what we have learned. Starting from the simplest formulation of QM, we have deduced 1) the universe, as a whole, has three spatially flat directions, 2) there is an equivalence between energy and curvature, and 3) there is a deep geometric connection between fermions and spatial directions. Space and fermions have emerged from a conformal bootstrap of Everettian QM. And where there are spinors, there is spacetime. A map always exists between spinors of order  $n$  and tensors of order  $2n$ . We deduced  $n=2$ , so it stands to reason there must exist a path to emerge time and energy. Moreover, the fiber bundle structure of the qubit is the Hopf fibration, and the symmetry group of the qubit is  $SU(2)$ . Quantum information emerges from quantum universality!

## A. geometry of quantum information

Quantum universality implies the world can be organized into two unique views: the "ant's-eye" view, where observers experience the flow of time, and the "God's-eye" view, where everything that can happen happens everywhere all at once. From the God's-eye perspective, the world is unified as one eternal and unchanging quantum object—the universal wave function. Envisioning the future of fundamental physics, Frank Wilczek wrote in 2016, "To me, ascending from the ant's-eye view to the God's eye-view of physical reality is the most profound challenge for fundamental physics in the next 100 years" [14]. Alas, this is precisely the challenge we face. And there are subtle clues at the intersection of geometry and quantum information that lead the way.

The mapping from the unit 3-sphere in a two-dimensional complex Hilbert space  $\mathbb{C}^2$  (otherwise known as the complex projective line  $\mathbb{CP}^1$  or the complex plane  $\mathbb{C}$  with a point at infinity) to the Bloch sphere is the Hopf fibration. There is a direct correspondence between each spinor in  $\mathbb{C}^2$  and a point on the Bloch sphere. Schematically we write the fibration as  $S^1 \hookrightarrow S^3 \rightarrow S^2$ , i.e., embedding a 1-sphere in the 3-sphere 'wraps' the 3-sphere around the 2-sphere. The  $S^3$  therefore lives on the surface of  $S^2$  by the identification of phase circles in  $S^3$  with points on  $S^2$ . Every possible state of a two-level system (i.e., qubit) lives on the surface of  $S^2 \cong \mathbb{CP}^1$ . The system under question (the entire Universe) is not a two-level system. The components of  $\Psi$  are not simply elements of  $\mathbb{CP}^1$ . There is more structure that captures the intrinsic quantum nature of the 2-sphere. Nevertheless, the geometry of quantum information is a foundational starting point in solving eq. (4) and emerging time and quantum fields from  $\Psi$ .

The Hopf fibration has a symmetry group: the action of the unitary group  $U(2)$  on  $\mathbb{C}^2$  leaves the  $S^3$  invariant. It thus descends to an action on the 2-sphere by ordinary rotations, carrying fibers into fibers as it commutes with the  $U(1)$  action [13]. By the exceptional spin isomorphism  $\text{Spin}(3,1) \cong \text{SL}(2, \mathbb{C})$ , one may identify the points  $x_\mu$  in Minkowski space with the infinitesimal generators of  $U(2)$ ,

$$X = \sigma^\mu x_\mu = Ix_0 + \sigma^1 x_1 + \sigma^2 x_2 + \sigma^3 x_3. \quad (6)$$

Here the Lorentz metric norm is  $\|x_\mu\| = 2\det(X)$ . From this identification one finds that  $x_\mu$  is lightlike precisely if there is a complex 2-spinor  $\mathbf{2}$  such that  $X = \mathbf{2}\bar{\mathbf{2}}$ . The *celestial sphere* can therefore be identified with complex 2-spinors modulo a rescaling, i.e.,  $S^2 \cong \mathbb{CP}^1$ . Minkowski space has the same fiber bundle structure as quantum information! There always exists a map between rays of the lightcone and points on the surface of the Bloch sphere. Seen from another perspective, the fundamental representations of the Lorentz group contain a pair of complex 2-spinors  $\mathbf{2}$  and  $\bar{\mathbf{2}}$ , i.e., two fermionic directions. The tensor product  $\mathbf{2} \otimes \bar{\mathbf{2}} = \mathbf{3} \oplus \mathbf{1}$  is the adjoint representation and can be identified with either Minkowski space

or a spin-1 field. This is the motivation for a supersymmetry between spatial and fermionic directions.

### B. quantum celestial holography

Under a change of variables, eq. (2) is the reduced radial equation of a zero-energy free particle in elementary QM. There is a direct correspondence between  $R_{n+1}$  and the effective centrifugal potential with  $n \leftrightarrow l$ , where  $l$  is the centrifugal term. The non-trivial action  $n \rightarrow -n$  sends  $\Psi(a) \rightarrow \Psi(1/a)$  and takes the Hamiltonian to  $\hat{H}_{n+1} = -\partial_a^2 + R_{n+1}$ . On the one hand, eq. (2) describes a zero-energy Lemaître point-like particle, or Cosmon, with charge  $M$  and position  $a$  from the origin, sourcing equal and opposite kinetic and potential energies that self-annihilate. On the other, it describes a charge  $M$  sourcing the scalar curvatures of an  $n$ -sphere and an  $n$ -hyperboloid that annihilate to flat space. The change of variables establishes a duality between *position* and *scale*. It follows the preferred basis of eq. (4) is the reduced radial or scale basis where  $D^2 = -\partial_a^2 I_2$  and  $I_2$  is the 2-dim identity matrix. The Hamiltonian then takes the form,

$$\hat{H} = \begin{pmatrix} \hat{H}_2 & 0 \\ 0 & \hat{H}_3 \end{pmatrix} \quad (7)$$

where the subscripts denote the dimension of the base space  $S^2$  and total space  $S^3$  of the Hopf bundle, respectively. The equation is timeless, so one can interpret the above Hamiltonian as describing a (quantum) celestial sphere at null infinity, dual to a theory in one time dimension higher, with gravity. The Everettian conformal bootstrap leads us to quantum celestial holography through the geometry of quantum information. (See, e.g., [15–18] for a review of semiclassical celestial holography.) The “inner mechanism” of holography appears to be the simplest non-trivial fibration between the spheres, i.e., where the base space  $S^2$  is one dimension lower than the total space  $S^3$ . But what, exactly, is a quantum sphere? What does it mean for geometry to be quantum? More precisely, what is the form of the quantum metric tensor? One can answer this question by solving eq. (4) exactly.

### C. quantum geometry

The  $\mathbb{Z}_2$  symmetry  $n \rightarrow -n$  leaves asymptotic infinity interchangeable with the cosmological singularity by taking  $\Psi(a)$  to  $\Psi(1/a)$ . This symmetry implies a compactification with a transition map that identifies zero and infinity as the same point, i.e., the inclusion of a point at infinity with a non-trivial topology that “glues” the singularity to asymptotic infinity. The quantum state  $\Psi$  belongs to 1) some conformally flat and compact spin manifold, i.e., a Calabi-Yau (with potential) embedded in  $\mathbb{C}^2$  with 2) a transition map that identifies zero and infinity as the same point. The simplest and most symmetric

Calabi-Yau that meets the first requirement is the Clifford torus. So perhaps our target space has the topology of a 2-torus embedded in  $\mathbb{C}^2$  with some spin structure.

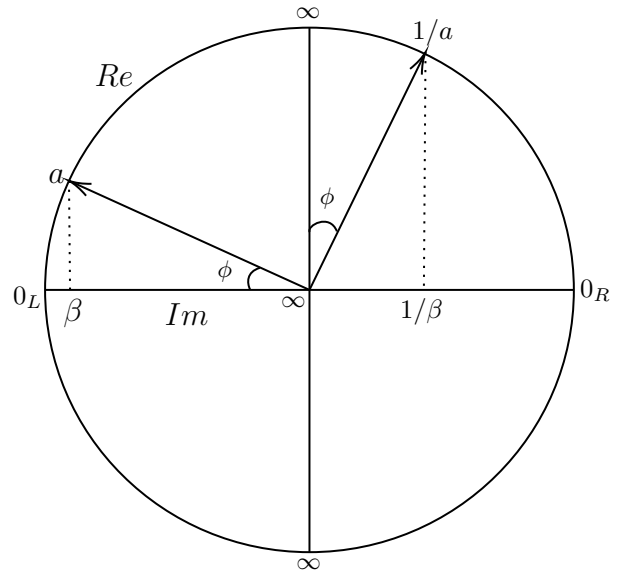


FIG. 1. The conformal Clifford torus  $\mathcal{CT}^2$ . The scale factor  $a$  goes around the ‘line at infinity’ and is real, while the imaginary axis  $\beta$  goes through the line at infinity. The left-hand side is defined by the pair  $(a, \beta) \in \mathbb{C}$ , whereas the right-hand side is defined by  $(1/a, 1/\beta) \in \mathbb{C}$ . The entire object lives in  $\mathbb{C}^2$  with the identification  $(a, \beta) \sim_\pi (1/a, 1/\beta)$  where  $\sim_\pi$  denotes  $(a, \beta)$  can be rotated into  $(1/a, 1/\beta)$  by a rotation of  $\pi$ . Above the imaginary axis, the scale factor is positive, below it is negative. A rotation from  $0_L$  to  $0_R$  takes  $2\pi$  radians and sends  $a \rightarrow -a$ . Thus, the space is, by construction, a spin manifold. The sign of  $\beta$  depends on the orientation of rotation: rotating from  $0_L \rightarrow \infty$  for positive  $a$  and  $\beta \in i\mathbb{R}^+$  with  $1/\beta \in i\mathbb{R}^-$ . Rotate from  $0_L \rightarrow \infty$  for negative  $a$  and the signs for  $\beta$  and  $1/\beta$  flip. Thus each quadrant has the sign sequence  $(++, +-, -+, --)$ , which is independent of the choice of clockwise or counterclockwise rotation and is nothing but the  $\mathbb{Z}_2 \times \mathbb{Z}_2$  symmetry.

Assembling eq. (4) with the potential in eq. (3) we have,

$$\begin{pmatrix} -\partial_a^2 + R_n & 0 \\ 0 & -\partial_a^2 + R_{n+1} \end{pmatrix} \begin{pmatrix} a^n \\ a^{-n} \end{pmatrix} = 0. \quad (8)$$

We determined eq. (4) has a  $\mathbb{Z}_2 \times \mathbb{Z}_2$  symmetry. By also requiring the invariance of  $\Psi$  under the  $\mathbb{Z}_2 \times \mathbb{Z}_2$  action, one has enough data to bootstrap the solution to eq. (4), fix the potential  $V$ , and write down the quantum scalar curvatures. Demanding the components of  $\Psi$  have the  $\mathbb{Z}_2 \times \mathbb{Z}_2$  invariance implies

$$\psi_n \sim a^n + (-a)^n, \quad \psi_{n+1} \sim a^{-n} + (-a)^{-n} \quad (9)$$

The components are not complex-valued, that is if  $n$  is an integer. Promoting the exponent to a continuous variable  $n \in [0, 2)$  and the bootstrap yields:

$$\Psi(a, \phi) = \begin{pmatrix} (1 + e^{i\phi})a^{\phi/\pi} \\ (1 + e^{-i\phi})a^{-\phi/\pi} \end{pmatrix} \quad (10)$$

which is a solution to eq. (4) in the scale basis with the potential

$$V(a, \phi) = \frac{\phi}{\pi a^2} \begin{pmatrix} \frac{\phi}{\pi} - 1 & 0 \\ 0 & \frac{\phi}{\pi} + 1 \end{pmatrix} \quad (11)$$

where  $\phi = n\pi$ . How is one to interpret this solution? Well, knowing the exact form of the quantum state is enough to "reverse engineer" the underlying spin manifold, i.e., fig. (1). And knowing the quantum scalar curvature is enough to deduce the *form* of the quantum metric tensor. The metric tensor  $g_{ij}$  for the  $n$ -sphere is an  $n \times n$  matrix. Reading off the quantum state  $\Psi$ , the metric tensor is promoted to a continuous matrix, i.e., an integral kernel operator  $K_g(i, j)$  acting on a continuous row vector  $f$ :

$$(\hat{K}_g f)(i) = \int K_g(i, j) f(j) dj. \quad (12)$$

The notion of a quantum metric tensor will become more precise later in the story.

One can stare at the conformal Clifford torus  $\mathcal{CT}^2$  in fig. (1) and convince themselves it is a candidate Hilbert space, with the rays the state vectors  $\Psi = (\psi_L, \psi_R)$ . A long-standing conceptual issue with Everettian QM is the derivation of the Born rule and the role of probabilities in a physically real theory. Can we use the geometry of  $\mathcal{CT}^2$  to derive the Born rule and normalize  $\Psi$ ? What does it mean for the wavefunction of the universe to evolve unitarily without time? It is obvious from figures (1) and (2) that unitary evolution is a phase rotation.

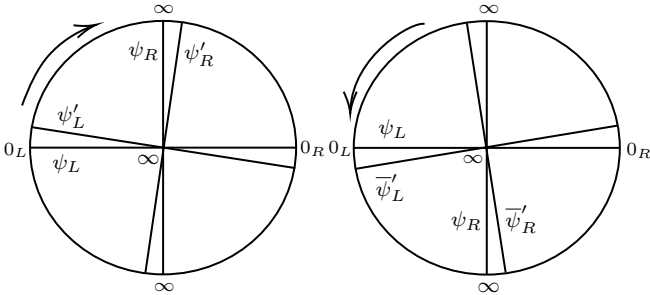


FIG. 2. Left-hand side: clockwise rotation of the state vectors leaves the imaginary unit  $i$  unchanged. Right-hand side: counterclockwise rotation of the state vectors sends  $i \rightarrow -i$ , conjugating the state vectors.

Note that  $\lim_{a \rightarrow \infty} \Psi = (\infty, 0)$  and that  $\lim_{a \rightarrow 0} \Psi = (0, \infty)$ . Rotating the  $\psi_L$  into infinity and  $\psi_R$  into zero results in a divergence. This implies the existence of an IR and UV scale  $\psi_L$  and  $\psi_R$  do not rotate past, respectively. The topology of the target Hilbert space  $\mathcal{CT}^2$  is not a circle; two of the four dimensions of the conformal Clifford torus are suppressed. There is another direction the state vectors can travel along for unitary evolution, that is if the UV mixes with the IR.

### 1. the Born rule & the observer

The inner-product space over  $\mathcal{CT}^2$  is thus defined by

$$\begin{aligned} \langle L|L \rangle &:= \int_0^{\lambda_\infty} \int_0^{2\pi} d\phi da \, \psi_L \bar{\psi}_L \\ &= 4\pi \int_0^{\lambda_\infty} da (a^4 - 1) \left( \frac{1}{\ln a} \cdot \frac{\pi^2 + 8 \ln^2 a}{\pi^2 + 4 \ln^2 a} \right) < \infty \end{aligned}$$

and

$$\begin{aligned} \langle R|R \rangle &:= \int_{\lambda_0}^{\infty} \int_0^{2\pi} d\phi da \, \psi_R \bar{\psi}_R \\ &= 4\pi \int_{\lambda_0}^{\infty} da \left( 1 - \frac{1}{a^4} \right) \left( \frac{1}{\ln a} \cdot \frac{\pi^2 + 8 \ln^2 a}{\pi^2 + 4 \ln^2 a} \right) < \infty, \end{aligned}$$

defining the (timeless) boundary Hilbert space of states. The born rule  $\rho = |\psi|^2$  follows from integrating over all possible phases,  $\rho_0(a) = \int_0^{2\pi} \psi_L \bar{\psi}_L d\phi$  and  $\rho_\infty(a) = \int_0^{2\pi} \psi_R \bar{\psi}_R d\phi$  are real physical quantities: they are the density of worlds with scale factor  $a$  in the multiverse.

One interprets the "cut-offs"  $\lambda_0$  and  $\lambda_\infty$  as the Compton wavelengths of the masses  $m_0$  and  $m_\infty$ , respectively. There is thus a natural mass matrix  $M = \text{diag}(m_0, m_\infty)$  that enters eq. (4) by multiplication of  $M^{-1}$ . Despite the fact there is a natural choice of  $M$ , the Hamiltonian still annihilates the quantum state. There is no fundamental scale. Equation (4) must be dimensionless, implying the existence of natural units where  $M^{-1} = I_2$ , i.e.,  $m_0$  and  $m_\infty$  depend only on fundamental constants.

To ensure eq. (4) remains dimensionless send  $a \rightarrow \frac{a}{\lambda_0}$  and  $a \rightarrow \frac{a}{\lambda_\infty}$  in  $\psi_L$  and  $\psi_R$ , respectively. A remarkable duality then follows:

$$\psi_L(\lambda_\infty, \phi) \bar{\psi}_L(\lambda_\infty, \phi) = \psi_R(\lambda_0, \phi) \bar{\psi}_R(\lambda_0, \phi). \quad (13)$$

The UV scale  $\lambda_0$  and the IR scale  $\lambda_\infty$  are dual. Unitary evolution is a phase rotation of  $\psi_L$  from  $a = 0_L$  through  $a = \lambda_\infty^L$  to  $a = \lambda_0^R$  (still labeled as  $\psi_L$ ) to  $a = 0_R$ . The UV and IR scales place a fundamental limit on what is, in principle, observable. It is clear  $\lambda_0$  is the Planck length and  $m_0$  is the Planck mass, i.e., the smallest possible black hole. So what is the ultra-light particle with mass  $m_\infty$  that determines the largest scale the observer shall ever see?

Nature has no fundamental scale, but the observer does. In the ant's-eye view, there is a fundamental limit to the physical information any apparatus (or observer) can collect. One concludes an observer is nothing more than a finite number of qubits.

The universal wave function, eq. 10., has no initial conditions. The timeless Schrödinger equation was solved from symmetries alone. Why define the universal wave function as an element of a normed Hilbert space? Because there is no supernatural observer that exists outside of the universe bestowed with the decision to choose

the initial conditions of the universe. All initial conditions and, hence, all paths consistent with the symmetries of the system are allowed. There is no Ptolemaic center to the Hilbert space of states—no beginning to the universe. This is the origin of the many worlds and why quantum mechanics has the structure that it does. Quantum mechanics is the Copernican principle in the limit of all physically realizable events.

#### D. the timeless boundary

Another way of calculating  $\Psi$  is purely algebraically. Every point in  $\mathbb{R}^3$  has the following matrix representation:

$$Q = \sigma^1 x_1 + \sigma^2 x_2 + \sigma^3 x_3 \quad (14)$$

where the  $\sigma^i$  are the Pauli matrices. Each eigenvalue is the Euclidean  $l^2$ -norm and  $\text{tr}(Q) = a + (-a) = 0$ . Using the spectral theorem to compute the function of a matrix, the left and right-handed states are computed as

$$\psi_L = \text{tr } Q^n = (1 + e^{in\pi})a^n \quad (15)$$

and

$$\psi_R = \text{tr } Q^{-n} = (1 + e^{-in\pi})a^{-n} \quad (16)$$

where  $n \in [0, 2)$ . One interprets  $Q$  as a qubit embedding of  $\mathbb{R}^3$  with an equivalence relation  $a \sim \lambda a$  for all real numbers  $\lambda \neq 0$  that identifies the 2-sphere (of any arbitrary size) as the Bloch sphere. (One can always find a  $\lambda$  such that  $\lambda a$  has unit norm and identify the 2-sphere as the Bloch sphere.) There is a qubit at every point in  $\mathcal{CT}^2$ . This algebra of physical information describes a *qubit continuum* (or  $Q$ -continuum) where points of a

manifold are qubits. Such models are non-trivial generalizations of  $n$ -level quantum systems and naturally resemble the structure of quantum fields in the continuum limit of lattice qubit models [19, 20]. Intriguingly, lattice qubit models display UV/IR mixing from global subsystem symmetries [21–23], similar in spirit to the UV/IR mixing that was encountered in the previous section. In our case, UV/IR mixing is required for unitarity. There is no other way to normalize the state vectors. Therefore, probability densities in the multiverse are physical densities of a quantum information continuum: the squared modulus of  $\Psi$  is the density of worlds.

#### E. the dynamic bulk

Recall from the section II A that the symmetry group of the Hopf fibration is  $U(2)$ . By the exceptional spin isomorphism  $\text{Spin}(3, 1) \cong \text{SL}(2, \mathbb{C})$ , one may identify the points  $x_\mu$  in Minkowski space with the infinitesimal generators of  $U(2)$ . In other words, points on the Bloch sphere can always be mapped to rays of the lightcone. Thus every point of  $\mathcal{CT}^2$  is also a celestial sphere. The boundary equations of motion, eq. (4), are defined by the Clifford algebra  $\mathcal{Cl}_3(\mathbb{R})$ . It follows from the exceptional spin isomorphism that the bulk equations of motion are defined by the Dirac algebra  $\mathcal{Cl}_{3,1}(\mathbb{C})$ , with the simplest holographic dictionary given by

$$D \leftrightarrow \not{D}, \quad V \leftrightarrow V_{\mu\nu} \quad (17)$$

where  $\not{D} = i\gamma^\mu \partial_\mu$  is the Dirac operator and  $V_{\mu\nu}$  is a second-rank tensor that decomposes into the following classical irreducible representations of the Lorentz group: an antisymmetric tensor  $F_{\mu\nu} = -F_{\nu\mu}$ , a symmetric ( $H_{\mu\nu} = H_{\nu\mu}$ ) and traceless ( $H^\mu_\mu = 0$ ) tensor  $H_{\mu\nu}$ , and a scalar trace component  $X \equiv X^\mu_\mu$ . Under the appropriate local phase (gauge) invariance conditions,  $H_{\mu\nu}$  is a massless spin-2 field—the graviton. The bulk equations of motion then take the following form:

$$\begin{aligned} (\not{D}^2 + V_{\mu\nu})\Psi &= (-\gamma^\mu \gamma^\nu \partial_\mu \partial_\nu + V_{\mu\nu})\Psi \\ &= (\eta^{\mu\nu} \partial_\mu \partial_\nu + F_{\mu\nu} + H_{\mu\nu} + X^\mu_\mu)\Psi \\ &= (\partial^\mu \partial_\mu + g_1 B_{\mu\nu} + g_2 W_{\mu\nu} + g_3 H_{\mu\nu} + m^2)\Psi \\ &= (\square + g_1(\partial_\mu B_\nu - \partial_\nu B_\mu) + g_2(\partial_\mu W_\nu^i - \partial_\nu W_\mu^i + g_w \epsilon_{ijk} W_\mu^j W_\nu^k) + g_3 H_{\mu\nu} + m^2)\Psi \\ &= 0 \end{aligned} \quad (18)$$

The action of the unitary group  $U(2)$  on  $\mathbb{C}^2$  leaves the 3-sphere invariant. Locally  $U(2)$  is diffeomorphic to the direct product  $G = SU(2) \times U(1)$ . Up to a local diffeomorphism, the compact gauge group  $G$ , together with the emergence of the antisymmetric tensor  $F = F_{\mu\nu}$ ,

implies the existence of Yang-Mills equations, where  $A$  denotes the gauge connection on  $G$ . The connection  $A$  is locally a one-form on space-time. The curvature or field strength tensor is the two-form:  $F = dA + A \wedge A$ . The classical field equations are therefore given by the

Yang-Mills equation:  $d_A \star F = 0$ , where  $d_A$  is the gauge-covariant extension of the exterior derivative and  $\star$  is the Hodge duality operator. Thus, the antisymmetric tensor  $F_{\mu\nu}$  is expanded into the electromagnetic and weak field strength tensors in eq. (18). The electroweak interactions with gravity emerge in the bulk!

### F. quantum gravity

In semiclassical gravity, the simplest metric is Minkowski, with some quantum fluctuations:

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu} \quad (19)$$

where  $h_{\mu\nu}$  is a symmetric and traceless rank-2 tensor. From eq. (12), it was deduced that the quantum metric tensor is an integral kernel operator; hence, so too is the spin-2 field as it appears in the bulk equations of motion. An educated guess on the form of this operator is an indefinite integral operator of the following form:

$$H_{\mu\nu} \rightarrow \int d\psi^\mu h(\psi_\mu, \psi_\nu). \quad (20)$$

Here, I use the notation where  $\psi_\mu$ , which denotes each element of the 4-spinor  $\Psi$ . A raised index  $\psi^\mu$  denotes the elements of the conjugate transpose of  $\Psi$ . The classical irreducible representation of the Lorentz group,  $H_{\mu\nu}$ , is promoted to a unique class of Hilbert-Schmidt integral operators where

$$\int \int d\psi_\mu d\psi^\nu h(\psi_\mu, \psi_\nu) h(\psi^\mu, \psi^\nu) < \infty, \quad (21)$$

(with bounds to be determined from the boundary theory) such that the kernel is a complex symmetric

$$h(\psi_\mu, \psi_\nu) = \overline{h(\psi_\nu, \psi_\mu)} := h(\psi^\nu, \psi^\mu), \quad (22)$$

traceless trace-class operator

$$h^\mu_\mu = \int d\psi^\mu h(\psi_\mu, \psi_\mu) = 0. \quad (23)$$

Gravity is exceptional in that it acts on the quantum state as an integral operator, whereas the other forces act on the quantum state as differential operators. The classical irrep.  $H_{\mu\nu}$  of the Lorentz group is fully quantized and makes eq. (18) a highly non-linear differential equation, where  $H_{\mu\nu}\Psi \sim V_g(\Psi)$  can be thought of as a quantum gravitational potential, and some complicated function of the 4-spinor field  $\Psi$  that arises from quantum gravitational self-interactions. In the spin-free limit where  $g_1 \rightarrow g_2 \rightarrow g_3 \rightarrow 0$ , eq. (18) reduces to the Klein-Gordon equation:

$$(\square + m^2) \Psi = 0, \quad (24)$$

hence why the scalar trace component  $X^\mu_\mu = m^2$  was chosen. The coupling constants  $g_i$  are such that the fields

have units of squared mass: the bulk equations of motions are four (gauge-coupled) non-linear Klein-Gordon equations. Because gravity is the weakest force, in almost all cases, the quantum gravitational backreaction is negligible at low energies, except for exotic scenarios that violate decoupling.

Eq. (18) is a formidable beast to solve. What are the appropriate boundary conditions? Once an appropriate boundary condition and a spin-2 kernel are chosen, one needs to update the 4-gradient  $\partial_\mu$  such that the equation is gauge invariant and then fix the gauge. Because the equation is non-linear and coupled with multiple gauge fields, these procedures are significantly more complicated than in quantum field theory (QFT) without gravity. The Everettian conformal bootstrap takes the principle of quantum universality and spins out a full-fledged theory of quantum gravity, albeit not a very well-understood one.

The first step in demonstrating a holographic duality between the timeless boundary and the dynamic bulk is to match the energy spectrum of the bulk and boundary theories. The boundary theory is based on the energy  $E$ , which is zero, whereas the bulk is based on the squared energy  $E^2$ , which is non-zero and has a negative energy solution. The conformal invariance of the boundary is locally broken from the ant's-eye perspective of the bulk observer. So, how can it be that these two theories are equivalent? How is a dynamical non-linear differential equation secretly a non-dynamical linear one? There must exist a highly non-trivial map, like a Fourier transform, between equations (4) and (18) for self-consistency.

The 4-spinor  $\Psi$  in eq. (18) decomposes into a pair of 2-spinors with equal and opposite energies,  $\chi_L$  and  $\chi_R$ , respectively, that satisfies two coupled non-linear Weyl-like equations

$$(-\sigma^\mu \sigma^\nu \partial_\mu \partial_\nu + V) \chi_L = 0 \quad (25)$$

$$(-\bar{\sigma}^\mu \bar{\sigma}^\nu \partial_\mu \partial_\nu + \bar{V}) \chi_R = 0 \quad (26)$$

where  $\sigma^\mu = (I_2, \sigma^i)$  and  $\sigma^\nu = (-I_2, \sigma^j)$ , i.e., the generators of  $U(2)$ . Recall what we learned from the geometry of quantum information: Minkowski space has a compact presentation  $U(2)$ , and the fundamental representation of the Lorentz group contains two fermionic directions. The potential  $V$  can be re-written to contain the same information as  $V_{\mu\nu}$  by recasting the field strength tensors in the standard Pauli matrix representation with the Clifford algebra  $\mathcal{Cl}_{3,0}(\mathbb{R})$ , otherwise known as the algebra of physical space or the Pauli algebra:

$$(\square + g_1 F + g_2 W + g_3 H + m^2) \chi_L = 0 \quad (27)$$

$$(\square + g_1 \bar{F} + g_2 \bar{W} + g_3 \bar{H} + m^2) \chi_R = 0 \quad (28)$$

In the limit that  $g_1 \rightarrow g_2 \rightarrow g_3 \rightarrow 0$ , the above reduces to the Klein-Gordon equation. Thus we conclude equation

(18) is the adjoint representation where the above is the fundamental representation.

The Dirac field can be written as a sum of chiral Weyl fields. The boundary theory has no timelike direction, so its solutions obviously can not be a linear combination of the non-linear states  $\chi_L$  and  $\chi_R$ . However, the quantum metric tensor is missing from our recipe. One can reasonably conjecture that the dynamic non-linear bulk is mapped to the timeless linear boundary by applying the Minkowski metric operator  $\hat{\eta}$  to the states  $\chi_L$  and  $\chi_R$ ,

$$\widehat{\chi}(a, \phi) = \int_{-\infty}^{\infty} \eta(a, t) \chi(a, t) dt \quad (29)$$

such that

$$\Psi \sim \widehat{\chi}_L + \widehat{\chi}_R \quad (30)$$

is a solution to  $(D^2 + V)\Psi = 0$ . The quantum Minkowski metric is an integral operator that integrates out the timelike direction and linearizes the chiral fields such that their linear combinations are solutions to the boundary equations of motion. One can now write the fully quantized metric operator as

$$\hat{g}_{\mu\nu} = \int_{-\infty}^{\infty} dt \eta(a, t) + \int d\psi^\mu h(\psi_\mu, \psi_\nu). \quad (31)$$

One interpretation of  $\eta(a, t)$  is a propagator of all possible isometries between a phase rotation on the boundary and the observer-dependent time evolution of a local patch in the bulk. The integral operator formalism is like a path integral over trajectories not in space but in time, i.e., an integral over all possible rates an observer's clock can tick.

Understanding the holographic dictionary at a deeper level requires a better understanding of the integral operator algebra that encodes the quantum geometry, which is essential to gauging and solving eq. (18). Nevertheless, one does not need to solve the equation to derive precise observational numbers.

### G. quantum cosmology

Negative energy solutions can be reinterpreted as positive energy solutions traveling backward in time. If we head back to fig. (1), it is clear the phase rotation of  $\psi_L$  and  $\psi_R$  describe expanding and contracting states, respectively. The contracting state is a perfect mirror image of the expanding state, as can be seen when plotting  $\rho_0(a) = \int_0^{2\pi} \psi_L \bar{\psi}_L d\phi$  and  $\rho_\infty(a) = \int_0^{2\pi} \psi_R \bar{\psi}_R d\phi$ . This mirror symmetry implies  $\psi_R$  is the time-reversed image of  $\psi_L$ . However, to be clear, the Universe is not in some *definite* state at some time  $t$ , at least not from the God's-eye view where everything that can happen happens everywhere all at once.

The imaginary axis  $\beta$  in fig. (1) does not have the topology of  $i\mathbb{R}$ ; it runs from zero through infinity and

back to zero. Recall two of the four dimensions are suppressed. The imaginary axis is the thermal circle  $S_\beta^1$ . One can see this clearly: at the cosmological singularity  $a = 0$ , the imaginary variable reads  $\beta = 0$ . Ergo,  $\beta$  is the inverse temperature. The equivalence of inverse temperature and cyclic imaginary time, expressed through the formula  $\beta = it$ , is manifest from the geometry of  $\mathcal{CT}^2 \cong S_a^1 \times S_\beta^1$ . One can, therefore, justify using the Wick rotation to simplify eq. (18). Quantum gravity is fundamentally Euclidean. The thermal circle implies the de Sitter or Hawking temperature:

$$T \sim \frac{H}{2\pi} \quad (32)$$

where  $H$  is the Hubble constant. The boundary state  $\Psi$  has the global phase symmetry  $U(1)^2 = \text{diag}(e^{-i\phi}, e^{i\phi})$ , i.e., the maximal torus of  $U(2)$ . The action of  $U(1)^2$  takes the components of  $\Psi$  to their complex conjugates. The charge is mass (energy) in gravity, so the conserved charge must be the gravitational charge  $m_\infty$ . The charge  $m_0 = M_{pl}$  can not be fundamental as it radiates away with Hawking temperature  $T \sim g/2\pi$ , where  $g$  is the surface gravity of the horizon at  $r = \lambda_0 = L_{pl}$ .

Restoring the inverse mass matrix  $M^{-1} = \text{diag}(1/m_0, 1/m_\infty)$  to  $V(a, \phi)$ , and it is clear  $m_0$  decays into  $m_\infty$ . The left-hand potential  $V_L$  is suppressed by a factor of  $\phi/\pi - 1$  whereas  $V_R$  is amplified by a factor of  $\phi/\pi + 1$ . Thus, one concludes  $m_0$  is not fundamental and must be a composite of  $m_\infty$ . **The gravitational charge  $m_\infty$  defines the boundaries of the observable universe, beyond which no measurement can be made.**

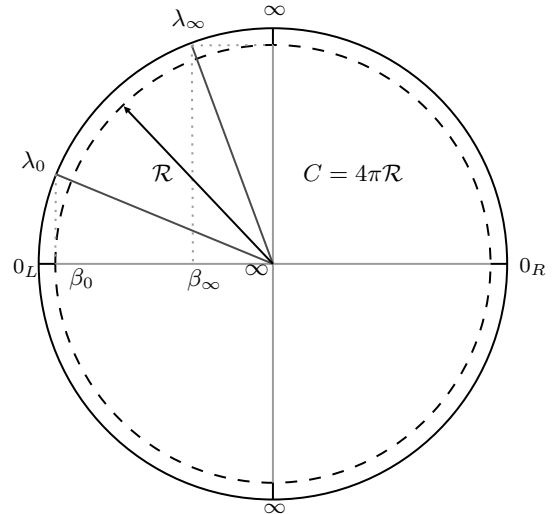


FIG. 3. From the ant's-eye view in  $\mathcal{CT}^2$ , the conformal horizon hides the cosmological singularity and its dual at future infinity. The dimensionless radius  $\mathcal{R}$  bounds all observables to the energy scale  $m_\infty \leq m \leq m_0$ . Naturally,  $\beta_0$  is the inverse Planck temperature, and  $\beta_\infty$  is the time of heat death, defined by the moment the universe becomes so dilute no measurement can be made.

Everything that can be empirically known of the universe is bounded by a finite number of qubits:

$$Z_{\text{obs}} \sim e^{2\pi\mathcal{R}} \quad (33)$$

where

$$\mathcal{R} = \frac{\lambda_\infty}{\lambda_0} \quad (34)$$

defines the dimensionless radius of the conformal horizon that hides the cosmological singularity and its dual at future infinity. The entropy of the cosmic event horizon is

$$S_{\text{CEH}} = \frac{1}{2}C = 2\pi\mathcal{R}, \quad (35)$$

i.e., one-half the circumference of the conformal horizon pictured as the dashed circle in fig. (3). The factor of  $1/2$  comes from the fact that there is a double counting of states from the double cover of Euclidean space.

One can calculate the location of the cosmic event horizon as witnessed by the ant from the God's-eye view. The spinor components  $\psi_L, \psi_R \in L^2(S_a^2 \times S_\beta^1)$ . Express the densities  $\rho_0(a)$  and  $\rho_\infty(a)$  as a function of the surface area of the 2-sphere with the scale transformation  $a \rightarrow \sqrt{\pi}a$ :

$$\rho_0(A) = 4\pi^2 \int_0^{2\pi} \cos^2\left(\frac{\phi}{2}\right) \left(\frac{s^2 A}{\lambda_0^2}\right)^{\phi/\pi} d\phi \quad (36)$$

and

$$\rho_\infty(A) = 4\pi^2 \int_0^{2\pi} \cos^2\left(\frac{\phi}{2}\right) \left(\frac{s^2 A}{\lambda_\infty^2}\right)^{-\phi/\pi} d\phi. \quad (37)$$

such that  $A = 4\pi a^2$  and the spin  $s = \pm 1/2$ . One can re-express the above as functions of the Bekenstein-Hawking entropy (the entropy from the ant's-eye perspective) by the identification:

$$S_\alpha = \frac{s^2 A}{\lambda_\alpha^2} = \frac{A}{4\lambda_\alpha^2} \quad (38)$$

with the conformal indices  $\alpha = 0, \infty$ . ( $\alpha = \infty$  is the  $\mathcal{R} \rightarrow 1/\mathcal{R}$  dual.) We now have two equivalent definitions of entropy as seen from the ant's-eye view and can calculate the radius of the cosmic event horizon:

$$\begin{aligned} \frac{\pi R_{\text{CEH}}^2}{\lambda_0^2} &= 2\pi \frac{\lambda_\infty}{\lambda_0} \\ R_{\text{CEH}} &= \sqrt{2\lambda_0\lambda_\infty} \\ &= \sqrt{\frac{2}{\Lambda}} \\ &\approx 14.26 \text{ billion ly} \end{aligned} \quad (39)$$

where the cosmological constant is identified as  $\Lambda = \frac{1}{\lambda_0\lambda_\infty}$ . It is straightforward to calculate  $m_\infty$  and verify that  $\frac{m_\infty}{m_0} = \Lambda\lambda_0^2$  where the vacuum energy density (in reduced Planck units) is given by  $\rho_\Lambda = \rho_\infty = \frac{m_\infty c^2}{\lambda_0^3}$ .

The presence of the cosmic event horizon  $R_{\text{CEH}}$  means there is a natural factorization of the cosmological Hilbert space of states from the ant's-eye view:  $\mathcal{H}$  separates into an infinite and finite-dimensional piece  $\mathcal{H}_{\text{env}} \otimes \mathcal{H}_{\text{obs}}$ , where  $\dim \mathcal{H}_{\text{obs}} \leq Z_{\text{obs}}$ . The implied **universal relativity** is this: everything that can be empirically known of the universe is relative to a conformal horizon that hides the cosmological singularity and its dual at future infinity. From the God's-eye view, there is nothing to factorize. There are no subsystems that interact with each other at some *definite* moment in time. On the boundary, everything that can happen happens everywhere all at once. The boundary Hilbert space has only one state:  $Z = e^S = 1$ . The boundary state  $\Psi$  is pure, and so  $S = 0$ . Any ray in  $\mathcal{CT}^2$  can be rotated into any other ray by a conformal transformation. The continuum of 2-spheres of radius  $a$  that were normalized to unity for identification with the Bloch sphere are all the same state—from the God's-eye view. In the bulk, from the ant's-eye view, the conformal horizon hides information from the observer. The hidden information is the entanglement entropy of the cosmic event horizon that separates the observable universe from the multiverse.

## H. dark energy holes & the dS limit

The Bekenstein-Hawking area entropy law is a geometric consequence of the fact that  $\psi \in L^2(S_a^2 \times S_\beta^1)$ . The action is computable in Hawking and Gibbons's original paper because the Euclidean section is non-singular: the entropy is evaluated on a region of a spacetime manifold  $M$  bounded by some surface  $r = r_0 > 2M$  with compact topology  $S^2 \times S^1$  (i.e., a 2-sphere cross periodic time) [24]. The Ricci scalar vanishes in the Schwarzschild metric, so the action is determined only by the Gibbons-Hawking-York boundary term and is thus an integral over the boundary  $S^2 \times S^1$ . The squared modulus  $\rho = |\psi|^2$  is nothing but an integral over the boundary  $S_a^2 \times S_\beta^1$  and precisely why one can write  $\rho = \rho(S)$  with  $S = \frac{A}{4\lambda^2}$ . But what are the microstates that the Bekenstein-Hawking area entropy counts?

Nature has no fundamental scale: the fundamental mass matrix  $M$  can be multiplied out of  $\hat{H}\Psi = 0$ . It can, therefore, have any arbitrary value such that  $\mathcal{R}$  remains invariant in all worlds. Geometrically, this is seen as a rotation of  $\lambda_0$  into  $\lambda'_0$  and  $\lambda_\infty$  into  $\lambda'_\infty$ , such that  $\mathcal{R} = \mathcal{R}'$ . Now  $r = \lambda'_0$  is the Compton wavelength of a black hole of arbitrary mass  $m'_0$ , a composite of  $m'_\infty$ . Since all massive objects dilute proportional to the inverse volume  $a^{-3}$  of Euclidean 3-space, all black holes must have a mass coupling  $m \sim a^3$  to be a dark energy species. **This observational consequence will soon provide the first experimental test of the multiverse.**

We have predicted the radius of the cosmic event horizon, so where is the de Sitter limit with the dark energy equation of state  $w = p/\rho_\Lambda = -1$ ? Is there an explicit



holographic construction where the charge  $m_\infty$  is a microstate of  $m_0$ ?

Consider a flat acceleration surface with  $2\pi k_B$  entropy per unit (Planck) area  $1/\lambda_0^2$ . Now multiply this quantity by the Hawking temperature per unit length of the accelerating surface:

$$\frac{T}{\lambda_0} = \frac{\hbar g}{2\pi c k_B \lambda_0}, \quad (40)$$

where  $g$  is the acceleration. The result is the pressure

$$p_0 = \left( \frac{c^2}{G\lambda_0} \right) g, \quad (41)$$

where the quantity in parentheses is an *area density* with units  $[\text{mass}][\text{area}]^{-1}$ . The physical construction is an accelerating membrane, like the surface of a glowing soap bubble. The above equation is the ideal gas law  $pV = k_B T$  where  $V = \lambda_0^3$  is the unit volume swept out by the membrane. The above is nothing but  $F = m_0 g$ , Newton's second law. Now consider the dual acceleration surface with  $4\pi k_B$  entropy per unit  $R_{CEH}^2$  and repeat the above steps to obtain:

$$p_\infty = \left( \frac{\Lambda \hbar}{c\lambda_0} \right) g, \quad (42)$$

which is just  $F = m_\infty g$  when multiplied by  $\lambda_0^2$  on both sides. The above pressures obey the ideal gas law, so we can construct the stress-energy tensor  $T_{\mu\nu} = \text{diag}(\rho_\infty, p_\infty, p_\infty, p_\infty)$ . In the UV limit,

$$\lim_{g \rightarrow -c^2/\lambda_0} T_{\mu\nu} = \begin{pmatrix} \rho_\Lambda & 0 & 0 & 0 \\ 0 & p & 0 & 0 \\ 0 & 0 & p & 0 \\ 0 & 0 & 0 & p \end{pmatrix} \quad (43)$$

one obtains the vacuum stress-energy tensor  $T_{\mu\nu}^{(\text{vac})}$ . The sign on  $g$  distinguishes the expanding and contracting states. Indeed, the first thing we learned from the bootstrap is that energy and curvature are equivalent. There are not many options to equate  $T_{\mu\nu}^{(\text{vac})}$  to curvature on the left-hand side. The second thing we learned is that the *form* of the laws of physics are independent of the chosen coordinate system—no coordinate system was used to solve eq. (1). The third thing we learned is that the fundamental charge of the vacuum,  $m_\infty$ , is equivalent to the inertial mass and the gravitational charge. These deductions are none other than the equivalence principle, general covariance, and a universal limit to the rate information can propagate in the universe and what is, in principle, observable. Given these constraints, the simplest equations that follow are none other than Einstein's field equations:

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \kappa T_{\mu\nu} \quad (44)$$

where  $R_{\mu\nu}$  is the Ricci curvature tensor,  $R$  is the scalar curvature,  $g_{\mu\nu}$  is the metric tensor, and  $\kappa =$

$8\pi G$ . Quantum mechanics—when assumed universal—naturally contains GR.

There is then the dual vacuum stress-energy tensor for the contracting state. As before, we can construct a stress-energy tensor  $T_{\mu\nu} = \text{diag}(\rho_0, p_0, p_0, p_0)$  for an ideal gas. In the IR limit,

$$\lim_{g \rightarrow c^2/\lambda_\infty} T_{\mu\nu} = \begin{pmatrix} \rho_0 & 0 & 0 & 0 \\ 0 & -p & 0 & 0 \\ 0 & 0 & -p & 0 \\ 0 & 0 & 0 & -p \end{pmatrix} \quad (45)$$

one obtains a bizarre substance with the Planck energy density and a positive vacuum energy pressure (with the minus sign absorbed)

$$p = \frac{\Lambda}{8\pi G}, \quad (46)$$

that satisfies the equation of state for dark matter:  $w = p/\rho_0 \approx 0$ . Are

$$G_{\mu\nu} = \kappa T_{\mu\nu}^{(\text{dual-vac})} \quad (47)$$

the classical field equations for dark matter? Does this explain how the cosmological constant  $\Lambda$  enters local galaxy dynamics through a universal acceleration scale  $a_0 \approx cH_0 \approx c^2 \Lambda^{1/2}$  [25], and how something as small as a galaxy "knows" about the dS radius associated with the whole of the observable universe? Are dark energy and the dark matter emergent properties of the universal quantum state  $\Psi$ , and is UV/IR mixing a general feature of Everettian quantum gravity?

If nature has no fundamental scale, is eq. (18) valid for astrophysical modeling? Can we use the equation to understand the dynamics of black holes, as suggested by the boundary equations of motion? What new and potentially exotic phenomena emerge from coupling quantum gravity with the electroweak force and solving eq. (18)? How do the strong interactions enter the picture? Where is the Higgs sector? Is the double-copy a clue [26]? What are the conceptual and technical foundations to fixing the spin-2 integral kernel operator  $K$ , gauge fixing eq. (18), and mapping its solutions to the boundary with the flat space quantum metric tensor  $K_\eta$ ? How does one solve for  $K_\eta$  and  $K$  and, therefore, the metric operator  $\hat{K}_g$ ?

Much work is to be done.

### III. IMPLICATIONS

The 'many worlds' in Everettian QM are causally disconnected when a classical global time coordinate is assumed. It is clear that if time is not fundamental, the classical notions of causality break down. When time drops out of the Schrödinger equation, the Hilbert space becomes causally indefinite. The conformal Clifford torus has no causal ordering—light cones can be superimposed. Remarkably, in the first of its kind, the

quantum switch experiment has demonstrated *causal indefiniteness* [27, 28]. Since there is no global time coordinate, there must exist a *causal reference frame* [29–32] for each event that establishes an observer-dependent time to describe the evolution of quantum subsystems. I expect causal reference frames to be key in gauge fixing and solving eq. (18).

If quantum theory is truly universal and if UV/IR mixing is a general feature of the quantum universe, what are the implications of causal indefiniteness? Can exotic UV/IR couplings that violate EFT reasoning together with quantum non-causality enable the quantum metric tensor to be technologically exploited? Looking at equations (25) – (30), it is, at least in principle, possible to engineer the quantum metric tensor with some highly tuned matter-antimatter reaction. This begs the question: does quantum universality allow travel between the many worlds? At face value, there do not appear to be any inconsistencies with a traversable multiverse. If quantum universality is true and the multiverse ex-

ists, then there must exist worlds where future humans master the quantum nature of spacetime and travel to “past-adjacent” light cones—a form of time travel in the multiverse. But if this were possible, then where are they?

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