



# Medial Axis Approximation of River Networks for Catchment Area Delineation

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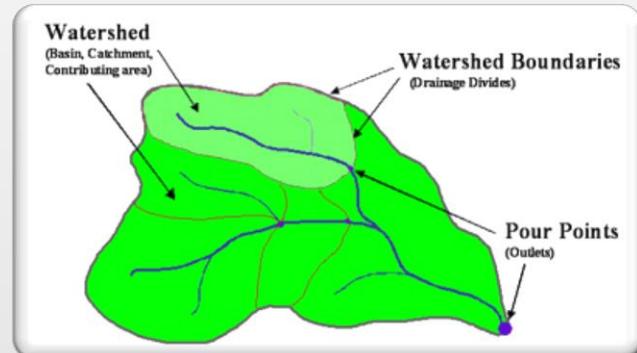
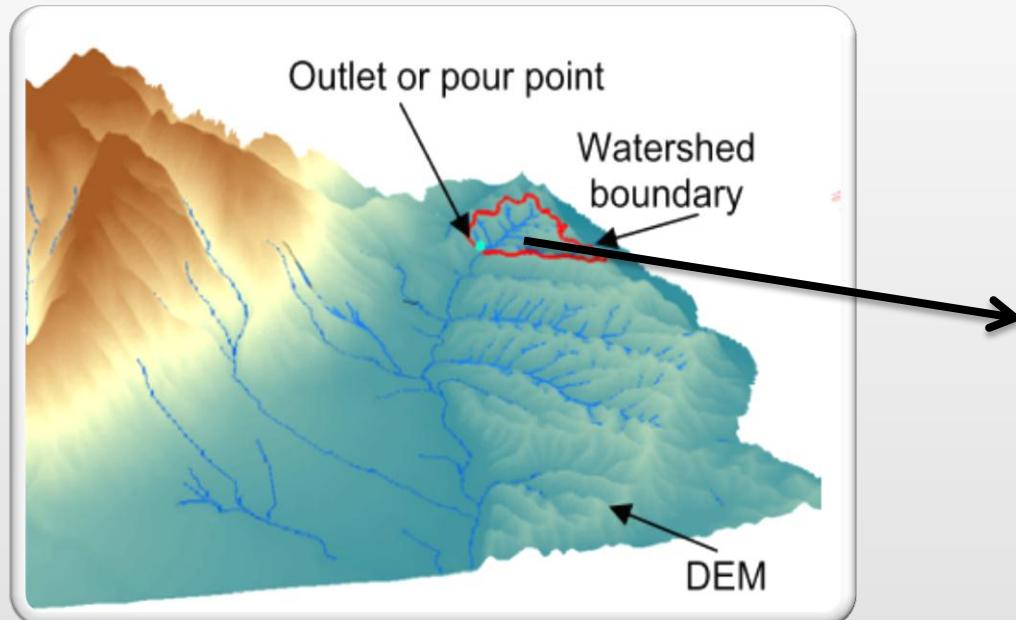
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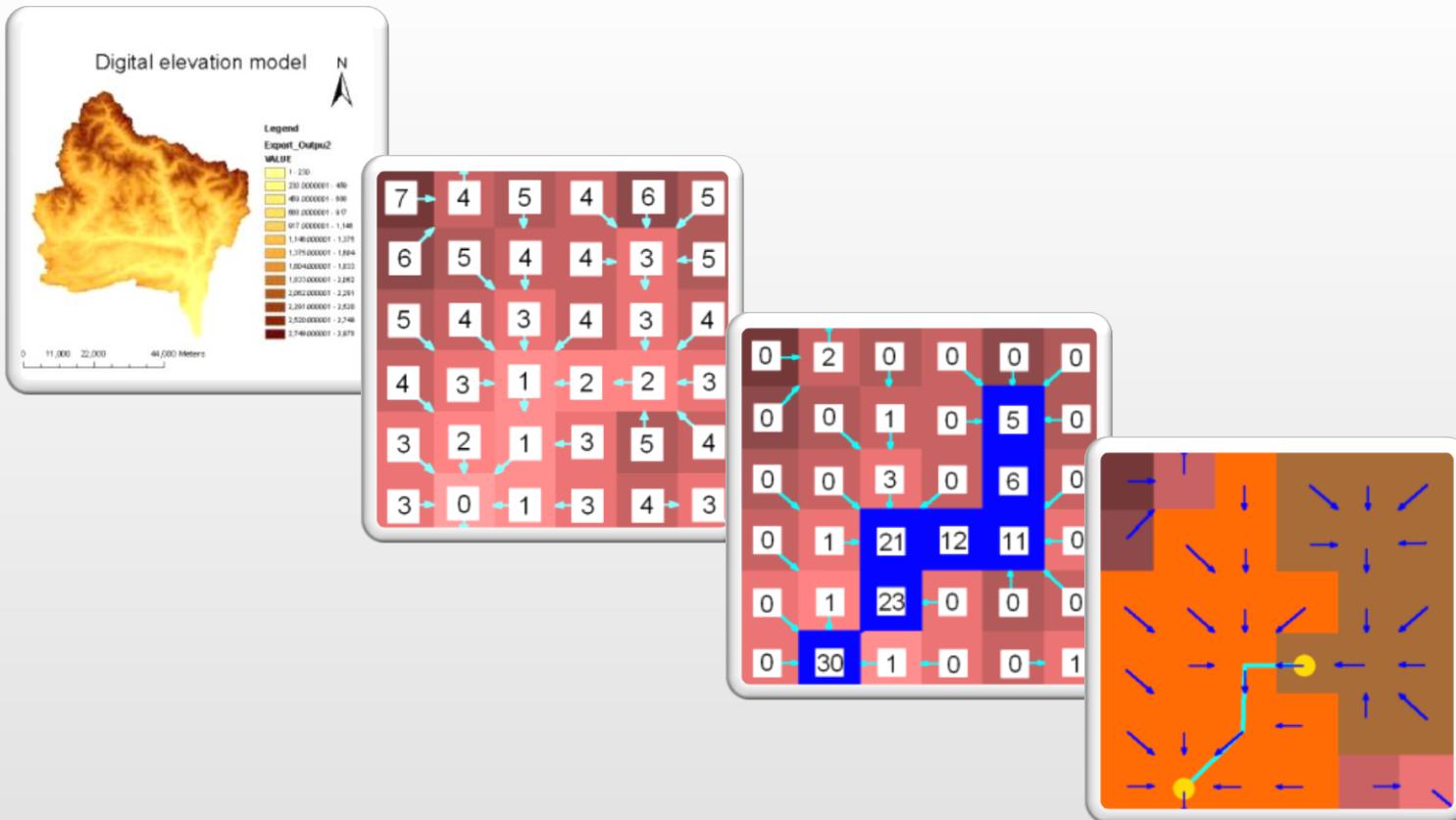
## Catchment (Watershed)

- A hydrological unit where precipitations that fall into this area, eventually ends up in the same river.



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## Catchment Area Delineation using DEM



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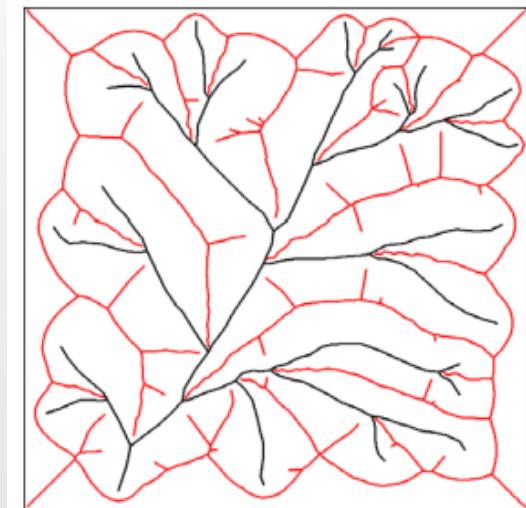
## Catchment Area Delineation using DEM

### Shortcomings

- The raster-based analyses can be time consuming.
- The accuracy depends on the quality and type of the DEM.
- The flow path is biased to the grid axes and the water is trapped in sinks and flat areas.
- The raster to vector conversion of boundaries may create some intersections and the boundaries are not explicitly defined.

## Catchment Area Delineation using the Medial Axis

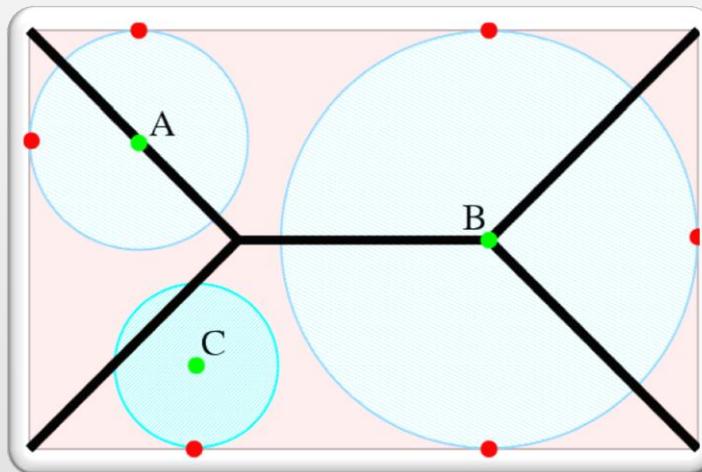
- A hypothesis stated by Gold and Snoeyink (2001)
- The river network is sampled with a set of points, and Delaunay triangulation and Voronoi diagrams are used to extract the medial axis results in an approximation of the catchment areas.



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## Definition

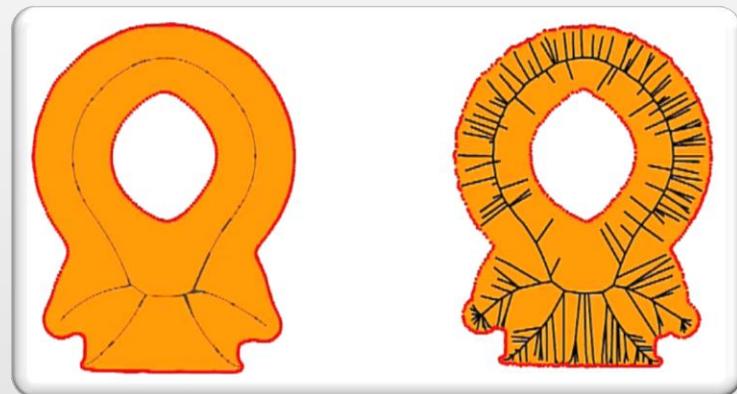
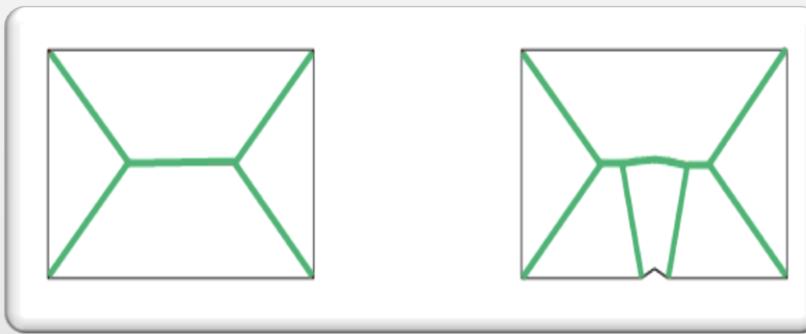
- **Medial Axis (Skeleton):** The closure of the set of points that have at least two closest points on the object's boundary



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## Extraneous Edges

- The medial axis is very sensitive to the small changes of the boundary, which produces many extraneous branches in the medial axis.

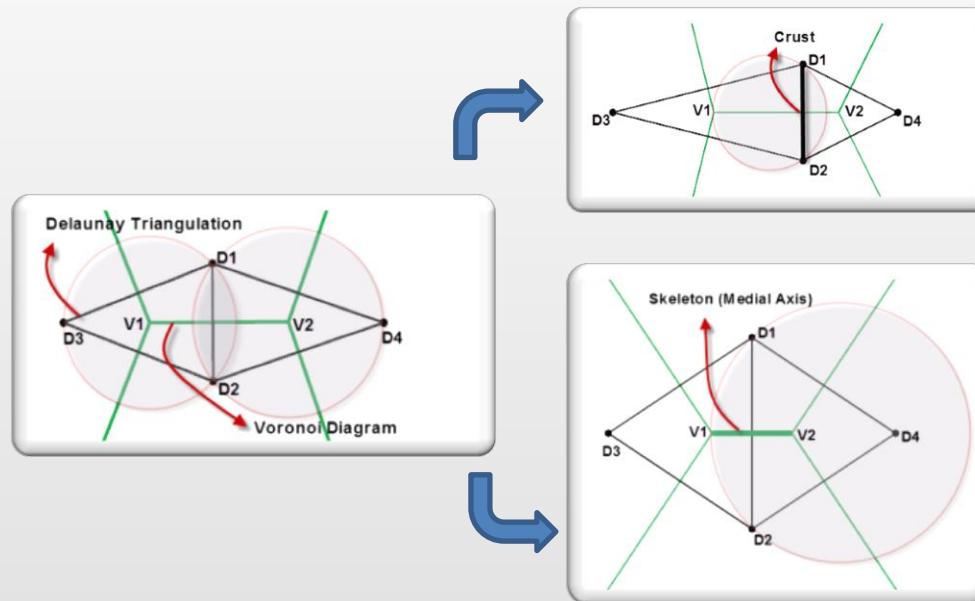


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# Media Axis Extraction

## One Step Crust and Skeleton Algorithm

Christopher Gold and Jack Snoeyink (2001)



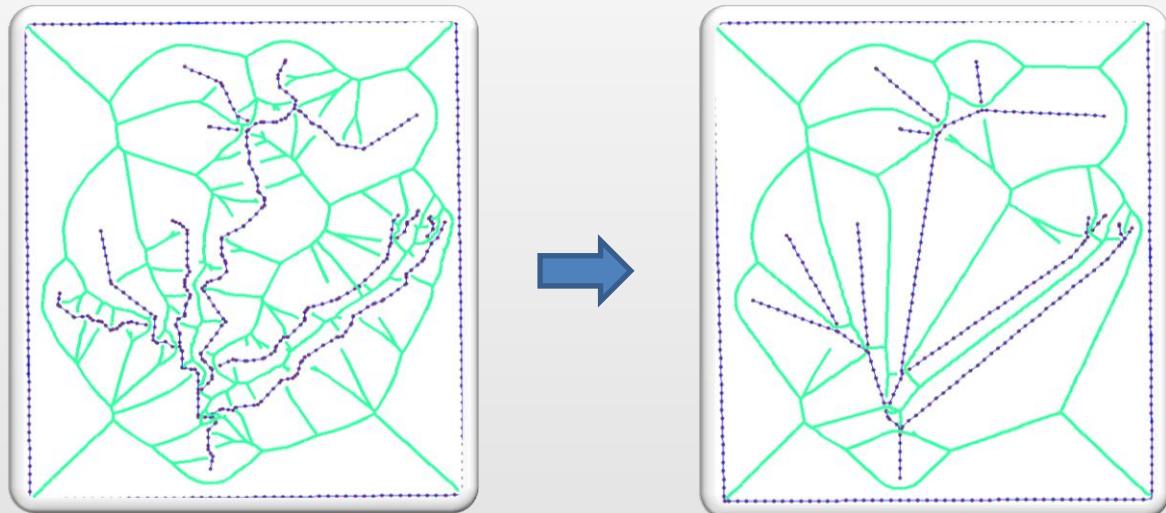
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## Filtering Algorithms

- Pre-processing (simplifying)
- Post-processing (pruning)

## Filtering Algorithms

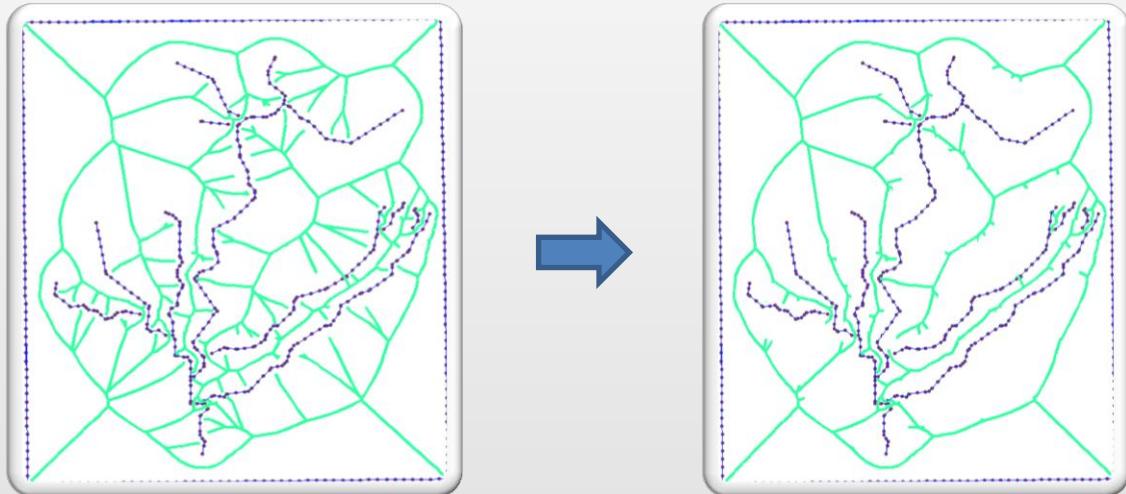
- Pre-processing (simplifying): Simplifying the boundary before computing the MA by removing perturbations or boundary noises.



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## Filtering Algorithms

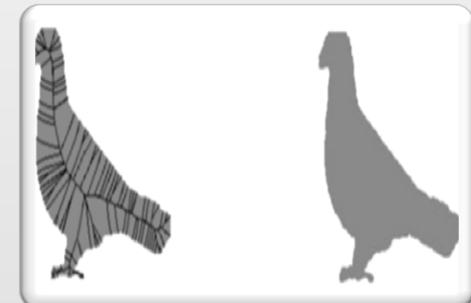
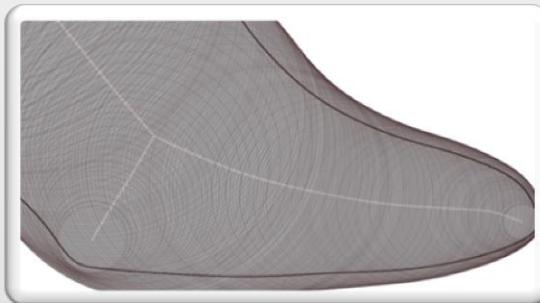
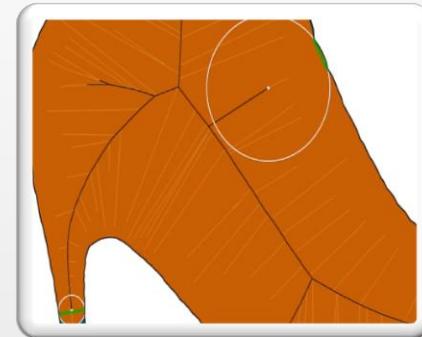
- **Post-processing (pruning):** Removing extraneous branches of the extracted MA, in order to preserve only the stable parts of the MA.



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# Pruning Algorithms

- Defining a criteria based on
  - Distance
  - Angle
  - Area
  - Scale



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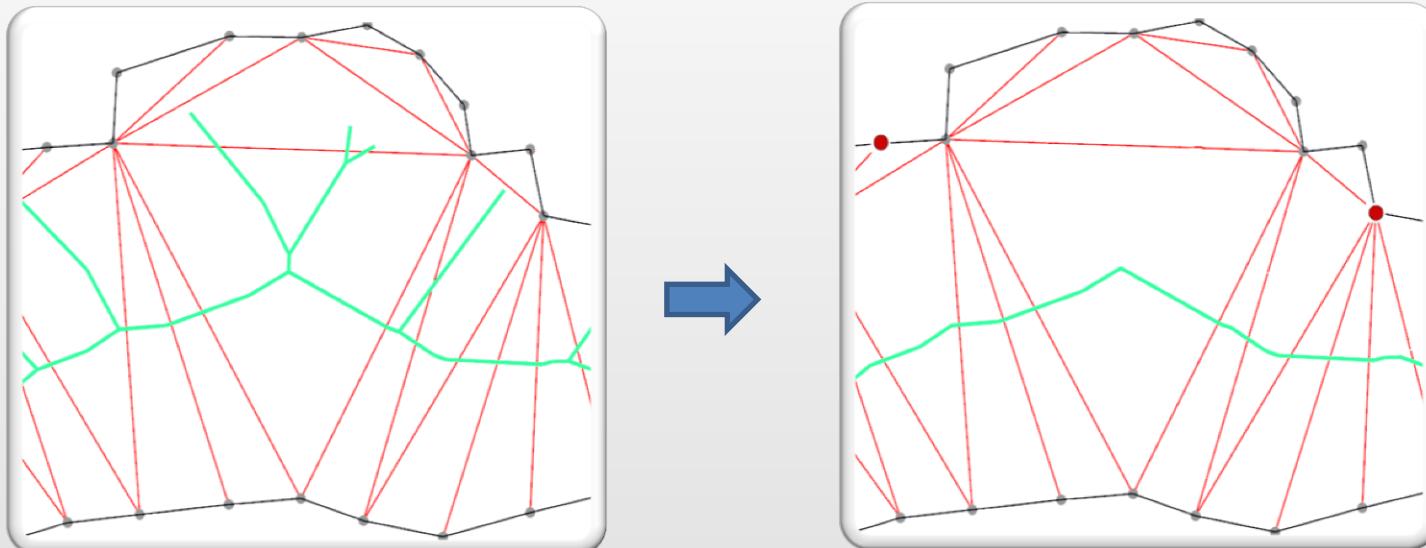
# Pruning Algorithms

## Shortcomings

- Do not prune all the irrelevant branches
- Shorten the main branches
- Disconnection in the main structure
- Cannot preserve the topology
- Do not work automatically

## Proposed Algorithm for Medial Axis Extraction

- **Observation:** Extraneous edges are the Voronoi edges created between the sample points lie on the same segment of the curve.



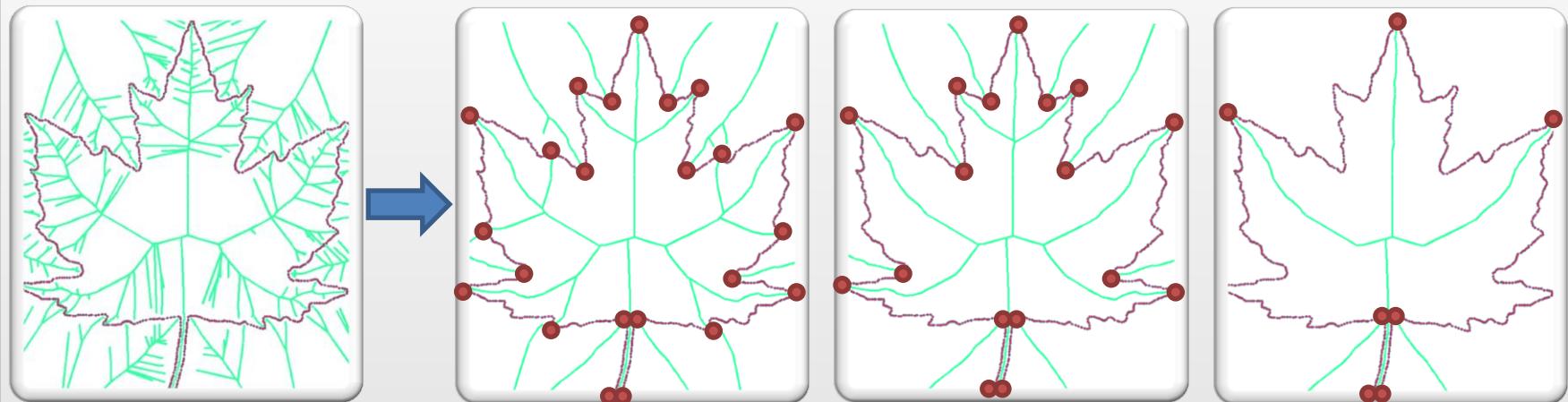
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## Proposed Algorithm for Medial Axis Extraction

- Labeling the sample points
  - Each segment of the shape is assigned a unique label; and all of its sample points are assigned the same label.
- Using the one-step crust and skeleton algorithm, but
  - Only the DT edges with the same label on both vertexes are added to the crust.
  - Only the dual of DT edges with different label on vertexes are added to the MA.

## Proposed Algorithm for Medial Axis Extraction

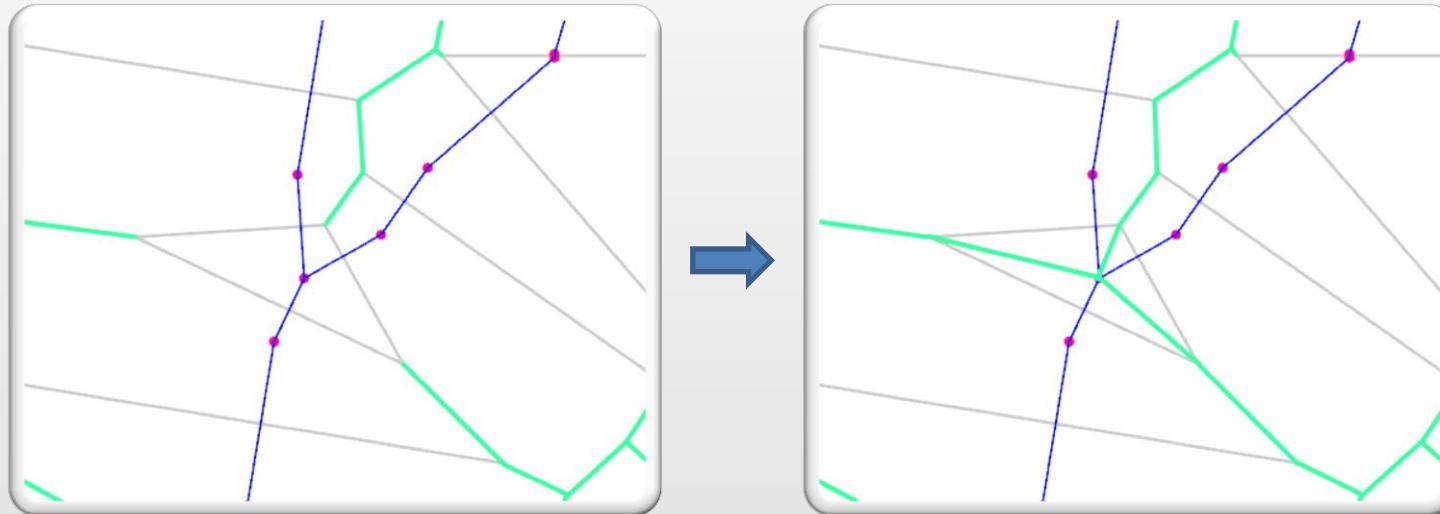
Example: MA extraction for different labelings



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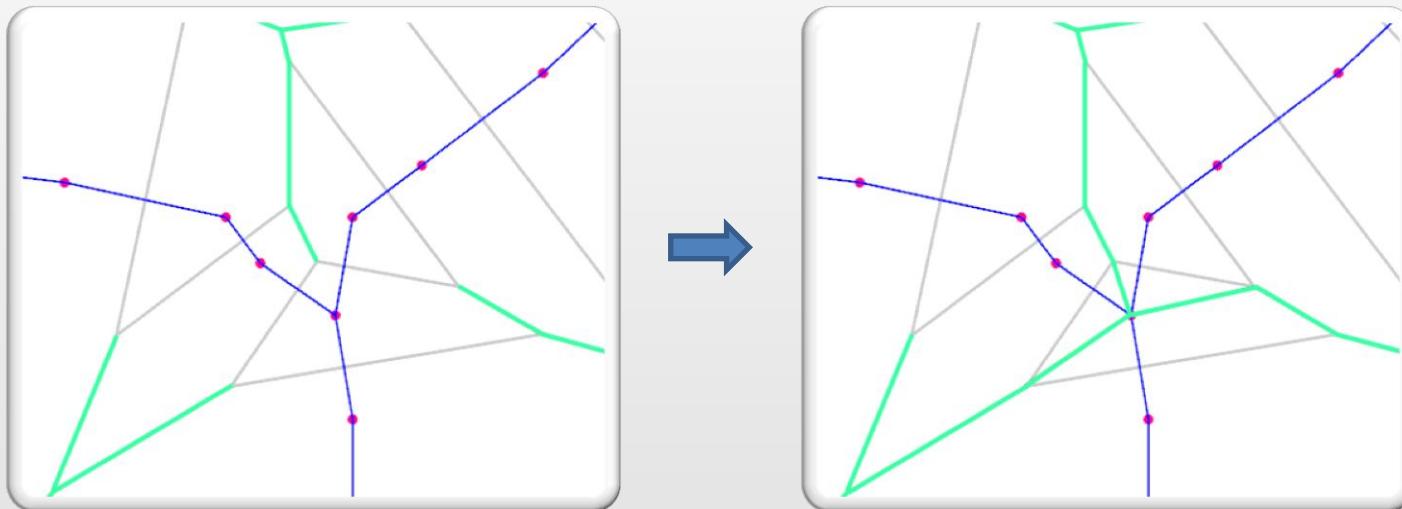
## Closing the Polygons

**Case 1:** The Voronoi cell of the junction point is a triangle



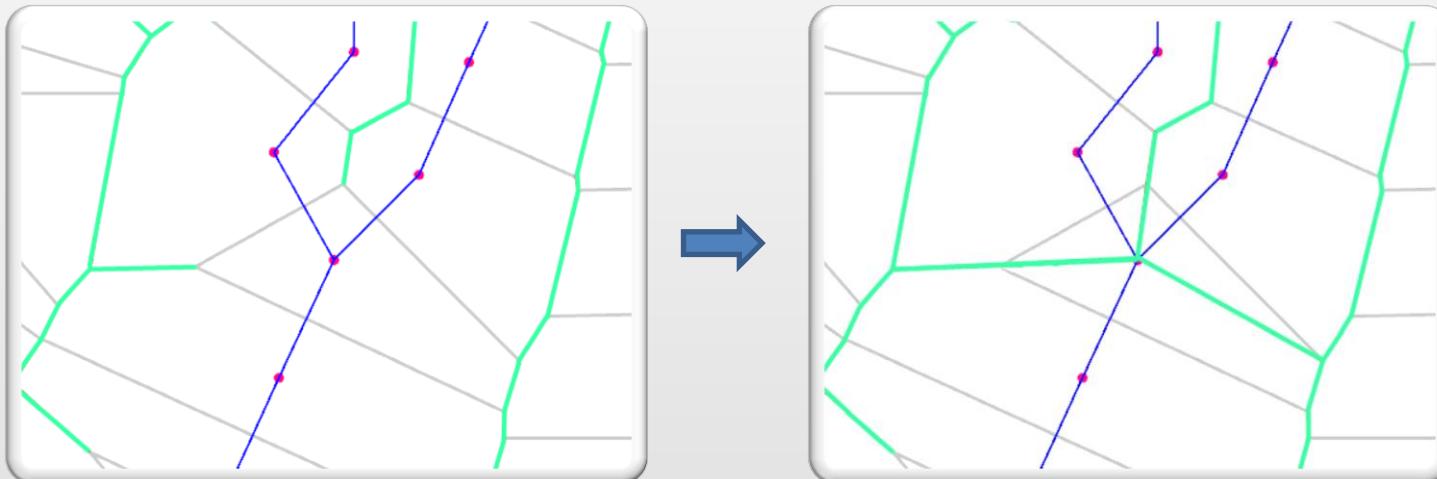
## Closing the Polygons

**Case 2:** The Voronoi cell of the junction point has more than three vertices, and 3 of these vertices are dangle nodes.



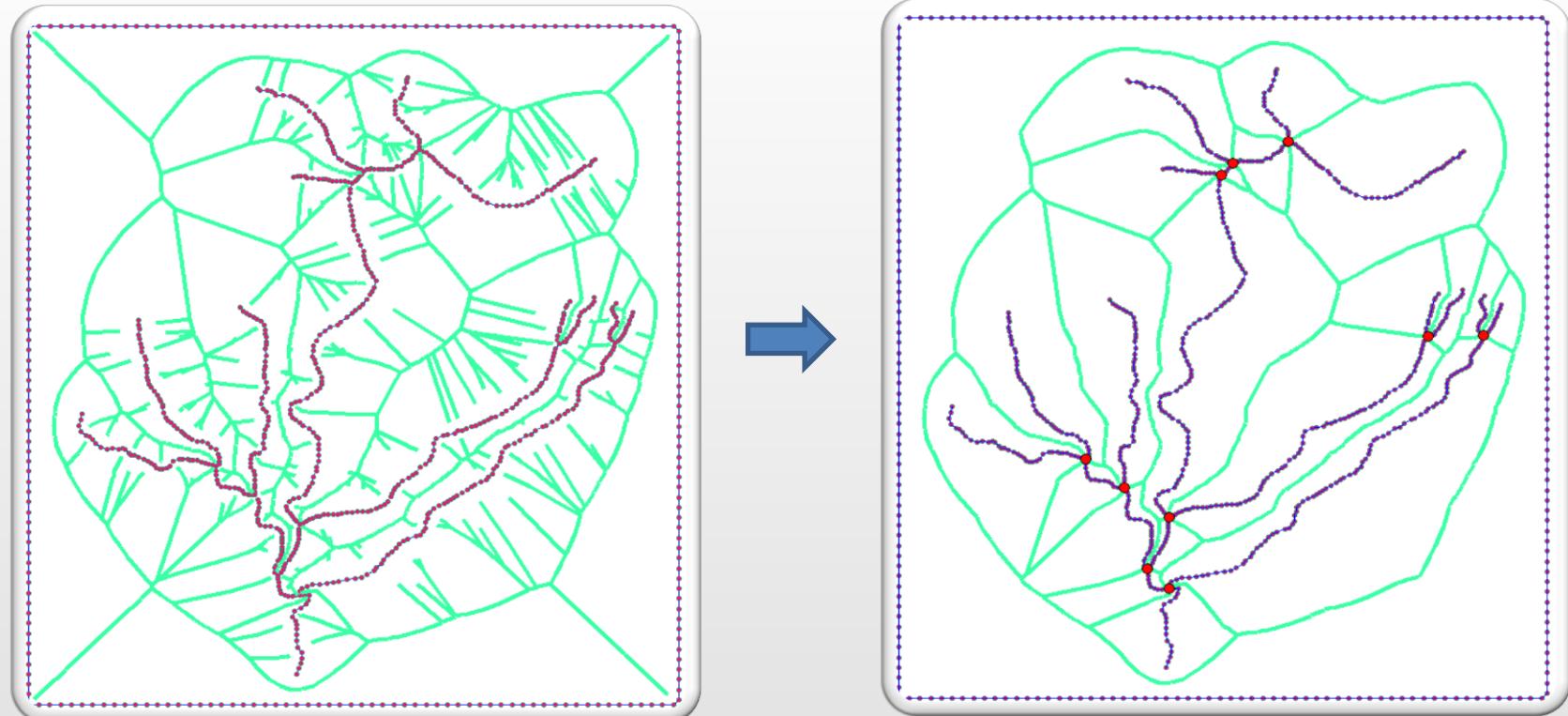
## Closing the Polygons

**Case 3:** The Voronoi cell of the junction point has more than three vertices, and more than 3 of these vertices are dangle nodes.



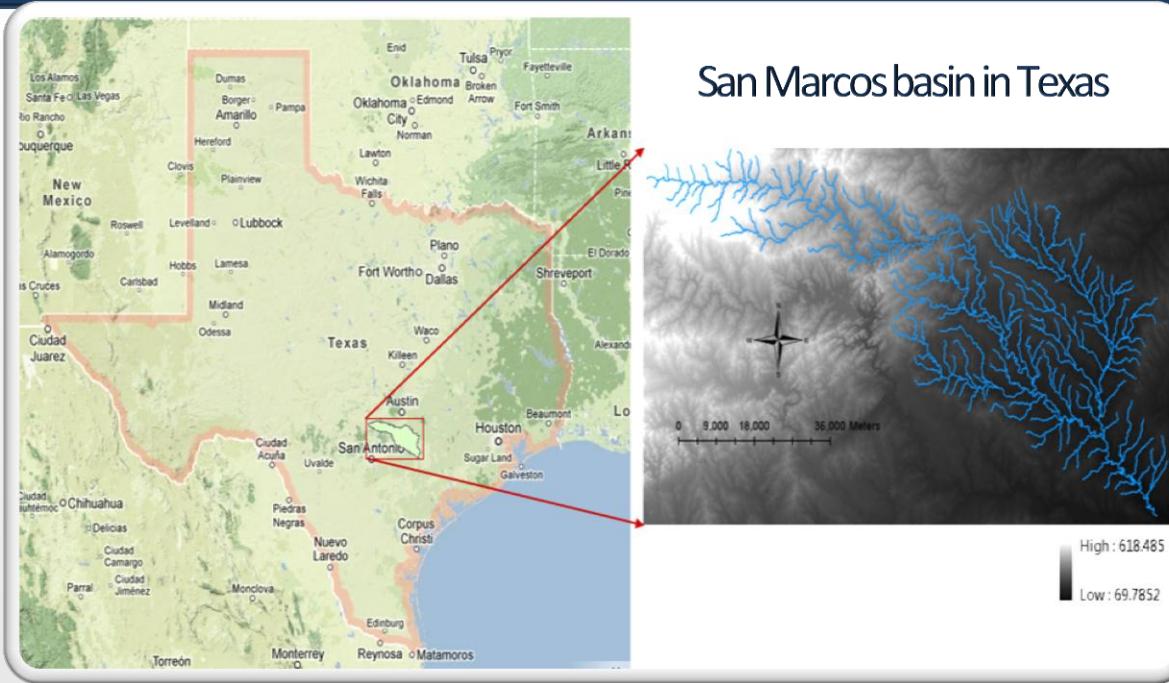
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## Catchment Area Delineation using the Proposed Method



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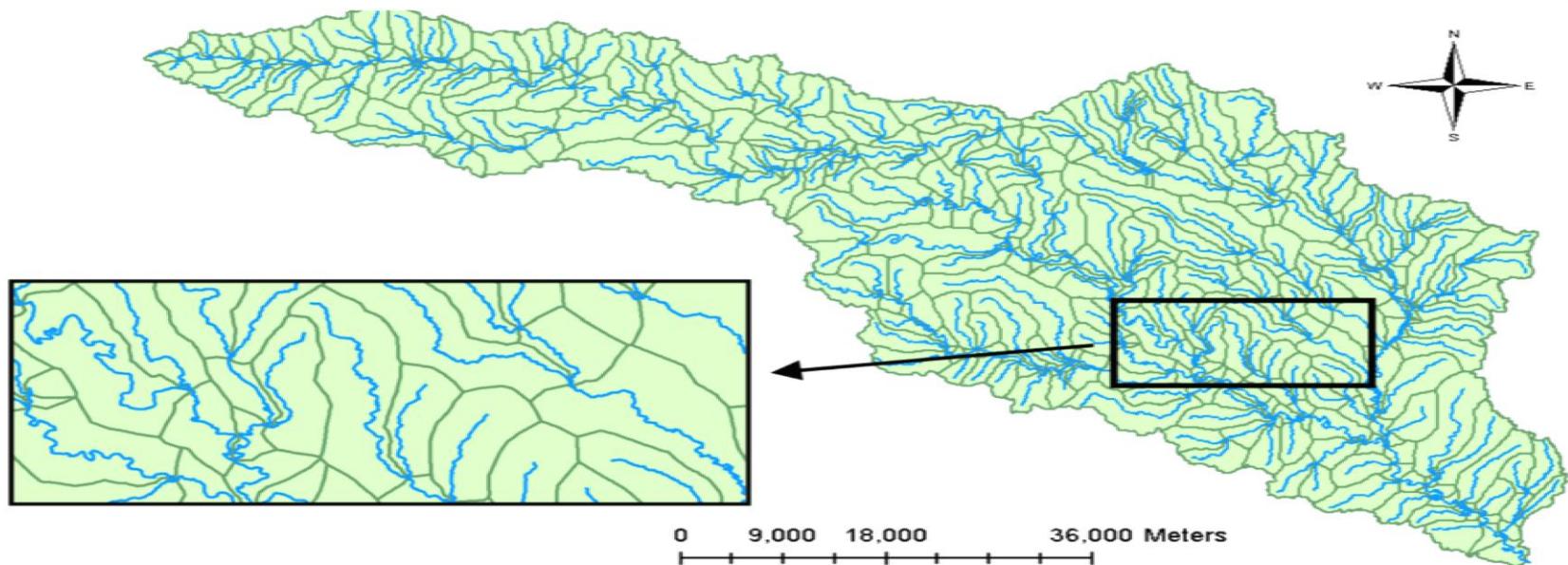
## Study Area & Data Set



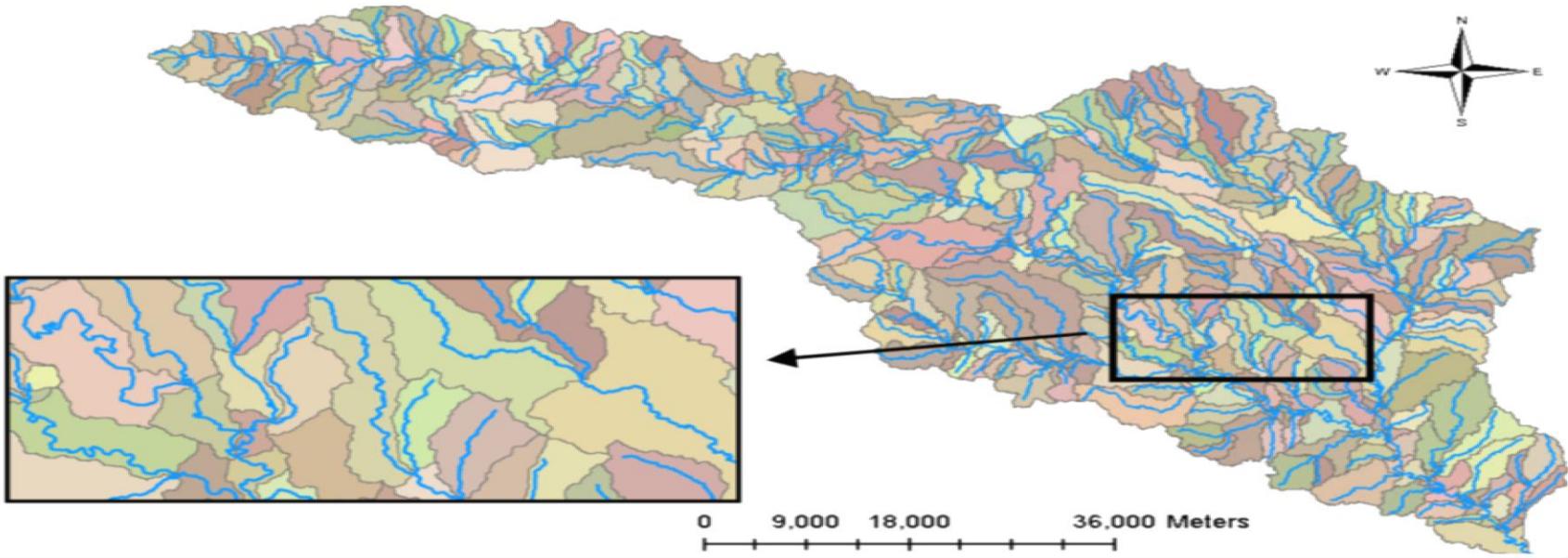
- River data: National Hydrography Dataset (NHD)
- Raster DEM: National Elevation Dataset (NED) with the spatial resolutions of 1 arc-second (approximately 30m)

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# Prposed Method



# DEM-based Method



# Conclusions

- Proposing a novel Voronoi-based algorithm to extract the medial axis through labeling sample points
- Creating a rational relation between labeling the sample points and extraneous edges in the medial axis structure
- Reducing the time of MA extraction by simultaneous filtering process
- Proposing a fast and automatic catchment area delineation algorithm that uses only the vector-based river network
- The results indicate that the medial axis of river network is a reasonable approximation of catchment area .
- The method can handle very large areas and produce catchment polygons quickly.

# **Thank You for Your Attention!**