

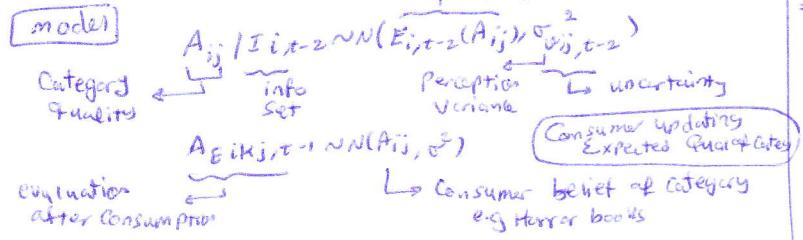
## Fire Fox Project Theory

Summary sheet

Quick math

Organized

- ① Modeling Consumer Learning from online product reviews  
(Zi Zhao Georgia State, Sha Yang USC, ...)
- ② Structured model (experiential products) - limited repeat  
Significant product category experiment (same genre)
- ③ Learn from experience, credibility modeling  
(Panel dataset)
- ④ Result: Learn more from others than their experience is the same genre
- ⑤ Profit input of product reviews (and how varies with # reviews): diminishing return; # reviews
- ⑥ Additional reviews may lower profit (Counterfactual)
- ⑦ Estimate optimum # of reviews for representative product
- ⑧ review credibility: degree of reflect consumer own experience (level)  $\equiv$  precision (credible info) / large effect on choice probability
- ⑨ Bayesian learning:
  - ① Product quality
  - ② Review credibility
- ⑩ False reviews increase consumer uncertainty (lower effect of negative reviews)



- $A_{Eikj,t-1} \in \{-\infty, 1, 2\}$  if  $R_{Eikj,t-1} = \text{observed evaluation}$
- $A_{Eikj,t-1} \in \{1, 2, 3\}$  if  $R_{Eikj,t-1} = 2$   $K_j$  = product item
- $A_{Eikj,t-1} \in \{2, 3, 3.5\}$  if  $R_{Eikj,t-1} = 3$
- $A_{Eikj,t-1} \in \{3, 3.5, 4, 4.5\}$  if  $R_{Eikj,t-1} = 4$
- $A_{Eikj,t-1} \in \{4, 4.5, +\infty\}$  if  $R_{Eikj,t-1} = 5$

use  $K_j$  item  $k_{t-1}$ :  $A_{ij} | I_{i,t-1} \sim N(E_{i,t-1}(A_{ij}), \sigma_{vij,t-1}^2)$

posterior belief

$$E_{i,t-1}(A_{ij}) = E_{i,t-2}(A_{ij}) + P_{ikj,t-1} B_{ij,t-1} (A_{Eikj,t-1} - E_{i,t-2}(A_{ij}))$$

Dummy of consumption  $\xrightarrow{\text{relating weight of Experience signal (greater for greater)}}$

$$\frac{1}{\sigma_{vij,t-1}^2} = \frac{P_{ikj,t-1}}{\sigma_e^2} + \frac{1}{\sigma_{vij,t-2}^2} \quad B_{ij,t-1} = \frac{\sigma_{vij,t-2}^2}{\sigma_{vij,t-2}^2 + \sigma_e^2}$$

$A_{ij} | I_{ii} \sim N(E_{i0}(A_{ij}), \sigma_{vij,0}^2)$ : prior

Rational expectation:  $E_{i0}(A_{ij}) = A_j$   $\sigma_{vij,0}^2 = \sigma_A^2 \Rightarrow A_{ij} \sim N(A_j, \sigma_A^2)$

$M_{Rk_j} \sim A_{Eikj,t-1} \sim N(0, \sigma_e^2)$  Per credibility of info

$\hookrightarrow$  population mean of evaluation (item  $k_j$ ): non-symmetric deviations

⑩ Credibility is unobserved  $\equiv$  higher precision

$R_{Eikj,t-1} \sim MR_{K_j} \sim N(0, \sigma_R^2)$   $\xrightarrow{\text{each review unbiased signal}}$

$\hookrightarrow$  eval of specific review  $\xrightarrow{\text{variance of deviation}}$  (representativeness of mean)

- since indiv. both cons. & rev:  $\sigma_R^2 = \sigma_e^2$

$\tilde{R}_{Eikj,t-1} \sim AEikj,t-1 \sim N(0, (1 + \frac{1}{n_{K_j,t-1}}) \sigma_R^2)$ ,  $\frac{1}{\sigma_R^2}$  precision

$\xrightarrow{\text{eval const}}$   $\# \text{reviews product } k_j \text{ after time}$

- more distance in evaluation  $\equiv$  less credible evolution of credibility of reviews for consumer over time:

$$\frac{1}{\sigma_R^2} | I_{i,t-2} \sim P(\alpha_{i,t-2}, \beta_{i,t-2}) \text{ prior belief } \sigma_R^2$$

$$\frac{1}{\sigma_R^2} | I_{i,t-1} \sim P(\alpha_{i,t-1}, \beta_{i,t-1}) \text{ posterior after review } \eta_{ij,t-1}, \text{ eval mean eval signal } \tilde{R}_{Eikj,t-1}$$

$$\alpha_{i,t-1} = \alpha_{i,t-2} + \frac{P_{ikj,t-1}}{2}$$

$$\beta_{i,t-1} = \beta_{i,t-2} + P_{ikj,t-1} \frac{(\tilde{R}_{Eikj,t-1} - AEikj,t-1)^2}{2(1 + \frac{1}{n_{K_j,t-1}})}$$

Integration of consumer's own experience reviews

2 src of info: own product  $\xrightarrow{\text{choice decision on } k_j^*}$   $N(E_{ikj,t-1}(A_{ij}), \sigma_{e_{ikj,t-1}}^2)$

② evaluation:  $A_{Eikj,t-1} \sim N(A_{ij}, \sigma_e^2)$  Prior cat. belief:  $A_{ij} | I_{i,t-1} \sim N$  of cons.  $i$

$$\Rightarrow A_{Eikj,t-1} \sim N(E_{ikj,t-1}(A_{ij}), \sigma_{e_{ikj,t-1}}^2)$$

② src: eval by revs (others)  $\rightarrow$  form Expect. of cred of revs

$$\frac{1}{\sigma_R^2} \sim P(\alpha_{i,t-1}, \beta_{i,t-1}) \Rightarrow E_{ikj,t-1}(\sigma_R^2) = \frac{\beta_{i,t-1}}{\alpha_{i,t-1} - 1}$$

mean eval  $\xleftarrow{k_j^* \text{ by revs}} \tilde{R}_{Eikj,t-1} \sim N(A_{Eikj,t-1} \sim (1 + \frac{1}{n_{K_j,t-1}}) \frac{\beta_{i,t-1}}{\alpha_{i,t-1} - 1})$

$\Rightarrow$  Expected qual item  $k_j^*$  cons. time + Dist Norm:

$$E_{ikj,t-1}(A_{Eikj,t-1}) = W_{ikj,t-1} E_{ikj,t-1}(A_{ij}) + (1 - W_{ikj,t-1}) \tilde{R}_{Eikj,t-1}$$

$$\text{Var}(A_{Eikj,t-1}) = \frac{1}{(\frac{1}{\sigma_{e_{ikj,t-1}}^2} + \frac{\alpha_{i,t-1} - 1}{\beta_{i,t-1}}) / (1 + \frac{1}{n_{K_j,t-1}})}$$

$$W_{ikj,t-1} = \frac{(\sigma_{e_{ikj,t-1}}^2 + \sigma_{vij,t-1}^2)^{-1}}{\frac{1}{\sigma_{e_{ikj,t-1}}^2} + \frac{\alpha_{i,t-1} - 1}{\beta_{i,t-1}} (1 + \frac{1}{n_{K_j,t-1}})^{-1}}$$

③  $\Rightarrow P_{i0} = (d_{i0} - 1) E_{i0}(\sigma_R^2) \xrightarrow{\text{magnitude of richness of cons. initial uncertainty of revs}}$  its initial exp. (inexp  $\Rightarrow$  for i0)

$$E_{i0}, E_{i0}(\sigma_R^2) > 0, \text{ estm} \Rightarrow \log(d_{i0}) \sim N(M_{d0}, V_{d0}^2)$$

$$\log(E_{i0}(\sigma_R^2)) \sim N(M_{R0}, V_{R0}^2)$$

heterogen. in initial cred. rev.

modeling consumer decisions

External cred. eval

own knowledge  $\rightarrow$  is about product cat.

$$\text{utility: } V_{ikj,t} = \text{expl-} \hat{r}_i (c_i A_{Eikj,t} + X_{ikj,t} Y_i + E_{ikj,t})$$

$\downarrow$  risk aversion  $\downarrow$  quality weight  $\downarrow$  calc. coeff. vector e.g. price

not know product quality prior  $\Rightarrow$  decide based on  $\tilde{r}_i, w_i, A_{Eikj,t}, X_{ikj,t}$

$$E_{it}(V_{ikj,t}) = -\hat{r}_i \tilde{r}_i E_{it}(A_{Eikj,t}) \rightarrow \hat{r}_i^2 (w_i)^2 [Var_{it}(A_{Eikj,t})]$$

$$+ X_{ikj,t} Y_i + E_{ikj,t}$$

$$\maximize \text{expected utility: } U_{ikj,t} = \hat{r}_i A_{Eikj,t} + E_{ikj,t} = \hat{r}_i^2 \tilde{r}_i^2 (w_i)^2, w_i [E_{it}(A_{Eikj,t})] - \hat{r}_i [Var_{it}(A_{Eikj,t})] + X_{ikj,t} Y_i + E_{ikj,t}$$

$$\text{unobserved heterogeneity: } \log(w_i) \sim N(\bar{w}, V_w^2)$$

$$\log(r_i) \sim N(\bar{r}, V_r^2)$$

$$A_{ij} \sim N(A_j, \sigma_A^2) \rightarrow \text{diagonal}$$

$$Y_i \sim MVN(\bar{Y}, \Sigma)$$

# FireFox project theory

Self Socio

$$U_{it} = d_j + \beta_i S_{it}$$

↓      ↓  
specificized stars    risk aversion  
↑

$$E_i U_{ikj,t}^* = \underbrace{w_i}_{\gamma_2 r_i(w_i)^2} [V_{ikj,t}(A_{Eikj,t}^*)] - r_i [V_{ikj,t}(A_{Eikj,t}^*)]$$

$$+ X_{ikj,t} Y_{ikj,t} + \varepsilon_{ikj,t}$$

$$w_{ikj,t-1} = \frac{(\sigma^2 + \sigma_{v_{ikj,t-1}}^2)^{-1}}{\frac{1}{\sigma^2 + \sigma_{v_{ikj,t-1}}^2} + \frac{\alpha_{i,t-1}^{-1}}{\beta_{i,t-1}} \left(1 + \frac{1}{n_{Kj,t-1}}\right)^{-1}}$$

$$E_i(A_{Eikj,t}) = w_{ikj,t-1} E_{i,t-1}(A_{ij}) + (1 - w_{ikj,t-1}) \bar{R}_{kj,t}$$

$$\bar{R}_{kj,t} = A_{E,kj,t} \sim N(0, (1 + \frac{1}{n_{Kj,t}}) \sigma_e^2)$$

$$\Rightarrow \frac{1}{\sigma_e^2} | I_{i,t-1} \sim N(\alpha_{i,t-1}, \beta_{i,t-1})$$

$$\underbrace{A_{ij}}_{\substack{\downarrow \\ \text{avg quality}}} | \underbrace{I_{i,t-1}}_{\substack{\text{inf score}}} \sim N(E_{i,t-2}(A_{ij}), \sigma_{v_{ij,t-2}}^2)$$

$$\underbrace{A_{Eikj,t-1}}_{\substack{\downarrow \\ \text{eval after consump}}} \sim N(A_{ij}, \sigma^2) \quad \xrightarrow{\text{eval after consump}} \text{const. belief of cutes} \quad \xrightarrow{\text{relative weight expr signal}}$$

$$E_{i,t-1}(A_{ij}) = E_{i,t-2}(A_{ij}) + D_{ikj,t-1} B_{ikj,t-1} (A_{Eikj,t-1} - E_{i,t-2}(A_{ij}))$$

$$B_{ikj,t-1} = \frac{\sigma_{v_{ikj,t-2}}^2}{\sigma_{v_{ikj,t-2}}^2 + \sigma^2}$$

$$\frac{1}{\sigma_{v_{ikj,t-2}}^2} = \frac{D_{ikj,t-1}}{\sigma^2} + \frac{1}{\sigma_{v_{ikj,t-1}}^2}$$

$$MR_{Kj} = A_{Eikj,t-1} \sim N(0, \sigma_R^2)$$

pop mean of eval item Kj

$$R_{i,Kj,t-1} - MR_{Kj} \sim N(0, \sigma_R^2)$$

+ eval specific rev

$$\text{Correl util item with cat } P \Rightarrow P(D_{ikj,t-1} | D_{ij,t-1}) = \frac{\exp(\hat{u}_{ikj,t})}{\sum_K \exp(\hat{u}_{ikj,t}) / (1-p)}$$

$$P(D_{ij,t-1}) = \frac{\sum_K \exp(\hat{u}_{ikj,t})}{\sum_j [\sum_K \exp(\hat{u}_{ikj,t}) / (1-p)]^{1-p}}$$

Covers of ① price  
② time elapse since public

Results:  
 ① profit impact of prod rev. diminishing return  
 ② earn more from others than own Exp Cmp<sup>3</sup>  
 ③ estimate opt # review  
 ④ take rev increase comp. unit.

Firefox project theory

Summary = short

Quick math

Organized

③

- utility of other goods ( $\alpha_j$ ):  $U_{ij,t} = \alpha_j + \epsilon_{ij,t}$   
Cat. spec. intercept other gds  $\leftarrow$

- Correl. util. item's within categ (nested logit):  $\rho$

$$P(D_{ikj,t} = 1 | D_{ij,t} = 1) = \frac{\exp(\frac{\alpha_{kj,t}}{1-\rho})}{\sum_k \exp(\frac{\alpha_{kj,t}}{1-\rho})}$$

Unconditional prob. purchase Categ. j:

$$P(D_{ij,t} = 1) = \frac{\left[ \sum_k \exp(\frac{\alpha_{kj,t}}{1-\rho}) \right]^{1-\rho}}{\sum_i \left[ \sum_k \exp(\frac{\alpha_{kj,t}}{1-\rho}) \right]^{1-\rho}}$$

① Price  
Covers time elapse  
since publication

- PPF** Prospect theory, Loss Aversion & Ref. Pcp effect Boundaries
- ② Brule-Houide, Eric Johnson, Fader 1993
  - ① multi attrib. gen. of prospect theory value func.
  - ② position of brand relative to multiattrib. ref. points
  - ③ Cons. weight loss from ref point more than equiv. sized gain (loss aversion)
  - ④ multinom. logit of ref dependent choice matrix Calib. Stevens data
  - ⑤ significant loss aversion in coeff (asymmetric responses to changes in prod. choice)
  - ⑥ Trans. Icarman theor. framework multiattrib. basis: (price & qual...)
    - (1) each choice alternates decompose into set of valuation attrib.
    - (2) each attrib. can be desc. by its own val. func. with own value on attrib.
    - (3) attrib. eval. relative to ref. points  - ⑦ three char. of val. func.:
    - (1) Ref. depend: carrier of an attrib. Val. not on absolute but rather deviation from ref. level  $\Rightarrow$  (Gain or loss)
    - (2) Loss aversion: value func. steeper for loss than for gain (can lose value more than an equiv. gain will rec. val.)
    - (3) Diminishing sensitivity: margs. val. of both gains & losses decrease with size (first dollar hurts the most)
  - ⑧ de-composability: e.g. additive  $U_r(m_1, q_1) = R_1(m_1) + R_2(q_1)$
  - ⑨ Constant loss aversion:  $R_q(q_H) = \int u_{q(H)} - u_{q(r)}$  if  $x_i \geq r_i$   
coeff of loss aversion  $\propto [u_{q(H)} - u_{q(r)}]$  if  $x_i < r_i$
  - ⑩ reference brand: most recent brand purchased by each household  
Purch. in memory  $\Rightarrow$  (2) status quo)
  - ⑪ loss aversion:  

$$\text{Household}_{ijt} = \beta_1 [\text{Qualgain}_{ijt} + \beta_2 \text{Qualloss}_{ijt}] + \beta_3 \text{Price}_{ijt} + \beta_4 \text{Feature}_{ijt}$$

$$+ \beta_5 \text{Fidelity}_{ijt}$$

$$\left\{ \begin{array}{l} \text{Qualgain}_{ijt} = Q_j - Q_r \\ \text{Qualloss}_{ijt} = Q_j - Q_r \\ \text{Price}_{ijt} = P_{ijt} - P_{rjt} \\ \text{Feature}_{ijt} = P_{ijt} - P_{rjt} \\ \text{Fidelity}_{ijt} = 0 \end{array} \right. \quad Q_j \geq Q_r$$

$$\left\{ \begin{array}{l} \text{Qualgain}_{ijt} = 0 \\ \text{Qualloss}_{ijt} = Q_j - Q_r \\ \text{Price}_{ijt} = P_{ijt} - P_{rjt} \\ \text{Feature}_{ijt} = P_{ijt} - P_{rjt} \end{array} \right. \quad P_{ijt} \leq P_{rjt}$$

$$\left\{ \begin{array}{l} \text{Qualgain}_{ijt} = 0 \\ \text{Qualloss}_{ijt} = 0 \\ \text{Price}_{ijt} = P_{ijt} - P_{rjt} \\ \text{Feature}_{ijt} = P_{ijt} - P_{rjt} \end{array} \right. \quad P_{ijt} > P_{rjt}$$
  - ⑫ temporal ref price model (smooth of past observed)  

$$\text{Price}_{ijt+1} = \gamma \text{price}_{ijt} + (1-\gamma) \bar{\text{Price}}_{ijt}$$
  - When is versioning optimal for info goods (Bhargava 2008) (Chaudhury)
  - ① When versioning optimal strategy for info goods
  - ② info goods: vrs. costs invar. with qual.
  - ③ monop. firm exist prod in mkt, opport. to seg. mkt by introd. additional lower qual vers. (single prod. max profit)
  - ④ optimal when share of low-qual vers. (offered alone)  $>$  mkt share of high qual vers. alone
  - ⑤ Incentive Compatibility
  - ⑥ vrs. cost  $P \rightarrow$  Consider only offering one version
  - ⑦ vrs. cost  $\rightarrow$  Explore adding lower qual. version
- ⑪ Feasible qualities: move  $\pi_i = (P_H - c)(1 - F(Q_H))$   
 $P_{ijt} \rightarrow P_H$   $\downarrow$  cumul. dist. of types  
 $\uparrow \sum_{j=1}^{H-1} (P_j - c)(F(Q_{j+1}) - F(Q_j))$
- s.t.  $U(L_j, q_j) - p_j = U(L_j, q_{j-1}) - p_{j-1} \quad (V_j = l_{j-1}, H)$   
 $V_j \geq D_{j-1} \geq 0 \quad \rightarrow$  valuation of type 2/ $j$   $\rightarrow$  price  
 $V_j$ : index cons. types (arranged increasing order)  
 $U_L(V_j, q_j) > 0$
- $c = \max q_j \quad q_j \text{ low qual} \Rightarrow q_2 \quad q_0 = 0 \quad U(L_0, q_0) = P_0 = 0$
- Own demand elast:
- $E(L_j, q_j) = \frac{\partial U(L_j, q_j)}{\partial P_j} = \frac{U(L_j, q_j)}{U_L(V_j, q_j)} \cdot \frac{(F(Q_j))}{(1 - F(Q_j))}$
- From elast. (elast.  $q_j$ , presence of lower qual  $q_{j-1}$ )  
 $q(V_j, q_{j-1}, q_j) = \frac{\partial U}{\partial P_j} = \frac{U(L_j, q_j) - U(L_j, q_{j-1})}{U(L_j, q_j) - U_L(V_j, q_{j-1})}$
- Versioning optimal when  $\exists q_j: (1 - F(Q_j)) > (1 - F(Q_H))$   
 = versioning not optimal linear valuation  $U(L_j, q_j) = V_j \cdot q_j$
- ⑫ Heterogeneity makes versioning optimal (in marginal value)  
 revenue loss by cannibalization & info rent  
 $c=0$ , versioning optimal when  $\exists q_j: E(0, q_H) = U(L_j, q_j) / U(L_j, q_H)$   
 $c=1$ , optimal when:  $\exists q_j: E(0, q_H) = \text{rel. surplus}: \frac{U(L_j, q_j) - c}{U(L_j, q_H) - c} \rightarrow V_j$   
 How? disable features
- (How Does The Variance of Prod. Rating Matter) (Monic Sun 2012)
- ① Info role of prod. rating. How vrt. help cons. Rtg. out more much enjoy
  - ② high Avg rating  $\equiv$  high prod. qual.
  - ③ high var. rating  $\equiv$  niche prod  $\Rightarrow$  higher subset demand  $\Rightarrow$  Avg. rat. low
  - ④ monopoly, risk neutral Cons. heterogen. tastes
  - ⑤ taste space: line of size 2, product mid point  
cons. taste diff.  $\times$  from prod. buys at price  $P$
  - prod.  $V - t - x - P = \text{utility}$   $\uparrow$  high  $t$  product: niche product  
 $\downarrow$  mismatch cost low  $t$  prod: mainstream, all cons. same utility
  - ⑥ beginning of game neither seller nor consumer know realization of  $V$  and  $t$  (exogen. given  $\neq$  95% fail.)
  - ⑦ joint prob. dist.  $f(V, t)$  common knowledge
  - ⑧ period 1: unit mass of early Cons. (no info on qual or mismatch cost)  
 $x \sim U(0, 1)$  Seller chooses price:  $P_1$   
 Cons. decides to buy & quickly consum & publish rating  $S(n) = V - t n$
  - ⑨ period 2: unit mass of late Cons.  $x \sim U(0, 1)$   
 observe 1st period demand, Avg. rating, Var. ratings.  
 Seller chooses  $P_2$ , Cons. decides whether to buy the product
  - ⑩ Subgame equilibrium:  
 first period no info  $\rightarrow$  use expectation  $E(V), E(t), \text{line } f(V, t)$   
 indiff. Cons.:  $E(V) - E(t) \cdot D_1 - P_1 = 0 \Rightarrow \exists t \in [0, D_1] \text{ purchase}$   
 First period demand  $D_1$   
 distance  $D_1$   
 rating uniformly dist.:  $[V - t + P_1, V]$   
 Avg rating:  $M = V - \frac{t \cdot D_1}{2}$  Var rating:  $V = \frac{1}{12} (t \cdot D_1)^2$
  - ⑪ not indep.  $\Rightarrow$  high Avg rating  $\Rightarrow V = 0 \Rightarrow D_1 = M + \sqrt{3} V$   
 low Avg  $\Rightarrow$  ① low quality or ② high mismatch cost  $t = \frac{2\sqrt{3}V}{D_1}$



KIM 2010

## Online Demand under Limited Consumer Search

Kim 2010  
Albuquerque  
isoonkang

① Amazon.com, durable

② optimal set size Proc. (Aggreg. indiv. OPT search size)

③ dynamic programming + choice model (Weitzman); heterogen.

④ answers Ques (1) Mkt struct (2) Competition (3) policy maker issues (lower cost)

⑤ own exogenous price elast., actual product search rank Predictive uncertainty

⑥ Benefit product recom. via lower search cost

⑦  $u_{ij} = V_{ij} + e_{ij}$        $V_{ij} = x_j b_i$        $b_i \sim N(0, \sigma_b^2)$        $e_{ij} \sim N(0, \sigma_e^2)$

outside Good Alternative      diagonal      costly resolved

(not req. search; cons. aware)      (cons. knows zero determinant)      (general cat pg)      (cons. not know)

Search Cost log normal:  $C_{ij} \sim \exp(\lambda_j V_{ij})$ ,  $\lambda_j \sim N(V_0, \sigma_\lambda^2)$

(to have positive availability of Prod. Known to Cons. (freq. in store, # recommended))

⑧ Search cost log normal:  $C_{ij} \sim \exp(\lambda_j V_{ij})$ ,  $\lambda_j \sim N(V_0, \sigma_\lambda^2)$

Search cost:  $c_{ij} \sim \exp(V_{0j} + V_{ij} \beta_j)$

$V_{0j} \sim N(V_0, \sigma_{V_0}^2)$ ,  $V_{ij} \sim N(V_1, \sigma_{V_1}^2)$

⑨ obj func: expected util - total search cost

⑩ Set search cost per cont: expected marginal benefit of search:

$$B_{ij}(u_i^*) = \int_{u_i^*}^{\infty} (u_{ij} - u_i^*) f(u_{ij}) du_{ij} \quad \text{→ density of } u_{ij}$$

left tail      highest utility among searched products

⑪ Cons. Cont search if at least one  $j$ :  $C_{ij} < B_{ij}(u_i^*)$ ⑫ Search strategy:  $S_i \cup \bar{S}_i$  (partition, searched options vs. unsearched)⑬ all info about  $S_i$  contained in  $u_i^* = \max_{j \in S_i} u_{ij}, e_{ij} + \epsilon$ ⑭ State of System  $(u_i^*, \bar{S}_i)$ 

⑮ Value func:  $W(u_i^*, \bar{S}_i) = \max(u_i^*, \max_{j \in \bar{S}_i} [C_{ij} + P_i F(u_i^*) \cdot W(u_i^*, \bar{S}_i - \{j\})])$

+  $\int_{u_i^*}^{\infty} W(u_{ij}, \bar{S}_i - \{j\}) f(u_{ij}) du_{ij}]$  Bellman equation

⑯ Assump: ① Cons. has full info prod attrn  $v_{ij}$ 

②  $E(e_{ij}|e_k) = 0$  (well defined prob prior search, not know about prob during search process)

③ no context or ret. effect

⑰ Reservation utility (Unit by search & not search):  $Z_{ij}$  def:

$$c_{ij} = B_{ij}(Z_{ij}) = \int_{Z_{ij}}^{\infty} (u_{ij} - Z_{ij}) f(u_{ij}) du_{ij} \quad Z_{ij} = B_{ij}^{-1}(c_{ij})$$

⑱ Component of search:

① Selection rule: Compute all  $Z_{ij}$  & sort descend. order (search list)② Stopping rule: Stop when  $u_i^* > \max_{j \in \bar{S}_i} (Z_{ij})$ ③ Choice rule: Once search stopped collect  $u_i^*$  by choosing max util alt. in  $S_i$ .⑯ Assump:  $e_{ij}$  indep  $V_{ij}$  (search aware product does not affect search behavior)

⑰ not curse of dimensionality, since Cons. samples descend. order, seq search

⑱  $R_{ij}$  inclusion in optimal search set cons.  $i \in \pi_{i,r(k)}$  incl. highest rank

$$\pi_{i,r(k)} = \Pr \left( \max_{k=1}^{r(k)} (V_{ij,r(k)} + e_{ij,r(k)}) < Z_{ij,r(k)} \right) = \prod_{j=1}^{r(k)} F(Z_{ij,r(k)} - V_{ij,r(k)})$$

all j in draws fell short  $\Rightarrow$  inclusion probability,  $\pi_{i,r(k)} = 1$  at least one

property: (1)  $\pi_{i,r(k)} > \pi_{i,r(k+1)}$  (2)  $\pi_{i,r(k)} \text{ and } r(j+k) = \pi_{i,r(k)} = \min(\pi_{i,r(i)}, \dots, \pi_{i,r(i+k)})$

prob  $r(j+k)$  is in the set

(3)  $P_r(S_i, r(k)) = \pi_{i,r(k)} - \pi_{i,r(k+1)}$

optimal set of  $S_i$   
size  $k$  for indiv.  $i$ 

⑲ Data: view rank data, average sales price, appearance on other prod wrt percentile ranking  $\hat{r}_{it} = \frac{r_{it}}{\max_{it} r_{it}}$  highest rank  $\hat{r}_i = \frac{\sum_b \hat{r}_{ib}}{T}$

⑳ Conclude: # appearances on view rank depend on attrib. & price

㉑ # product detail page view  $\hat{d}_i$

㉒ appearance on different count  $\rightarrow$  effect search cost

㉓ Commonality index: relationship b/w products

$C_{ijk} = \frac{n_{jk}}{\sqrt{n_j} \sqrt{n_k}}$   $(j,k) > (i,j) \leftrightarrow C_{ijk} < C_{ijj}$

$$㉔ u_{ij} = X_{ij} \beta_i + \epsilon_{ij} \quad \log(\epsilon_{ij}) \sim N(\beta_p, \sigma_p^2)$$

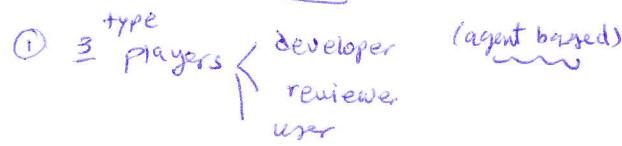
$\beta_i \sim N(\beta_0, \Sigma_\beta)$

Search cost:  $c_{ij} \sim \exp(V_{0j} + V_{ij} \beta_j)$

$V_{0j} \sim N(V_0, \sigma_{V_0}^2)$ ,  $V_{ij} \sim N(V_1, \sigma_{V_1}^2)$

## FreeFox project theory

①



② developer:  $\max R \times d - g \cdot c$

rate      ↓      ↓  
download Cost of versioning

Given Opportunity Cost Constraint

③ user:

- decide to download Given type
- Mixture of type
  - review searcher  $\Rightarrow$  last reviews weight
  - (signaling) general signal searcher
    - $\frac{1}{\# \text{ users}}$
    - $\frac{1}{\# \text{ stars}}$

④ Reviewer:  
find error  $\rightarrow$  exponentially distributed time  
decide to share or not: Poisson split p  
 $\Rightarrow$  Erlang time of 2nd & 3rd....  
① depend on # users    ② selection model

⑤ if review searcher Search cost  $C_s$ : Sequential  
search  $\Rightarrow$  learning

Stopping rule: explanation close to the need  
(remove uncertainty)

⑥ prospect theory: different effect of positive vs.

negative  $\rightarrow$  Hau model } MSCI  
Reference stars as # stars of top 2 rates

⑦ outcome of paper:  
what signaling

- Search cost by each party
- policy                  ① party
- ② platform owner

⑧ cost of usage of open source product

(FPP) Optimal Number of Versions (JmIS): Hui, Yoo, TAM 2008 ①

- ① Pricing  $\rightarrow$  as many versions as possible
- ② marginal benefit of an additional version decreases rapidly
- ③ Cognitive Costs have more profound effects on versioning than menu cost

## summer project

what drives decision to download?

if in first look found not related discuss

CSR

## ① List of Correlates:

Experiencing good reviews

- ① Interaction significant b/w reviews & product variety  
(context popular vs. niche products)
- ↑ Prod. Vari → ↑ positive rev. vs. rev. (more on popular prod)
  - ↑ ↳ helps niche prod (get more downloads)
- (Zhang, Duan 2012 EC research snippets) Quantile Reg

- ② Michael Trusov, Decker 2010 (Journal of research in marketing) → Perceived strength & weakness of product
- aggregate cons. pref (product development, Conjoint)
  - preprocessing NLP
  - relative role of ① product attribute ② brand name on overall evaluation (heterogeneity) - mobile phone mkt
  - clarify pros & Cons (remove unrelated, aggregate redundant, implicit → explicit elements less frequent, binary coding (Duminy))
  - discrete distribution of pref. (latent class)
  - 3 model: (1) Homogen (2) Heterogen (disc) (3) Heterog (Conting)
  - $\sum_{km} (\lambda_{km})$  brand m (left) -  $\pi_k \lambda_{km}$ : func. attrib. get level  $\frac{m}{\sum_{m=1}^M \pi_m \lambda_{km}}$
  - $\text{Prob}^{PR}(Y_{ikj}) = \frac{\lambda_{ikj}}{y!} e^{-\lambda} \quad (\text{Poisson}) \lambda = e^{\alpha + \sum_{l=1}^L (\beta_{lkj} x_{lkj} + \gamma_{lkj} z_{lkj} + \delta_{lkj} s_{lkj})}$
  - ↳ obscuring evaluation Given certain product summary
  - $\Delta \text{LL} (\Phi PR) = \ln \left( \prod_{k=1}^K \frac{\lambda_{ikj}}{y_{ikj}!} e^{-\lambda_{ikj}} \right) = \sum_{k=1}^K y_{ikj} \ln(\lambda_{ikj}) - \lambda_{ikj} - \ln(y_{ikj}!)$  (AIC)
  - heterogen. Neg binom-Poisson prior (Conditional mean  $\lambda = \mu e^{-\epsilon}$ )
  - ② latent class poisson:  $\Delta \text{LL} = \sum_{k=1}^K \ln \left( \sum_{i=1}^I \pi_i \lambda_{ikj} \frac{y_{ikj}}{y_{ikj}!} e^{-\lambda_{ikj}} \right)$  attrib. Brand and sensitivity of product eval to var. qual. of func. attrib:  $\frac{\partial \Delta \text{LL}}{\partial \text{attrib. brand}}$

- ③ Quantifying social influence in an online culture market (Peris J., 2012)

- ① two step process of ① decision to sample (social influence)  
② role of placement in mediating social signals

→ informational rather than normative

- ④ availability: prob. of being sampled:  $V_i = \sum_p \frac{I_{ip}}{\sum_j I_{jp}}$
- appeal function of friend listener:  $A_i = Z_i / \sum_k L_k$
- conditional prob. of download corr. w/ avail. score (Polya urn)
- prob. song i sampled:  $\frac{V_{it}}{\sum_j V_{jt}} \frac{(D_{it} + d_{it})}{(D_{it} + d_{it} + A_i)}$

- ⑤ what makes a helpful online review (Mudambi 2010)
- perceived helpfulness (① Extremity ② review depth ③ product type)
- ↳ helpful positive (moderator)
- ↳ experience good (more for search goods) Search or word count
- ↳ star rating Experience

User Generated Open Source Products: Founder's Soc Capital  
⇒ Time to prod. Release: Muliapra, Gudar, Grewal & Lien 2012

- ① success measure: time to prod. release.
- ② how ① location of Proj. founder in soc. netw. ② interplay of developers & end users & ③ proj. prod. choice. ⇒ affect time to prod. release ⇒ (hazard model)

## Scratch

$$\text{① } p_{\text{prob}}(\text{prod}) = \sum_{\text{prod}} p(\text{signal}) \cdot \pi(\text{core signal})$$

$$\text{prob}(\text{core signal}) = \sum \text{prob}(\text{core signal} | \text{Contributor}) \cdot p(\text{Contributor})$$

② Decision to use open src prod.

- ⑥ plot decision making poem & equations
- ⑦ Game theory (competition like?)

③ Candidate theory: modules available

- ① prospect theory (loss model)
- ② multi stage decision making

③ social learning

④ Bayes model?

⑤ flat firm decision making (versioning)  $\rightarrow$  policy

⑥ search theories (fix sample size, sequential)

⑦ advertising, signaling

① policy  
② signaling

④ what info set available?

① depth of review  $\rightarrow$  information seeker (first paper scratch)

② credibility of reviewer

③ type of consumer:
 

- ① CNF: consult but not follow
- ② NC: not consult: since have more info to process
- ③ CF: consult & follow prod recomm

⑥ intensity of prod rev.

entities:

- ① Risk aversion
- ② product category
- ③ product attribute
- ④ search cost: navigation
- ⑤ Business model: firm related

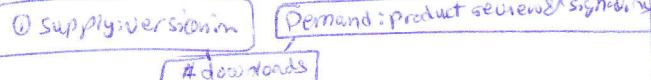
two main related papers

- ① Shi, Yang 2012
- ② NYU paper
- ③ Monic 2012
- ④ Bhargava, Chaudhury (Courses)
- ⑤ Kim 2010

Math to model your own theory

Theoretical framework: architecture

two sides



idea  $\rightarrow$  use the literature here to create research proposal  
for Google exam

\* \* \* \* \* intuition, ① [theory] \*

Corresponding

popularity context

- ① price  $\rightarrow$  stars (as indicator of cost & usage)
- ② credibility  $\rightarrow$  variance of stars
- ③ versioning  $\rightarrow$  like markdown shock (Best response)
- ④ time as variable
- ⑤ segmentation of ① price = stars  
② credibility
- ⑥ sequential search of products & reviews
- ① restrictive website (lower search cost)  $\rightarrow$  implication of structure
- ② add new browsing for reviews (search)

① proposed list of theories to explain means:

① often used with (theory?)

② part of collection (theory?)

③ other by this author (theory?)  $\rightarrow$  popularity # users

④ Tags (theory)  $\rightarrow$  ⑬ from which channel?

⑤ Category (theory)  $\rightarrow$  (World Series)

⑥ Featured (theory?)  $\rightarrow$  in first page of categories

⑦ business model (theory)

⑧ age, tenure & reviewer (theory?)

⑨ # reviews of reviewer (theory?)

⑩ Avg rate of review (Our estimator vs. understanding)

⑪ is reviewer developer? (theory?)  $\times$  popularity of developer plug in

$\rightarrow$  ⑫ platform, language, application, user, download, status

proposed category  $\rightarrow$  ① web development

- ② Condition on most popular & featured
- ③ reported

Result

- No direct marketing theory Except those papers for tag, and often used

$\Rightarrow$  find computational processes that are currently used & include customer perspective for profit maximization best response

idea

- the same way that post purchase affects reviewing behavior
- reviewing consumption affects download behavior (Meerschweid 2012) decision to download [like household production]

Data

- evolution is available from start but need method to screen  $\rightarrow$  not difficult (JavaScript)  $\Rightarrow$  all available on one page

challenge products not independent & may be purchased together

explain

- ① Download (BH)
  - ② Share (BH)
  - ③ Source (BH)
  - ④ Application
  - ⑤ Langauge (BH)
  - ⑥ Addon status (BH)
- two observable shocks:
- ① own version
  - ② platform version
  - ③ learning boosters

model

- ① prob of finding a fault (exp)
- ② hazard of time bias versions.

Data

- two groups of often used with products

How to solve simple: transform/translate  
know to what you know/have (side by side)  
② limit & concrete problem ③ having even wrong goal is more efficient than not having any (e.g. eye to search)

## Summer Project ideas

Speed is important  
by conditioines

intuition

- ① Core sha Yang's paper
- ② BLP model
- ③ prospect theory of different response
- ④ observable versioning shock on supply side process  
based on market (like Genc's paper)  $\Rightarrow$  Data Reuse
- ⑤ poisson download process (?) (visit)
- ⑥ mixture model (what signal to consider)

e.g.

① availability
② segmentation
③ two utilities
④ mark down time
⑤ mark down Depth

Next Step

- ① write utility using those papers (Deliverable)
- ② write likelihood using those papers
- ③ find cov's explaining + theory
- ④ solve problem like math problem
- ⑤ teach what you learn (multiple summary)
- ⑥ write fiction novel

## priorities

- ① Data (① model of Fairman & prospect) (② what affect?) (decision to download)
- ② Theory (e.g. model of Fairman & prospect) (recall Noris adv paper)
- ③ Decisions & what will affect them (room)
- ④ Hypothesis to check & theory Behind
- ⑤ integration of components (story)
- ⑥ simulation of Best response
- ⑦ Divide data into two parts & check prediction

Contribution

- ① Rate of Company is affecting each variable  
e.g. feature products, classification (variance), ...

② problem of endogeneity & instrument

## Keywords

- ① marketing, MIS
- ② Decision making process (experience good)
- ③ product review, social learning

## two types of search

- ① Horizontal
- ② Vertical
- ③ targeted for module

Experiencess

- ① university website is much better to find src's  
since it checks ESSCO, MBSQ, JMR, MS, ...
- ② TEP
- ③ method: ① quick abstract ② math

## Theories

- ① is key
- ② is about process (just like software methodology)
- ③ organizes thought
- ④ simplifies things
- ⑤ make things quick, efficient, time reduction
- ⑥ rationalizes tree of solution (Foc.)
- ⑦ helps you to not get lost
- ⑧ best response, durability max, profit max, cost min, rents
- ⑨ modular thinking

## Decision?

- Same problem in Big Data
- Price, promotion, Display Feature → Store level & household
- People type? → Searcher  
Non searcher  
unobservable → Theory
- what theory in experience good?

Time series

- Version time
- Downloads & two
- # stars

What likelihood?

- $p(\text{type})$
- Gamma
  - Exponential
  - Beta
  - probit, logit

selection

Decision of developer:

when to respond to reviews

problem) Data lack of Demand time series for the rest of products

Decision of customer

Stars as reputation system

- threshold that customer changes his mind about product
- (unobserved)

Good Category

Free development

Plan A

5 products download count

instruments could be download of other Plugins

→ Simply define reputation elasticity  
rather than price elasticity: # stars on →

# downloads

Independent shock

Questionable Combine with time series

Plan B

or even simply just run time series on download & stars

Step: Translation

even wrong code is good since it is complex & he has to debug

signalling theory, perfect Bayesian equilibrium

Idea: read R code understand & convert to MATLAB

Simulated  
Run Bijs code on old data  
check the Bijs & then can read data

Robust analysis!

- ① last page
- ② last two pages
- ③ last three pages
- ④ overall

stress rather than price

① Econometrics theory?  $y_{it} = \beta_{0i} + \alpha_{it} + \epsilon_{it}$ ?

② Game theory? what decision?

③ G&L model? mixture, random coefficient

④ Data analysis? fixed effect or product?

checks { ① Versioning  
② product review

[idea] ① clustering → topic  
② anthology

[Question] ① what is main goal to be curious about?  
② what is decision?   
③ how use dates? Solution comes in days

[sample answer] ① how people search product reviews?

[sample Research question] ① how developer respond to reviews  
and how this define success  
② which strategy is better? lower version - higher version  
more frequent, less frequent

[key] ① Compare your data with scanner data   
other data  
② Think about others' models also helps you to adjust  
→ how versioning by competitors affects your versioning

[?] Convert to days: and look at dummy?

[idea] ↗ heterogeneity in price of usage is a key?

[Next step:] ① write mixture model in MATLAB  
② write Bayesian (estimator) in MATLAB  
③ write selection model in Bayesian

[less learned] ⑥ key is translation → to understand

① lock to subject, screw to understand

② go forward & backward b/w model, reality  
intuition, but more weight on model &  
intuition

③ when people are intelligent they have  
practiced more & ruled out problems & know  
them (e.g. structural models)

modeling:  $u_t = \rho u_{t-1} + \varepsilon_t$

→ mixture: # obs per household is not important  
= even one could help

Task list

- ✓ ① # write normal BLP in MATLAB & Get same results
- ② write Bayesian in MATLAB & Get same results
- ③ Run Code & Download data
- ④ write time series Bayesian in MATLAB
- ⑤ run time series on download data
- ⑥ write mixture model in MATLAB
- ⑦ run mixture on signaling str & MATLAB

main trick: write modular and if not work  
just submit module & result of normal  
BLP



Date extraction "on\_n" n n n ✓

- Effect of release on product success

$$\text{type}_i = \frac{e^{v_i}}{1 + e^{v_i}}$$

$v_i \rightarrow$  # reviews  
activeness in reviewing others product

**Assump!** today is equilibrium  
everybody thus made Best choice

**G** - how model best response? to Bug?  
- how identify Bug is found?

**Short Answer** check how stars evolve?  
**Curves**

**Task** → Date Refinement → first get dates  
→ 2nd ~~put it~~ condition in excel & check how executes

Ideas → Dummy & Versioning → Higher Exposure

## Activity list

① website procen & data audit: 1 day

② Gonca paper and model: 0.5 day

③ Hartonen paper: 0.5 days

④ BLP audit: 0.5 day

⑤ text mining of ling pipe  
Word net 1 day

⑥ modeling, significance, unobservable 1 day

## Next step

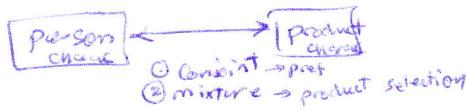
- Download and extract

- { ① Versioning info (Date, Version, topic)
- { ② Review (Date, Version, Content, Person)
- ③ all person's review for reviewers
- ④ Download data for one plugin

## First priority

- how time to solve bug will affect marketing success  
measure: # downloads

[lesson learned] - degree of freedom of system is decision making controls



## method strategy

① Framework fit

② interdisciplinary nice

## problems

- ① Good data (one layer unobservable) (Sci) aggregate demand
- ② Cool model (Combination, interdisciplinary) (Sci) aggregate demand
- ③ significance & implication for decision making (Sci) Bias? ② Good questions!
- ④ Good Game theory behind! (Sci) best response?

## idea

- ① what problem to solve first as developer, prioritize?
- ② which product review is more valuable to consider? Best response
- ③ How timely (biased)? Content of review is more important than # of stars
- text mining

## Logit problem

- ① consumer choices? (II) ← (III) unobserved
- ② whether as developer I have to be active reviewer?

[types] ① those only stars to date  
② those who read content

Complementary tools (why?)  $\rightarrow$  intuition

① wordnet  $\rightarrow$  java interface

② Yago

2 main panel Data

- ① Reviewing  $\rightarrow$  person # of reviews
- ② Versioning, review time

search  $\rightarrow$

slice of Data  
with lots of info

problem:

Download

① not exist

② aggregate demand

,

① product category selection  
(narrow down & simplify)

② Granular to product

③ one product  $\rightarrow$  effect of its version  
& competitor's entrance & leaving  
or usage ④ reviews

mixture ① panel

② multiple observations per item

① Collection Dummy

② used with Dummy

main question now: ① what is likelihood and model  
(hint you can use instruments)

idea:

email them and ask for stats

$\rightarrow$  help them decide better

$\rightarrow$  my contribution to open source community

Signals {  
of Quality }  
① Download: # users  
② star distribution  
③ # reviews  
④ # versions

objective: explain a behavior and predict it

Statistics May 1st  
per Household/individual (over T)

$$\frac{1}{T} \sum_{i=1}^N [q_i v_i(s) + (1-q_i) u_i(s)]$$

$$q_i = \frac{e^{v_i}}{\sum e^{v_i}}$$

$$\text{Likelihood} = \prod_{t=1}^T \frac{\pi_1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(y_t - x_t \beta_1)^2}{2\sigma^2}} I[s_t=0] + \frac{\pi_2}{\sqrt{2\pi\sigma^2}} e^{-\frac{(y_t - x_t \beta_2)^2}{2\sigma^2}} I[s_t=1]$$

→ what weighted average?

(5)

review

3,811

11243

1,285

11207

380

331

116

275

334

X 161

users

5,811,652

2,213,551

1,826,1848

1,889,185

4,921,742

1,218,912

1,213,672

1,006,915

590,552

840,096

video download helper  
Easy YouTube video

Download them all

Download Statistica

FlashGet

Flash video downloader

Microsoft.NET

FireFTP

Ant video downloader

Download Flash & video

Q: opinion leaders after usage?

type of comments

2SLS, endogeneity

Good product

more versions

more opinion leader

Dummy Developer

whether → activity

↓ unobservable

structure = theory → common knowledge

Review

version

review

succes

↳ success of review

↳ success of other reviews

mixture of reviews

success mix

- location instrument

Niche of text mining

① what decisions? strategic interactions?

② what types unobservable

③ what bias? or significance?

→ ④ what competing forces or equilibrium?

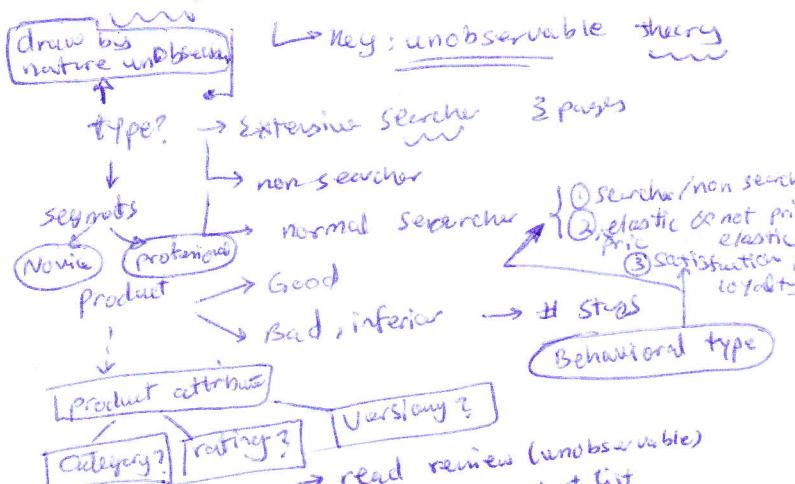
## Questions:

- ① why download variation in different days  
AreP?
- ② effect of number of version on downloads and reviews
  - ↳ indogeneity?  
Game theory behind
- ③ why some products often used with others?
- ④ how revealing stat about product affects number of reviews?
- ⑤ why popular additions are used with non popular?
- ⑥ Precision: product category
  - ↳ when to release?
  - ↳ category decision
  - ↳ work to collaboration
  - ↳ Version history
  - ↳ category: same - not same : Explain
  - ↳ Common reviewer → opinion leader
  - ↳ user centrality
  - ↳ # stars
  - ↳ positive versus negative reviews
  - ↳ # reviews
  - ↳ Same collections?

f implication

need crawler

- ⑦ Question: cool part of model?



- ⑧ type signals → read review (unobservable) posted with product list
- ⑨ unobservables → elasticity (high vs low) → type
- ⑩ searcher/non searcher
- ⑪ utility - preference
- ⑫ learning - equilibrium time - thresholds
- ⑬ relevant: ① Distance (cost) ② time cost savings

- ① opinion leaders
- ② intrinsic preference
- ③ product category only candidate → (+ downloads)?
- ④ timing effect (versioning)
- ⑤ packaging effect

Q why less popular products used with high popular?

↳ Based on usage, number of reviews, but high number of usage? / category

explain:

- ① Role of products in product category
- ② number of stars ① main ② distribution
- ③ number of product reviews
- ④ Versioning history (time) {① number ② time}
- ⑤ part of collection (3 collections)

less costly ↑ negative idea

Dependent

- ① often used with collection: 6 products
- ② # users b

unobservable, theory, contributor, lifetime review contribution

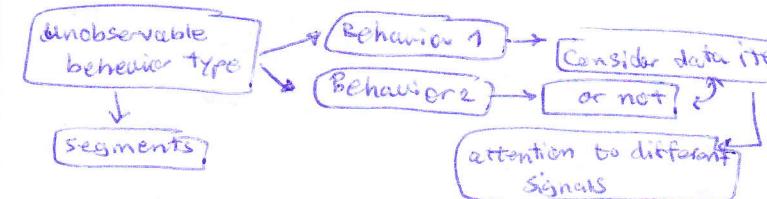
- Technical vs. social product review contribution
- ↳ free rider
- 

why interesting?

what decisions? controls

- ① packaging?
- ② engage customer review?
- ③ which product category to compete in?
- ④ release management aggregate or frequently?

④ Bayesian mixed logit-probit



⑤ Data aggregate Demand

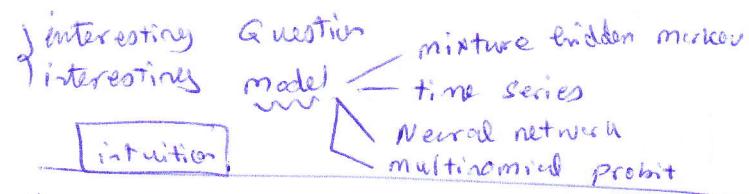
plan B  
tentative

wage

BLP in Bayesian?

↳ predeep code of Google  
run within Concur Bayesian  
& run on this data

- significance: if not taken into account → biased  
reference



- ① How download is going on
- ② is there a trend or correlation?
- ③ what to explain?
- ④ what are competing mechanisms

- ① learning
- ② - Breaks (PID)  $\rightarrow$  Policy
- ③ - signaling, prospect, asymmetry
- ④ - behavioral (trust, fairness, regret)
- ⑤ - stock piling
- ⑥ - forward looking
- ⑦ - myopic
- ⑧ - variety seeking

- ⑤ what consumer decisions?
- ⑥ state of people and how move
- ⑦ Dummy variable, fixed effect
- ⑧ Theory underpinning

- ⑨ panel data
- ⑩ why interesting?  $\rightarrow$  Curiosity
- $\rightarrow$  (2) policy implication

- ⑪ what observable?
- ⑫ what non observable?

## ⑫ multi data source

- ⑬ what is hypothesis
- ⑭ list of stakeholders:
  - ① customer
  - ② reviewer
  - ③ platform owner
  - ④ product owner

- ⑮ what decisions?  
 $\rightarrow$  what implication for policy?
- $\rightarrow$  app store
- Competing forces?

- ⑯ panel data?  $\rightarrow$  for change state mixture

## ⑰ Granger causality

## ⑱ how crawler?

## ⑲ likelihood function?

## ⑳ what is game? strategic interaction?

## ㉑ interactions?

## ㉒ objective function of platform owner?

① Releaser  $\rightarrow$  Dummy

② Nickel bias of time series

③ # stages of the game & decision parameters

- ④ matching  $\rightarrow$  deviation-indifference
- ⑤ patient & time discount
- ⑥ product diff.  $\rightarrow$  vertical differentiation
- ⑦ Coalition-Optimal  $\rightarrow$  single entities
- ⑧ search cost  $\rightarrow$  core
- ⑨ non cooperative vs cooperation
- ⑩ limited resources  $\rightarrow$  Bass model
- ⑪ ZSLS - endorsements biased
- ⑫ SOR best performance
- ⑬ multi stage entry

- ① add on status = 0
- ② play term down
- ③ downloads & usage  $\rightarrow$  down on weekends
- ④ languages the same except drop
- ⑤ users: downward trend
- ⑥ Tags - product categories
- ⑦ often used with collections
- ⑧ stats:
  - ① Download through
  - ② Open download
  - ③ download manager through

## Q. Data

- ① multi product
- ② Commenter name  $\rightarrow$  Demographic ethnicity  $\rightarrow$  like site
- ③ application life time (Bass model)
- ④ add on versions lifetime
- ⑤ panel data?
- ⑥ share of channels of download (detail page add on manager)
- ⑦ Version history

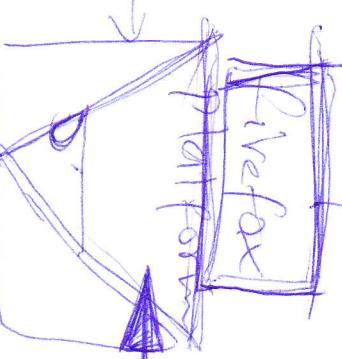
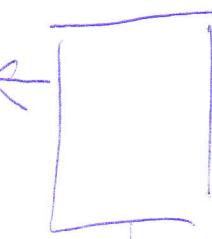
expert (in computers)

novice

competition → switch to chrome

user

developer



→ Timeseries  
→ Selection

1. Need it!

2. Suggested to me

↳ I've seen it sw

↳ Software refer

Addon

for dev characterising

↳ control

↳ download without reading Review

↳ why? → bc ~~this is~~ the cost is trivial

2. I may look at star reviews

low risk

↳ Cost of search  
↳ price → free

expert →

prior knowledge

o → review become more important

Search { narrow  
wide }

1. Is firefox the primary browser?

User { Opinion → Review bad opinion

review { Opinion → Review }

Add on { Opinion → Review + Review }

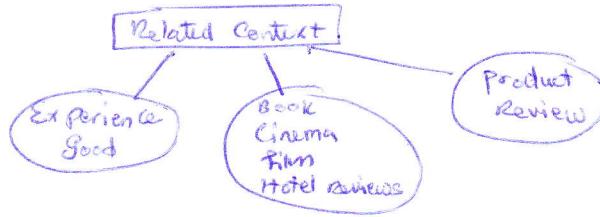
Review Log { Opinion → Review Log }

Developer → Published

→ Data to DL

## product Review literature

①



- ① Compare what?
- ② Control everything help to infer counterintuitive
- ③ different with other contexts.

## product review literature

(2)

- ① Tried and tested: The impact of online hotel reviews on consumer consideration (2009, Tourism management, Vermeulen, Steeghs)
- ② Consideration set theory (Impact of online reviews on consumer choice)
- ① review valence (positive vs. negative review)
  - includes ② hotel familiarity (well known vs. lesser known)
  - ③ reviewer expertise (experts vs. non-expert reviews)

H: exposure to online reviews enhances hotel consideration in

Consumers:  
positive : improves attitude positive & Neg: increase awareness

$A = [a_{ij}] \rightarrow$  # sit

$s_i = (s_i^1, \dots, s_i^n) \log(s_i)$  per c.  $\rightarrow$  how many sits

$R_t = (R_t^1, \dots, R_t^n)$

per t, site

(1) how many taken out  
diff. Reserves

remove index

1  
2  
3  
4  
5

simply

Overbook

no over

Cert. if not

$F_p(r) \rightarrow$  distri.  $R_p(r)$  finite max

(2) API  $\rightarrow$  E  $\rightarrow$  Src - add on msr  
BW  $\rightarrow$  search  
BR - collection

most pop: C + Y + AM + HZ + ATK

Search  $\rightarrow$  C + W + AT + I + J + Q + AA  
H + B + D + B + H + B + F +  
add on ati: AG BF primary detail

282

① search most popular

C + I + L + Q + W + AA +  
AE + AX + BD + BH + BL

Universe likes speed

Don't care result just

more than 1000 # versions

choice of not  
energetically do  
is always future

hash

precision

greed

give heart

0.1 \$B6

hashable

sort

dict

ul. 126

end 6/8/2010

User disabled: AF

User enabled: Z

sum (linux, may wind)

open mind

Solution

creativity

Translation

Guts

Quick

Data is gold

total user

disabled

Status =  
disabled  
enabled

Generalize  
= more data

reviews

① path

② # pages

Date Extractor

per

③ MLC score no blank

Observable stars

ObsStars

mean

{  
① mean ✓  
② Variance ✓  
③ # reviews ✓

3/22/2007

problem of missing dates  
old data

$\sqrt{E(X^2) - E^2(X)} \times \frac{n}{n-1}$  → ③ match Date

Versions (later)

multi col {  
linux share vs mac share vs windows share  
AVG - str, std - str  
src downloads

eye for plugin

only significant:

④ Download server down today

Complete daily push up  
⑤ Version  $\rightarrow$  output  
⑥ Spec date

last year is fine

same xls

Sum(C6: ) Shift  $\leftarrow$  End  
 $\$B6 \times 0.1$

dis/enab

last year  $\Rightarrow$  -2 days

⑦ look for date

$\frac{P6}{B6} = \frac{F6}{B6} = \frac{E6}{B6}$

win in p2

2013 ENG R6 + AR6 + BG6 + BH6 + BY6 + CD6 (length) / B6  
(same sheet)

2012 R6 + AL6 + BF6 + BG6 + BX6 + CC6

2011 N6 + AE6 + AY6 + A26 + BG6 + BV6

one leg

one URL

2013

AN6 + BL6 + CE6 + CJ6 + T6  
Q6 + AJ6 + BD6 + BE6 + BF6 + CA6

Date Extractor

Date Extractor

Stars  $\rightarrow$  Stars output

Orig Date  $\rightarrow$  Date output

Completdates  $\rightarrow$  ObsStars

①

first row empty

6

→ Right-left-enter

→ Control range

for download

spc date first

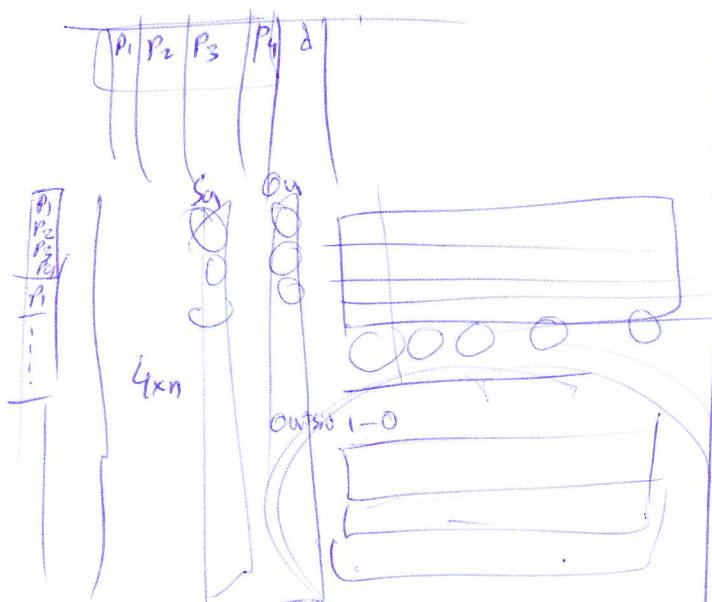
$$\underline{(\alpha_i, \beta_i)} \sim (0, \Sigma)$$

$$(\alpha_i, \beta_i) \begin{bmatrix} i \\ x_i \end{bmatrix} = \underline{\underline{v_i}}$$

$\underline{\underline{v_i}}$  means

$$\begin{array}{l} \text{cholesoc}(\Sigma) \\ \text{unions} \\ \text{P} \\ \text{S} \Rightarrow \underline{\underline{Z}} \Rightarrow \underline{\underline{S}}_{jt} \Rightarrow \underline{\underline{\zeta Z}}^{\top} (\underline{\underline{Z}} \underline{\underline{Z}}^{\top})^{-1} \end{array}$$

✓ 15

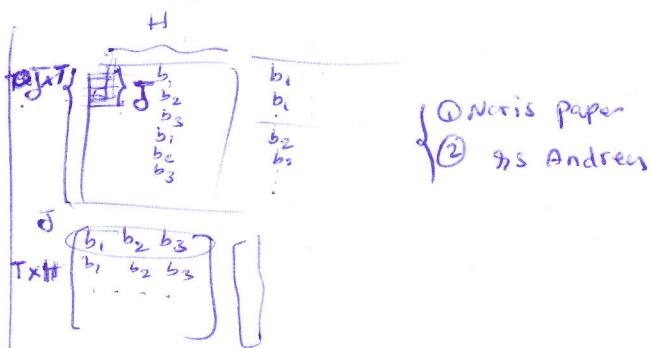


$$\text{Logist} = p = \frac{e^{X'\beta}}{1 + e^{X'\beta}}$$

$$\Rightarrow p + pe^{x' \beta} = e^{x' \beta} \overset{!}{=} e^{x' \beta} - p$$

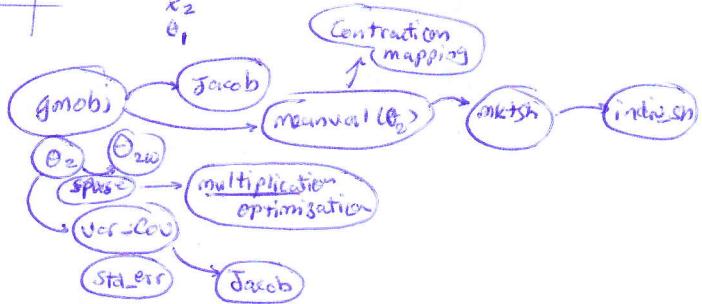
$$\text{err} = y - x\beta$$

$$\text{Varianza} = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$



$$18000 \text{ f} (300 \times 50) = T \times H$$

$$R^2 = 1 - \frac{MSE_{\text{res}}}{MST} = \frac{(y_{\text{obs}} - \hat{y}_{\text{pred}})^2}{S_{\text{res}}^2}$$

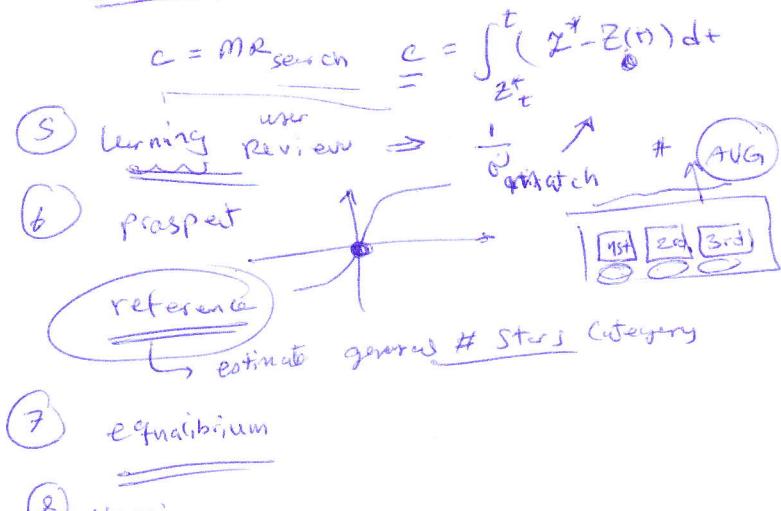
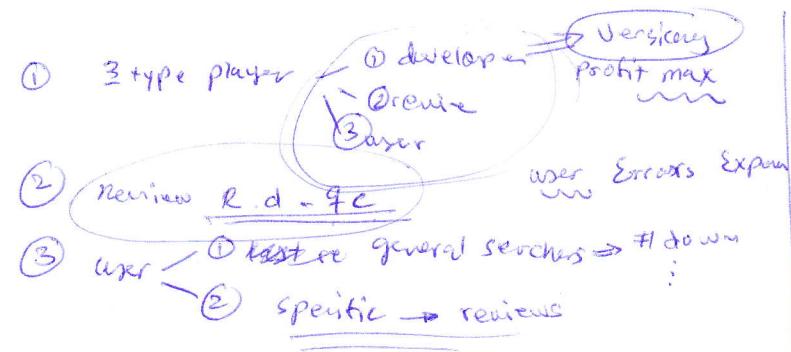


Ind-sh: indiv prob. of choosing each Brand  
mkt-sh: mkt shr for each prod.  
meanval: mean utility level

## List of hypothesis's

- 1 Consumer's variance of Star rating will reduce over time
  - 2 Learning ~~with~~ rate will decrease over time
  - 3 At the beginning of life cycle of product learning is more effective than the later phases
  - 4 Quick versioning will increase the product downloads
  - 5 Time between versioning decreases as number of ~~positive~~ negative product reviews increases
  - X ⑥ whether consumers learn Bayesian from product reviews of experience goods
  - ⑦ whether quick versioning is a good idea
  - ⑧ whether # tags affect consumer's decision by reducing search cost
  - ⑨ negative product reviews will harm usage & downloads more at the beginning of prod. life cycle than the end.

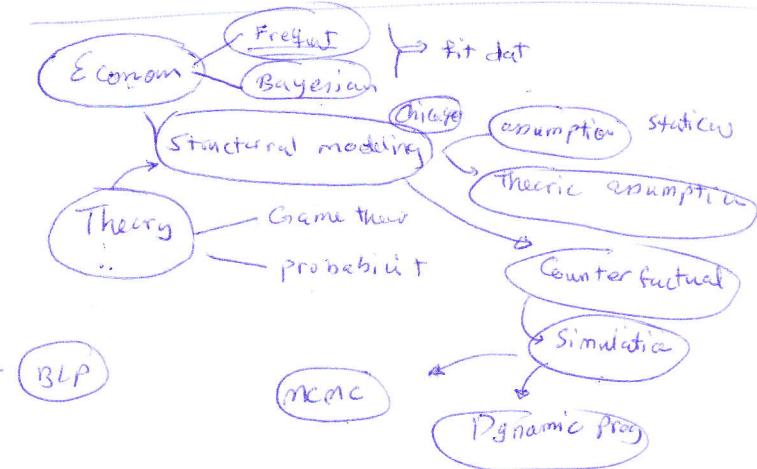
- (10) Consumers learn more about negative product reviews than positive product reviews.



① sequential decision Review  $\rightarrow$  user  $\rightarrow$  Reviewer

② extra cost of feedback from somewhere else  $\rightarrow$  but cost

③ the 3 test prod review impact



- ① developer selects time of version (b/w) whether to version pummery
- ② explain # releases developers. ③ cost of versioning opportunity cost = # plug-in developed
- ④ # total downloads
- ⑤ # stars
- ⑥ Binary? hazard?
- Developer Question: what other information to take into account?
- ⑦ like requires system of operating system?
- ⑧ or like economic theory?
- $c = M \mathbb{E}_{\text{search}} \quad c = \int_0^T (\mathbb{E}[Z] - Z(t)) dt$
- ⑨ learning user review  $\Rightarrow$   $\frac{1}{t} \uparrow$  # AVG
- ⑩ prospect reference estimate general # Stars Category
- ⑪ equilibrium
- ⑫ Version
- ⑬ sequential decision Review  $\rightarrow$  user  $\rightarrow$  Reviewer
- ⑭ extra cost of feedback from somewhere else  $\rightarrow$  but cost
- ⑮ the 3 test prod review impact
- ⑯ daily: specific version
- $p(D=1 \text{ or } c) = \frac{\exp(\alpha_i + \beta_i d_j + \gamma_i n_{dj} + \delta_i t_{sj})}{1 + \exp(\dots)}$
- ⑰ Dynamic programming? what is probabilistic?
- what is Expected rather than real value?
- probability of the same error or another product review in the next period (how mainstream or niche the error is, how effective the response is (at Cons. to neg prod rev.))
- how estimate this prob? (1) # users (2) # stars
- (3) # positive reviews on current version
- = assume correct expectation
- $u_{ijt} = \alpha_i + \beta_i d_j + \gamma_i n_{dj} + \delta_i t_{sj} + \epsilon_{ijt}$
- $u_{jto} = \mathbb{E}[u_{ijt+1} | \max\{u_{ijt}(s_{t+1}), u_{jto}(s_{t+1})\}]$
- $M_{j,t+1} = g(u_{j,t}, s_{t+1})$
- $u_{ijt} = \alpha_i + \beta_i d_j + \gamma_i n_{jt} + \delta_i t_{jt} + \epsilon_{ijt}$
- $u_{j,t}$
- Sha Yang paper is individual level
- I want to do it in aggregate form
- how? how high level estimate of # downloads?

Q6 + R6 + AF6 + A06 + AV6 + BM6

V6 + W6 + AI6 + AS6 + A26 + BG6

V6 + W6 + AF6 + AS6 + AY6 + BO6

Q6 + S6 + AF6 + Q6 + AV6 + BN6

J6 + W6 + K6 + AT6 + BA6 + BSG

S6 + T6 + AF6 + A06 + AU6 + BM6

L6 + AB6 + AS6 + AT6 + BI6 + BP6

Q6 + R6 + AF6 + A06 + AT6 + BJ6

Start simple

- ① Comment should be opened
- ② wait for loading of twitter timeline
- ③ sequential file name

- ① first pilot for one

- ② spec date problem  $\Rightarrow$  full date (version)

- ③ weekly aggregation  $\xrightarrow{\text{stays}}$  scratch sale trend

- ④ cross sectional search of these people  
(race, gender, ...)

so  $\times$  > 100  
people      observations

- ⑤ dummy of whether post exists &  
AVG based on that weekly &  
dummy of week creation

- ⑥ # Posts per week

- ⑦ prepared: UGC  $\rightarrow$  {  
 ① tag  
 ② title # words  
 ③ time of the day  
 ④ day of the year  
 ⑤ # pages
 }

- Responses {  
 ① Facebook  
 ② Twitter  
 ③ G+  
 ④ LinkedIn  
 ⑤ Commute
}

Control topic

② life cycle

③ Good will creation during time