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# Product review, an insight about consumer search

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Data and Defnitions

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Frequentist Binary Probit

Bayesian Binary Pro

### Data and Definitions

### Data

- Firefox Download them all plug in product reviews for one year (365 days)
- Number of of product reviews availabe: 1212
- Number of categories available 20
- Variation of downloads between 12,000 to 26,000 per day
- Stem of words used by reviewers: 2603 stems categorized by human reviwer

### Notation:

- $\Psi$  Word category matrix [2603  $\times$  20]
- Θ Review word matrix [1212 × 2603]
- $\Omega = \Theta * \Psi$  Review category matrix [1212 × 20]

### Data and Defnitions

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Bayesian

Frequentist

Bayesian

### Data and Definitions cont.

### List of categories:

- Information source, complement products, alternative products, experience, lack of experience
- usage, product attribute, product human interaction, selection criteria
- Cost (time and effort), Terminology, positive valance, negative valance, comparison
- Social network, feeling intensity, uncertainty, politeness, broad, narrow

### Model

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- Model 1: Effect of review attributes on download count
  - $D = \beta * \Omega + \Sigma$
  - where D is number of daily download vector
- Variation of Model 1
  - Frequentist regression
  - poisson regression
  - Bayesian regression
  - Tobit regression
- Model 2: Effect of review attributes on number of star selection
  - $S = \beta * \Phi + \Sigma$  where:
  - S is number of stars selected
  - Φ is attribute of the review (in term of categories)
  - Σ would have normal error term
  - Model would be Ordinal Probit

### Model

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Model cont.

- Model 3: Effect of review attributes on selection of each star level
  - $S_i = \beta * \Phi + \Sigma$  where:
  - S<sub>i</sub> is whether i star is selected
  - Φ is attribute of the review (in term of categories)
  - ullet  $\Sigma$  would have be normal or Gambel error term
  - Model: both binary probit and binary logit is checked

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Result of Normal regression

Variable	Estimate	Std. Error	Pr(> t )
(Interc.)	1.939e+04	2.040e+02	i 2e-16 ***
Info Src	1.215e+04	3.781e+03	0.001436 **
complement	2.041e+03	4.664e+02	1.61e-05 ***
substitute	-3.915e+03	1.164e+03	0.000855 ***
experience	1.784e+03	1.207e+03	0.140302
Naive	-2.602e+03	2.557e+03	0.309565
Usage	-3.996e+02	1.317e+02	0.002597 **
Prod. attrib	1.107e+01	2.194e+02	0.959810
P. intrection	-3.796e+27	3.587e+27	0.290583
Sel. Crit.	-3.904e+03	1.172e+03	0.000961 ***

Signif.codes: 0 \* \* \* 0.001 \* \* 0.01 \* 0.05.0.11s

Result of Normal regression

Result of Normal regression cont.

Variable	Estimate	Std. Error	Pr(> t )
Cost	-1.637e+04	2.178e+03	4.93e-13 ***
Terminology	-2.225e+03	3.875e+02	2.07e-08 ***
Positive	5.483e+01	2.205e+02	0.803747
Negative	7.713e+02	3.121e+02	0.013959 *
Comparison	3.178e+03	1.303e+03	0.015273 *
Social NW	-4.046e+03	8.172e+02	1.16e-06 ***
Extreme fl.	-6.964e+02	3.573e+02	0.052117 .
Uncertainty	-2.343e+02	9.585e+02	0.806995
Politeness	-1.079e+04	7.862e+03	0.170868
Broad	4.218e+02	1.099e+03	0.701423
Narrow	1.333e+02	8.181e+01	0.104270

*Signif.codes*: 0 \* \* \* 0.001 \* \*0.01 \* 0.05.0.11s

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Bayesian Ordinary Probit

Frequentist Binary Probit

Bayesian Binarv Prol Result of Normal regression cont.

DF	344	
$R^2$	0.4641	
Adjusted $R^2$	0.4329	
p-value	< 2.2e - 16	

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### Poisson Regression

Variable	Estimate	Std. Error	Pr(> t )
(Interc.)	9.874e+00	1.355e-03	; 2e-16 ***
Info Src	6.878e-01	2.526e-02	; 2e-16 ***
complement	1.112e-01	3.108e-03	; 2e-16 ***
substitute	-2.130e-01	7.821e-03	; 2e-16 ***
experience	1.020e-01	7.977e-03	; 2e-16 ***
Naive	-1.469e-01	1.703e-02	; 2e-16 ***
Usage	-2.169e-02	8.725e-04	; 2e-16 ***
Prod. attrib	-7.314e-04	1.466e-03	0.61799
P. intrection	-2.150e+23	2.357e+22	i 2e-16 ***

Signif.codes: 0 \* \* \* 0.001 \* \*0.01 \* 0.05.0.11

Three Fisher scoring iteration

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Poisson Regression

Poisson Regression cont.

			- ( )
Variable	Estimate	Std. Error	Pr(> t )
Sel. Crit.	-2.128e-01	7.879e-03	; 2e-16 ***
Cost	-8.865e-01	1.461e-02	; 2e-16 ***
Terminology	-1.229e-01	2.591e-03	; 2e-16 ***
Positive	3.737e-03	1.467e-03	0.01085 *
Negative	4.214e-02	2.090e-03	; 2e-16 ***
Comparison	1.640e-01	8.625e-03	; 2e-16 ***
Social NW	-2.192e-01	5.455e-03	; 2e-16 ***
Extreme fl.	-3.872e-02	2.382e-03	; 2e-16 ***
Uncertainty	-1.029e-02	6.391e-03	0.10726
Politeness	-5.791e-01	5.177e-02	; 2e-16 ***
Broad	2.031e-02	7.290e-03	0.00534 **
Narrow	7.439e-03	5.419e-04	; 2e-16 ***

Signif. codes: 0 \*\*\* 0.001 \*\* 0.01 \* 0.05 . 0.1 1 Three Fisher scoring iteration

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Regression Regression

Bayesian Gaussian Linear Regression

Bayesian Tobis

Ordinary Probit

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# Bayesian Gaussian Linear Regression

Variable	Mean	SD
(Interc.)	1.9e+04	0.32
Info Src	1.2e+04	0.32
complement	2.0e+03	0.32
substitute	-3.9e+03	0.32
experience	1.8e+03	0.32
Naive	-2.6e+03	0.32
Usage	-4.0e+02	0.32
Prod. attrib	1.1e+01	0.31
P. intrection	-3.8e+27	0.00
Sel. Crit.	-3.9e+03	0.32

Probability 
$$(s) = 0.95$$

Bayesian Gaussian Linear Regression

# Bayesian Gaussian Linear Regression cont.

Variable	Mean	SD
Cost	-1.6e+04	0.32
Terminology	-2.2e+03	0.31
Positive	5.5e+01	0.32
Negative	7.7e+02	0.31
Comparison	3.2e+03	0.32
Social NW	-4.0e+03	0.32
Extreme fl.	-7.0e+02	0.32
Uncertainty	-2.3e+02	0.32
Politeness	-1.1e+04	0.31
Broad	4.2e+02	0.32
Narrow	1.3e+02	0.32
Sigma	1231559	89247

Probability (s) = 0.95

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# Bayesian Tobit

Variable	Estimate	SD
(Interc.)	1.939e+04	2.041e+02
Info Src	1.214e+04	3.813e+03
complement	2.042e+03	4.669e+02
substitute	-3.9e+03	0.32
experience	1.779e+03	1.207e+03
Naive	-2.601e+03	2.581e+03
Usage	-3.995e+02	1.322e+02
Prod. attrib	1.007e+01	2.213e+02
P. intrection	-3.797e+27	3.609e+27
Sel. Crit.	-3.908e+03	1.179e+03

Not that much different from Bayesian regression model Probability (s) = 0.95

### Bayesian Tobit

Bayesian Tobit cont.

Estimate	SD
-1.637e+04	2.189e+03
-2.224e+03	3.891e+02
5.621e+01	2.213e+02
7.698e+02	3.120e+02
3.174e+03	1.304e+03
-4.048e+03	8.190e+02
-6.981e+02	3.584e+02
-2.341e+02	9.574e+02
-1.081e+04	7.871e+03
44.275e+02	1.100e+03
1.332e+02	8.120e+01
1.249e+06	9.608e+04
	-1.637e+04 -2.224e+03 5.621e+01 7.698e+02 3.174e+03 -4.048e+03 -6.981e+02 -2.341e+02 -1.081e+04 44.275e+02 1.332e+02

Not that much different from Bayesian regression model Probability (s) = 0.95

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# Bayesian Ordinary Probit

Variable	Estimate	SD
(Interc.)	2.4602	0.0861
Info Src	0.0249	0.2070
complement	0.0334	0.0402
substitute	0.0205	0.1367
experience	0.0058	0.0705
Naive	0.1426	0.2439
Usage	-0.0744	0.0167
Prod. attrib	-0.0725	0.0301
P. intrection	-0.3579	0.4702
Sel. Crit.	-0.0649	0.2166

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### Bayesian Ordinary Probit cont.

Variable	Estimate	SD
Variable		
Cost	0.7268	0.3572
Terminology	0.1061	0.0705
Positive	0.2215	0.0326
Negative	-0.0881	0.0255
Comparison	-0.0509	0.0923
Social NW	0.0279	0.0904
Extreme fl.	0.0910	0.0438
Uncertainty	-0.1971	0.0938
Politeness	0.5938	0.3750
Broad	-0.2004	0.1027
Narrow	-0.0038	0.0072

Bayesian Ordinary Probit

# Bayesian Ordinary Probit cont.

mean	STD
0.00	0.000
0.33	0.045
0.86	0.071
1.78	0.079
	0.00 0.33 0.86

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# Frequentist Binary Probit

Variable	Estimate	SD	Pr(> z )
(Interc.)	-0.933384	-16.468	i 2e-16 ***
Info Src	0.266610	0.258385	0.3021
complement	-0.031706	0.046578	0.4961
substitute	0.076687	0.153450	0.6173
experience	0.107060	0.081933	0.1913
Naive	0.014478	0.260034	0.9556
Usage	0.091107	0.021076	1.54e-05 ***
Prod. attrib	-0.030762	0.036012	0.3930
P. intrection	-0.594659	0.609818	0.3295
Sel. Crit.	-0.420550	0.298737	0.1592

Signif.codes: 0 \* \* \* 0.001 \* \*0.01 \* 0.05.0.11

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Frequentist Binary Probit

### Frequentist Binary Probit

Variable	Estimate	SD	Pr(> z )
Terminology	-0.116154	0.083958	0.1665
Positive	-0.174933	0.036411	1.55e-06 ***
Negative	0.014374	0.030931	0.6421
Comparison	-0.104262	0.114742	0.3635
Social NW	-0.170967	0.105617	0.1055
Extreme fl.	0.087655	0.049576	0.0770
Uncertainty	0.218757	0.111400	0.0496 *
Politeness	0.244508	0.435486	0.5745
Broad	-0.035015	0.125350	0.7800
Narrow	0.011943	0.008273	0.1488

Signif.codes: 0 \* \* \* 0.001 \* \*0.01 \* 0.05.0.11

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### Bayesian Binary Probit

Estimate	SD
-0.9339	0.0559
0.3099	0.2801
-0.0330	0.0456
0.0607	0.1546
0.1075	0.0821
-0.0088	0.2680
0.0934	0.0202
-0.0315	0.0360
-0.6773	0.6010
-0.4534	0.3166
	-0.9339 0.3099 -0.0330 0.0607 0.1075 -0.0088 0.0934 -0.0315 -0.6773

Somehow similar to frequentist estimate

Bayesian

### Bayesian Binary Probit

Variable	Estimate	SD
Cost	-0.8793	0.5247
Terminology	-0.1181	0.0835
Positive	-0.1795	0.0368
Negative	0.0139	0.0289
Comparison	-0.1134	0.1137
Social NW	-0.1761	0.1048
Extreme fl.	0.0891	0.0508
Uncertainty	0.2204	0.1115
Politeness	0.2663	0.4254
Broad	-0.0353	0.1237
Narrow	0.0114	0.0084

Somehow similar to frequentist estimate

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# Frequentist Binary Logit

Variable	Estimate	SD	Pr(> z )
(Interc.)	-1.54729	0.10058	i 2e-16 ***
Info Src	0.42794	0.44572	0.3370
complement	-0.06649	0.08214	0.4182
substitute	0.16701	0.26707	0.5318
experience	0.19751	0.13781	0.1518
Naive	0.05007	0.45324	0.9120
Usage	0.15809	0.03646	1.45e-05 ***
Prod. attrib	-0.06275	0.06278	0.3175
P. intrection	-1.22210	1.15394	0.2896
Sel. Crit.	-0.67191	0.53827	0.2119

*Signif* .codes : 0 \* \* \* 0.001 \* \*0.01 \* 0.05.0.11

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# Frequentist Binary Logit

Variable	Estimate	SD	Pr(> z )
Cost	-1.18657	0.84149	0.1585
Terminology	-0.20762	0.15033	0.1673
Positive	-0.30409	0.06622	4.39e-06 ***
Negative	0.02858	0.05400	0.5966
Comparison	-0.19581	0.20370	0.3364
Social NW	-0.32325	0.18751	0.0847
Extreme fl.	0.15999	0.08616	0.0633 .
Uncertainty	0.38933	0.18779	0.0382 *
Politeness	0.45152	0.73675	0.5400
Broad	-0.06837	0.21904	0.7549
Narrow	0.02104	0.01399	0.1326

Signif.codes: 0 \* \* \* 0.001 \* \*0.01 \* 0.05.0.11

# Bayesian Binary Logit

Model worked for low dimension x, but since mine had 20 variable, the code did not work.

### Conclusion

1 Bayesian is good, but it generates somehow same result as frequentist approach