

# Pointfrip Language Reference

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## Naming Conventions

<b>name</b>	the name itself
<i>name</i>	the type / the class
(?)	Uncertainties
*	Footnote / Note

## Data Types

<u>Data type</u>	<u>Syntax</u>	<u>Type identifier</u>
<i>data</i>		// General
<i>null</i>	( )	_null
<i>int*</i>	[_123]	_integer
<i>real</i>	_31.415e_123	_real
<i>string</i>	"abc"	_string
<i>ident</i>	abc <u>or</u> +-* /	_ident
<i>prefix</i>	@...	_prefix
<i>index</i>	[abc]	_index
<i>array</i>	{a b c}	_array
<i>error</i>	( <i>index_error</i> ... ..)	_error
<i>table*/dict*</i>	(a x b y c z)	// In pairs
<i>list</i>	(a ; b ; c ;)	;
<i>object</i>	( <i>ident</i> :: a x b y c z)	::
<i>turtle</i>	( <i>turtle</i> :: ... ..)	// Object
<i>combi</i>	( <i>term_combine</i> .. <i>arg</i> )	_combine
<i>monad</i>	( <i>int_act</i> ... ..)	_act
<i>bool</i>	true <u>or</u> false	// Idents
etc...		

\* note that *int*- and *dict*-literals require the constant combinator!

## Comments

*codetext* // *comment*

## Definition of Identifiers

*ident == term*

*ident ≡ term*

## Script Structure

*term definition1 definition2 definition3 ...*

## Ddot

*prop = head infix .. tail*

## Include Files

**coreimport** == "*Script1.txt*" ; "*Script2.txt*" ; "*Script3.txt*" ; ... ;

**userimport** == "*Script1.txt*" ; "*Script2.txt*" ; "*Script3.txt*" ; ... ;

corepath?

userpath?

## List/Dict Functions and Operators

*dict* = (first<sub>1</sub> infix<sub>1</sub> first<sub>2</sub> infix<sub>2</sub> ... ... first<sub>m</sub> infix<sub>m</sub>)

*list* = (element<sub>0</sub> ; element<sub>1</sub> ; element<sub>2</sub> ; ... ; )

**[ i ]** ° *list*                      --        *element<sub>i</sub>*

**head** ° *dict*                      --        *first*

**head** ° *list*                      --        *first*

First element of the list.

**head** ° *object* --

**tail** ° *dict*                      --        *rest*

**tail** ° *list*                      --        *rest*

List without the first element and first infix.

**tail** ° *object* --

**infix** ° *dict*                      --        *infix value*

**infix** ° *object*                      --

**prop** ° *first,infix,rest,*                      --        *dict*

**top** ° *dict*                      --        *first*

**top** ° *list*                      --        *first*

<b>pop</b> ° <i>dict</i>	--	rest	
<b>pop</b> ° <i>list</i>	--	rest	
<b>tag</b> ° <i>data</i>	--	typus	// als typeof
<b>tag</b> ° <i>dict</i>	--	infix value	
<b>term</b> ° <i>combi</i>	--	term value	
<b>arg</b> ° <i>combi</i>	--	arg value	
termoarg	--	term o arg	
<i>first</i> , <i>rest</i>	--	list	
Appendleft			
<b>length</b> ° <i>dict</i>	--	<i>real</i>	
<b>length</b> ° <i>list</i>	--	<i>real</i>	
<b>length</b> ° object	--		
Number of list items.			
<b>reverse</b> ° <i>dict</i>	--	<i>dict</i>	
<b>reverse</b> ° <i>list</i>	--	<i>list</i>	
<b>reverse</b> ° <i>object</i>	--		
Reverses the list items.			
<i>data</i> <b>distl</b> <i>list</i>	--	matrix	
<i>list</i> <b>distr</b> <i>data</i>	--	matrix	
<i>dict</i> ++ <i>dict</i>	--	<i>dict</i>	
<i>list</i> ++ <i>list</i>	--	<i>list</i>	
Concatenate the lists.			
<i>dict</i> <b>take</b> <i>num</i>	--	<i>dict</i>	
<i>list</i> <b>take</b> <i>num</i>	--	<i>list</i>	
Takes the first <i>num</i> elements from the list.			
<i>dict</i> <b>drop</b> <i>num</i>	--	<i>dict</i>	
<i>list</i> <b>drop</b> <i>num</i>	--	<i>list</i>	
Drops the first <i>num</i> elements in the list.			
<b>trans</b> ° <i>matrix</i>	--	matrix	
<b>transpose</b> ° <i>matrix</i>	--	matrix	
<i>num</i> <b>pick</b> <i>list</i>	--	element	
<i>num</i> <b>sel</b> <i>list</i>	--	element	
<b>last</b> ° <i>list</i> -	-		
( <i>num</i> <b>r</b> ) ° <i>list</i>	--		
<b>tailr</b> ° <i>list</i>	--	list	

**tailr** ° *dict*            --       dict

**rotl** ° *list*            --       list

**rotr** ° *list*            --       list

*list* **count** *data*       --       real

*data* **make** *num*       --       list

*list* **find** *data*       --       real

**iota** ° *num*            --       *list*

**l** ° *num*                --       *list*

Generates a list of numbers from 1 to *num*.

**iota0** ° *num*           --       *list*

Generates a list of numbers from 0 to *num*-1.

*int* **to** *int*            --       list

*real* **to** *real*        --       list

*int* **upto** *int*        --       list

*real* **upto** *real*     --       list

*int* **downto** *int*     --       list

*real* **downto** *real* --       list

**swap** ° *x,y,list*       --       *y,x,list*

## Math Functions and Operators

*int* **+** *int*            --       *int*

*real* **+** *real*        --       *real*

Addition of numbers.

*int* **-** *int*            --       *int*

*real* **-** *real*        --       *real*

Subtraction of numbers.

*int* **\*** *int*            --       *int*

*real* **\*** *real*        --       *real*

*int* **×** *int*            --       *int*

*real* **×** *real*        --       *real*

Multiplication of numbers.

*num* **/** *num*           --       *real*

*num* **÷** *num*        --       *real*

Division of numbers.

*int* **^** *int*            --       *int*

*real* ^ *real*            --        *real*

Power of numbers.

*int* **idiv** *int*            --        *int*

Integer division

*int* **imod** *int*            --        *int*

Integer modulo

**pred** ° *int*            --        *int*

**pred** ° *real*            --        *real*

Predecessor function

**succ** ° *int*            --        *int*

**succ** ° *real*            --        *real*

Successor function

**sign** ° *int*            --        *int*

**sign** ° *real*            --        *real*

Sign function

**abs** ° *int*            --        *int*

**abs** ° *real*            --        *real*

Absolute value function

**neg** ° *int*            --        *int*

**neg** ° *real*            --        *real*

**\_** ° *int*            --        *int*

**\_** ° *real*            --        *real*

Negation of a number.

**round** ° *num*            --        *int*

**round** ° *complex*    --        *int*

Rounding to an integer.

**trunc** ° *num*            --        *int*

Truncate to an integer.

**int** ° *num*            --        *real*

Integer part of the number as a real number.

**frac** ° *num*            --        *real*

Fraction part of a real number.

**float** ° *num*            --        *real*

**float** ° *complex*    --        *real*

Conversion to the real number.

*num* **roundto** *num*    --        *real*

**exp** ° *real*            --        *real*

Exponential function

<b>ln</b> ° <i>real</i>	--	<i>real</i>
Natural logarithm.		
<b>lg</b> ° <i>real</i>	--	<i>real</i>
Decadic logarithm.		
<b>ld</b> ° <i>real</i>	--	<i>real</i>
Binary logarithm.		
<b>sq</b> ° <i>int</i>	--	<i>int</i>
<b>sq</b> ° <i>real</i>	--	<i>real</i>
Square of a number.		
<b>sqrt</b> ° <i>num</i>	--	<i>real</i>
Square root of a number.		
<b>pi</b>	--	3.141592653589793
Ludolph's number $\pi$		
<b>2pi</b>	--	6.283185307179586
Scope of the unit circle.		
<b>sin</b> ° <i>real</i>	--	<i>real</i>
Sine function		
<b>cos</b> ° <i>real</i>	--	<i>real</i>
Cosine function		
<b>tan</b> ° <i>real</i>	--	<i>real</i>
Tangent function		
<b>cot</b> ° <i>real</i>	--	<i>real</i>
Cotangent function		
<b>sec</b> ° <i>real</i>	--	<i>real</i>
<b>csc</b> ° <i>real</i>	--	<i>real</i>
<b>arcsin</b> ° <i>real</i>	--	<i>real</i>
Arcsine function		
<b>arccos</b> ° <i>real</i>	--	<i>real</i>
Arccosine function		
<b>arctan</b> ° <i>real</i>	--	<i>real</i>
Arctangent function		
<i>num</i> <b>arctan2</b> <i>num</i>	--	<i>real</i>
<b>arccot</b> ° <i>real</i>	--	<i>real</i>
<b>arcsec</b> ° <i>real</i>	--	<i>real</i>

<b>arccsc</b> ° <i>real</i>	--	<i>real</i>	
<b>sinh</b> ° <i>real</i>	--	<i>real</i>	
Hyperbolic sine function			
<b>cosh</b> ° <i>real</i>	--	<i>real</i>	
Hyperbolic cosine function			
<b>tanh</b> ° <i>real</i>	--	<i>real</i>	
Hyperbolic tangent function			
<b>coth</b> ° <i>real</i>	--	<i>real</i>	
<b>sech</b> ° <i>real</i>	--	<i>real</i>	
<b>csch</b> ° <i>real</i>	--	<i>real</i>	
<b>arsinh</b> ° <i>real</i>	--	<i>real</i>	
<b>arcosh</b> ° <i>real</i>	--	<i>real</i>	
<b>artanh</b> ° <i>real</i>	--	<i>real</i>	
<b>arcoth</b> ° <i>real</i>	--	<i>real</i>	// Library "complex.txt"
<b>arsech</b> ° <i>real</i>	--	<i>real</i>	// Library "complex.txt"
<b>arcsch</b> ° <i>real</i>	--	<i>real</i>	// Library "complex.txt"
<i>real</i> <b>root</b> <i>real</i>	--	<i>real</i>	// Library "complex.txt"
<b>deg</b> ° <i>num</i>	--	<i>real</i>	
Radiant-to-Degree function			
<b>rad</b> ° <i>num</i>	--	<i>real</i>	
Degree-to-Radiant function			
<b>hex</b> ° <i>num</i>	-	<i>string</i>	
Number as hexadecimal string.			
<i>real</i> <b>mod</b> <i>real</i> -	-	<i>real</i>	
Modulo of real numbers.			
<b>sum</b> ° <i>list</i>	--	<i>num</i>	
Sum of the list items.			
<b>prod</b> ° <i>list</i>	--	<i>num</i>	
Product of the list items.			
<b>avg</b> ° <i>list</i>	--	<i>real</i>	
Average value of the list items.			
integral			

dd

**zero** ° *data*            --

**one** ° *data*            --

**half** ° *data*            --            ...            // Library "complex.txt"

## Dictionary Operators and Combinators

*dict* is a table for pattern matching treatment

*dict* = (*value0 key0 value1 key1 value2 key2 ... ...*)

### **\_super**

Key for the super dictionary.

*dict* **get** *key*            --            *value*  
Get the *value* for the *key* from a *dict*.

*dict* **put** *key,value,*    --            *dict*  
Replaces the *value* to a *key* in the *dict*.

*dict* **iget** *ident*        --            *value*  
*dict* **iget** *index*        --            *value*  
API-Get for identical keys.

*dict* **iput** *ident,value,*        --            *dict*  
*dict* **iput** *index,value,*        --            *dict*  
API-Put for identical keys.

**#ident** ° *dict*            --            *value*  
**(ident\_v)** ° *dict*        --            *value*  
Instance variable value.

**(ident := value)** ° *dict*        --            *dict*  
Substitution of an instance variable with a *value*.

*func* <- *key1 ; key2 ; ... ;*  
*func* ← *key1 ; key2 ; ... ;*  
Assign combinator, general.

*func* <- *key1 isfunc1 key2 isfunc2 ... ...*  
*func* ← *key1 isfunc1 key2 isfunc2 ... ...*  
Assign combinator, typed.

**keys** ° *dict*            --            list

**values** ° *dict*        --            list



## Boolean Functions and Operators

*bool* = **true** or **false**

**'true'** -- *bool*

Value for true.

**'false'** -- *bool*

Value for false.

*data* = *data* -- *bool*

Check for equality.

*data* <> *data* -- *bool*

*data* != *data* -- *bool*

*data* ≠ *data* -- *bool*

Check for inequality.

*data* < *data* -- *bool*

Checks whether smaller.

*data* > *data* -- *bool*

Checks whether larger.

*data* <= *data* -- *bool*

Checks whether less than or equal.

*data* >= *data* -- *bool*

Checks whether greater than or equal to.

¬ ° *bool* -- *bool*

**not** ° *bool* -- *bool*

**not** ° *int* -- *int*

NOT function

*bool* **and** *bool* -- *bool*

*int* **and** *int* -- *int*

AND operator

*bool* **or** *bool* -- *bool*

*int* **or** *int* -- *int*

OR operator

*bool* **xor** *bool* -- *bool*

*int* **xor** *int* -- *int*

Exclusive-OR operator

**isatom** ° *data* -- *bool*

Checks whether the *data* is a basic data type. (?)

**isprop** ° *data* -- *bool*

Checks whether the *data* is a triple value. (?)

**islist** ° *data*            --        *bool*

Checks whether the *data* is a list.

**isbool** ° *data*            --        *bool*

Checks whether the *data* is a Boolean identifier.

**isnum** ° *data*            --        *bool*

Checks whether the *data* is a number. Generic function.

**iszero** ° *data*            --        *bool*

Checks whether the *data* is zero. Generic function.

**ispos** ° *data*            --        *bool*

Checks whether the *data* is greater than zero. Generic function.

**isneg** ° *data*            --        *bool*

Checks whether the *data* is less than zero. Generic function.

isnil (?)

ispreg (?)

**isnull** ° *data*            --        *bool*

**isint** ° *data*            --        *bool*

**isreal** ° *data*            --        *bool*

**isstring** ° *data*            --        *bool*

**isident** ° *data*            --        *bool*

**isprefix** ° *data*            --        *bool*

**isindex** ° *data*            --        *bool*

**isarray** ° *data*            --        *bool*

**iscons** ° *data*            --        *bool*

**iscombi** ° *data*            --        *bool*

**isalt** ° *data*            --        *bool*

**isobj** ° *data*            --        *bool*

**isquote** ° *data*            --        *bool*

**isivar** ° *data*            --        *bool*

**isact** ° *data*            --        *bool*

Predicates to check the appropriate data type.

**isbound** ° *ident*        --        *bool*

**isbound** ° *prefix*        --        *bool*

Checks whether an identifier is bound.

**isundef** ° *data*            --        *bool*

Testing for `_undef`

**iscomplex** ° *complex*        --        *bool*

Checks whether it is a complex number. (?)

**ismatrix** ° *object*        --        *bool*

**isodd** ° *int*                --        *bool*

**isodd** ° *real*                --        *bool*

*object* **is** *ident*            --        *bool*

Checks whether the *ident* is the same as the class identifier of the *object*. (?)

(*ident* **hashtag**) ° *data*            --        *bool*    (?name)

## Combinators for Program Execution (?)

*combi* = (*term* **\_combine** .. *arg*)

*func\_s*

Single function evaluation

' *literal*

*literal* **k**

*literal\_q*

Constant combinator

*f* : *x*

Application                // to be used for closed and lift

*func1* ° *func2*

*func1* **o** *func2*

*func1* ° *func2*

Composition of functions.

*functional* **app** *argument*

Apply operator

*func1* , *func2* , *func3* , ... ,

Construction of lists.

*test* -> *then* | *else*

*test* → *then* | *else*

*test* -> *then* ; *else*

Condition with Alternat/Cons

*test* ->\* *func*

*test* →\* *func*

while Loop

*func* **loopif** *test*

do-while Loop

(*func* **do**)° *num*,*num*,*num*,

*functional* **for** *num*,*num*,*num*,

*list* **map** *functional*

Map operator

*(func aa)* ° *list*

*(func α)* ° *list*

Apply-to-all combinator

*list* **insl** *functional*

Insertl operator

*list* **insr** *functional*

Insertr operator

*(func \)* ° *list*

Insertr combinator

*list* **filter** *functional*

Filter operator

*(list, arg1, arg2, ...,)* **map0** *functional*

*(func aa0)* ° *list, arg1, arg2, ...,*

Combination of **aa** and **distr**, extended.

*func1 ee func2*

**ee** ° *data, data,*

Eval-Eval combinator for infix notation.

*func1 swee func2*

**swee** ° *data, data,*

Swap-Eval-Eval combinator

*(func1 eea func2)* ° *argum* -- (x ; y ; argum ;)

*(func dip)* ° *list*

*(func dip)* ° *object*

Dip combinator (stolen from Joy)

*(test try then | else)* ° *argument*

in then/else with *(testresult ; argument ;)*

*'expr step list, akku,*

*'expr times rep, akku,*

*ifnull*

*ifprop*

*data1 ?? data2* -- *data*

*(func Y)*

Y-Combinator...

<b>quote</b> ° <i>data</i>	--	func
Quote functional		
<i>func1</i> <b>comp</b> <i>func2</i>	--	func
Compose functional		
( <i>func</i> <b>any</b> ) ° <i>list</i>	--	bool
( <i>func</i> <b>all</b> ) ° <i>list</i>	--	bool

## Misc Functions and Operators

<b>undef</b>	--	<i>error</i>	
Function is defined as undefined.			
<b>id</b> ° <i>argument</i>	--	<i>argument</i>	
Identity function.			
<b>out</b> ° <i>argument</i>	--	<i>argument</i>	// *Side effect
Output for debugging.			
<i>data</i> <b>min</b> <i>data</i>	--	<i>data</i>	
<b>min</b> ° <i>data,data,</i>	--	<i>data</i>	
Minimum of two values.			
<i>data</i> <b>max</b> <i>data</i>	--	<i>data</i>	
<b>max</b> ° <i>data,data,</i>	--	<i>data</i>	
Maximum of two values.			
<b>name</b> ° <i>ident</i>	--	<i>string</i>	
Print name of an identifier.			
<b>body</b> ° <i>ident</i>	--	<i>value</i>	
The assigned <i>value</i> of an identifier.			
<b>address</b> ° <i>data</i>	--	<i>real</i>	
Address value of the triple cell.			
<b>identlist</b>	--	<i>list</i>	
List of all used identifiers. (?)			
<b>indexdict</b>	--	<i>dict</i>	
<i>Dict</i> of all index types with integers.			
<b>maxcell</b>	--	int	
<b>_reserve</b>			
Value for an unbound identifier.			
<b>_undef</b>			
Value for undefined.			

**gc** ° *argument*      --      *argument*  
Turns on the garbage collector.

## String Functions and Operators

**substring** ° *string,num,num,*      --      *string*

*string* **concat** *string*      --      *string*

*string* **&** *string*      --      *string*

Concatenates the strings.

*string* **indexof** *substr*      --      *real*

*list* **join** *sepstr*      --      *string*

*string* **split** *sepstr*      --      *list*

*string* **repeat** *num*      -      *string*

*string* **delete** *num,num,*      --      *string*

*string* **insert** *num,string,*      --      *string*

**length** ° *string*      --      *real*

Length of the string.

*string* **mid** *num,num,*      --      *string*

*string* **left** *num*      --      *string*

*string* **right** *num*      --      *string*

**char** ° *num*      --      *string*

**unicode** ° *string*      --      *real*

**trim** ° *string*      --      *string*

Trims the *string* on the left and right side.

**triml** ° *string*      --      *string*

Trims the *string* on the left.

**trimr** ° *string*      --      *string*

Trims the *string* on the right.

**upper** ° *string*      --      *string*

AnsiUpperCase of the string.

**lower** ° *string*      --      *string*

AnsiLowerCase of the string.

**capitalize** ° *string*      --      *string*

**parse** ° *string*                      --        *list*  
 Precompiles the *string* into a *list*.

**value** ° *string*                      --        *data*  
 Converts the *string* to a *data* type.

**string** ° *data*                        --        *string*  
 Converts the *data* to its text representation.

**unpack** ° *string*                      --        *list*  
 Splits the *string* into a list of individual string characters.

**pack** ° *list*                        -        -        *string*  
 Concatenates the strings in the *list*.

**timetostring** ° *real*                      --        *string*

**datetostring** ° *num*                      --        *string*

**weekday** ° *num*                      --        *num*                      (?)

## OOP

*object* = (*cap* :: *inst*)                      // Object classes

*pair* = *object* , *parameter* ,

**self** ° *pair*

**para** ° *pair*

*index* **op** *func*

*index* **swop** *func*

*index* **fn** *func*

(*object* (*index* **cb** *func*) *parameter*) ° *argum*                      --        *method* ° [0],[1],*argum*,

**cap** ° *list*                              --        ( )

**cap** ° *object*                              --        (*cap* ::)

*ident* **obj** *list*                              --        (*ident* :: *list*)

*ident* **obj** *dict*                              --        (*ident* :: *dict*)

*ident* **new** *parameter*

*object* **as** *ident* (?)                      --        *object*

**box** ° *primdata*                              --        *object*

**unbox** ° *object*                              --        *primdata*

(*func* **objdip**) ° *pair* - object

**object** == .. { ( ) ... .. }  
Object class

**list** == .. { object ... .. }  
List class

**dict** == .. { object ... .. }  
Dict class

## Monads and Effects

*monad* = (*int* **\_act** .. *dict*) // absolute  
*monad* = (*index* **\_act** .. *dict*) // relative

**it** ° *dict* -- #\_it ° *dict*  
Result of a monad action. // monad ... name (?)

#\_it

#\_self

#\_para

\_bind  
Continuation

\_eff  
Effects

*monad* >> *term* -- monad // \_bind := *term*

*int* **act** *dict* -- monad

*index* **act** *dict* -- monad

*monad* **act** *dict* -- monad

nun auch die Möglichkeit gegeben eine actbox zu bauen //bitte in engl!  
(verschachteltes Act)

*monad* **eff** *array* -- monad

*monad* **eff** *ident* -- monad

*monad* **var** *data* -- monad

*monad* **var** *dict* -- monad

(*ident* **define** *data*) ° *dict* -- monad  
//(prefix define data) ° *dict*

(*ident* **redefine** *data*) ° *dict* -- monad  
//(prefix redefine data) ° *dict*



```

(data showgraph) ° dict      --      monad      // *+ (x eff 'io)
(data showinfo) ° dict      --      monad      // *+ (x eff 'io)
(data print) ° dict         --      monad      // *+ (x eff 'io)
(string input) ° dict       --      monad      // *+ (x eff 'io)
(string input string) ° dict
(fname loadtext) ° dict     --      monad      // *+ (x eff 'io)
(fname savetext string) ° dict --      monad      // *+ (x eff 'io)
(string run) ° dict         --      monad      // *+ (x eff 'io)

quit                      --      monad

time ° dict                --      monad      // *+ (x eff 'io)
date ° dict                --      monad      // *+ (x eff 'io)
beep ° dict                --      monad      // *+ (x eff 'io)

io == .. { ... .. .. }
System effects class

```

## Runtime Errors(?)

```

error = (index _error string ; ... ..)

index error string,  --      error

fail ° argument      --      error
Use for selector signatures(?)

stop ° argument      --      error
Generally, e.g. Program termination, etc

raise ° string       --      exception
An exception is thrown.

_error == .. { ... .. .. }
Class for redirects...

// try

```

## Complex Numbers

```

complex = (complex :: real re real im)           // Library "complex.txt"

```

**i** -- (complex :: 0 re 1 im)

Square root of  $-1$

*real* **j** *real* -- complex // für schnelle Schreibweise

*real* **cval** *real* -- complex

To form a complex number from real numbers.

**re** ° complex -- real

Real part of the complex number.

**im** ° complex -- real

Imaginary part of the complex number.

*complex* + *complex* -- complex

Addition of complex numbers.

*complex* - *complex* -- complex

Subtraction of complex numbers.

*complex* \* *complex* -- complex

*complex* × *complex* -- complex

Multiplication of complex numbers.

*complex* / *complex* -- complex

*complex* ÷ *complex* -- complex

Division of complex numbers.

**zero** ° complex -- (complex :: 0 re 0 im)

**one** ° complex -- (complex :: 1 re 0 im)

**half** ° complex -- (complex :: 0.5 re 0 im)

**iszero** ° complex -- bool

**isnum** ° complex -- true

*complex* = *complex* -- bool

**conj** ° complex -- complex

**neg** ° complex -- complex

**abs** ° complex -- real

**phase** ° complex -- real // wie Arg(z)

**sq** ° complex -- complex

**exp** ° complex -- complex

**ln** ° complex -- complex // Hauptzweig

<b>lg</b> ° <i>complex</i>	--	complex	// Log10(z)
<b>ld</b> ° <i>complex</i>	--	complex	// Log2(z)
<i>complex</i> ^ <i>complex</i>	--	complex	
<i>complex</i> <b>root</b> <i>complex</i>	--	complex	
<b>sqrt</b> ° <i>complex</i>	--	complex	
<b>sin</b> ° <i>complex</i>	--	complex	
<b>cos</b> ° <i>complex</i>	--	complex	
<b>tan</b> ° <i>complex</i>	--	complex	
<b>cot</b> ° <i>complex</i>	--	complex	
<b>sec</b> ° <i>complex</i>	--	complex	
<b>csc</b> ° <i>complex</i>	--	complex	
<b>arcsin</b> ° <i>complex</i>	--	complex	
<b>arccos</b> ° <i>complex</i>	--	complex	
<b>arctan</b> ° <i>complex</i>	--	complex	
<b>arccot</b> ° <i>complex</i>	--	complex	
<b>arcsec</b> ° <i>complex</i>	--	complex	
<b>arccsc</b> ° <i>complex</i>	--	complex	
<b>sinh</b> ° <i>complex</i>	--	complex	
<b>cosh</b> ° <i>complex</i>	--	complex	
<b>tanh</b> ° <i>complex</i>	--	complex	
<b>coth</b> ° <i>complex</i>	--	complex	
<b>sech</b> ° <i>complex</i>	--	complex	
<b>csch</b> ° <i>complex</i>	--	complex	
<b>arsinh</b> ° <i>complex</i>	--	complex	
<b>arcosh</b> ° <i>complex</i>	--	complex	
<b>artanh</b> ° <i>complex</i>	--	complex	
<b>arcoth</b> ° <i>complex</i>	--	complex	
<b>arsech</b> ° <i>complex</i>	--	complex	

**arcsch** ° *complex*            --        complex

**iscomplex** ° *object*            --        bool

**complex** == .. { dict ... .. }  
Complex-class with the complex methods.

## Matrix Functions and Operators

*matrix* = (*list*; *list*; ... ;)  
*matrix* = (**matrix** :: *list*; *list*; ... ;)

// Library "matrix.txt"

**IP** ° *list*,*list*,  
*list* **IP** *list*

// Backus Turing Lecture

**MM** ° *matrix*,*matrix*,  
*matrix* **MM** *matrix*

// Backus Turing Lecture

**det** ° *matrix*                    --        real

**inv** ° *matrix*                    --        matrix

*matrix* + *matrix*                    --        matrix

*matrix* - *matrix*                    --        matrix

*matrix* \* *matrix*                    --        matrix

*matrix* x *matrix*                    --        matrix

**trans** ° *matrix*                    --        matrix        // transpose

*num* **scale** *matrix*                --        matrix        // (?) scalar

*matrix* **each** 'func                --        matrix        // (?)

**sq** ° *matrix*                    --        matrix

**zero** ° *matrix*                    --        matrix        // zeromatrix

**one** ° *matrix*                    --        matrix        // idmatrix

*num* **zeromatrix** *num*            --        matrix

*num* **onematrix** *num*            --        matrix

**idmatrix** ° *num*                    --        matrix

**ismatrix** ° *data*                --        bool

**tomatrix** ° *list*                --        matrix

*num* **like** *data*                --        *num*            // with type of *data*

**matrix** == .. { list ... .. }

Matrix-class for MM (\*), det, inv, trans, add, sub, Aij, negifodd

## Turtle Graphics

```
turtle = ( turtle :: list stack real x real y real angle  
           bool pen num color num size num brush )           // Library  
"turtlegraphics.txt"
```

*pair* = (*x* , *y* ,)

// 2pi

**initturtle**

'*turtle new* // recommended

*pair moveto turtle*

*pair moverel turtle*

*real move turtle*

*real turnto turtle*

*real turn turtle*

**penup** ° *turtle*

**pendown** ° *turtle*

*num pencolor turtle*

*num pensize turtle*

*num brushcolor turtle*

*real circle turtle*

**rectangle** ° *turtle* // rect

(*turtle (draw eff 'io)*) ° *dict* -- monad  
For drawing the turtle trail.

**#x** ° *turtle* -- real

**#y** ° *turtle* -- real

**#angle** ° *turtle* -- real

etc

Attributes of the turtle object.

**colors** == '(... ..)

#red ° *colors* for the color value red.

```
turtle == .. { dict ... .. }
```

Turtle class,

own turtle classes can also be created through inheritance.

```
(xlist (plot0 eff 'io) 0-y) ° dict      --      monad
```

**(CC0)**