

# TL;DR

This proposal presents a practical trustless Bitcoin bridge using Nillion's NMC (Nil Message Compute) protocol. The bridge leverages secure encryption, secret sharing, and cross-chain witness validation to enable the secure and decentralized transfer of Bitcoin to other blockchains.

## Background

Interoperability between different blockchains is crucial for the growing decentralized ecosystem. Trustless bridges allow secure transfers of assets and information across blockchain networks without relying on a central trusted authority. Nillion's NMC protocol provides a framework for creating such trustless bridges.

## Proposal

The proposed trustless Bitcoin bridge consists of the following steps:

1. Initial Encryption

:

- The Bitcoin secret key (  $K$  )

is encrypted using a symmetric encryption scheme (  $E = (\text{Enc}, \text{Dec})$  )

with a condition-based ciphertext (  $C$  )

dependent on a predefined condition (  $\Phi$  )

on a separate blockchain, such as Ethereum:

$$C = \text{Enc}(K, \Phi)$$

1. The Bitcoin secret key (  $K$  )

is encrypted using a symmetric encryption scheme (  $E = (\text{Enc}, \text{Dec})$  )

with a condition-based ciphertext (  $C$  )

dependent on a predefined condition (  $\Phi$  )

on a separate blockchain, such as Ethereum:

$$C = \text{Enc}(K, \Phi)$$

1. Generating Particles

:

- A One-Time Mask (OTM) is applied to the ciphertext (  $C$  )

to generate masked particles  $\{p_i\}_{i=1}^n$

:

$$p_i = C \oplus b_i \quad \text{for all } i \in [1, n]$$

where  $\{b_i\}_{i=1}^n$

are random blinding factors.

1. A One-Time Mask (OTM) is applied to the ciphertext (  $C$  )

to generate masked particles  $\{p_i\}_{i=1}^n$

:

$$p_i = C \oplus b_i \quad \text{for all } i \in [1, n]$$

where  $\{b_i\}_{i=1}^n$

are random blinding factors.

## 1. Blinding Factor Sharing

:  
• Linear Secret Sharing (LSS) is used to distribute the blinding factors  $\{b_i\}_{i=1}^n$  among a decentralized network of nodes  $\{N_i\}_{i=1}^n$

.  
• Polynomials  $f_i(x)$  of degree  $t$  are constructed for each blinding factor  $b_i$

:  
$$f_i(x) = b_i + a_1 x + a_2 x^2 + \dots + a_t x^t$$

•  $n$  shares  $\{s_{i,j}\}_{j=1}^n$  are generated for each blinding factor  $b_i$  by evaluating  $f_i(x)$  at distinct points  $x_j \in \mathbb{F}_p$

:  
$$s_{i,j} = f_i(x_j) \quad \text{for all } j \in [1, n]$$

• The shares are distributed to the corresponding nodes  $N_j$

.  
1. Linear Secret Sharing (LSS) is used to distribute the blinding factors  $\{b_i\}_{i=1}^n$  among a decentralized network of nodes  $\{N_i\}_{i=1}^n$

.  
1. Polynomials  $f_i(x)$  of degree  $t$  are constructed for each blinding factor  $b_i$ :  
$$f_i(x) = b_i + a_1 x + a_2 x^2 + \dots + a_t x^t$$

1.  $n$  shares  $\{s_{i,j}\}_{j=1}^n$  are generated for each blinding factor  $b_i$  by evaluating  $f_i(x)$  at distinct points  $x_j \in \mathbb{F}_p$

:  
$$s_{i,j} = f_i(x_j) \quad \text{for all } j \in [1, n]$$

1. The shares are distributed to the corresponding nodes  $N_j$

## 1. Particle Distribution

:

- The masked particles  $\{p_i\}_{i=1}^n$

are distributed across the decentralized network of nodes  $\{N_i\}_{i=1}^n$

.

- Each node  $N_i$

holds a single particle  $p_i$

.

1. The masked particles  $\{p_i\}_{i=1}^n$

are distributed across the decentralized network of nodes  $\{N_i\}_{i=1}^n$

.

1. Each node  $N_i$

holds a single particle  $p_i$

.

1. Witness Condition Validation

:

- Upon fulfillment of the predefined condition  $\Phi$

on the Ethereum blockchain, a witness proof  $\pi$

is generated.

- Nodes validate the witness proof  $\pi$

to initiate the reconstruction process.

1. Upon fulfillment of the predefined condition  $\Phi$

on the Ethereum blockchain, a witness proof  $\pi$

is generated.

1. Nodes validate the witness proof  $\pi$

to initiate the reconstruction process.

1. Reconstruction and Decryption

:

- Nodes collaborate to reconstruct the blinding factors  $\{b_i\}_{i=1}^n$

using the LSS shares:

$$b_i = \sum_{j \in I} s_{i,j} \prod_{k \in I \setminus \{j\}} \frac{x_k}{x_k - x_j}$$

where  $I \subseteq [1, n]$

and  $|I| = t + 1$

.

- With the reconstructed blinding factors  $\{b_i\}_{i=1}^n$

, nodes unmask their particles  $p_i$

to recover the original ciphertext  $C$

:

$$C = p_i \oplus b_i \quad \text{for all } i \in [1, n]$$

- The recovered ciphertext  $C$

is decrypted using  $\text{Dec}$

and the condition  $\Phi$

to obtain the Bitcoin secret key  $K$

:

$$K = \text{Dec}(C, \Phi)$$

1. Nodes collaborate to reconstruct the blinding factors  $\{b_i\}_{i=1}^n$

using the LSS shares:

$$b_i = \sum_{j \in I} s_{i,j} \prod_{k \in I \setminus \{j\}} \frac{x_k}{x_k - x_j}$$

where  $I \subseteq [1, n]$

and  $|I| = t + 1$

.

1. With the reconstructed blinding factors  $\{b_i\}_{i=1}^n$

, nodes unmask their particles  $p_i$

to recover the original ciphertext  $C$

:

$$C = p_i \oplus b_i \quad \text{for all } i \in [1, n]$$

1. The recovered ciphertext  $C$

is decrypted using  $\text{Dec}$

and the condition  $\Phi$

to obtain the Bitcoin secret key  $K$

:

$$K = \text{Dec}(C, \Phi)$$

## Advantages

The proposed trustless Bitcoin bridge has several advantages:

- Decentralization

: The use of a decentralized network of nodes eliminates the need for a central trusted authority.

- Security

: The encryption and secret sharing techniques ensure the confidentiality and integrity of the Bitcoin secret key.

- Cross-chain interoperability

: The bridge enables the secure transfer of Bitcoin to other blockchains, such as Ethereum, based on predefined conditions.

- Fault tolerance

: The use of Linear Secret Sharing provides fault tolerance, as the secret can be reconstructed even if some nodes are unavailable or malicious.

## Applications

The trustless Bitcoin bridge has various applications, including:

- Cross-chain asset transfers

: Enabling the seamless transfer of Bitcoin to other blockchains for use in decentralized applications (DApps) and decentralized finance (DeFi) protocols.

- Atomic swaps

: Facilitating atomic swaps between Bitcoin and other cryptocurrencies without the need for a trusted intermediary.

- Conditional payments

: Allowing for conditional Bitcoin payments based on events or conditions on other blockchains.

## Conclusion

The proposed trustless Bitcoin bridge using Nillion's NMC protocol provides a secure, decentralized, and interoperable solution for transferring Bitcoin across different blockchain networks. By leveraging cryptographic techniques such as encryption, secret sharing, and cross-chain witness validation, the bridge ensures the integrity and confidentiality of the transferred assets. This proposal opens up new possibilities for cross-chain asset transfers, atomic swaps, and conditional payments, further enhancing the interoperability and composability of the decentralized ecosystem.

[Nillion Whitepaper](#)