My problem is rather simple. I want to create a smart contract which will hold a merkle root committing it's state with internal book-keeping. Clients who interact with this contract will need to send a merkle branch on which their action is based.

Lets say that the internal book keeping consists of 1024 data-points of uint256

type.

Most obvious approach that comes to me is to use as hashing function $H \{1\}(a,b) = \frac{256(a,b)}{a}$

- , which returns unit256
- . A client who wants to prove to smart contract a data point will need to provide 640 bytes, calculated as:

2 \cdot 10 \; \textrm{levels} \cdot 32 \; \textrm{bytes} = 640 \; \textrm{bytes}

640 bytes is not terrible, but I want to make the system as gas-efficient as possible, so I'm looking to possibly use smaller hashes.

Somewhat attractive approach would be to use as hashing function H_{2}(a,b) = bytes4(keccak256(a, b))

For H_{2}

the size of the proof for merkle tree with 1024 leafs would be:

2 \cdot 32\;\textrm{bytes} + 2 \cdot 9 \; \textrm{levels} \cdot 4 \; \textrm{bytes} = 136 \; \textrm{bytes}

Which sounds much better.

So I have few questions regarding the scheme above, perhaps someone can point me to some research on the subject.

1. Is H_{2}

secure enough, can an attacker efficiently falsify a merkle branch using brute force ?

1. If H_{2}

is not secure, does anyone know what is practical minimal length of hash that can be considered secure for this problem?

1. Perhaps someone knows even better hashing function for this problem? By "better" I mean more secure and gasefficient.