In contexts where committee sizes are sufficiently large, it could make sense to use <u>Algorand</u>-style privately selected committees, in order to improve lookahead privacy to improve DoS resistance and resistance against other kinds of adaptive adversary attacks.

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Algorand-style private selection works as follows. Suppose that each validator V_i
has a private preimage C_{V_i}
(a la RANDAO), and there is a common randomness source R
; for any given proposal P
, we derive a randomness R_P
(eg. R P = H(R, C P)
, where C_P
is the proposer's
preimage). If there are in total N
validators and we want a committee of size M
, then anyone can make a signature by revealing C_{V_i}
and showing that C_{V_i} \le 2^{256} * \frac{M}{N}
. On average, M
of the N
validators will be able to do so for any given proposal, with standard deviation \sqrt{M}
and so at least M - 3\sqrt{M}
\sim99.85% of the time (and at most M + 3\sqrt{M}
99.85% of the time).
Suppose an attacker has fraction p
of proposers, and the committee threshold is \frac{2}{3} * M
; we can try to estimate the probability that a fraudulent proposal will get through for various values of p
and M
with publicly selected committees (which are guaranteed to have size exactly M
) and privately selected committees (using Poisson distributions, so assuming N
approaching infinity, values for N = 20000
are very close to the limit at N \rightarrow \infty
):
   • M = 200, p = \frac{1}{4}
: public selection safety failure 6.25 * 10^{-35}
, private selection 1.89 * 10^{-22}
   • M = 100, p = \frac{1}{4}
, public selection safety failure 1.21 * 10^{-18}
, private selection 2.75 * 10^{-12}
   • M = 200, p = \frac{1}{3}
: public selection safety failure 1.07 * 10^{-21}
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, private selection 5.64 * 10^{-13}
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•
$$M = 100, p = \frac{1}{3}$$

, public selection safety failure 6.45 * 10^{-12}

, private selection 1.90 * 10^{-7}

•
$$M = 200, p = \frac{1}{2}$$

: public selection safety failure 1.77 * 10^{-6}

, private selection 9.35 * 10^{-4}

•
$$M = 100$$
, $p = \frac{1}{2}$

: public selection safety failure 4.36 * 10^{-4}

, private selection 1.24 * 10^{-2}

In summary, private selection unfortunately does have the weakness that it nearly doubles required safe committee sizes.