

Here's the code for elliptic curve signature recovery, copied from pybitcointools, and cleaned of details that are irrelevant to our exposition

```
def ecdsa_raw_recover(msghash, vrs): v, r, s = vrs y = # (get y coordinate for EC point with x=r, with same parity as v) Gz = jacobian_multiply((Gx, Gy, 1), (N - hash_to_int(msghash)) % N) XY = jacobian_multiply((r, y, 1), s) Qr = jacobian_add(Gz, XY) Q = jacobian_multiply(Qr, inv(r, N)) return from_jacobian(Q)
```

Suppose that we feed in $\text{msghash}=0$, and $s=r*k$ for some k . Then, we get:

- $Gz = 0$
- $XY = (r, y) * r * k$
- $Qr = (r, y) * r * k$
- $Q = (r, y) * r * k * \text{inv}(r) = (r, y) * k$

Hence, the elliptic curve signature feeds out k

times the point (r, y)

, where r

and k

are values you feed in, and you specify the parity of y

via v

.

Unfortunately, the `secp256k1` precompile outputs the truncated hash of Q , and not Q itself. But you can get around that by requiring the function caller to submit Q as a witness. The extra cost of 64 bytes of data is ~ 4000 gas, so altogether you can get an ECMUL with $< 10k$ gas, under a quarter of what you need if you use the ECMUL precompile that uses the `alt_bn128` curve.

This could be used as a ghetto hack to optimize ring signatures in the EVM today, as well as other applications.