GAM modelling workshop: computer lab exercises

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Software installation

The main packages we will need are mgcv, mgcViz, qgam and mgcFam which should have been installed by doing

```
install.packages("devtools")
library(devtools)
install_github("mfasiolo/mgcFam")
install_github("mfasiolo/testGam")
```

If this worked, stop reading this section and go to the exercises. Otherwise, if install_github fails saying "Rate limit remaining: 0/60", then Plan B consists in running the code:

and then

```
# I will pass you these packages via a USB stick
install.packages("mgcFam_0.0.2.tar.gz", repos = NULL, type = "source")
install.packages("testGam_0.0.1.tar.gz", repos = NULL, type = "source")
```

If plan B fails (e.g. no internet connection), we follow Plan C (!!). I will give you a USB containing all the dependencies, then you need to run:

Assuming that this worked, we continue as in Plan B:

```
# I will pass you these files via a USB stick
install.packages("mgcFam_0.0.2.tar.gz", repos = NULL, type = "source")
install.packages("testGam_0.0.1.tar.gz", repos = NULL, type = "source")
```

GAM exercises

All the data sets we will use in the workshop should now be available in your R system. The rest of the material for the workshop can be downloaded from https://github.com/mfasiolo/workshop_BOZEN19. If you download it as a zip file and extract it, the solutions can be found in the exercises/solutions folder. You might also want to look at the files (in the R_demos subfolder):

- Extra_things.html explains few extra things you might encounter, such as offsets;
- Intro.html introduces the mgcv R package;
- mgcViz.html introduces the mgcViz R package;
- Big_Data.html introduces the Big Data methods in mgcv and mgcViz;
- gamlss.html and qgam.html introduce GAMLSS and quantile GAMs.

First session

In the first session you could try one or more of the following exercises (suggested track is ex 3 and 2, and the number of *'s indicates the difficulty level):

- 1. Retinopathy among diabetics (solution in: "Retinopathy_mgcv.html"). Simple exercise on basic GAM modelling in mgcv. *
- 2. C0₂ modelling (sol: "CO2_mgcv.html"). Featuring cyclic seasonal smooths and the dangers of extrapolation. **
- 3. Ozone modelling (sol: "Ozone_mgcv.html"). Exercise focusing on manual variable selection via p-values and residual checking, and adjusting the mean-variance relationship. *

Second session

In this session you could try:

- 4. Mackerel egg data (sol: "Mackerel.html"). Featuring 2D spatial interactions. *
- 5. Bone mineral density modelling (sol: "bone_density.html"). Featuring simple random effects. *

Third session

In this session you could try (suggested track is either 6 or 7 and then either 8 or 9):

- 6. Big GAM modelling of GEFCom14 electricity demand data (sol: "gefcom_big.html"). Featuring Big Data GAM methods and 2D tensor interactions. **
- 7. Individual electricity demand modelling (solution in: "Ind_elect.html"). Featuring Big Data GAM methods and by-customer smooth effects. **
- 8. GAMLSS modelling Body Mass Index (BMI) of Dutch boys (sol: "bmi_GAMLSS.html"). Basic exercise featuring adaptive smoothers and visual interactive model building. *
- 9. GAMLSS modelling of rent prices in Munich (sol: "Rent_munich_GAMLSS.html"). Featuring linear interactions. *

Fourth session

In this session you could try:

- 10. QGAM modelling of UK electricity demand (sol: "UKload_QGAM.html"). QGAM model-building on UK aggregate electricity demand. *
- 11. QGAM modelling of rainfall in Switzerland (sol: "Swiss_rainfall_QGAM.html"). Featuring spatio-temporal effects constructed using tensor product bases. **

1 Retinopathy among diabetics

Data frame wesdr (taken from Chong Gu's gss package) contains a subset of data from a Wisconsin study on development of retinopathy among diabetics. The following variables are provided:

- ret, a binary indicator of development of retinopathy by first follow up of study.
- bmi, the body mass index at entry to the study (between 18 and 25 is considered healthy).
- dur, the duration of diabetes, in years, at entry.
- gly, the percentage of glycosylated haemoglobin (HbA1C) in the blood (haemoglobin to which glucose has bound). 2.5-3.5% is normal for non-diabetics. 6.5% is generally considered good control for diabetics.

The aim is to model the probability of retinopathy as a function of the other variables. Questions:

- 1. Load testGam, mgcv and the data (data(wesrd)). Have a look at the relation between the different variables using pairs(wesdr) or other exploratory visualisations.
- 2. Start by fitting a logistic regression model (family = binomial), with smooth effects for duration and body mass index. Use summary and plot to verify whether the effects are strong.
- 3. Use qq.gam to get a QQ-plot of the residuals (you can set the rep argument to, say, 100 to get simulation-based reference intervals). Is the plot interpretable? Now plot the residuals against the values of wesdr\$gly, do you see any pattern?
- 4. Include a smooth effects for gly in the model formula and refit. Looks at the fitted effects and verify their significance using plot and summary. Compare the new model to the first model you fitted using AIC. Use gam.check to produce further diagnostics. Does the text suggest that the you should modify the number of basis functions used?

2 CO₂ modelling

This question is about modelling data with seasonality, and the need to be very careful if trying to extrapolate with GAMs (or any statistical model). The data frame co2s contains monthly measurements of CO₂ at the south pole from January 1957 onwards. The columns are co2, the month of the year, month, and the cumulative number of months since January 1957, c.month. There are missing co2 observations in some months.

- 1. Load mgcv and the data with library(gamair); data(co2s)
- 2. Plot the CO₂ observations against cumulative months.
- 3. Fit a Gaussian additive model with a smooth effect for c.month, using the gam function. Use the cr basis, and a basis dimension of 100.
- 4. Obtain the predicted CO₂ for each month of the data, plus 36 months after the end of the data, as well as associated standard errors. Produce a plot of the predictions with twice standard error bands. Are the predictions in the last 36 months credible? NB: to produce the plot you have to write your own code, mgcv does not produce such plots.
- 5. Fit the model $\mathbb{E}(CO_2) = f_1(c.month_i) + f_2(month_i)$ where f_1 and f_2 are smooth functions. Use a basis of dimension 50 for f_1 and a cyclic basis for f_2 . In the gam call, you will need to set argument knots to list(month=c(1,13)) to make so that that the effect of January is the same as January, not that December and January are the same!
- 6. Repeat the prediction and plotting in question 4 for the new model. Are the predictions more credible now? Explain the differences between the new results and those from question 4.

3 Ozone modelling

Data frame ozone contains daily(ish) ozone measurements over Los Angeles (03, ppm), along with:

vh the height at which the atmospheric pressure is 500mb, in metres.

wind the wind speed (reported as miles per hour, but this seems improbable).

humidity (usual % scale).

temp air temperature (Fahrenheit).

ibh the inversion layer base height in feet.

ibt the inversion base temperature (Fahrenheit).

dpg 'Dagget air pressure gradient' (mmhg).

vis visibility in miles.

doy Julian day, where 1 is Jan 1 1976.

The aim is to build a GAM model to explore the relationship between ozone and the other variables. Questions:

- 1. Load testGam and the data (data("ozone")), and use something like pairs(ozone) to have a look at it.
- 2. Load mgcv and use gam to fit a Gaussian GAM with 03 as response, where log(E(03)) is given by a sum of smooth functions (e.g. s(wind)) of each of the predictors. You will need to use the log-link, which requires using the argument family=gaussian(link=log) in the call to gam. Plot the fitted effects using plot.
- 3. Check the model residuals using the gam.check functions. Do you see any residual pattern when you plot the residuals against the fitted values or linear predictor?

- 4. Refit the model using a Gamma as response distribution (Gamma(link=log)), and re-check the residuals. Does the residual distribution look better?
- 5. Fit an alternative model where you are using the identity-link (Gamma(link=identity)). Does a model with an additive (i.e. identity-link) structure do better than that with a multiplicative (log-link) structure in terms of AIC?
- 6. Plot the smoothed effects again and use the **summary** function to see which effects are significant. Try simplifying the model.
- 7. Once you have converged on a model, plot it and interpret the fitted smooth effects: do they make sense?

4 Mackerel egg data

The following code loads and plots some data from a fish egg survey, for the purposes of spatial modelling.

```
library(testGam); library(mgcViz); data("mack"); data("coast")
## plot data....
with(mack,plot(lon,lat,cex=0.2+egg.dens/150,col="red"))
lines(coast)
ind <- c(1,3,4,5,10,11,16)
pairs(mack[,ind])</pre>
```

The main variables of interest in the mack data set are:

- egg.count number of eggs found in the net;
- c.dist distance from 200m seabed contour;
- b.depth depth of the ocean;
- temp.surf surface temperature of the ocean;
- temp.20m water temperature at a depth of 20 meters;
- lat latitude:
- lon longitude;
- salinity;
- net.area the area of the net used in m².

- 1. Use the code above to load and plot the data;
- 2. Create a new variable mack\$log.net.area <- log(mack\$net.area), and use gamV to fit a Poisson GAM with egg.count as response variable and 1D smooth effects for all the other variables, with the exceptions of net.area and log.net.area. Instead, include in the model formula the term offset(log.net.area), meant to take into account the fact that the number of eggs captured is proportional to the net area.

- 3. Look at the model residuals using qq. What kind of problem do you see? Re-fit the models using a negative binomial (family=nb) or Tweedie (family=tw) response distribution, and check which model is better in terms of residuals QQ-plots and AIC.
- 4. Let fit be the best of the three GAM models you just fitted. Use fit<-getViz(fit,nsim=50) to get some simulated residuals, and then use the check2D function with the l_gridCheck2D layer to look for residual patters across lon and lat. Then refit the model using a bivariate isotropic effect s(lon, lat, k=100), re-check the residuals and see whether AIC has improved.
- 5. Use check to verify whether the number of basis functions used for the smooth effects is sufficiently large. Then use the check1D function with the l_gridCheck1D layer look for residual patterns across some of the variables. If necessary, modify the model.
- 6. Plot the fitted effects using plot. Which effects look more important (look at the scales)? Use the plotRGL function to manipulate spatial effect interactively.

5 Bone mineral density modelling

This dataset is taken from the package lava. It consists of 112 girls randomized to receive calcium or placebo. The response variable of interests consists of longitudinal measurements of bone mineral density (g/cm^2) measured approximately every 6th month for 3 years. All girls are approximately 11yo at the start of the trial. The main variables are:

- bmd bone mass density;
- group placebo or supplement;
- person factor indicating the id of each girl;
- age the age of each girl at the time of each measurement;

- 1. Load testGam, mgcViz and the data data("calcium"). Then use gamV to fit a Gaussian GAM model with bmd as response and linear effects for age and group. In the call to gamV set the argument aViz=list(nsim = 50) to have some simulated responses for residuals checks. Use summary to print the model output. Is the placebo effect significant? (which is the same as asking whether the treatment effect is significant)
- 2. Use check1D with the l_gridCheck1D layer to check that the mean of the negative residuals does not depart too much from 0, for any of the subjects. If you see significant departures add a random effect for person to the models formula (s(person, bs="re")), then re-fit and re-check the residuals. Print the model output again using summary.
- 3. Now modify the model formula to use a smooth effect for age, and plot the fitted effects using plot. Use the function AIC to compare the model with a smooth effects for age with the model which uses a linear age effect.
- 4. Verify whether the smooth age effect is different between the placebo and the treatment group, by using a by-factor smooth. To do this substitute s(age) with s(age, by=group) in the model formula, refit and then plot the fitted effects. To see the difference between the two smooths more clearly, use the plotDiff function with the l_fitLine and l_ciLine layers.

6 Big GAM modelling of GEFCom14 electricity demand data

Here we use again data from the GEFCom14 challenge, but this data set is 24 times larger than the one used in the previous exercise. This is because it contains data corresponding to all the 24 hourly slots. The variable Instant indicates the hourly window corresponding to each row of the data set. All remaining covariates have the same interpretation as before. Questions:

- 1. Load testGam, mgcViz and the data (data("gefcom_big")). Create a model formula with smooth effects wM, wM_s95, Instant, Trend and Posan. Use regression splines bases (bs='cr') for all smooths apart from Posan, for which you should use a cyclic basis (bs='cc'). Use k = 6 for Trend and k = 20 for Posan. Leave k to its default for the other smooths. Use parametric fixed effects for Dow and NetDemand.24. Use this formula within a bamV call to fit a Gaussian GAM. When calling bamV set aGam=list(discrete=TRUE) to speed up computations (do this in all subsequent bamV calls) and aViz = list(nsim = 50) to perform the response simulations needed for residuals checking. Having fitted the model, look at the effects using plot (recall that you can use argument allTerms=TRUE to plot also the parametric effects).
- 2. Use check to verify whether the number of basis functions used for the smooth effects is sufficiently large. Also, use the check1D function with the l_gridCheck1D layer to look for residual patterns across the variables.
- 3. Double k for any of the effects where the number of basis functions seems to small, and re-fit. After re-fitting, check whether AIC has improved and repeat the residual checks.
- 4. We expect that several of the effects might depend on the time of day. Use the check2D function with the l_gridCheck2D layer to look for interactions between Instant and NetDemand.24, wM, wM_s95 and Posan. Notice that the binned mean residuals should ideally fall in the range (-2, 2) if the model was correct. Do you see any residual pattern? If so, fit a model which includes the necessary tensor product interactions (e.g. ti(wM, Instant, k = c(10, 10))) and repeat the checks. Are the patterns still there?
- 5. Assuming that we are now satisfied with our model, we'll now have a detailed look at the fitted smooth effects. First, look at the marginal effects using the plot function. Use the expression print(plot(fit2, select = ???), pages = 1) to plot all the marginal effects on one page (substitute ??? with the indexes of the univariate effects in your model). Do the same to plot the 2D interactions. Think about whether each effect makes physical sense to you. As an alternative to plot, recall that you can extract any effect using the sm function and produce a plot with customized layers. You can use the listLayers function to get a list of the available layers. Then, use the plotRGL function to manipulate each bivariate effect interactively.
- 6. Extra question: the model could be improved further. For instance, use the check2D function with the l_gridCheck2D layer to look at how the standard deviation and skewness of the residuals vary across pairs of covariates (the e1071 package provides a skewness function, then you simply need to set gridFun = skewness in the call to l_gridCheck2D). Do you see any pattern? At this point we could consider a GAMLSS model with linear predictors for location, variance and skewness (e.g. the gaulss or shash family). However, bam methods does not yet support such models, so you'll need to use gam which can be much slower for large models.

7 Individual electricity demand modelling

Here we consider electricity demand from 28 commercial customers. The dataset covers roughly three months and it contains the following variables:

- load power usage from an individual customer (in KW, I guess);
- DateTime the date and the time of day;
- instant the time of day, where 1 corresponds to 00:00-00:30, 2 to 00:30-01:00 and so on;
- dow factor variable indicating the day of the week;
- temp instantaneous temperature;
- tempL exponential smooth of temp, that is tempL[i] = a*temp[i] + (1-a)*tempL[i-1] with a=0.95;
- ID the unique ID of each individual customer;
- load48SM lagged version of smoothed load, where the smoothing was performed as for tempL.
- day a counter depending on the day.

- 1. Load testGam, mgcViz and the data (load("Ind_elect")). Then use bamV to fit a Gaussian GAM model with smooth effects for instant, temp and day, and parametric effects for dow and ID. In the call to bamV set aViz = list(nsim = 50) to perform the response simulations needed for residuals checking. Look at the model output using plot and summary.
- 2. Now we start looking for interactions. Use the check2D function with the l_gridCheck2D layer to look for interactions between ID and instant, temp and day. Notice that the binned mean residuals should ideally fall in the range (-2, 2), if the model is correct. Do you see large deviation? If so, for which customer(s) in particular?
- 3. Modify the model formula to include by-factor smooths, that is s(instant, by = ID, id = 1) s(temp, by = ID, id = 2) and s(day, by = ID, id = 3). The id argument make so that each of the 3 by-factor smooths has its own smoothing parameter, but the same smoothing parameter is used across all customers. Refit the model using bamV, and set the argument aGam=list(discrete=TRUE) to speed up computation by discretisation. Compare this model to the previous one using AIC, and repeat the residuals checks. Any improvement?
- 4. Use check to verify whether the number of basis functions used for the smooth effects is sufficiently large. Double k for any of the effects where the number of basis functions seems to small, and re-fit. After re-fitting, check whether AIC has improved.
- 5. Use the check2D function with the 1_gridCheck2D layer to look for interactions between ID and load48SM. If the effect of load48SM seems important, include the corresponding by-factor smooth by adding s(load48SM, by = ID, id = 4) to the model and re-fit.
- 6. Look at the model output using plot, using the select argument to plot any specific effect (you can't plot them all together, because the model includes tens of them). Compare the consumption of some of the individual customers with the model predictions (which you can find in fittedModel\$fitted.values). Do some customers look much harder to predict than others?

8 Body Mass Index (BMI) of Dutch boys

This simple data set comes from the Fourth Dutch Growth Study, which is a cross-sectional study that measures growth and development of the Dutch population between the ages 0 and 21 years. Here we have only two variables: bmi and age. The data is taken from the gamlss.data package. Questions:

- 1. Load testGam, mgcViz and the data (data("dbbmi")). Then use gamV to fit a Gaussian GAM with simply a single smooth effect for age. Set argument aViz=list(nsim = 50) to have some simulated responses for residuals checks. Then plot the data (a scatterplot bmi vs age) and add a line representing the fitted mean BMI (you can use the predict function).
- 2. Check the residual distribution using qq: do you see any problem? Then use the check1D function together with the l_gridCheck1D(gridFun=sd) layer to check whether the conditional standard deviation of the residuals varies with age. If so, address this by fitting a Gaussian GAMLSS model (family = gaulss), with model formula list(bmi ~ s(age), ~ s(age)). Then repeat the residuals checks. Any improvement?
- 3. Use check to verify whether the number of basis functions used for the smooth effects is sufficiently large. Then increase the number of basis functions used for each effect to 20 (k=20), and use an adaptive basis fom the effect of age on mean BMI (bs = "ad"). Is this model better in terms of AIC? Does the output of check look ok now? Plot the smooth effects, and decide whether they make sense. Do you see why we used an adaptive smooth for the effect of age on mean BMI?
- 4. Now we look at residual skewness. Load the e1071 package, and use the check1D function together with the l_gridCheck1D(gridFun=skewness) layer to check whether the conditional skewness of the residuals varies with age. To take skewness into account, load the mgcFam package, and fit a shash GAM model (family=shash) with model formula:

```
list(bmi ~ s(age, k = 20, bs = "ad"), ~ s(age, k = 20), ~ s(age), ~ 1)
```

Do we get lower AIC, and how does a residuals QQ-plot look? Plot all the smooth effect and use check to verify that everything is ok.

5. Now we plot the fitted conditional distribution. Let fit4 be the shash model you just fitted, then you can plot several estimated conditional quantiles by doing:

```
plot(bmi~age, data=dbbmi, col = "grey")
pr <- predict(fit4)
for(.q in c(0.01, 0.25, 0.5, 0.75, 0.9)){
    q_hat <- fit4$family$qf(.q, pr, wt = fit4$prior.weights, scale = 1)
    lines(dbbmi$age, q_hat, col = 2)
}</pre>
```

9 Rent modelling in Munich

This data set comes from gamlss.data package. The main variables are:

- R rent response variable, the monthly net rent in DM;
- F1 floor space in square meters;

- A year of construction;
- B a binary indicating whether there is a bathroom, 1, (1925 obs.) or not, 0, (44 obs.);
- H a binary indicating whether there is central heating, 1, (1580 obs.) or not, 0, (389 obs.);
- L a binary indicating whether the kitchen equipment is above average, 1, (161 obs.) or not, 0, (1808 obs.);
- loc a factor indicating whether the location is below, 1, average, 2, or above average 3.

Questions:

- 1. Load testGam, mgcViz and the data (data("munich_rent")) and have a look at it by doing pairs(munich_rent). Then use gamV to fit a Gaussian GAM with rent as response, smooth effects for Fl and A and fixed effects for the remaining covariates. Set argument aViz=list(nsim = 50) to have some simulated responses for residuals checks. Use summary and plot to see which are the most important effects.
- 2. The effect of F1 looks fairly linear, but it should depend on the location's desirability (loc). Substitute the smooth effect for F1 with a linear effect for F1 and the interaction F1:loc. Is there any improvement in AIC? Do the fitted coefficient reported by summary make sense?
- 3. Use the check1D function together with the l_gridCheck1D(gridFun=sd) layer to check whether the conditional standard deviation of the residuals varies with any of the covariates. If so address this by fitting a Gaussian GAMLSS model (family = gaulss), with the same formula for mean and for scale. Then repeat the residuals checks. Any improvement? Do you get lower AIC?
- 4. Now look at the residuals distribution using qq. Do you see any departure from normality? Check whether the conditional skewness of the residuals varies with any of the covariates by loading the e1071 package, and using the check1D function together with the l_gridCheck1D(gridFun=skewness) layer. To take skewness into account, load the mgcFam package, and fit shash GAM model (family=shash) with model formula:

Do we get lower AIC, and how does a residuals QQ-plot look? Do the skewness checks obtained with check1D look better now? Finally plot the smooth effects.

10 Quantile modelling of UK electricity demand

Here we consider a UK electricity demand dataset, taken from the national grid. The dataset covers the period January 2011 to June 2016 and it contains the following variables:

- NetDemand net electricity demand between 11:30am and 12am.
- wM instantaneous temperature, averaged over several English cities.
- wM_s95 exponential smooth of wM, that is $wM_s95[i] = a*wM[i] + (1-a)*wM_s95[i-1]$ with a=0.95.

- Posan periodic index in [0, 1] indicating the position along the year.
- Dow factor variable indicating the day of the week.
- Trend progressive counter, useful for defining the long term trend.
- NetDemand.48 lagged version of NetDemand, that is NetDemand.48[i] = NetDemand[i-1].
- Holy binary variable indicating holidays.
- Year and Date should obvious, and partially redundant.

Questions:

- 1. Load mgcViz and the data (data("UKload")). Then create a model formula (e.g. y~s(x)) containing: smooth effects for wM, wM_s95, Posan and Trend with 20, 20, 50 and 4 knots and cubic regression splines bases (bs='cr'); parametric effects for Dow, NetDemand.48 and Holy.
- 2. Use the qgamV function to fit this model for the median. Call (say) fit the fitted model and use plot(fit) and summary(fit) to visualise the fitted effects and to see which effects are significant. Do you notice anything problematic about the effect of Posan? How many degrees of freedom are we using for this smooth effect (you can read it from the output of summary)?
- 3. Modify the effect of Posan to use an adaptive (bs='ad') spline basis. Then refit the model and plot the smooth effects. Has the effect of Posan changed? How many degrees of freedom are we using now for Posan? Explain what happened.
- 4. Use mqgamV to fit this model to the five quantiles qu=seq(0.1,0.9,length.out=5). Use plot to visualize the smooth effects corresponding to each quantile. You can set allTerms=TRUE to plot also the parametric effects. How do the smooth and parametrics effects differ between quantiles? NB: here we are plotting the smooth effects, not the predicted quantiles, hence the effects corresponding to, say, quantile 0.9 can fall below that of quantile 0.1.
- 5. Now we check the median fit. If the output of mqgamV is called fitM then the median fit is fitM[[3]]. Use check1D with the l_gridQCheck1D layer to check that the fraction of negative residuals does not depart too much from 0.5 along any of the covariates.

11 Rainfall modelling in Switzerland

This question is about modelling extreme rainfall in Switzerland, mainly using spatio-temporal effects. The main variables are:

- exra: the highest rainfall observed in any 12 hour period in that year, in mm;
- N: degrees North;
- E: degrees East;
- elevation: metres above sea level;
- climate.region: factor variable indicating one of 12 climate regions;
- nao: annual North Atlantic Oscillation index, based on the difference of normalized sea level pressure (SLP) between Lisbon, Portugal and Stykkisholmur/Reykjavik, Iceland. Positive values are generally associated with wetter and milder weather over Western Europe;

• year: year of the observation;

- 1. Load mgcViz, gamair and the data with data(swer). Use qgamV to fit an additive quantile regression model for the median of exra, with smooth effects for nao, elevation and year (use k=5 for the latter), an isotropic smooth for E and N (i.e. s(E,N)), and a fixed effect for climate.region. Look at the significance of the fitted effects using summary and plot them using plot.
- 2. We might be interested in verifing whether the rainfall trend is different depending on the climate region. To assess this, modify the model formula to include a by-factor smooth as follows s(year, climate.region, bs = "fs", k = 5) (you will have to remove the fixed climate.region effect). Refit and use summary to verify whether the by-region trend term is significant, and plot the by-region trends by extracting it using sm and the l_fitLine(alpha = 1) layer.
- 3. We can also verify whether the bivariate spatial effect changes with time, by creating a tensor product between the 2D effect of E and N, and the effect of year. Such an effect can be set up using te(E, N, year, d = c(2, 1), k = c(20, 5)). Fit the corresponding median QGAM model, and plot several slices of the 3D tensor product across year, using the plotSlice function with the l_fitRaster and l_fitContour layers.
- 4. Visualize individual 2D slices (across year) of the 3D spatio-temporal smooth using the plotRGL function (see ?plotRGL.mgcv.smooth.MD for examples).
- 5. Go back to the simpler model formula used in the first question and fit the corresponding model to the quantiles qu = seq(0.1, 0.9, length.out = 9), using mqgamV. Plot only the univariate effects using plot and its select argument, and see how they differ between quantiles. Do the same for the spatial effect and for the effect of the climate region.