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TMLE step by step

Code ▼

By: Miguel Angel Luque Fernandez miguel-angel.luque@lshtm.ac.uk (<mailto:miguel-angel.luque@lshtm.ac.uk>)

October 25th, 2016

1 Introduction

During the last 30 years, the modern epidemiology has been able to identify some important drawbacks of the classic epidemiologic methods (bivariate or multivariate adjusted models) when the focus is to explanation the main effect of a risk factor on a disease or outcome.

Causal Inference, first introduced in Social Science by Donal Rubin (Rubin, 1974) and later in Epidemiology and Biostatistics by James Robins (Greenland and Robins, 1986), the **Neyman-Rubin Potential Outcomes framework** (Rubin, 1974), (Rubin, 2011) has provided the theory and statistical methods needed to identify and overcome recurrent problems in observational epidemiologic research, such as:

1. non collapsibility of the odds and hazard ratios,
2. impact of paradoxical effects due to conditioning on colliders,
3. left truncation,
4. prevalent cases,
5. selection bias related with the vague understanding of the effect of time on exposure and outcome and,
6. effect of time dependent confounding and mediators,
7. etc.

To control for confounding, the classical epidemiologic methods require making the assumption that the effect measure is constant across levels of confounders included in the model.

Alternatively, James Robins in 1986 demonstrated that using standardization, implemented through the use of the **G-formula**, allowed to obtain unconfounded marginal estimation of the causal average treatment effect (ATE) under causal nontestable assumptions (Greenland and Robins, 1986), (Robins *et al.*, 2000). The most commonly used estimator for a binary treatment effect is the risk difference or $ATE = \psi(P_0)$.

2 The G-Formula

$$\psi(P_0) = \sum_w \left[\sum_y P(Y = y | A = 1, W = w) - \sum_y P(Y = y | A = 0, W = w) \right] P(W = w)$$

1 Introduction

2 The G-Formula
where,

3 TMLE

4 Structural causal framework

$$P(Y = y | A = a, W = w) = \frac{P(W = w, A = a, Y = y)}{\sum_y P(W = w, A = a, Y = y)}$$

4.1 Direct Acyclic Graph

(DAG) is the conditional probability distribution of $Y = y$, given $A = a$, $W = w$ and,
4.2 DAG interpretation5 Causal assumptions

$$P(W = w) = \sum_{y,a} P(W = w, A = a, Y = y)$$

5.1 CMI or

Randomization • Classical epidemiologic methods require making the

5.2 Positivity assumption that the effect measure is constant across levels of confounders included in the model. However,

5.3 Consistency or **Standardization** allows us to obtain an unconfounded summary effect measure without requiring this assumption.
SUTVA:

6 TMLE The G-formula is a generalization of standardization (Greenland and Robins, 1986).

7 Data generation

• The ATE can be estimated **non-parametrically** using the G-formula. However, the curse of dimensionality in

7.1 Simulation observational studies limits its estimation.

7.2 Data visualization

8 TMLE simple implementation
• Hence, the estimation of the ATE using the G-formula relies mostly on **parametric modelling** assumptions and8.1 Step 1: $Q_0(A, W)$ likelihood estimation. The **correct model**8.2 Step 2: $g_0(A, W)$ **specification** in parametric modelling is crucial to obtain unbiased estimates of the true ATE (Rubin, 2011).8.3 Step 3: HAW and ϵ

However, Mark van der Laan and collaborators have developed a

8.4 Step 4: Q^* double robust estimation procedure **to reduce bias against**8.5 Step 5: g^* **misspecification**. The targeted maximum likelihood estimation

(TMLE) is a semiparametric, efficient substitution estimator

9 TMLE vs. AIPW (Laan and Rose, 2011).

10 TMLE using the Super-

Learner

3 TMLE

11 R-TMLE

TMLE allows for data-adaptive estimation while obtaining valid

12 R-TMLE improving statistical inference based on the targeted minimum loss-based estimation and machine learning algorithms to minimize the risk prediction

13 Appendix One or model misspecification (Laan and Rose, 2011). The main characteristics of **TMLE** are:

1. **TMLE** is a general algorithm for the construction of double-robust, semiparametric, efficient substitution estimators. **TMLE** allows for data-adaptive estimation while obtaining valid statistical inference.

2. TMLE implementation uses the G-computation estimand

(G-formula). Briefly, the **TMLE** algorithm uses information

1 Introduction in the estimated exposure mechanism $P(A|W)$ to update the

2 The G-Formula initial estimator of the conditional expectation of the

3 TMLE outcome given the treatment and the set of covariates W ,

$E_0(Y|A, W)$.

4 Structural causal

framework 3. The targeted estimates are then substituted into the

parameter mapping Ψ . The updating step achieves a

4.1 Direct Acyclic Graph targeted bias reduction for the parameter of interest $\psi(P_0)$

(DAG) (the true target parameter) and serves to solve the efficient

4.2 DAG interpretation score equation, namely Influence Curve (IC). As a result,

5 Causal assumptions **TMLE** is a double robust estimator.

5.1 CML **TMLE** it will be consistent for $\psi(P_0)$ if either the

Randomization conditional expectation $E_0(Y|A, W)$ or the exposure

5.2 Positivity mechanism $P_0(A|W)$ are estimated consistently.

5.3 Consistency of **TMLE** will be efficient if the previous two functions are

SUTVA: consistently estimated achieving the lowest asymptotic

variance among a large class of estimators. These

6 TMLE flow chart asymptotic properties typically translate into lower bias and

7 Data generation variation in finite samples (Bühlmann *et al.*, 2016).

7.1 Simulation The general formula to estimate the ATE using the TMLE

method:

7.2 Data visualization

8 TMLE simple implementation $\psi^{TMLE}_n = \Psi(Q_n^*) = \frac{1}{n} \sum_{i=1}^n \bar{Q}_n^1(1, W_i) - \bar{Q}_n^1(0, W_i). (1)$

8.1 Step 1: $Q_0(A, W)$

7. The efficient influence curve (IC) based on Hampel seminal

8.2 Step 2: $q_0(A, W)$ paper (Hampel, 1974) is applied for statistical inference using

8.3 Step 3: HAW and ϵ

8.4 Step 4: $\bar{Q}_n^* = \left(\frac{I(A_i = 1)}{g_n(1|W_i)} - \frac{I(A_i = 0)}{g_n(0|W_i)} \right) [Y_i - \bar{Q}_n^1(A_i, W_i)] + \bar{Q}_n^1(1, W_i) - \bar{Q}_n^1(0, W_i) - \psi^{TMLE}_n. (2)$

8.5 Step 5: Inference

9 TMLE vs. AIPW where the variance of the ATE:

10 TMLE using the Super-Learner $\sigma(\psi_0) = \sqrt{\frac{Var(IC_n)}{n}}. (3)$

11 R-TMLE

8. The procedure is available with standard software such as

12 R-TMLE The **tmle** package in R (Gruber and Laan, 2011).

prediction

13 Appendix One

4 Structural causal framework

4.1 Direct Acyclic Graph (DAG)

Back-door criterion
Minimal sufficient sets for estimating the total effect of A on Y.

Under conditional exchangeability: $A \perp Y_1, Y_0 \mid W$
 $\Psi(P_0) \text{ (ATE)} = E[E(Y \mid A = 1; W) - E(Y \mid A = 0; W)]$

1 Introduction

2 The G-Formula

3 TMLE

4 Structural causal framework

4.1 Direct Acyclic Graph (DAG)

4.2 DAG interpretation

Figure 1: Direct Acyclic Graph
Source: Miguel Angel Luque-Fernandez

5 Causal assumptions

5.1 CMI or Randomization

4.2 DAG interpretation

5.2 Positivity

5.3 Consistency or SUTVA

6 TMLE flow chart

7 Data presentations

7.1 Simulation

7.2 Data visualization

8 TMLE simple implementation

5 Causal assumptions

8.1 Step 1: $Q_0(A, W)$

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: \bar{Q}_n^*

8.4 Step 4: \bar{Q}_n^*

8.5 Step 5: Inference

5.1 CMI or Randomization

9 TMLE vs. AIPW

10 TMLE using the Super-Learner

5.2 Positivity

11 R-TMLE

12 R-TMLE improving prediction

13 Appendix One

The ATE is interpreted as the population risk difference in one-year mortality for lung cancer patients diagnosed via emergency presentations versus non-emergency presentations. Under causal assumptions, and compared with non-emergency presentations of lung cancer, the risk difference of one-year mortality for emergency presentations increases by approximately 20%.

$\Psi(P_0) = 0.198$

5.3 Consistency or SUTVA:

The observed outcome value, under the observed treatment, is equal to the counterfactual outcome corresponding to the observed treatment for identical independent distributed (i.i.d.)

variables.

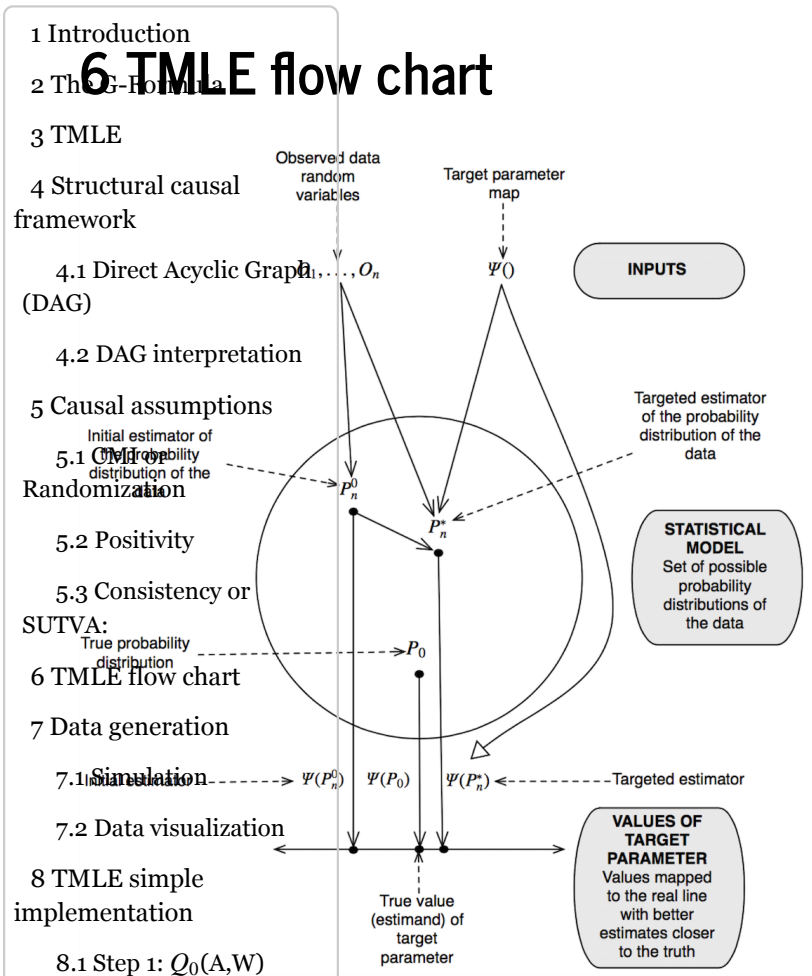


Figure 2. TMLE flow chart (Road map)

8.2 Step 2: $g_0(A, W)$

Source: Mark van der Laan and Sherri Rose. Targeted learning:

8.3 Step 3: HAW and 6 causal inference for observational and experimental data Springer

Series in Statistics, 2011.

8.4 Step 4: Q_n

8.5 Step 5: Inference

7 Data generation

9 TMLE vs. AIFW

10 TMLE using the Super-Learner

7.1 Simulation

11 R-TMLE create a function to generate the data. The function will have as input **number of draws** and as output the generated **observed data** (ObsData) including the counterfactuals (Y_1, Y_0).

12 R-TMLE improving prediction

The simulated data replicating the DAG in Figure 1:

13 Appendix One

1. Y: mortality binary indicator (1 death, 0 alive)
2. A: binary treatment for emergency presentation at cancer diagnosis (1 EP, 0 NonEP)
3. W1: Gender (1 male; 0 female)
4. W2: Age at diagnosis (0 <65; 1 >=65)

5. W3: Cancer TNM classification (scale from 1 to 4)

6. W4: Comorbidities (scale from 1 to 5)

1 Introduction

2 The G-Formula

Hide

3 TMLE

`install.packages("broom")``options(digits=4)`

4 Structural causal framework

`generateData <- function(n){` `w1 <- rbinom(n, size=1, prob=0.5)` `w2 <- rbinom(n, size=1, prob=0.65)` `w3 <- round(runif(n, min=0, max=4), digits=3)` `w4 <- round(runif(n, min=0, max=5), digits=3)` `A <- rbinom(n, size=1, prob= plogis(-0.4 + 0.2` `*w1 + 0.3*w2 + 0.25*w3 + 0.2*w4 + 0.15*w2*w4))` `Y <- rbinom(n, size=1, prob= plogis(-1 + A -0.` `*w1 + 0.3*w2 + 0.25*w3 + 0.2*w4 + 0.15*w2*w4))`

5.1 CMI or Randomization

 `Y.1 <- rbinom(n, size=1, prob= plogis(-1 + 1 -0` `*w1 + 0.3*w2 + 0.25*w3 + 0.2*w4 + 0.15*w2*w4))`

5.2 Post-treatment consistency or SUTVA:

 `Y.0 <- rbinom(n, size=1, prob= plogis(-1 + 0 -0` `*w1 + 0.3*w2 + 0.25*w3 + 0.2*w4 + 0.15*w2*w4))`

6 TMLE flow chart

7 Data generation

`# return data.frame` `data.frame(w1, w2, w3, w4, A, Y, Y.1, Y.0)` `}` `set.seed(7777)`

8 TMLE simple implementation

 `ObsData <- generateData(n=10000)` `True_Psi <- mean(ObsData$Y.1-ObsData$Y.0);` `cat("\n True_Psi:", True_Psi)` `cat("\n")` `cat("\n")` `cat("\n")` `cat("\n")` `cat("\n")` `cat("\n")` `cat("\n")`

9 TMLE vs. AIPW

10 TMLE using the Super-Learner

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 `cat("\n Naive_Biased_Psi:",summary(Bias_Psi)$coef` `[2, 1])`

12 R-TMLE improving prediction

13 Appendix One

`Naive_Bias <- ((summary(Bias_Psi)$coef[2, 1])-True_Psi); cat("\n Naives bias:", Naive_Bias)`

Hide

`Naive_Bias <- ((summary(Bias_Psi)$coef[2, 1])-True_Psi); cat("\n Naives bias:", Naive_Bias)`

1 Introduction

Naives bias: 0.06509

2 The G-Formula

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3 TMLE

Naive_Relative_Bias <- (((summary(Bias_Psi)\$coef[2,1])-True_Psi)/True_Psi)*100; cat("\n Relative Naives bias:", Naive_Relative_Bias,"%")

4 Structural causal framework

4.1 Direct Acyclic Graph (DAG)

4.2 DAG interpretation

Relative Naives bias: 32.88 %

5 Causal assumptions

5.1 TMLE of Randomization

72 Data visualization

5.2 Positivity

Hide

5.3 Confounding

SUTVA# install.packages("DT") # install DT first

library(DT)

6 TMLE flow chart

dataTable(head(ObsData, n = nrow(ObsData)), options = list(pageLength = 5, digits = 2))

7 Data generation

7.1 Simulation

Show 5 entries Search:

7.2 Data visualization

8 TMLE simple implementation	w1	w2	w3	w4	A	Y	Y.1	Y.o
1	0	1	3.282	3.541	1	1	0	0
8.1 Step 1: $Q_0(A,W)$								
2	0	0	0.047	1.425	1	1	0	0
8.2 Step 2: $g_0(A, W)$								
3	0	0	3.354	4.158	1	1	1	0
8.3 Step 3: HAW and ϵ_0								
4	1	1	2.085	1.737	1	1	0	0
8.4 Step 4: \bar{Q}_n^*								
5	0	1	2.487	0.419	1	1	0	1
8.5 Step 5: Inference								
9 TMLE vs. AIPTW								

8 TMLE simple implementation

8.1 Step 1: $Q_0(A,W)$

Estimation of the initial probability of the outcome (Y) given the treatment (A) and the set of covariates (W), denoted as $Q_0(A,W)$.

To estimate $Q_0(A, W)$ we can use a standard logistic regression

model:

1 Introduction

2 The G-Formula $\text{logit}[P(Y = 1|A, W)] = \beta_0 + \beta_1 A + \beta_2^T W$.

3 TMLE

Therefore, we can estimate the initial probability as follows:

4 Structural causal

framework

$$\bar{Q}^0(A, W) = \text{expit}(\hat{\beta}_0 + \hat{\beta}_1 A + \hat{\beta}_2^T W).$$

4.1 Direct Acyclic Graph

(DAG)

The predicted probability can be estimated using the Super-

Learner library implemented in the R package "Super-Learner"

4.2 DAG interpretation

(van der Laan *et al.*, 2007) to include any terms that are functions

5 Causal assumptions

of A or W (e.g. polynomial terms of A and W , as well as the interaction terms of A and W , can be considered).

5.1 CMI or

Randomization. Currently, for each subject, the predicted probabilities for

both potential outcomes $\bar{Q}^0(0, W)$ and $\bar{Q}^0(1, W)$ can be estimated

by setting $A = 0$ and $A = 1$ for everyone respectively:

5.2 Positivity

5.3 Consistency or

SUTVA:

$$\bar{Q}^0(0, W) = \text{expit}(\hat{\beta}_0 + \hat{\beta}_2^T W),$$

6 TMLE flow chart

and,

7 Data generation

7.1 Simulation $\bar{Q}^0(1, W) = \text{expit}(\hat{\beta}_0 + \hat{\beta}_1 A + \hat{\beta}_2^T W)$.

7.2 Data visualization

Note: see appendix one for a short introduction to the Super-

8 TMLE simple ensemble learning techniques.

implementation

Hide

8.1 Step 1: $Q_0(A, W)$

```
ObsData <- subset(ObsData, select=c(w1, w2, w3, w4, A,
```

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: QAW and QW

```
A <- ObsData$A
```

8.4 Step 4: QW

```
w1 <- ObsData$w1
```

8.5 Step 5: Inference

```
w2 <- ObsData$w2
```

```
w3 <- ObsData$w3
```

```
w4 <- ObsData$w4
```

9 TMLE vs. AIPW

```
Q <- cbind(QAW = predict(m) + w1 + w2 + w3 + w4, family=binom
```

Learnerial, data=ObsData)

10 R-TMLE

```
Q1W = predict(m, newdata=data.frame(A
```

11 R-TMLE improving

```
prediction Q0W = predict(m, newdata=data.frame(A
```

```
= 0, w1, w2, w3, w4), type="response"))
```

12 Appendix One

```
Q0 <- as.data.frame(Q); mean(Q0$Q1W-Q0$Q0W)
```

```
[1] 0.1992
```


8.2 Step 2: $g_0(A, W)$

1 Introduction

Estimation of the probability of the treatment (A) given the set of covariates (W), denoted as $g_0(A, W)$. We can use again a logistic regression model and to improve the prediction algorithm we can

use the SuperLearner library or any other machine learning

framework:

4.1 Direct Acyclic Graph (DAG) $\text{logit}[P(A = 1|W)] = \beta_0 + \beta_1^T W$.

4.2 DAG interpretation: Then we estimate the predicted probability of $P(A|W) = \hat{g}(1, W)$ using:

5 Causal assumptions

5.1 CMI or Randomization $\hat{g}(1, W) = \text{expit} = (\hat{\beta}_0 + \hat{\beta}_2^T W)$.

5.2 Positivity

5.3 Consistency or SUTVA?

```
glm(A ~ w2 + w3 + w4, family = binomial)
glw = predict(g, type = "response");summary(glw)
```

6 TMLE flow chart

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
7 Data generation	0.358	0.594	0.681	0.671	0.759	0.875

7.1 Simulation

7.2 Data visualization

8.3 Step 3: HAW and ϵ

8 TMLE simple

implementation

This step aims to find a better prediction model targeted at

8.1 Step 1: $Q^0(A, W)$ mean squared error (MSE) for the potential outcomes by using the so-called efficient IC estimation equation.

8.2 Step 2: $g_0(A, W)$ For the ATE on step convergence is guaranteed given \bar{Q}^0 and

8.3 Step 3: HAW and ϵ

8.4 Step 4: \bar{Q}^0 The fluctuating parameter is modelled using a parametric working model to estimate the fluctuation parameters ϵ_0 and ϵ_1 as follows:

8.5 Step 5: Inference

9 TMLE as WIPFW $\text{expit} \left[\text{logit} \left(\bar{Q}^0(A, W) \right) + \hat{\epsilon}_0 H_0(A, W) + \hat{\epsilon}_1 H_1(A, W) \right] \quad (5)$

10 TMLE using the Super-Learner $Q^1(0, W) = \text{expit} \left[\text{logit} \left(\bar{Q}^0(A, W) \right) + \hat{\epsilon}_0 H_0(A, W) \right]$

11 R-TMLE- $Q^1(1, W) = \text{expit} \left[\text{logit} \left(\bar{Q}^0(A, W) \right) + \hat{\epsilon}_1 H_1(A, W) \right]$

12 R-TMLE improving prediction

Where,

13 Appendix One

$$H_0(A, W) = \frac{I(A = 0)}{\hat{g}(0|W)} \text{ and, } H_1(A, W) = \frac{I(A = 1)}{\hat{g}(1|W)}$$

are referred to as clever covariates (note that $\hat{g}(A|W)$ is estimated from step 2).

The fluctuation parameters $(\hat{\epsilon}_0, \hat{\epsilon}_1)$ are estimated using

maximum likelihood procedures by setting $\text{logit}(\bar{Q}^0(A, W))$ as an offset in a intercept-free logistic regression with H_0 and H_1 as independent variables.

2 The G-Formula

Afterwards, the estimated probability of the potential outcomes is

3 TMLE

updated by the substitution parameters ($\hat{\epsilon}_0$, $\hat{\epsilon}_1$). The substitution

4 Structural equation model

the initial estimate probability of the potential outcomes

4.1 Direct Acyclic Graph (DAG)

4.2 DAG interpretation

[Hide](#)

5 Causal assumptions

Model (5): Clever covariate and fluctuating/substitution parameteres

5.1 CM for Randomization

```
h <- cbind(A/glw ~ (1-A)/(1-glw), 1/glw, -1/(1-glw))
```

5.2 Positivity

```
epsilon <- coef(glm(Y ~ -1 + h[,1] + offset(Q[, "QAW"]), family = binomial));epsilon
```

5.3 Consistency or

SUTVA:

6 TMLE flow chart

0.001189

7 Data generation

7.1 Simulation

7.2 Data visualization

8.4 Step 4: \bar{Q}_n^*

8 TMLE simple implementation

For the ATE, the updated estimate of the potential outcomes only needs one iteration $\Psi(\bar{Q}_n^*)$ from $\bar{Q}^0(A, W) \Rightarrow \bar{Q}^1(A, W)$.

8.1 Step 1: $\bar{Q}_n(A, W)$

Therefore, model (5) targets $E[\hat{Y}_{A=0}]$ and $E[\hat{Y}_{A=1}]$ simultaneously

8.2 Step 2: $\bar{Q}_n(A, W)$

by including both $H_0(A, W)$ and $H_1(A, W)$ in the model. Hence ψ

is finally estimated as follows:

8.3 Step 3: HAW and ϵ

8.4 Step 4: \bar{Q}_n^*

TMLE, $n = \Psi(\bar{Q}_n^*) = \frac{1}{n} \sum_{i=1}^n \bar{Q}_n^1(1, W_i) - \bar{Q}_n^1(0, W_i). (1)$

8.5 Step 5: Inference

9 TMLE vs. AIPTW

[Hide](#)

10 TMLE using the Super

```
Qstar <- predict(Q + epsilon*h)
Psi <- mean(Qstar[, "Q1W"] - Qstar[, "Q0W"]); cat("T
```

11 R-TMLE

```
TMLE_Psi:", Psi)
```

12 R-TMLE improving

prediction
TMLE_Psi: 0.04594

13 Appendix One

[Hide](#)

```
cat("\n TMLE.SI_bias:", abs(True_Psi-Psi))
```

1 Introduction: $\text{TMLE.SI_bias} = 0.1521$

2 The G-Formula

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3 TMLE

4 Structural causal framework
 $\text{cat}("\n \text{Relative_TMLE.SI_bias}:", \text{abs}(\text{True_Psi} - \text{Psi}) / \text{True_Psi} * 100, "\%")$

4.1 Direct Acyclic Graph (DAG)

$\text{Relative_TMLE.SI_bias} = 76.8 \%$

4.2 DAG interpretation

5 Causal assumptions

8.5 Step 5: Inference

5.1 CM of

Randomization: TMLE uses the efficient influence curve (IC) for inference (i.e., to obtain standard errors for ψ).

5.2 Positivity

5.3 Consistency:
$$E_n(IC_i) = \left(\frac{I(A_i = 1)}{g_n(1|W_i)} - \frac{I(A_i = 0)}{g_n(0|W_i)} \right) \left[Y_i - \bar{Q}_n^1(A_i, W_i) \right] + \bar{Q}_n^1(1, W_i) - \bar{Q}_n^1(0, W_i) - \psi_{TMLE, n}. \quad (2)$$

SUTVA:

6 TMLE flow chart
 where the standard deviation for ψ is estimated as follows:

7 Data generation

7.1 Simulation

$$\sigma(\psi_0) = \sqrt{\frac{\text{Var}(IC_n)}{n}}. \quad (3)$$

7.2 Data visualization

Note: see appendix two for a short introduction to the Influence

8 TMLE with theory.

implementation

Hide

8.1 Step 1: $Q_0(A, W)$

$Q \leftarrow \text{as.data.frame}(Q)$

8.2 Step 2: $g_0(A, W)$
 $\text{IC} \leftarrow n[1] * (Y - Q\$QAW) + Q\$Q1W - Q\$Q0W - \text{Psi}; \text{summa}$

8.3 Step 3: HAW and ϵ

8.4 Step 4: \bar{Q}_n^*

8.5 Step 5: Inference

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
-3.610	-1.550	-0.878	-0.678	-0.073	13.500	

9 TMLE vs. AIPTW

10 TMLE using the Super-

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Learner

$n \leftarrow \text{nrow}(\text{ObsData})$

11 R-TMLE
 $\text{varHat.IC} \leftarrow \text{var}(\text{IC})/n; \text{varHat.IC}$

12 R-TMLE improving prediction

$[1] \quad 0.0002032$

13 Appendix One

Hide

#Psi and 95%CI for Psi
 $\text{cat}("\n \text{TMLE_Psi}:", \text{Psi})$

1 Introduction	TMLE.Psi: 0.04594
2 The G-Formula	Hide
3 TMLE	
4 Structural causal framework	cat("\n 95%CI:", c(Psi-1.96*sqrt(varHat.IC), Psi+1.96*sqrt(varHat.IC)))
4.1 Direct Acyclic Graph (DAG)	95%CI: 0.018 0.07388
4.2 DAG interpretation	
5 Causal assumptions	Hide
5.1 Causal Randomization	cat("\n TMLE.SI_bias:", abs(True_Psi-Psi))
5.2 Positivity	
5.3 Consistency or SUTVA:	TMLE.SI_bias: 0.1521
6 TMLE flow chart	Hide
7 Data generation	cat("\n Relative TMLE.SI_bias:", abs(True_Psi-Psi)/True_Psi*100,"%")
7.1 Simulation	
7.2 Data visualization	
8 TMLE simple implementation	Relative TMLE.SI_bias: 76.8 %
8.1 Step 1: $Q_0(A,W)$	
8.2 Step 2: $g_0(1,W)$	
8.3 Step 3: HAW and Q_*	
8.4 Step 4: Q_* analyses	
8.5 Step 5: Inference	
9 TMLE vs. AIPTW	
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9 TMLE vs. AIPTW

1. The advantages of **TMLE** have been repeatedly demonstrated in both simulation studies and applied analyses (Laan and Rose, 2011).

2. Evidence shows that **TMLE** provides the less unbiased ATE

estimator compared with other double-robust estimators

(Neugebauer and Laan, 2005), (Laan and Rose, 2011) such as the combination of regression adjustment with inverse probability of treatment weighting (IPTW-RA) and the augmented inverse

probability of treatment weighting (AIPTW). The **AIPTW**

estimation is a two step procedure with two equations (propensity score equation and, mean outcome equation).

To estimate the ATE using the **AIPTW** estimator one can set the estimation equation (EE) (4) equal to zero and use bootstrap to derive 95% confidence intervals (CI). However, solving the EE using the generalized method of moments (GMM), stacking both equations (propensity score and outcome), reduces the estimation and inference steps to only one. However, given that the propensity score in

equation (4) can easily fall outside the range [0, 1] (if for some observations $g_n(1|W_i)$ is close to 1 or 0) the estimation can be unstable (near violation of the positivity assumption). This represents the price of not being a substitution estimator as **TMLE**.

$$\bar{Q}_n^{IPTW} = \frac{1}{n} \sum_{i=1}^n \left(\frac{I(A_i = 1)}{g_n(1|W_i)} - \frac{I(A_i = 0)}{g_n(0|W_i)} \right) [Y_i - \bar{Q}_n^0(A_i, W_i)] + \frac{1}{n} \sum_{i=1}^n \bar{Q}_n^0(1, W_i) - \bar{Q}_n^0(0, W_i). \quad (4)$$

4.1 Direct Acyclic Graph (DAG)

Hide

4.2 DAG interpretation

IPTW

5 Causal assumptions

5.1 CMI or Randomization

5.2 Positivity

Hide

5.3 Consistency or
SUTVA

6 TMLE flow chart

7 Data generation
AIPTW_bias: 0.003211

7.1 Simulation

7.2 Data visualization

Hide

8 TMLE simple implementation

8.1 Step 1: $Q_0(A, W)$

8.2 Step 2: $g_0(A, W)$

Relative AIPTW_bias: 1.622 %

8.3 Step 3: HAW and ϵ

8.4 Compared with AIPTW, TMLE showed smaller relative bias.

8.5 Step 5: Inference

9 TMLE vs. AIPTW

10 TMLE using the Super-Learner

With TMLE we can call the Super-Learner (SL). The SL is a R-package using V-fold cross-validation and ensembled learning (prediction using the all the predictions of multiple stacked

prediction algorithms) techniques to improve model prediction performance (Breiman, 1996).

13 Appendix One

The basic implementation of TMLE in the R-package **tmle** uses by default three algorithms:

1. SL libraries SL.glm (main terms logistic regression of A and W),
2. SL.step (stepwise forward and backward model selection using AIC criterion, restricted to second order polynomials) and,

10 TMLE using the Super-Learner

3. SL.glm.interaction (a glm variant that include second order polynomials and two by two interactions of the main terms included in the model).

1 Introduction

2 The G-Formula

The principal interest of calling the Super-Learner is to obtain the

3 TMLE less-biased estimated for $\bar{Q}_n^0(A, W)$ and $g_0(A, W)$. It is achieved

4 Stochastic targeting the smallest expected loss function for Y or A (binary outcomes), respectively. For instance, the negative logarithmic

4.1 Direct Acyclic Graph (DAG) loss function for Y is computed as the minimizer of the expected squared error loss:

$$4.2 \text{ DAG interpretation } \bar{Q}_0 = \arg \min_{\bar{Q}} E_0 L(O, \bar{Q}),$$

5 Causal assumptions

5.1 TMLE of $\bar{Q}_0(O, \bar{Q})$ is:

Randomization

$$5.2 \text{ Positivity } (Y - \bar{Q}(A, W))^2$$

5.3 Consistency of

SUTVA Learner and ensemble learning techniques.

6 TMLE Step One: $\bar{Q}_n^0(A, W)$ prediction

7 Data generation

Hide

7.1 Simulation

7.2 Data simulation

```
#Specify SuperLearner libraries
```

8 TMLE simple

```
SL.library <- c("SL.glm", "SL.step", "SL.glm.interaction")
```

8.1 Step 1: $Q_0(A, W)$ with X with baseline covariates and exposure

```
8.2 Step 2:  $g_0(A, W)$   
X <- subset(ObsData, select=c(A, w1, w2, w3, w4))
```

8.3 Step 3: How to use

```
#Create data frames with A=1 and A=0
```

8.4 Step 4: \bar{Q}_n

8.5 Step 5: Inference

```
X0$A <- 0
```

9 TMLE vs. AIPTW

```
#Create new data by stacking
```

10 TMLE using the SuperLearner

```
#Call superlearner  
Qinit <- SuperLearner(Y=ObsData$Y, X=X, newX=newdata,
```

11 R-TMLE

```
SL.library=SL.library, family="binomial")
```

12 R-TMLE improving prediction

13 Appendix One

1 Introduction

2 The G-Formula

3 TMLE

4 Structural causal framework

4.1 Directed Acyclic Graph (DAG)

4.2 DAG interpretation

5 Causal assumptions

5.1 CMI or Randomization

5.2 Positivity

5.3 Consistency or SUTVA:

6 TMLE flowchart

7 Data generation

7.1 Simulation

7.2 Data visualization

8 TMLE simple implementation

8.1 Step 1: $Q_0(A, W)$

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: $Q_1(A, W)$

8.4 Step 4: $Q_2(A, W)$

8.5 Step 5: Inference

9 TMLE vs. AIPTW

10 TMLE using the Super-Learner

11 R-TMLE

12 R-TMLE improving prediction

13 Appendix One

	Risk	Coef
SL.glm_All	0.1766	0.6002
SL.step_All	0.1766	0.0000
SL.no.white.Chap.All	0.1767	0.3998

Hide

Call:

```
SuperLearner(Y = ObsData$Y, X = X, newX = newdata, family = "binomial", SL.library = SL.library)
```

```
#Pred prob of survival given A, W
QbarAW <- Qinit$SL.predict[1:n]
#Pred prob of surv for each subject given A=1 and
Qbar1W <- Qinit$SL.predict[(n+1):(2*n)]
#Pred prob of surv for each subject given A=0 and
Qbar0W <- Qinit$SL.predict[(2*n+1):(3*n)]
#Simple substitution estimator Psi(Q0)
PsiHat.SS <- mean(Qbar1W-Qbar0W);PsiHat.SS
```

7.1 Simulation

Hide

8.1 Step 1: $Q_0(A, W)$

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: $Q_1(A, W)$

8.4 Step 4: $Q_2(A, W)$

8.5 Step 5: Inference

Hide

9 TMLE vs. AIPTW

10 TMLE using the Super-Learner

11 R-TMLE

12 R-TMLE improving prediction

13 Appendix One

	Risk	Coef
SL.glm_All	0.2091	0.0000
SL.step_All	0.2091	0.3803
SL.no.white.Chap.All	0.2090	0.6197

argument is not numeric or logical: returning NA

[1] NA

Hide

1 Introduction
#Generate the pred prob of A=1 and, A=0 given covariates

2 The C-F formula
`gHat1W <- gHatSL$SL.predict`

3 TMLE
`gHat0W <- 1-gHat1W`

4 Structural causal framework
#Step 3: clever covariate
`HAW <- as.numeric(ObsData$A==1)/gHat1W - as.numeric(ObsData$A==0)/gHat0W; mean(HAW)`

4.1 Direct Acyclic Graph (DAG)

4.2 DAG interpretation

```
[1] 0.002954
```

5 Causal assumptions

Hide

5.1 CMI or Randomization
`H1W <- 1/gHat1W`
`H0W <- -1/gHat0W`

5.2 Positivity

5.3 Consistency
3 Steps 3 and 4: fluctuation step and substitution
 SUTVA: estimation for for for $\bar{Q}_n^0(A, W)$ to $\bar{Q}_n^1(A, W)$

6 TMLE flow chart

Hide

7 Data generation
#Step 4: Substitution estimaiton Q^ of the ATE.*
Logit model
`logitUpdate <- glm(ObsData$Y ~ -1 + offset(qlogis(QbarAW))+HAW, family='binomial')`
Data visualization
`eps <- logitUpdate$coef; eps`

8 TMLE simple implementation

`HAW`
 8.1 Step 1: $Q_n^0(A, W)$

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: HAW and ϵ

Hide

8.4 Step 4: Q_n^1
#Calculating the predicted values for each subject under each txt

8.5 Step 5: Inference
`Qbar1W.star <- plogis(qlogis(QbarAW)+eps*HAW)`

9 TMLE vs. AIPW

`Qbar1W.star <- plogis(qlogis(Qbar1W)+eps*H1W)`

`Qbar0W.star <- plogis(qlogis(Qbar0W)+eps*H0W)`

10 TMLE using the Super Learner

`cat("PsiHat.TMLE.SL:", PsiHat.TMLE.SL)`

12 R-TMLE improving prediction

`PsiHat.TMLE.SL: 0.1995`

13 Appendix One

Hide

```
cat("\n PsiHat.TMLE.SL_bias:", abs(True_Psi-PsiHat.TMLE.SL))
```


1 Introduction	Relative_TMLE.SL_bias: 0.001456
2 The G-Formula	Hide
3 TMLE	
4 Structural causal framework	cat("\n Relative_PsiHat.TMLE.SL_bias:",abs(True_Psi-PsiHat.TMLE.SL)/True_Psi*100,"%")
4.1 Direct Acyclic Graph (DAG)	Relative_PsiHat.TMLE.SL_bias: 0.7354 %
4.2 DAG interpretation	
5 Causal assumptions	
5.1 CMI of Randomization	Using the R-package tmle
5.2 Positivity	Hide
5.3 Consistency or SUTVA	library(tmle) w <- subset(ObsData, select=c(w1,w2,w3,w4))
6 TMLE flow-chart	tmle <- tmle(Y, A, W=w)
7 Data generation	cat("TMLE_Psi:", tmle\$estimates[[2]][[1]],";","95%CI(", tmle\$estimates[[2]][[3]],")")
7.1 Simulation	
7.2 Data visualization	TMLE_Psi: 0.1994 ; 95%CI(0.1799 0.2189)
8 TMLE simple implementation	Hide
8.1 Step 1: $Q_0(A,W)$	cat("\n TMLE_bias:", abs(True_Psi-tmle\$estimates[
8.2 Step 2: $g(A,W)$	
8.3 Step 3: HAW and ϵ	
8.4 Step 4: \bar{Q}_n^*	TMLE_bias: 0.001407
8.5 Step 5: Inference	
9 TMLE vs. AIPTW	Hide
10 TMLE using the Super Learner	cat("\n Relative_TMLE_bias:",abs(True_Psi-tmle\$estimates[[2]][[1]])/True_Psi*100,"%")
11 R-TMLE	
12 R-TMLE improving prediction	Relative_TMLE_bias: 0.7108 %
13 Appendix One	

12 R-TMLE improving prediction

In addition to the default algorithms implemented in the R-tmle package, we can improve our estimation calling more efficient machine learning algorithms, such as generalized additive models

and the Random Forest in this particular example:

1 Introduction

Hide

2 The G-Formula

```
SL.TMLE.Psi <- tmle(Y=Y, A=A, W=w, family="binom
```

3 TMLE

```
Q.SL.library = c("SL.glm", "SL.step", "SL.glm
```

4 Structural causal framework

```
.interaction", "SL.gam", "SL.randomForest"),
```

```
g.SL.library = c("SL.glm", "SL.step", "SL.glm
```

```
4.1 Directed Acyclic Graph "SL.gam", "SL.randomForest"))
```

```
(DAG) cat("SL.TMLE.Psi:", SL.TMLE.Psi$estimates[[2]][
```

```
[[1]], ";", "95%CI(", SL.TMLE.Psi$estimates[[2]][[3
```

```
[[1]], ")]")
```

5 Causal assumptions

```
5.1 Simulation SL.TMLE.Psi: 0.1994 ; 95%CI( 0.1799 0.2189 )
```

Randomization

5.2 Positivity

Hide

```
5.3 Consistency cat("SL.TMLE.Psi_bias:", abs(True_Psi-SL.TMLE
```

```
SUTVA.R.Psi$estimates[[2]][[1]]))
```

6 TMLE flow chart

7 Data generation

```
SL.TMLE.Psi_bias: 0.001398
```

7.1 Simulation

7.2 Data visualization

Hide

8 TMLE simple implementation

```
cat("Relative SL.TMLE.Psi_bias:", abs(True_Psi
```

```
-SL.TMLE.Psi$estimates[[2]][[1]])/True_Psi*100,"
```

```
8.1 Step 1:  $Q_0(A, W)$ 
```

```
8.2 Step 2:  $g_0(A, W)$ 
```

```
8.3 Step 3: HAW and  $\epsilon$ 
```

```
Relative_SL.TMLE.Psi_bias: 0.7061 %
```

```
8.4 Step 4:  $\bar{Q}_n^*$ 
```

```
We have demonstrated:
```

```
8.5 Step 5: Inference
```

9 TMLE vs. AIPW

1. TMLE **excels** the AIPW estimator and,

2. TMLE **best performance** is obtained when calling more

10 TMLE using the Super-advanced **Super-Learner** algorithms.

11 R-TMLE

12 R-TMLE improving prediction

13 Appendix One

Efron in 1982 showed that the empirical **Influence Curve**

estimate of standar error is the same as the one obtained using the

13 Appendix One

infinitesimal jackknife and the nonparametric deltha method

(Efron and Efron, 1982). 1. The Delat Method = First order of the

Taylor series expansion:

$$f(x) \approx f(\mu) + (x - \mu)f'(\mu);$$

where $f'(\mu)$ is the derivative of the function with respect to X

evaluated at the mean of X . Therefore, squaring both terms, the

variance is approximately:

$$E[f(x) - f(\mu)]^2 \approx E(x - \mu)^2 \times [f'(\mu)]^2;$$

The left-hand side of the above equation is approximately the

variance of $f(x)$ and applied to the empirical distribution of X , the sample estimate of variance for X replaces:

4.1 Direct Acyclic Graph

(DAG)

$$E(x_i - \mu)^2.$$

4.2 DAG interpretation

The infinitesimal jackknife estimate of the standard error is

5 Causal assumptions:

5.1 CMI or

Randomization

$$SD_{ij}(\theta_e) = \left(\frac{\sum_{i=1}^n U_i^2}{n^2} \right)^{1/2};$$

5.2 Positivity

where θ_e is the estimate of the parameter θ and U_i is a

directional derivative in the direction of the i th coordinate centered at the mean of the empirical distribution function.

6 TMLE flow chart

7 Data generation

7.1 Simulation

7.2 Data visualization

8 TMLE simple implementation

8.1 Step 1: $Q_0(A, W)^{E(\hat{\theta})}$

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: HAW and ϵ

8.4 Step 4: \bar{Q}^* Estimate of the ψ Standard Error using the efficient

8.5 Step 5: Inference

Image credit: Miguel Angel Luque-Fernandez.

9 TMLE vs. AIPTW

10 TMLE using the Super

Learner

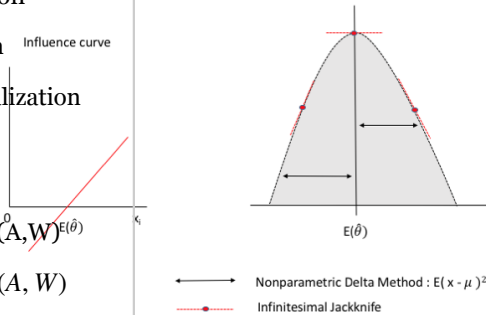
11 With TMLE we can call the R-package **Super-Learner (SL)**.

The **SL** uses **cross-validation** and **ensembled learning** (using

all the predictions of multiple stacked learning algorithms)

techniques to improve model prediction performance (Breiman,

13 Appendix One



14 Appendix Two

The **SL** algorithm provides a system based on V-fold cross-validation (Efron and Gong, 1983) (10-folds) to combine adaptively multiple algorithms into an improved estimator, and returns a function we can also use for prediction in new datasets.

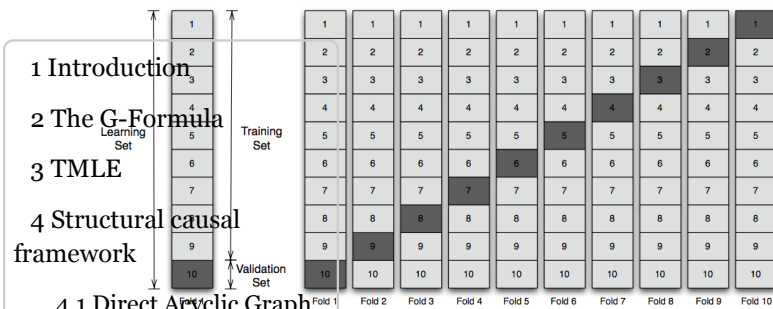


Figure 4: 10-fold cross-validation algorithm.

Source: Sherri Rose in *Ensembles in Public Health and Health*

Policy. May 4, 2016.

5 Causal assumptions

The basic implementation of TMLE in the R-package **tmle** uses

5.1 by default three algorithms: 1. SL libraries **SL.glm** (main terms Randomization logistic Regression of A and W),

5.2 **SL.step** (stepwise forward and backward model selection using AIC criterion, restricted to second order polynomials) and, 3.

5.3 **Consistency** or **SL.glm.interaction** (a **glm** variant that include second order polynomials and two by two interactions of the main terms

6 TMLE included in the model).

7 Data generation

The principal interest of calling the Super-Learner is to obtain the

7.1 **less unbiased** estimated for $\bar{Q}_n^0(A, W)$ and $g_0(A, W)$. It is achieved

by obtaining the smallest expected loss function for Y or A (binary outcomes), respectively. For instance, the negative logarithmic

8 TMLE simple for Y is computed as the minimizer of the expected implementation squared error loss:

$$8.1 \text{ Step 1: } Q_0(A, W) \quad \bar{Q}_0 = \arg \min_{\bar{Q}} E_0 L(O, \bar{Q}),$$

$$8.2 \text{ Step 2: } g_0(A, W)$$

$$8.3 \text{ Step 3: HAW and } \epsilon \text{ where } L(O, \bar{Q}) \text{ is:}$$

$$8.4 \text{ Step 4: } \bar{Q}_n^* \quad (Y - \bar{Q}(A, W))^2$$

$$8.5 \text{ Step 5: Inference}$$

9 TMLE vs. APTW The **SL** algorithm first split the data into 10 blocks and fits each of the selected algorithms on the training set (non-shaded blocks),

10 TMLE using the Super-Learner then predicts the estimated probabilities of the outcome (Y) using the validation set (shaded block) for each algorithm, based on the

11 **corresponding** training set. Afterwards, the **SL** estimates the the cross-validating risks for each algorithm averaging the risks across

12 **R-TMLE** improving validation sets resulting in one estimated cross-validated risk for each algorithm. Finally, the **SL** select the combination of Z that

13 **minimizes** the cross-validation risk, defined as the minimum mean square error for each of the selected algorithms using Y and Z . A weighted combination of the algorithms (ensemble learning) in Z is then used to predict the outcome (Y) (see Figure 5).

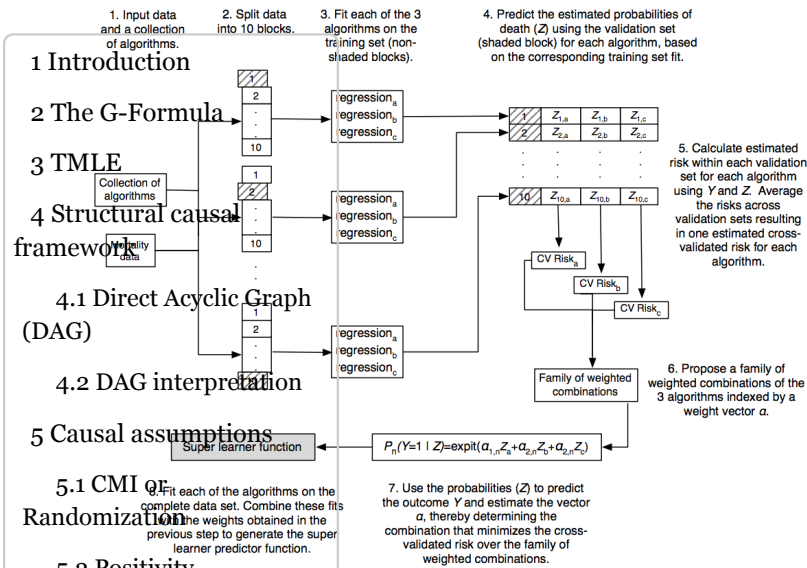


Figure 5: Flow Diagram for the Super-Learner algorithm.

Source: Mark van der Laan and Sherri Rose. Targeted learning: causal inference for observational and experimental data Springer Series in Statistics, 2011.

7 Data generation

7.1 Simulation

7.2 Data visualization

Hide

8 TMLE simple implementation

8.1 Step 1: $Q_0(A, W)$

Session info -----

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: HAW and ϵ

8.4 Step 4: Q_n

setting* value
version R version 3.3.0 (2016-05-03)

8.5 Step 5: Inference

system x64_64, darwin13.4.0
ui RStudio (1.0.44)

9 TMLE vs. AIPTW

language (EN)

10 TMLE using the Super-Learner

locale of OS: UTF-8

Learner tz Europe/London

date 2016-11-01

12 R-TMLE improving prediction

Packages -----

13 Appendix One

	package	* version	date	source
1 Introduction				
2 The G-Formula	assertthat	0.1	2013-12-06	CRAN (R 3.3.0)
3 TMLE	base64enc	0.1-3	2015-07-28	CRAN (R 3.3.0)
4 Structural causal framework	codetools	0.2-14	2015-07-15	CRAN (R 3.3.0)
4.1 Directed Acyclic Graph (DAG)	directAcyclicGraph	1.12.0	2016-06-24	CRAN (R 3.3.0)
4.2 DAG interpretation	digest	0.6.10	2016-08-02	CRAN (R 3.3.0)
5 Causal Assumptions	causaleval	* 0.2	2016-08-09	CRAN (R 3.3.0)
5.1 CMI or Randomization	causaleval	0.10	2016-10-11	CRAN (R 3.3.0)
5.2 Positivity	causaleval	* 1.4.3	2015-10-13	CRAN (R 3.3.0)
5.3 Consistency or SUTVA	causaleval	1.4	2016-05-09	CRAN (R 3.3.0)
6 TMLE flow chart	causaleval	* 1.14	2016-09-10	CRAN (R 3.3.0)
7 Data generation	htmltools	0.3.5	2016-03-21	CRAN (R 3.3.0)
7.1 Simulation	htmlwidgets	0.7	2016-08-02	CRAN (R 3.3.0)
7.2 Data visualization	htmlwidgets			
8 TMLE implementation	jsonlite	1.0.8	2015-10-13	CRAN (R 3.3.0)
8.1 Step 1: $Q_0(A, W)$	jsonlite	1.1	2016-09-14	CRAN (R 3.3.0)
8.2 Step 2: $g_0(A, W)$	jsonlite	1.14	2016-08-13	CRAN (R 3.3.0)
8.3 Step 3: HAW and ϵ	magrittr	1.5	2014-11-22	CRAN (R 3.3.0)
8.4 Step 4: \bar{Q}_n^*	memoise	1.0.0	2016-01-29	CRAN (R 3.3.0)
8.5 Step 5: Inference	memoise			
9 TMLE vs. AIPW	randomForest	* 1.4	2012-03-19	CRAN (R 3.3.0)
10 TMLE using the Super-Learner	randomForest	* 4.6-12	2015-10-07	CRAN (R 3.3.0)
11 R-TMLE	rsconnect	0.12.7	2016-09-05	CRAN (R 3.3.0)
12 R-TMLE improving prediction	rmarkdown	1.1.9007	2016-10-25	Github (rstudio/rmarkdown@746d0eb)
13 Appendix	stringi	1.0-2	2016-03-28	CRAN (R 3.3.0)
	rsconnect	0.5	2016-10-17	CRAN (R 3.3.0)
	rstudioapi	0.6	2016-06-27	CRAN (R 3.3.0)
	stringi	1.1.2	2016-10-01	CRAN (R 3.3.0)

1 Introduction	stringr	1.1.0	2016-08-19	CRAN	(R 3.3.0)
2 The G-formula	SuperLearner	* 2.0-19	2016-02-04	CRAN	(R 3.3.0)
3 TMLE	tibble	1.2	2016-08-26	CRAN	(R 3.3.0)
4 Structural causal framework	tmle	* 1.2.0-4	2014-03-09	CRAN	(R 3.3.0)
4.1 Direct Acyclic Graph (DAG)	withr	1.0.2	2016-06-20	CRAN	(R 3.3.0)
4.2 DAG interpretation	ACM	2.1.13	2014-06-12	CRAN	(R 3.3.0)
5 Causal assumptions					

5.1 CMI or Randomization

16 Thank you

5.2 Positivity
Thank you for participating in this tutorial.

5.3 Constructive updates or changes that you would like to make, please send me (<https://github.com/migariane/MALF>) a pull request.

6 TMLE flow chart
Alternatively, if you have any questions, please e-mail me. You can cite this repository as:

7 Data generation
Luque-Fernandez MA, (2016). Targeted Maximum Likelihood

7.1 Estimation
Estimation: A Step by Step Guided Implementation. GitHub

7.2 Data visualization
repository, <http://migariane.github.io/TMLE.nb.html>

(<http://migariane.github.io/TMLE.nb.html>).

8 TMLE implementation
Miguel Angel Luque Fernandez
E-mail: miguel-angel.luque@lshtm.ac.uk

8.1 Step 1: $Q_0(A, W)$
Twitter: @MATWILEI

8.2 Step 2: $g_0(A, W)$

17 References

8.3 Step 3: $Q_n(A, W)$

8.4 Step 4: Q_n
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8.5 Step 5: Inference

Bühlmann P, Drineas P, Laan M van der, Kane M. (2016).

9 TMLE vs. AIPTW.
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10 TMLE using the Super-Learner
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11 R-TMLE
Efron B, Gong G. (1983). A leisurely look at the bootstrap, the

12 R-TMLE improving prediction
jackknife, and cross-validation. *The American Statistician* **37**: 36–48.

13 Appendix One
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1 Introduction

383–393.

2 The G-Formula

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3 TMLE

inference for observational and experimental data. Springer Series

4 Structural Causal

framework

Neugebauer R, Laan M van der. (2005). Why prefer double robust

4.1 Directed Acyclic Graph (DAG)

and Inference **129**: 405–426.

4.2 DAG interpretation

Robins JM, Hernan MA, Brumback B. (2000). Marginal structural

5 Causal models and causal inference in epidemiology

models and causal

550–560.

5.1 CMI or Rubin DB. (2011). Causal inference using potential outcomes.

Journal of the American Statistical Association.

5.2 Positivity

Rubin DB. (1974). Estimating causal effects of treatments in

5.3 Consistency of randomized and nonrandomized studies. *Journal of educational Psychology* **66**: 688.

SUTVA.

6 TMLE flow chart

Van der Laan MJ, Polley EC, Hubbard AE. (2007). Super learner.

7 Data generation *Statistical applications in genetics and molecular biology* **6**.

7.1 Simulation

7.2 Data visualization

8 TMLE simple

implementation

8.1 Step 1: $Q_0(A, W)$

8.2 Step 2: $g_0(A, W)$

8.3 Step 3: HAW and ϵ

8.4 Step 4: \bar{Q}_n^*

8.5 Step 5: Inference

9 TMLE vs. AIPTW

10 TMLE using the Super-

Learner

11 R-TMLE

12 R-TMLE improving

prediction

13 Appendix One