

Generative Pattern Dissemination for Collaborative Intrusion Detection

A thesis presented for the degree of Master of Science
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July 2021

Abstract

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Chapter 1

Introduction

1.1 Motivation

1.2 Objectives

1.3 Structure

Chapter 2

Preliminaries

2.1 Intrusion Detection

This section introduces the topic of intrusion detection and some important subcategories in the context of the thesis. First, Intrusion Detection Systems (IDSs) are described and categorized according to different characteristics. The advantages and disadvantages of individual types of IDS are explained and examples are referred to individually. The topic of network flow monitoring is then addressed, since it is an essential component of network monitoring that is incorporated in the proposed architecture. The role of network flows in the context of network monitoring and management is motivated and the typical processes of a flow exporter are described. In the context of the shortcomings of conventional IDSs for protecting large scale systems against coordinated and distributed attacks Collaborative Intrusion Detection Systems (CIDSs) are introduced. For this purpose, it is first described what coordinated and distributed attacks are. Then it is explained what constitutes a CIDS, what requirements exist for the realization of CIDS, and what components and processes CIDS typically consist of.

2.1.1 Intrusion Detection Systems

Classic security mechanisms, such as encryption or firewalls, are considered as preventive measures for protecting IT infrastructures. However, in order to be able to react to security breaches that have already occurred, additional reactive mechanisms are required. To complement preventive measures, IDSs have been commercially available since the late 1990s [WM18, p. 27]. Generally, the main reason for operating an IDS is to monitor and analyze computer networks or systems in order to identify anomalies, intrusions or privacy violations [Hin+20]. Specifically, the following three significant advantages are pointed out [WM18, p. 391].

- IDSs can detect the preliminaries of attacks, in particular the organized gathering of information about networks and defense mechanisms (attack reconnaissance), and thus enable the prevention or mitigation of damage to information assets.
- IDSs can help protect information assets when known vulnerabilities cannot be fixed fast enough, notably in the context of an rapidly changing threat environment.
- The occurrence of unknown security vulnerabilities (zero day vulnerabilities) is not predictable, meaning that no specific preparations can be made for them. However, IDSs can identify processes in the IT system that deviate from the normal state and thus contribute to the detection of zero day attacks

For an effective IDS, it is important to be able to detect as many steps as possible within the prototypical attack sequence, also called kill chain [WM18, p. 393]. Since a successful intrusion into a system can be stopped at several points in this sequence, the effectiveness of the IDS increases with its functionality. The following categorization (see Figure 2.1) of intrusion attempts according to [Ken99] reflects parts of that chain.

Probing refers to the preambles of actual attacks, also known as attack reconnaissance. This includes obtaining information about an organization and its network behavior (footprinting) and obtaining detailed information about the used operating systems, network protocols or hardware devices (fingerprinting).

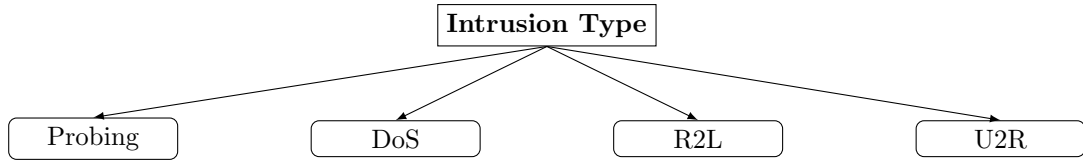


Figure 2.1: A categorization of intrusions into different subtypes

Denial of Service (DoS) refers to an attack aimed at disabling a particular service for legitimate users by overloading the target systems processing capacity. Remote to Local (R2L) attacks attempt to gain local access to the target system via a network connection. And one step further, User to Root (U2R) attacks start out with user access on the system and gain root access by exploiting vulnerabilities. Individual intrusion types can but do not have to be executed consecutively. For example, it is not mandatory to render a system incapable of action by DoS in order to subsequently gain local access to the target. However, this may be part of a strategy.

Additionally, IDSs are generally categorized by the detection scope and the employed attack detection method [Mil+15]. Hence, a distinction is made between Host-based Intrusion Detection Systems (HIDSs) and Network-based Intrusion Detection Systems (NIDSs). While a HIDS resides on a system, known as host, only monitoring local activities, a NIDS resides on a network segment and monitors remote attacks that are carried out across the segment. In general, HIDS are advantageous if individual hosts are to be monitored. NIDS, on the other hand, are able to monitor traffic coming in and out of several hosts simultaneously. The disadvantage of NIDS, however, is that attacks can only be detected if they are also reflected in the network traffic. Pioneering examples in the context of HIDS are the Intrusion-Detection Expert System (IDES) [LTG92] and the Multics Intrusion Detection and Alerting System (MIDAS) [Seb+88]. A prominent representative in the area of NIDS is NetSTAT [VK98] [VK99].

Furthermore, IDSs are categorized into misuse-based detection and anomaly-based detection (see Figure 2.2). A misuse-based approach defines a model that describes intrusive behaviour and compares the system or network state against that model. An anomaly-based IDS, on the other hand, creates a statistical baseline profile of the system's or network's normal state and compares it with monitored activities. The concept of the NIDS origins from [Den87].

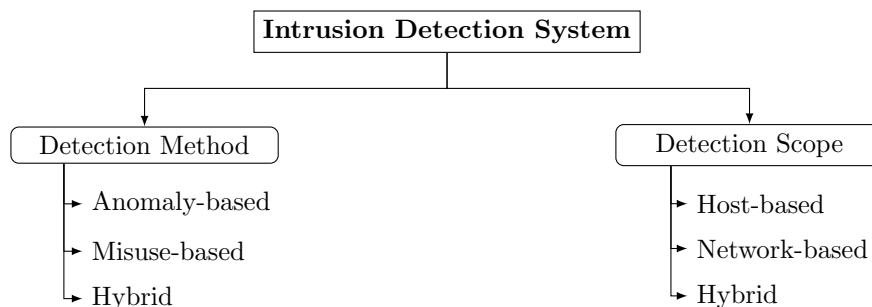


Figure 2.2: A taxonomy for IDS that distincts systems based on the utilized detection method or the scope in which it operates

Obviously, these two opposing approaches offer different advantages and disadvantages and are capable of complementing each other. Misuse-based systems can detect malicious behavior with a low false positive rate, but assume that the exact patterns are known. Typically, this method cannot detect novel [WM18, p. 403], metamorphic or polymorphic attacks [Szo05, p. 236]. An anomaly-based approach allows both known and unknown attacks to be detected, but the frequent occurrence of false-positive estimations is a major challenge. Given the amount of data that occurs in computer systems and networks nowadays, the generation of false alarms for even a fraction of this amount can render the IDS operationally unusable, since no network administrator can investigate such a large number of incidents in detail [Axe00]. Most implementations of misuse-based systems rely on the creation of signatures. A signature is similar to a collection of rules that describes an attack pattern. The most prominent signature-based IDS is Snort [Roe+99]. The payload-based anomaly detector PAYL [WS04] is an example for an anomaly-based system. Hybrid approaches are conceivable in order to circumvent the respective disadvantages of different subcategories of IDSs. The interested reader is referred to the following works [Dep+05] [ZZ06] [Bee21].

2.1.2 Network Flow Monitoring

Network monitoring is a key component for network management as network administrators derive decisions based on data that results from monitoring activities. By collecting data from network devices, such as switches, routers or clients, the current behaviour of the network is measured. Commonly, this behaviour has to meet some minimum application requirements, which can be summarized by the term Quality of Service (QoS) [TFW21, p. 406]. In this context, the most early and vague definition of a network flow was introduced as a sequence of packets traveling from the source to the destination [Cla88]. Here, no further characteristics of a flow are given and it is not clear how one flow is differentiated from another flow. Later in the 1990s, however, the demand arose for a finer-grained view of network traffic than that provided by interface-level counters, but without the disadvantage of the huge amounts of data generated by packet tracking. Evidently, the concept of network flows has filled this gap in demand and has gained a central role in network management and research today [TB11].

Since the first attempts at standardization in the 1990s through the efforts of the Internet Engineering Task Force (IETF), a number of proprietary standards have emerged as each network device vendor has implemented its own flow export protocol. In order to improve interoperability in the area of network flow measurement, the IETF, established the IP Flow Information Export (IPFIX) working group. This working group defined the IPFIX standard (RFC 5101), which defines the term network flow as follows.

Definition 1 (Network Flow). A network flow is an aggregation of all network packets that pass an observation point of a network during a certain time interval and share a set of common properties. These properties are defined as the result of applying a function to the value of

1. one or more packet, transport or application header fields,
2. one or more characteristics of the packet itself,
3. one or more fields derived from packet treatment.

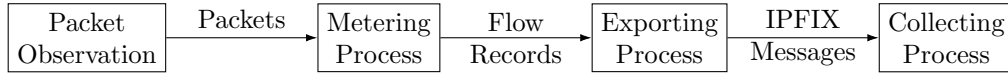


Figure 2.3: General Flow Monitoring Architecture

This definition is loose enough to cover the range from a flow containing all packets observed at a network interface to a flow that consists only of a single packet between two applications. Note, that this definition of the set of properties is also less strict than the conventional definition of the five-tuple consisting of source IP address, source port, destination IP address, destination port and protocol [Cla08].

In general, network flows can appear either as unidirectional flow, which aggregates all packets from one host to another host, or as bidirectional format, that aggregates all packets regardless of direction. Depending on which flow format and flow exporter is used, additional information, e.g. statistical calculations on bytes per second, can be obtained. Other common network flow protocols are NetFlow [Cla04], OpenFlow [McK+08] and sFlow [Pha].

Systems that generate flow data and extract additional information are called flow exporters. Generally, flow exporters are part of a general flow monitoring architecture [Hof+14], that consists of four different processes (see Figure 2.3). The packet observation is done on interfaces of packet forwarding devices by capturing network packets and executing specific preprocessing steps like timestamping and truncation. The process of flow metering describes the aggregation of packets into flow records. There, a set of functions, including packet header capturing, timestamping, sampling and classifying is applied on values of the packet stream listed above. Furthermore, flow records are maintained, which may include creating, deleting or updating records, or computing statistical flow features. After that, the exporting process places flow records in a datagram of the deployed export protocol and sends them to one or more collecting processes. Finally, the collection process is responsible for the reception, storage and preprocessing of flow records, produced by the preceding step. Typically, the collected data is analyzed. This can be done, for example, in the context of an IDS.

Using network flows for intrusion detection has several advantages over Deep Packet Inspection (DPI). For example, DPI requires highly complex and expensive infrastructure for storage and analysis of the data [Hof+14]. Since flow exporter setups rely on packet header fields and statistical aggregations, a significant data reduction is achieved, which is why an analysis of network flows is scalable and also applicable for high-speed networks [Hof+14]. In addition, discarding the payload results in a better compliance with data retention laws and privacy policies.

2.1.3 Collaborative Intrusion Detection

With the commercialization of cloud products, various aspects related to the security of computer networks have also become more stringent. Not only has part of the responsibility for securing servers and networks shifted from the end customer to the service provider. The fact that computing resources within large data centers that are operated by public cloud providers are publicly accessible offers, on the one hand, a large contiguous attack surface. And on the other hand, a large amount of potential resources for executing so-called large-scale coordinated attacks are accessible to attackers.

Typically, large-scale coordinated attacks target a large number of hosts which are spread over a wide geographical area [ZLK10]. There, attackers make use of automation and sophisticated tools to target all vulnerable services at once instead of manually targeting services [Sav05]. In the context of cloud environments, attackers can hijack mismanaged user accounts and hack into poorly secured cloud deployments [KG19]. In this way, attackers can gain access to a variety of different resources to spread attacks across as many sources as possible, thus avoiding detection by security systems.

According to [ZLK10], large-scale coordinated attacks are difficult to detect by isolated IDS, because of their limited monitoring scope. For instance, in [RGH12] the authors show that a distributed portscan can be executed with relatively few resources without being detected when deploying Snort IDS and a commercial firewall solution. The experimental results show that the detection by the IDS can be bypassed most effectively by distributing the sources of a scan, whereas the detection by the firewall can be evaded by slowing down single executions of scans.

In order to detect large-scale coordinated attacks, evidence of intrusions from multiple different sources need to be combined. This idea leads to the development of CIDS, where the aggregation and correlation of data originating from different IDSs creates a holistic picture of the network to be monitored and enables the detection of distributed and coordinated attacks [Vas16, p. 24]. CIDS are also a solution to zero day attacks, because information about novel attacks can be shared with participants of the CIDS in order to mitigate such attacks at an early stage. In addition to the aspect of improved detection, another advantage is the improved scaling for the protection of large IT systems. CIDSs can monitor large-scale networks more effectively with the realization of a loadbalancing strategy. By sharing IDS resources across different infrastructures peak loads can be served resulting in a reduced downtime of individual IDSs.

In general, a CIDS is defined as a network of several intrusion detection components that collect and exchange data on system security. The tasks of a CIDS can be allocated across two main components, namely the monitoring units and the analysis units. Monitoring units can be considered as conventional IDS that monitor a sub-network or a host and by that, generate low-level intrusion alerts. Analysis units are responsible for merging the low-level intrusion alerts and their further post-processing. This includes, for instance, the correlation of the alerts, the generation of reports or the distribution of the information to the participants of the network. The communication between the monitoring and analysis units is largely determined by the architecture of the CIDS.

CIDS architectures can be categorized into centralized, hierarchical and decentralized approaches [ZLK10] (see Figure 2.4). Centralized architectures [CM02][MI03], consisting of multiple monitoring units and a central analysis unit, suffer from a conceptual single point of failure (SPoF) and are limited in their scalability due to a bottleneck, which is introduced by the central analysis unit. However, in practice the SPoF can be avoided if individual components are implemented redundantly and form a centralized architecture only at the logical level. A bottleneck, on the other hand, is usually avoided by a distributed implementation of the logically centralized architecture. Hierarchical designs exhibit multiple monitoring and analysis units organized in a tree-based topology [PN97] [Zha+01] [Ngu+19]. These systems are restricted in their scalability by the respective instances on higher levels, whose failure results in a malfunction of the respective sub-trees [ZLK10].

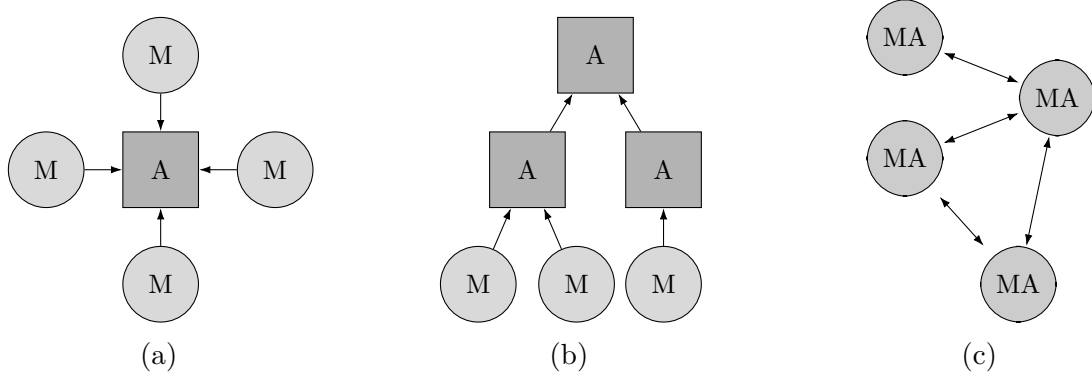


Figure 2.4: CIDS architectures: (a) hierarchical, (b) hierarchical or (c) distributed layout of monitoring (M) and aggregation units (A)

Again, such disadvantages only play a major role in non-redundantly implemented systems. Additionally, there exist approaches that are inherently distributed. Distributed architectures [JWQ03] [Fun+08] [Vas+15], wherein each participating system consists of both a monitoring and analysis unit and where the communication is based on some form of data distribution protocol, are considered as scalable by design. However, they depend on effective and consistent data dissemination and the data attribute selected for correlation may affect load distribution among participants [ZLK10].

The authors in [Vas+15] describe the most important requirements that a CIDS has to meet. Additionally, they further categorize the components of a CIDS by function. The following is a summary of these requirements and components. Six requirements are defined, namely accuracy, minimal overhead and scalability, resilience, privacy, self-configuration and lastly interoperability. In this context, accuracy generally describes a collection of evaluation metrics for assessing the performance of the CIDS. Frequently used metrics are, for example, the Detection Rate (DR), i.e. the ratio of correctly detected attacks to the total number of attacks, or the False Positive Rate (FPR), which sets the number of normal data classified as an attack in relation to the total number of normal data. Obviously, a CIDS is expected to have higher accuracy in terms of attack detection than isolated IDSs. The requirement for minimal overhead and scalability addresses the operational overhead and the scalability of the system. First, the algorithms and techniques for collecting, correlating, and aggregating data must require minimal computational overhead. Second, data distribution within the CIDS must be efficient. The performance required to operate the system should increase linearly with the resources used, so that computer systems of any size can be protected by the CIDS. This property can be measured in theoretical terms by considering the complexity of the algorithms used. In practical terms, the passed time from the collection of a data point to the decision-making process can be measured. Resilience describes the ability of the system to be resistant to attacks, manipulations and system failures. A distinction is made between external attacks, such as DoS, and internal attacks by infiltrated CIDS components. Moreover, it also covers fail-safety in general, which can be achieved, for example, by avoiding SPoFs.

With regard to the protection and regulation of privacy in the CIDS, a distinction is made between internal and external communication. Data that is exchanged internally in the CIDS network between members may contain potentially sensitive information,

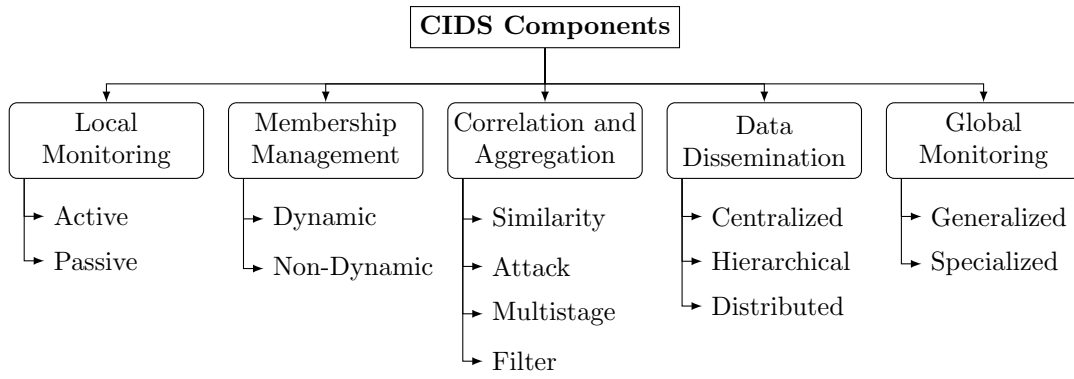


Figure 2.5: Components of CIDS according to functions

Such information should not be disclosed directly to other participants for reasons of data privacy. This includes, among other things, legal aspects when it comes to sharing log and network data. In connection with the resilience of the system, securing communication against third parties using cryptographic methods also plays a role and represents a major challenge, especially in dynamically distributed architectures. Self-configuration describes the degree of automation of a system with regard to configuration and operation. Particularly in distributed and complex architectures, a high degree of automation is desired in order to avoid operating errors and enable automatic resolution of component failures. Finally, individual components of the overall system, which were deployed in different system and network environments, should be able to interact with each other in the context of the CIDS. In addition to system-wide standards for data collection, processing and exchange, there exists a trade-off between interoperability and privacy.

The domains into which the components of the CIDS can be grouped are referred to as local monitoring, membership management, correlation and aggregation, data dissemination, and global monitoring. In the context of local monitoring, a distinction is made between active and passive monitoring. Active monitoring refers to the use of honeypots that reveal themselves as attack targets in the infrastructure in order to collect attack data. Passive monitoring involves intrusion detection activity at the host or network level, which in turn can be divided into misuse-based or anomaly-based methods according to the type of detection technique used (see Section 2.1.1).

Membership management refers to ensuring secure communication channels in the form of an overlay network. Generally, membership management is categorized according to the organization and structure of the system topology. In terms of organization, there are either static approaches, in which members are added or removed manually, or dynamic approaches, in which components are organized automatically via a central entity or a protocol. Furthermore, the structure of the overlay network is relevant for the type of communication in the CIDS network. This means that connections between the monitoring and analysis units are either centralized, hierarchical or distributed.

Before collected and analyzed data are shared with other participants in the CIDS network, the data is correlated and similar data points are aggregated. The main purpose of generating global and synthetic alerts is firstly to reduce the amount of alerts overall and secondly to improve data insights. Correlation mechanisms can be categorized into single-monitor and monitor-to-monitor approaches.

Single-monitor methods correlate data locally without sharing data with other monitor entities. Monitor-to-monitor approaches, on the other hand, share data with other monitoring units in order to correlate local data with shared data and thus enable insights that go beyond isolated methods. Further, a classification can be made according to the correlation techniques used, grouping four different approaches.

Similarity-based approaches correlate data based on the similarity of one or more attributes. For instance, [DW01] suggests using the 5-tuple information of the network data to detect duplicates within NIDSs. The computation of similarity can be done in a variety of ways. For example, [VS01] defines a similarity function for each attribute and computes the overall data similarity by combining the functions using an expectation of similarity. High-dimensional data is usually problematic, as the difficulty for an effective calculation of similarity increases with the number of attributes [ZLK09].

Attack scenario-based approaches detect complex attacks based on databases that provide patterns for attack scenarios [Gar+04] [DC02]. Such approaches have high accuracy for already known attacks. However, the accuracy decreases as soon as the patterns in the real data deviate from those in the database, since the definition of the scenario-rules are of a static quality in these approaches.

Multistage alert correlation aims to detect unknown multistage attacks by correlating defined pre- and post-conditions of individual alerts [CM02] [CLF03]. The idea behind the approach is based on the assumption that an attack is executed in preparation for a next step. The system states before and after an alert are modeled as pre- and postconditions, which are correlated with each other. While these approaches are more flexible than the all-static definition of attack scenarios, they still require the prior modeling of pre- and postconditions, which are based on expert knowledge.

Filter-based approaches filter irrelevant data in order to reduce the number of alerts within the intrusion detection context. For example, [PFV02] filters alerts by a ranking based on priorities of incidents. Priorities are calculated through comparing the target's known topology with the vulnerability requirements of the incident type. The rank that each alert is assigned to provides the probability for its validity. The accuracy of the filters is based on the quality of the description of the topology to be protected and require reconfiguration when changes are made to the infrastructure.

Data Dissemination describes the efficient distribution of correlated and aggregated data in the CIDS network. How the data is disseminated is strongly influenced by the topology and membership management of the system. Centralized topologies have a predefined flow of information from the monitoring units to the central analysis unit. If the system is organized hierarchically, information flows statically or dynamically organized from lower monitoring units in the hierarchy to higher units. Distributed topologies allow the use of versatile strategies, such as flooding, selective flooding or publish-subscribe methods.

Global monitoring mechanisms are needed for the detection of distributed attacks which isolated IDSs cannot detect due to the limited information base. Thus, the detection of distributed attacks relies on the insight obtained by combining data from different infrastructures. This means that global monitoring is strongly dependent on the employed correlation and aggregation techniques. The overall strategy of the CIDS is described by global monitoring and can have both generic and specific objectives.

2.2 Locality Sensitive Hashing

Finding similar objects, formally known as the nearest-neighbour search problem, is a central problem in computer science in general. And besides the exact search, it is also an important topic in the field of intrusion detection. For example, exact searches allow to compare the signatures of known malware with low false positive rates. Considering polymorphic attacks, however, it is essential to also detect all objects that are similar to the known attack and thus detect modified forms of it. In this context, this section presents a well-studied approach called *Locality Sensitive Hashing* (LSH) that solves an approximate version of the nearest-neighbour search problem by partitioning the search space with a hash function. This way, the searching problem is reduced to pairs that are most likely to be similar. Besides the application for solving the NN search problem, for which LSH was originally conceived, the concept has been proven to be effective for numerous other use cases, such as dimensionality reduction, clustering or classification. As the proposed generative pattern database integrates a locality-sensitive hash function for enabling both similarity search and data parallelism, LSH and a specific variant called *Random Projection* (RP) is described in detail in this section.

Section 2.2.1 introduces the approximate version of the nearest neighbour search problem as it is a prerequisite for the general definition of LSH. After that, Section 2.2.2 begins by clarifying the core idea of LSH and subsequently explains how to construct a locality-sensitive hash function. Lastly, a specific family of LSH that uses the cosine distance for similarity calculations, also known as *Random Projection* is presented in Section 2.2.3.

2.2.1 The Approximate Nearest Neighbour Problem

For general definitions of the nearest-neighbour search problem (NN) and its variants, a set of points $\mathcal{P} = \{\mathbf{p}_1, \dots, \mathbf{p}_N\}$, $N \in \mathbb{N}$ in a metric space (\mathcal{X}, d) with $\mathcal{P} \subset \mathcal{X}$ and where d is a metric on \mathcal{X} , i.e., a function $d : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$ is considered. It is assumed that d is a proper metric, which means that it is

1. *symmetric*: $d(\mathbf{p}, \mathbf{q}) = d(\mathbf{q}, \mathbf{p})$,
2. *reflexive*: $d(\mathbf{p}, \mathbf{q}) \leq 0$, $d(\mathbf{p}, \mathbf{q}) = 0 \iff \mathbf{p} = \mathbf{q}$ and satisfies the
3. *triangle inequality*: $d(\mathbf{p}, \mathbf{q}) \leq d(\mathbf{p}, \mathbf{s}) + d(\mathbf{s}, \mathbf{q})$.

Then, the general NN is stated as follows [IM98].

Definition 2 (Nearest-neighbour search problem). Construct a data structure so as to efficiently answer the following query: Given any query point $\mathbf{q} \in \mathcal{X}$, find some point $\mathbf{p} \in \mathcal{P}$ such that

$$\min_{\mathbf{p} \in \mathcal{P}} d(\mathbf{p}, \mathbf{q}). \quad (2.1)$$

As the algorithms in the presented approach operate on vectors of statistical flow features (see Section 2.1.2), the input set for specific definitions is usually restricted to \mathbb{R}^D , $D \in \mathbb{N}$. Thus, a specific example of Definition 2 in the context of this work includes high-dimensional data in $\mathcal{P} \in \mathbb{R}^D$ with $D \gg 1$ and could define d as, e.g., the euclidean distance. In this case, an exhaustive search would require a query time of $O(DN)$. Unfortunately, all exact algorithms that provide a better time complexity

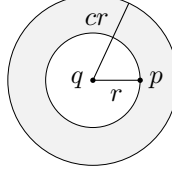


Figure 2.6: In the cr -approximate nearest-neighbour problem some point within cr is accepted, if there exists a point \mathbf{p} where $d(\mathbf{p}, \mathbf{q}) \leq r$.

than an exhaustive search require $O(2^D)$ space [Rub18]. This tradeoff between time and space complexity is usually referred to as “curse of dimensionality” and can only be resolved by accepting approximate solutions. The c -approximate nearest-neighbour problem (c -ANN) is defined as follows [IM98].

Definition 3 (c -Approximate nearest-neighbour search problem). For any given query point $\mathbf{q} \in \mathcal{X}$ and some approximation factor $c > 1$, find some point $\mathbf{p} \in \mathcal{P}$ such that

$$d(\mathbf{p}, \mathbf{q}) < c \cdot \min_{\mathbf{s} \in \mathcal{P}} d(\mathbf{s}, \mathbf{q}). \quad (2.2)$$

Thus, the distance from the query point \mathbf{q} to the approximate nearest neighbour \mathbf{p} is at most c times the distance to the true nearest neighbour \mathbf{s} . However, LSH does not solve the c -ANN directly. Instead, the problem is relaxed first by introducing the cr -approximate nearest-neighbour problem (cr -ANN) as follows [IM98].

Definition 4 (cr -Approximate nearest-neighbour search problem). For any given query point $\mathbf{q} \in \mathcal{X}$, some approximation factor $c > 1$ and some target distance $r > 0$, if there exists a point $\mathbf{p} \in \mathcal{P}$ where $d(\mathbf{p}, \mathbf{q}) \leq r$, then return a point $\mathbf{p}' \in \mathcal{P}$ where

$$d(\mathbf{p}', \mathbf{q}) \leq cr. \quad (2.3)$$

Figure 2.6 illustrates the cr -ANN. The target distance r represents the distance of the query object from its nearest neighbour. If there is such a point, the algorithm returns points within cr distance from the query object. Otherwise it returns nothing. It is shown that LSH can solve the c -ANN by solving the cr -ANN for different settings of r [IM98].

2.2.2 Locality-Sensitive Hash Functions

Introduced by Indyck and Motwani in 1998 [IM98] as an algorithm that solves the c -ANN, locality-sensitive hashing (LSH) has since been extensively researched and is now considered among the state of the art for approximate searches in high-dimensional spaces.¹ The basic idea of the approach is to partition the input data using a hash function that is sensitive to the location of the input within the metric space. This way, similar inputs collide with a higher probability than inputs that are far apart. Thus, LSH exhibits fundamental differences to conventional hash functions.²

A hash function is a function that maps a large input set to a smaller target set. The elements of the input set are called *messages* or *keys* and may be of arbitrary different

¹See [NBJ21] for an exhaustive survey of NN Techniques.

²Cryptographic and non-cryptographic hash functions are referred to as conventional hashing.

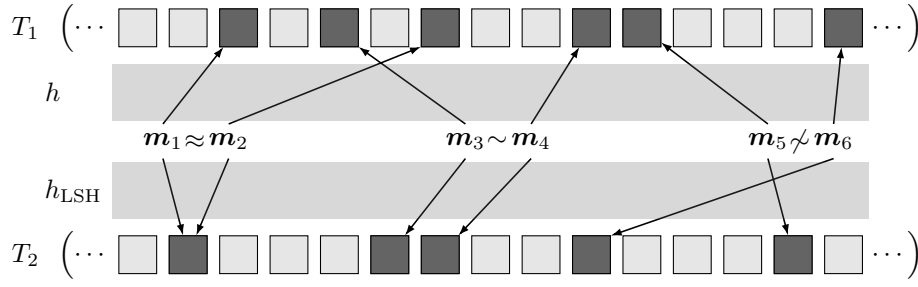


Figure 2.7: The behaviour of a conventional hashing function h and a locality-sensitive hashing function h_{LSH} when hashing very similar messages $\mathbf{m} \approx \mathbf{m}$, similar messages $\mathbf{m} \sim \mathbf{m}$ and non-similar messages $\mathbf{m} \not\sim \mathbf{m}$ into the slots of a hash table T_1 and T_2 respectively.

lengths. The elements of the target set are called *digests* or *hash values* and are of fixed size length. We define a conventional hash function as $h : \mathcal{M} \rightarrow \mathcal{B}$ where $\mathcal{M} \subset \mathcal{X}$ is the input set and $\mathcal{B} = \{0, 1\}^K$ with $K \in \mathbb{N}$ the target set of all bit sequences of fixed size K , with $K < D$. It follows that messages $\mathbf{m} \in \mathcal{M}$ can only be mapped to 2^K different binary strings $\mathbf{b} \in \mathcal{B}$. The probability that a given \mathbf{m} hashes to $\mathbf{b} = h(\mathbf{m})$ is $\frac{1}{K^2}$. Typically, conventional hashing is used for the realization of, e.g., hash tables, data integrity checks, error correction methods or database indexes. Such applications require a randomly uniform distribution of messages on hashes. Thus, a conventional hash function should therefore ideally assign hash values uniformly distributed with probability $\frac{1}{K^2}$ for all \mathbf{m} and all \mathbf{b} . A related property in this context is the probability of a *collision*. A collision occurs when two messages $\mathbf{m}_1 \neq \mathbf{m}_2$ are projected onto the same hash value $h(\mathbf{m}_1) = h(\mathbf{m}_2)$. For example, cryptographic hash functions are used in systems, where adversaries try to break such systems. Thus, different security requirements are defined for cryptographic hash functions [Wil, p. 349]. In particular, these hash functions are designed to be resistant against collisions. Applications that do not require the hash function to be resistant against adversaries, e.g., hash tables, caches or de-duplication, are usually implemented by using a non-cryptographic hash function that exhibits relaxed guarantees on the security properties in exchange for significant performance improvements. However, both cryptographic and non-cryptographic hash functions behave relatively similar with respect to the distribution of messages on hashes and the probability of a collision. In contrast, locality-sensitive hash functions behave more or less inversely as illustrated in Figure 2.7. A conventional hashing function h does not incorporate the similarity of messages into the calculation of the hash value. As a result, the messages are hashed evenly distributed into the slots of T_1 . A locality-sensitive hashing function h_{LSH} on the other hand, hashes more similar messages into the same slot or neighbouring slots of T_2 as the hashes reflect the similarity of the input messages. In this regard, the notation of a hash table is introduced. A hash table is defined as a tuple $T = (\mathbf{m}_{h(\mathbf{m})} \mid \mathbf{m} \in \mathcal{M})$ where \mathcal{M} is the set of all messages that are selected to be stored in T . Thus, we simply say that a message \mathbf{m} hashes to a slot $\mathbf{b} = h(\mathbf{m})$. Additionally, we define that the subset $h^{-1}(\mathbf{b})$ is made up of all the values associated with the key \mathbf{b} . Additionally, within an algorithm description the notation $T[\mathbf{b}]$ refers to the slot \mathbf{b} of the hash table T , which enables a clearer expression for accessing nested hash table data structures.

As a locality-sensitive hashing function can be constructed as a general concept, specific

families of functions can be derived. We refer to a *family* of hash functions $\mathcal{H} = \{h : \mathcal{M} \rightarrow \mathcal{B}\}$ as a collection of hash functions that have the same domain and range, share a basic structure and are only differentiated by constants. Three basic requirements are demanded for such a family of functions [LRU14, p. 99].

1. Close pairs of input should be hashed into the same bucket with higher probability than distant pairs.
2. Different functions within a family need to be statistically independent from one another, such that the FPR and FNR can be improved by combining two or more functions.
3. Functions need to be efficient, i.e., be faster compared to an exhaustive search.

The first step is to define LSH generally. Applied on the *cr*-ANN, the first requirement states, with high probability, two points \mathbf{p}, \mathbf{q} should hash to the same hash value if their distance is at most r , i.e., $d(\mathbf{p}, \mathbf{q}) \leq r$. And if their distance is at least cr , the points should hash to different hash values, i.e. $d(\mathbf{p}, \mathbf{q}) > cr$. Thus, A formal definition of a locality-sensitive hash function is given as follows [AI06].

Definition 5 (Locality-Sensitive Hash Function). Given a target distance $r \in \mathbb{R}, r > 0$, an approximation factor $c \in \mathbb{R}, c > 1$ and probability thresholds $p_1, p_2 \in \mathbb{R}$, a family $\mathcal{H} = \{h : \mathcal{P} \rightarrow \mathcal{B}\}$ is called (r, cr, p_1, p_2) -sensitive if for any two points $\mathbf{p} \in \mathcal{P} \subset \mathcal{X}, \mathbf{q} \in \mathcal{X}$ and any hash function h chosen uniformly at random from \mathcal{H} the following conditions are satisfied:

$$\begin{aligned} d(\mathbf{p}, \mathbf{q}) \leq r &\implies P[h(\mathbf{p}) = h(\mathbf{q})] \geq p_1, \\ d(\mathbf{p}, \mathbf{q}) \geq cr &\implies P[h(\mathbf{p}) = h(\mathbf{q})] \leq p_2. \end{aligned}$$

Ideally, the gap between p_1 and p_2 should be as big as possible as depicted in Figure 2.8c, which in fact represents an exact search. This is, as already discussed, no option due to its time and space requirements. Considering a single locality-sensitive function as shown in Figure 2.8a, where the probability gap between p_1 and p_2 is relatively close, the false negative rate would be relatively high. Increasing the gap would require to increase c and lead to a high number of false positives. Therefore, a single function would provide only a tradeoff. But it is possible to increase p_1 close to 1 and decrease p_2 close to $1/N$ while keeping r and cr fixed as shown in Figure 2.8b by introducing a process called *amplification*. Two different forms, namely the AND-construction and the OR-construction, can be applied.

By applying a logical AND-construction on \mathcal{H} the threshold p_2 is reduced. For that, K hash functions are sampled independently from \mathcal{H} and each point \mathbf{p} is hashed to a K -dimensional vector with a new constructed function $g \in \mathcal{H}^K$ as

$$g(\mathbf{p}) = [h_1(\mathbf{p}), h_2(\mathbf{p}), \dots, h_K(\mathbf{p})]. \quad (2.4)$$

Since all hash functions $\{h_1, \dots, h_K\} \in \mathcal{H}$ are statistically independent the product rule applies and for any two points \mathbf{p} and \mathbf{q} , a collision occurs if and only if $h_k(\mathbf{p}) = h_k(\mathbf{q})$ for all $k \in \{1, \dots, K\}$. The probability gap is then defined as follows:

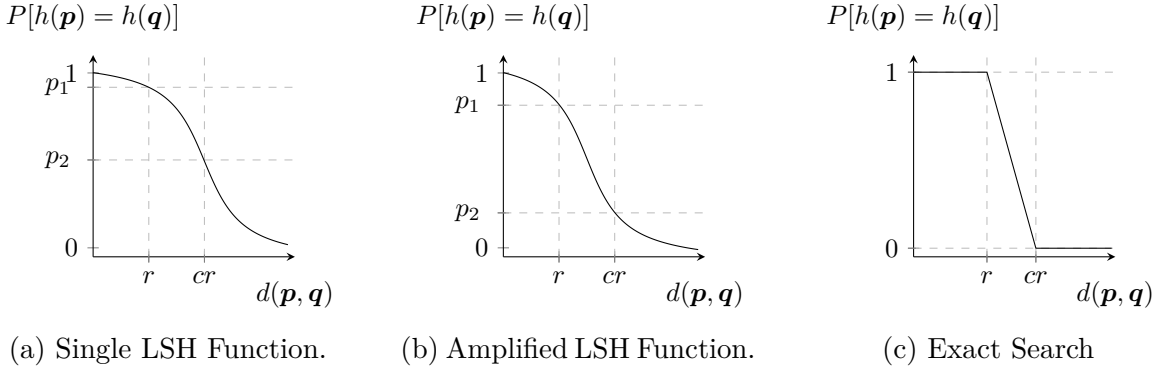


Figure 2.8: The behaviour of a (r, cr, p_1, p_2) -sensitive function in (a) and (b) (adapted from [LRU14, p. 100]) approaching the ideal probability gap in (c) resembling the behaviour of an exact search.

$$\begin{aligned}
 P[h_k(\mathbf{p}) = h_k(\mathbf{q})] \geq p_1 &\implies P[g(\mathbf{p}) = g(\mathbf{q})] \geq p_1^K \\
 P[h_k(\mathbf{p}) = h_k(\mathbf{q})] \leq p_2 &\implies P[g(\mathbf{p}) = g(\mathbf{q})] \leq p_2^K.
 \end{aligned}$$

Thus, by increasing K the threshold p_2 can be arbitrarily decreased and approaches zero. However, the AND-construction lowers both p_1 and p_2 . In order to improve p_1 , the OR-construction is introduced. For that, a number of $L \in \mathbb{N}$ functions $\{g_1, \dots, g_L\}$ are constructed, where each function g_l , $l \in \{1, \dots, L\}$ stems from a different family \mathcal{H}_l . Note, that the algorithm is successful, when the two points \mathbf{p}, \mathbf{q} collide at least once for some g_l . Therefore, hashing a point \mathbf{p} with each g_l results in the following probability for collision.

$$\begin{aligned}
 P[\exists l, g_l(\mathbf{p}) = g_l(\mathbf{q})] &= 1 - P[\forall l, g_l(\mathbf{p}) \neq g_l(\mathbf{q})] \\
 &= 1 - P[g_l(\mathbf{p}) \neq g_l(\mathbf{q})]^L \\
 &\geq 1 - (1 - p_1^K)^L
 \end{aligned}$$

As the AND-construction lowers both p_1 and p_2 , similarly the OR-construction rises both thresholds. By choosing K and L judiciously, p_2 approaches zero while p_1 approaches one. Both constructions may be concatenated in any order to manipulate p_1 and p_2 . Of course, the more constructions are used and the higher the values for the parameters K and L are picked, the more time is considered for the application of the function.

The general algorithm for solving the cr -ANN using LSH consists of two consecutive steps. First, a set of points is required for the construction of the data structure as described in Algorithm 1. For each function g_l a corresponding hash table T_l is initialized that will store all data points \mathbf{p}_n . In other words, all data points are preprocessed and stored L times. The resulting data structure represents the database, which is searched through, when answering a query. Note, that a common collision handling method, such as separate chaining for example, is applied if a certain slot is already occupied.

Answering a query point \mathbf{q} is done by hashing it multiple times for each g_l as in the preprocessing step (see Algorithm 2). Each time, the set of points \mathcal{P} , stored in the

Input: N points $\mathbf{p}_n \in \mathcal{P}$ with $n \in \{1, \dots, N\}$, $N \in \mathbb{N}$

Output: data structure $\mathcal{T} = \{T_1, \dots, T_L\}$

```

1:  $\mathcal{T} \leftarrow \emptyset$ 
2: construct hash functions  $g_1, \dots, g_L$  each of length  $K$  (see Equation 2.4)
3: for each  $g_l \in \{g_1, \dots, g_L\}$  do
4:    $T_l \leftarrow$  new hash table
5:   for each  $\mathbf{p}_n \in \mathcal{P}$  do
6:      $T_l[g_l(\mathbf{p}_n)] \leftarrow \mathbf{p}_n$ 
7:   add  $T_l$  to  $\mathcal{T}$ 
8: return  $\mathcal{T}$ 

```

Algorithm 1: LSH Preprocessing

corresponding hash table T_l at the slot $g_l(\mathbf{q})$, are retrieved. That is, identify all \mathbf{p}_n , such that $g_l(\mathbf{p}_n) = g_l(\mathbf{q})$. For each identified \mathbf{p}_n , a distance function evaluates if the distance $d(\mathbf{p}_n, \mathbf{q})$ is within the search perimeter cr . If positive, the point is added to the result set \mathcal{S} , which is returned at the end of the algorithm.

Input: a query point \mathbf{q} and data structure $\mathcal{T} = \{T_1, \dots, T_L\}$

Output: a set \mathcal{S} of nearest neighbours of \mathbf{q}

```

1:  $\mathcal{S} \leftarrow \emptyset$ 
2: for each  $g_l \in \{g_1, \dots, g_L\}$  do
3:    $\mathcal{S}_l \leftarrow T_l[g_l(\mathbf{q})]$ 
4:   if  $|\mathcal{S}_l| > 0$  then
5:     for each  $\mathbf{p}_n \in \mathcal{S}_l$  do
6:       if  $d(\mathbf{p}_n, \mathbf{q}) \leq cr$  then
7:         add  $\mathbf{p}_n$  to  $\mathcal{S}$ 
8: return  $\mathcal{S}$ 

```

Algorithm 2: LSH Query

With regard to preprocessing, the consideration of space complexity of Algorithm 1 is interesting, whereas the runtime of Algorithm 2 is the most relevant when examining the execution of queries. Fortunately, lower bounds on both quantities have been proven in [MNP06], resulting in the following theorem.

Theorem 6. Let (\mathcal{X}, d) be a metric on a subset of \mathbb{R}^D . Let be a (r, cr, p_1, p_2) -locality sensitive hash family \mathcal{H} and write $\rho = \frac{\log(1/p_1)}{\log(1/p_2)}$. Then for $\mathcal{P} \subset \mathcal{X}$ and $N = |\mathcal{P}|$ and for any $N \geq \frac{1}{p_2}$ there exists a solution to cr -ANN with space complexity $O(DN + N^{1+\rho})$ and query time of $O(N^\rho)$.

Therefore, it follows that the query time of LSH can only be sublinear, if $\rho < 1$, which is the case if the inequality $p_1 > p_2$ is satisfied.

2.2.3 Random Projection

This section presents a specific technique that is a locality-sensitive hashing function. The algorithm that bases on this technique is known as Gaussian Random Projection (GRP). This approach utilizes the cosine similarity of two real vectors in order to determine their similarity. In the course of this section, basic definitions for Cosine

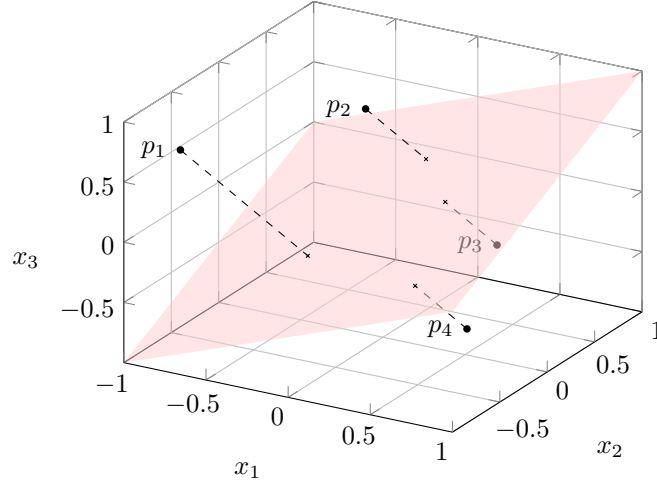


Figure 2.9: Illustration of a random hyperplane (red) partitioning the space

Distance and Cosine Similarity are introduced. Then, the individual calculation steps of the approach are specified. Finally, a visual proof verifies that gaussian random projection (GRP) is a form of LSH.

The cosine distance can be applied in euclidean spaces and discrete versions of euclidean spaces [LRU14, p. 95]. For two real vectors \mathbf{p}_1 and \mathbf{p}_2 , the cosine distance between is equal to the the angle between \mathbf{p}_1 and \mathbf{p}_2 , regardless of the dimensionality of the space. Note, that by applying the arc-cosine function, the result is in the range $[0, 180]$. The following definition formalizes what has been stated so far.

Definition 7 (Cosine Distance). Given two vectors \mathbf{p}_1 and \mathbf{p}_2 , the cosine distance $\theta(\mathbf{p}_1, \mathbf{p}_2)$ is the dot product of \mathbf{p}_1 and \mathbf{p}_2 divided by their euclidean distances from the origin (L_2 -norm):

$$\theta(\mathbf{p}_1, \mathbf{p}_2) = \cos^{-1} \left(\frac{\mathbf{p}_1^\top \mathbf{p}_2}{\|\mathbf{p}_1\| \|\mathbf{p}_2\|} \right). \quad (2.5)$$

The angle θ can be normalized to the range $[0, 1]$ by dividing it by π . This way, the cosine similarity is simply given by the following definition.

Definition 8 (Cosine Similarity). The cosine similarity is computed as

$$1 - \frac{\theta(\mathbf{p}_1, \mathbf{p}_2)}{\pi} \quad (2.6)$$

Introduced in [Cha02], the GRP is defined as follows. Given a point $\mathbf{p} \in \mathcal{P} \subset \mathbb{R}^D$ and a randomly selected hyperplane defined as $\mathbf{M} = (a_{ij}) \in \mathbb{R}^{D \times K}$ where $a \sim \mathcal{N}(0, I)$, a *gaussian random projection (GRP)* aims to (I) reduce the dimensionality from D to K dimensions and (II) provide a binary encoding by first projecting \mathbf{p} onto \mathbf{M} and subsequently applying the sign function to each element of the result, which can be formalized as

$$h(\mathbf{p}) = [h(\mathbf{p}, a_1), \dots, h(\mathbf{p}, a_k)] \text{ with } h(\mathbf{p}, a) = \text{sign}(\mathbf{p}^\top a) \quad (2.7)$$

$$\text{with } \text{sign}(x) = \begin{cases} 0 & \text{if } x < 0, \\ 1 & \text{if } x \geq 0. \end{cases} \quad (2.8)$$

An illustration of a random hyperplane that dissects the three-dimensional space and partitions the data space is given in Figure 2.9. The resulting digest is a binary vector $h(\mathbf{p}) = \mathbf{b} \in \mathcal{B}$ with $\mathcal{B} = \{0, 1\}^K$ that is used as bucket index for storing \mathbf{p} in a hash table. For any two messages $\mathbf{p}_1, \mathbf{p}_2$, the probability of being hashed to the same bucket increases with a decreasing distance, given as

$$P[h(\mathbf{p}_1) = h(\mathbf{p}_2)] = 1 - \frac{\theta(\mathbf{p}_1, \mathbf{p}_2)}{\pi}. \quad (2.9)$$

For a visual proof of the claim in Equation 2.9 consider Figure 2.10, where two vectors \mathbf{p}_1 and \mathbf{p}_2 , regardless of their dimensionality, define a plane and an angle θ in this plane. Pick a hyperplane r that intersects the plane that is spanned by \mathbf{p}_1 and \mathbf{p}_2 in a line (depicted as a red dashed line). Actually, a normal vector r_0 is randomly selected and r is the set of points whose dot product with r_0 is zero. Since \mathbf{p}_1 and \mathbf{p}_2 are on different sides of the hyperplane, their projections given by $\mathbf{p}_1^\top r_0$ and $\mathbf{p}_2^\top r_0$ will have different signs. Such a scenario, where two points have different signs, is interpreted as a notion of dissimilarity. Thus, the hyperplane acts as a clustering primitive that partitions the original input set into two disjunct sets.

The opposite scenario is illustrated by a random normal vector r'_0 that is normal to the hyperplane r' , which is represented by the blue dashed line. Both $\mathbf{p}_1^\top r'_0$ and $\mathbf{p}_2^\top r'_0$ will have the same sign. This in turn is interpreted as a notion of similarity, since both points are clustered into the same set. All angles between the intersection line of the random hyperplane and the plane spanned by \mathbf{p}_1 and \mathbf{p}_2 are equally likely. Thus, the probability that the hyperplane looks like the red line is θ/π and like the blue line $1 - \theta/\pi$.

Therefore, GRP is a $(r, cr, (1 - r/\pi), (1 - cr/\pi))$ -sensitive family for any r and cr . As already explained in Section 2.2.2, such a family can be amplified as desired. The AND-construction refers to the selection of a number of K different random hyperplanes r_k . According to the construction in Equation 2.7, all projections $\mathbf{p}_n^\top r_k$ for a single point are concatenated into a K -bit vector. Likewise, the OR-construction refers to the initialization of a number of L such AND-constructions. The algorithmic procedures for preprocessing and queries from Algorithm 1 and Algorithm 2 can be applied without change.

2.3 Gaussian Mixtures

2.3.1 The Gaussian Distribution

The Gaussian normal distribution forms the basic building block for GMMs. Depending on the observed random variable, different types of normal distributions exist. In particular, the multivariate normal distribution is focused on when considering statistical

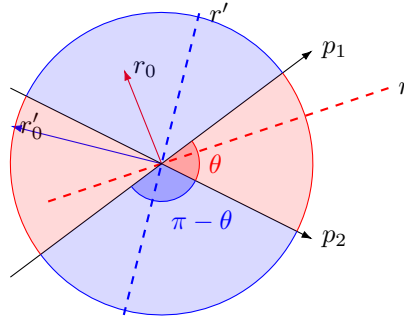


Figure 2.10: Visual Proof of claim in equation 2.9

flow features, which are typically continuous and high dimensional. In the following, different definitions for the normal distribution are introduced and important properties are presented that are essential for calculations during the learning phase of GMMs.

Let be a multivariate random variable $\mathbf{X} = (X_1, \dots, X_D)^T$, where each element X_d with $d \in \{1, \dots, D\}, D \in \mathbb{N}$ is a univariate random variable that follows a normal distribution, which is referred to as $X_d \sim \mathcal{N}(\mu, \sigma^2)$.

Definition 9 (Univariate Gaussian Distribution). [DFO20, p. 175] A continuous, univariate random variable X is said to follow a normal distribution, if it exhibits a probability density function

$$p(x|\mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(x - \mu)^2}{2\sigma^2}\right),$$

with $x \in \mathbb{R}$ and where μ refers to the mean and σ^2 is the variance of the distribution. Then, if \mathbf{X} follows a normal distribution, this is expressed as a multivariate Gaussian distribution, denoted by $\mathbf{X} \sim \mathcal{N}_D(\boldsymbol{\mu}, \boldsymbol{\Sigma})$, which is fully described by its mean vector $\boldsymbol{\mu}$ and its covariance matrix $\boldsymbol{\Sigma}$.

Definition 10 (Multivariate Gaussian Distribution). [DFO20, p. 175] A multivariate random variable \mathbf{X} follows a normal distribution, if it is described by a probability density function

$$p(\mathbf{x}|\boldsymbol{\mu}, \boldsymbol{\Sigma}) = (2\pi)^{-\frac{D}{2}} |\boldsymbol{\Sigma}|^{-\frac{1}{2}} \exp\left(-\frac{1}{2}(\mathbf{x} - \boldsymbol{\mu})^T \boldsymbol{\Sigma}^{-1}(\mathbf{x} - \boldsymbol{\mu})\right),$$

with $\mathbf{x} \in \mathbb{R}^D$. The mean vector specifies the estimate of the expected value of the distribution, with each of its components describing the mean μ of the corresponding dimension. The empirical covariance $\boldsymbol{\Sigma}$ models the estimate of the variance along each dimension as well as the correlation between the different dimensions. The diagonal elements of $\boldsymbol{\Sigma}$ describe the variance of the random variable corresponding to the respective dimension and the off-diagonal elements describe the covariance relationship between the respective random variables.

An illustration of the influence of the described parameters on the location and shape of a multivariate distribution is given in Figure 2.11. Specifically, three bivariate normal distributions are considered, whose random variables each have different values with respect to their correlation, while the mean vector is the same for all distributions.

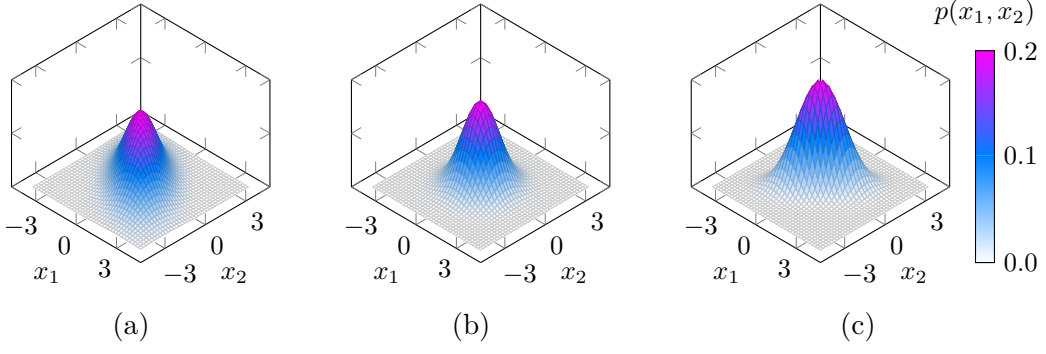


Figure 2.11: Bivariate gaussian distributions exhibit different shapes with a changing correlation value between the random variables x_1 and x_2 : (a) negative, (b) zero and (c) positive correlation

Having introduced the basic definition of Gaussian distributions, it is now examined how they can be manipulated to obtain information necessary for parameter learning of Gaussian mixture models. Two practical algebraic properties of normal distributions, namely closure under *conditioning* and *marginalization* are detailed for this purpose. Being closed under conditioning and marginalization in this case means that when one or more components of a Gaussian distribution is marginalized out or conditioned on, that the resulting distribution is still Gaussian. This not only distinguishes Gaussian distributions from other distributions, but also makes them easier to handle mathematically. Since both marginalization and conditioning act on subsets of the original distribution, the following notation is introduced first. Considering a multivariate Gaussian random variable $\mathbf{X} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$, we partition \mathbf{X} according to

$$\mathbf{X} = \begin{bmatrix} \mathbf{X}_M \\ \mathbf{X}_N \end{bmatrix},$$

with $\mathbf{X}_M \in \mathbf{R}^M$, where $M < N$, and $\mathbf{X}_N \in \mathbf{R}^N$, where $N = D - M$. In general, \mathbf{X}_M is chosen to be the first M elements of \mathbf{X} and \mathbf{X}_N the rest. Accordingly, $\boldsymbol{\mu}$ and $\boldsymbol{\Sigma}$ are partitioned as

$$\begin{bmatrix} \mathbf{X}_M \\ \mathbf{X}_N \end{bmatrix} \sim \mathcal{N} \left(\begin{bmatrix} \boldsymbol{\mu}_M \\ \boldsymbol{\mu}_N \end{bmatrix}, \begin{bmatrix} \boldsymbol{\Sigma}_{MM} & \boldsymbol{\Sigma}_{MN} \\ \boldsymbol{\Sigma}_{NM} & \boldsymbol{\Sigma}_{NN} \end{bmatrix} \right).$$

With this form, it is now possible to express the extraction of partial information from multivariate probability distributions by means of marginalization.

Definition 11 (Marginal of a Gaussian Distribution). [DFO20, p. 177] Given $\mathbf{X} \sim \mathcal{N}_D(\boldsymbol{\mu}, \boldsymbol{\Sigma})$, with partitions $\mathbf{X}_M, \mathbf{X}_N$, the distributions of \mathbf{X}_M and \mathbf{X}_N are called marginals and their corresponding probability density function can be obtained by

$$p(\mathbf{x}_M) = \int p(\mathbf{x}_M, \mathbf{x}_N) d\mathbf{x}_N.$$

Furthermore, each partition $\mathbf{X}_M, \mathbf{X}_N$ only depend on its corresponding entries in $\boldsymbol{\mu}$ and $\boldsymbol{\Sigma}$, which leads to the following theorem.

Theorem 12. [DFO20, p. 177] The marginal distribution of a Gaussian distribution is also a Gaussian and determined by

$$\mathbf{X}_M \sim \mathcal{N}(\boldsymbol{\mu}_M, \boldsymbol{\Sigma}_{MM}).$$

The conditional Gaussian is typically utilized in the context of posterior distributions, such as in the process of density estimation of GMMs, and is defined as follows.

Definition 13 (Conditional of a Gaussian Distribution). [DFO20, p. 177] Given $\mathbf{X} \sim \mathcal{N}_D(\boldsymbol{\mu}, \boldsymbol{\Sigma})$, with partitions $\mathbf{X}_M, \mathbf{X}_N$, the conditional distribution is defined as

$$\begin{aligned} p(\mathbf{x}_M | \mathbf{x}_N) &= \mathcal{N}(\boldsymbol{\mu}_{M|N}, \boldsymbol{\Sigma}_{M|N}), \\ \boldsymbol{\mu}_{M|N} &= \boldsymbol{\mu}_M + \boldsymbol{\Sigma}_{MN} \boldsymbol{\Sigma}_{NN}^{-1} (\mathbf{x}_N - \boldsymbol{\mu}_N), \\ \boldsymbol{\Sigma}_{M|N} &= \boldsymbol{\Sigma}_{MM} - \boldsymbol{\Sigma}_{MN} \boldsymbol{\Sigma}_{NN}^{-1} \boldsymbol{\Sigma}_{NM}. \end{aligned}$$

Theorem 14. [DFO20, p. 177] The conditional distribution of a Gaussian distribution is also a Gaussian and defined by

$$\mathbf{X}_{M|N} \sim \mathcal{N}(\boldsymbol{\mu}_{M|N}, \boldsymbol{\Sigma}_{M|N}).$$

A line of arguments proving the stated theorems can be found in section 2.3 in [Bis06]. An example for marginal and conditional Gaussians can be found in Figure 2.12. The functions of $p(x_M)$ and $p(x_N)$ are plotted on the side grids. The conditional cuts through the plot of the joint distribution $p(x_M, x_N)$.

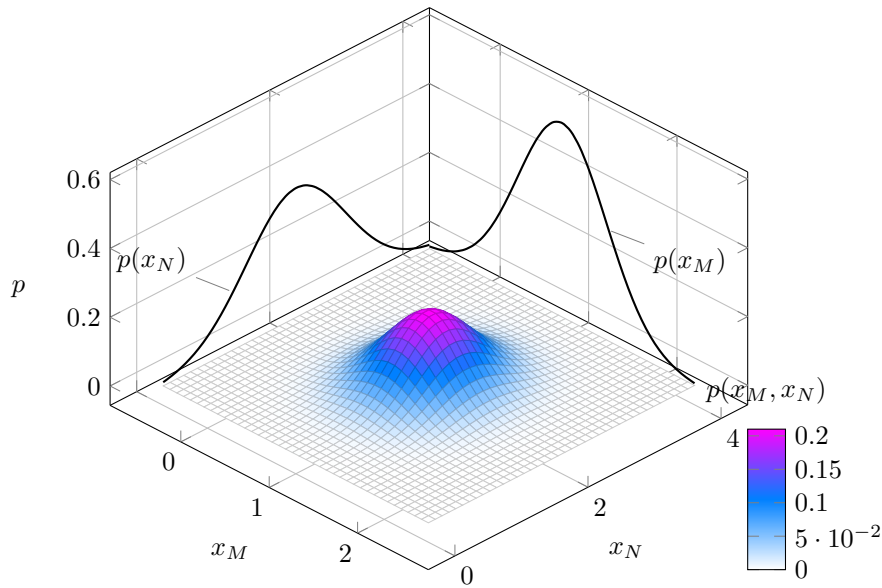


Figure 2.12: Marginals $p(x_M)$, $p(x_N)$ and Conditional Gaussian $p(x_{M|N})$

2.3.2 The Gaussian Mixture Model

2.3.3 The Expectation Maximization Algorithm

2.4 Principal Component Analysis

2.4.1 Dimensionality Reduction

2.4.2 Signal and Noise

2.4.3 Formal Description

Chapter 3

State of the Art

- 3.1 Data Dissemination in Collaborative Intrusion Detection
- 3.2 Similarity Hashing in Malware Detection
- 3.3 Generative Algorithms and Intrusion Detection

Chapter 4

Generative Pattern Database

Three main challenges in the context of data dissemination in CIDS were identified. First, intrusion related data is usually of sensitive nature. Thus, the exchange mechanism must not compromise any policies and regulations related to data *privacy*. At the same time, the usability of the data has to be preserved. Second, the data that is subject of the exchange may exhibit large volumes. That constitutes a challenge, since the dissemination is desired to be executed with *minimal overhead* in a timely and scalable fashion. Lastly, the *interoperability* of the CIDS with existing local IDS is an important aspect that influences the practical adoption into security architectures. In summary, existing approaches for data dissemination mainly provide mechanisms for exchanging alert data or single attributes, e.g. IP addresses, as they focus on the correlation of intrusion detection incidents that originate from different sensors. The exchange of actual training data is neglected, possibly due to high data volumes. Thus, these systems lack of mechanisms for the extraction and global persistence of novel attack patterns, e.g. from zero day exploits, that can be used for the training of an intrusion detection sensor.

The approach that is presented in this chapter exchanges attack patterns by sharing generative machine learning models that have been trained on partitions of similar data points. Such a model-based dissemination enables the receiving side to sample a synthetic dataset that enhances existing local datasets. This provides two main advantages. First, no original data leaves a local network and therefore does not violate any privacy restrictions. Second, the data is compressed considerably by representing it in form of a generative model. In order to make that mechanism scalable, the monitored data is clustered using random projections. This way, similar data points are partitioned into globally common clusters, which is exploited as a data parallelism mechanism. Given that, bursty workloads can be served effectively in a cloud deployment. Furthermore, this mechanism enables a similarity-based correlation of distributed intrusion events. The integration of both a similarity based correlation of intrusion incidents and a mechanism for sharing attack knowledge makes it possible to extract novel patterns of distributed attacks and provide them globally within the CIDS, resulting in an improved attack detection.

Section 4.1 introduces the idea and key concepts of the approach. After that, Section 4.2 specifies the proposed architecture in detail. A comprehensive description of algorithms and processing steps are described in Section 4.3.

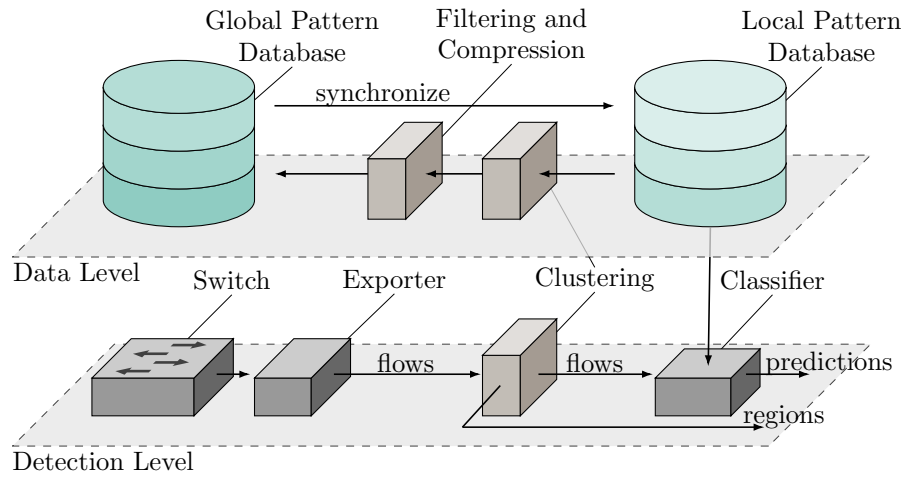


Figure 4.1: Example integration of the generative pattern database into a generic NIDS deployment, separated by data and detection level

4.1 High Level Overview

Several members exist in the CIDS, each of which manages an isolated IDS. Every IDS operates according to a specific set of rules, that is essentially based on the content of a local database. The goal of the generative pattern database is to close the knowledge gaps of local databases and thus increase the detection rate of associated IDSs. By providing a *global view* on all local databases, individual IDSs can benefit from the collective knowledge of the CIDS.

Section 4.1.1 starts with a reference example to illustrate the idea that is described above and discusses the integration of the CIDS into existing infrastructures. Subsequently, Section 4.1.2 and Section 4.1.3 show the key concepts that enable data distribution and correlation under the given requirements. Finally, Section 4.1.4 combines the individual elements to present the strategy for the creation and utilization of the global view.

4.1.1 Example Integration

An exemplary integration of the CIDS into a generic NIDS is shown in Figure 4.1. The exemplary NIDS deployment consists of three components, that can be found on the detection layer. A flow exporter computes statistical flow features based on the network packets of a switch. A discriminative model serves as a classifier that operates on the specific feature set that the exporter extracts. After completing the training of a classifier instance on a given dataset, it is deployed within the detection pipeline. There, the classifier receives a stream of network flows and predicts them.

The CIDS mainly integrates at the data level, where the training data for the classifier is provided by the *local pattern database*. At this point, the local pattern database only contains the *local view* of the intrusion detection data from that particular member. In order to provide a global view, a synchronization process between its local pattern database and the *global pattern database* has to be initiated. Before the data is transferred to the global pattern database, it is subject to a set of clustering, filtering and compression operations. This way, data privacy is maintained and overhead is minimized by reducing the data volume.

On the receiving side, the global pattern database combines data from all members into a global view. Upon each update of the global pattern database, the new state of the global view is synchronized to each local pattern database and subsequently enhances the classifier on the detection level by extending the local intrusion detection dataset. Furthermore, an identical clustering operation as on the data level is applied on the detection level. Each incoming flow is assigned to a certain cluster, which is referred to as *region*. While the predictions from the classifier are suitable for detecting attacks that are known to the CIDS, regions are leveraged for the detection of novel data patterns and similarity-based correlations that uncover large-scale coordinated attacks, which are executed on the resources of multiple CIDS members simultaneously.

4.1.2 Clustering

The clustering operation has to meet certain requirements in this approach. First, the results of the clustering operation should be consistent while it is executed among all members of the CIDS in a distributed fashion. Additionally, the algorithm should be scalable, since it is to be applied on whole databases on the data level and on streams of live data on the detection level. Given these requirements, gaussian random projection (GRP) (see Section 2.2.3) is selected. By using GRP, real data points are clustered according to their angular distance. Furthermore, the projection result is a binary string, which can be used for storing similar data points into a common bucket of a hash table by using the binary string as an index. In the context of the generative pattern database, the combination of GRPs and hash tables is exploited as the main controlling primitive for data persistence and retrieval. Instead of using randomly selected projection planes, a shared seed results in the application of a common projection function among all members of the collaboration. In other words, similar data points from different datasets are indexed to a common global bucket, i.e. region. Each region is subject to the transformations individually, which is utilized as a data parallelism mechanism. Thus, this approach is natively suited for cloud deployments where bursty workloads can be served effectively by balancing the load on an arbitrary number of instances. Lastly, this mechanism enables a similarity-based correlation of distributed intrusion events. As incoming data is monitored on the detection level, the clustering is applied, which results in a pattern that can be used for novelty checks or global occurrences within the CIDS.

4.1.3 Filtering and Compression

Two types of data are extracted within individual regions. First, metadata of local datasets is collected by counting label occurrences, which serve as indicator for determining if the respective region needs to be subject to the second extraction type. Second, models that are trained with generative algorithms on local attack data are the exchange medium for disseminating information within the CIDS. This provides two main advantages. For one, no original data leaves a local network and therefore does not violate any privacy restrictions. For another, the data is compressed considerably by representing it in form of a generative model.

4.1.4 Global View

As shown in Figure 4.2, each view is partitioned by a common projection function into an identical set of regions. Each local view contains original datapoints from the local dataset of the respective CIDS member. In this example, there exist three different classes globally, which occur differently in each local dataset. Examining a specific region, the combination of unique classes within all local views determines its complexity on a global level. For instance, the yellow region (global view) is simple, because within all local views, there occurs only a single class. A complex region in the global view, on the other hand, is formed by the occurrence of multiple classes within the same region in all local views. If a region in the global view contains more than one class, it potentially exhibits a non-linear decision boundary, hence it is called complex. This complexity information is distributed to all members of the CIDS by tagging the corresponding local regions with the complexity state of the region from the global view. After that, all local regions that are tagged as complex are modeled by a generative algorithm by using the corresponding local data points as training data. Subsequently, the resulting models are transferred to the global view. A synchronization process disseminates the region complexity estimations and the generative models to all local views. Within each local view, data points are sampled from generative models which are subsequently assembled into a synthetic dataset. Finally, the synthetic datasets are blended into the respective local datasets for enhancing the subsequent training of discriminative models.

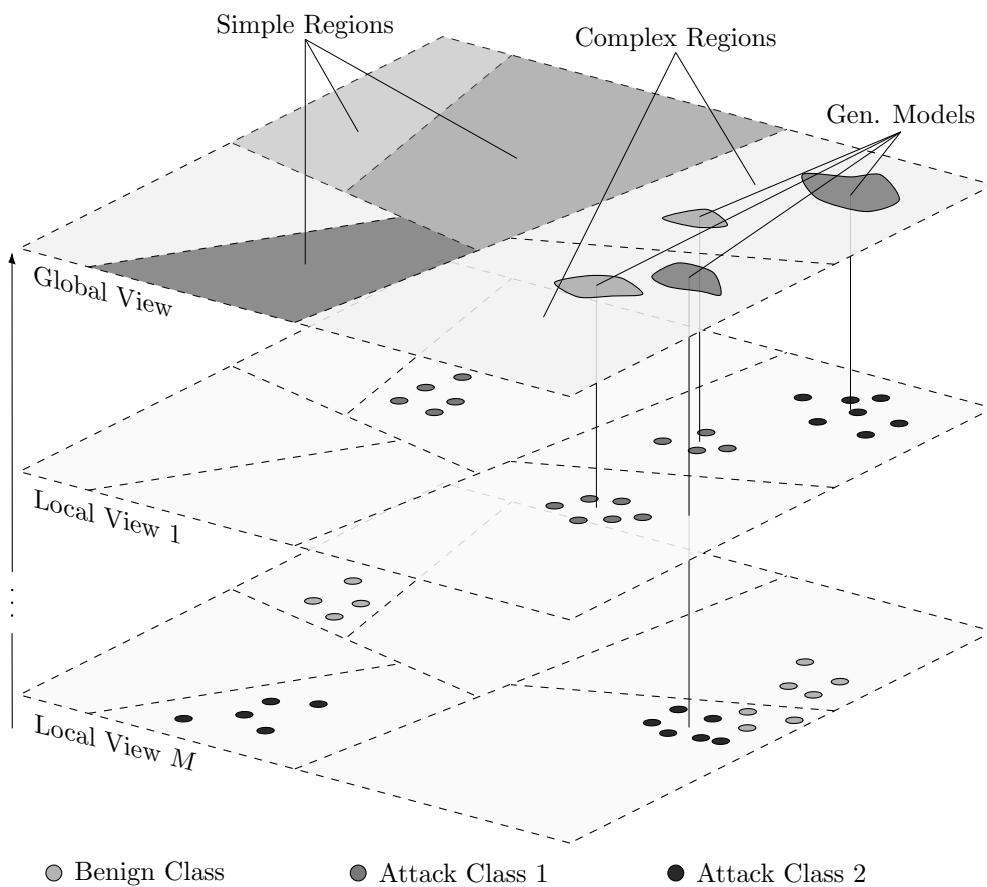


Figure 4.2: Building the global view by combining M local views

4.2 Architecture Specification

Logically, the proposed CIDS exhibits a hierarchical architecture (see Figure 4.3). For one, the global infrastructure G represents the collection of $M \in \mathbb{N}$ CIDS participants and their knowledge on an abstract level. For another, it provides specific services, that are globally available to each local infrastructure $L_m, m \in \{1, \dots, M\}$ that includes all CIDS components and services within the IT infrastructure boundaries of a corresponding CIDS member. Each local infrastructure L_m agrees to a specified feature extraction process that provides the monitoring data $\mathcal{X} \subset \mathbb{R}^D$ with a total number of features $D = |\mathbf{x}| \in \mathbb{N}$ for the attack detection. As the deployed NIDS is considered to be a supervised classification task, the ultimate goal is to find an approximation of an unknown target function $c : \mathcal{X} \rightarrow \mathcal{Y}$ that maps examples $\mathbf{x} \in \mathcal{X}$ to classes $y \in \mathcal{Y}$. In order to find an approximation $\hat{c} \sim c$, an individual training dataset $\mathcal{D}_m = \{(\mathbf{x}_n, y_n) : 1 \leq n \leq N_m\}$ of size $N_m = |\mathcal{D}_m| \in \mathbb{N}$ is provided in every L_m . True target values $c(\mathbf{x}) = y$ are given by the domain expert that assembled \mathcal{D}_m . In addition, in the CIDS network, a common \mathcal{Y} is agreed upon, so that there is a global consensus on class memberships.

CIDS communication across local boundaries occurs exclusively in a vertical direction. Thus, the exchange of information between individual L_m takes place indirectly via the global pattern database (PDB_G) and the global event channel (C_G). Each L_m includes a local pattern database (PDB_{L_m}), a local event channel (C_{L_m}) and an event-based data processing pipeline that consists of four services, namely *Local Indexing*, *Complexity Estimation*, *Generative Fitting* and *Classifier Fitting*.

Each instance of a pattern database (PDB) is realized as a key-value store and depending on the scope different tasks are considered. Each PDB_{L_m} is responsible for storing \mathcal{D}_m and corresponding metadata. The PDB_G stores global metadata and the generative models that resemble the original data from each \mathcal{D}_m . The notation for operations on a PDB corresponds to the notation for hash table operations defined in Section 2.2.2. Note, that if a locality-sensitive hash function is used to construct a key, in practice a hash table will internally apply a non-cryptographic hash function on the key to ensure an even distribution of the keys across the slots.

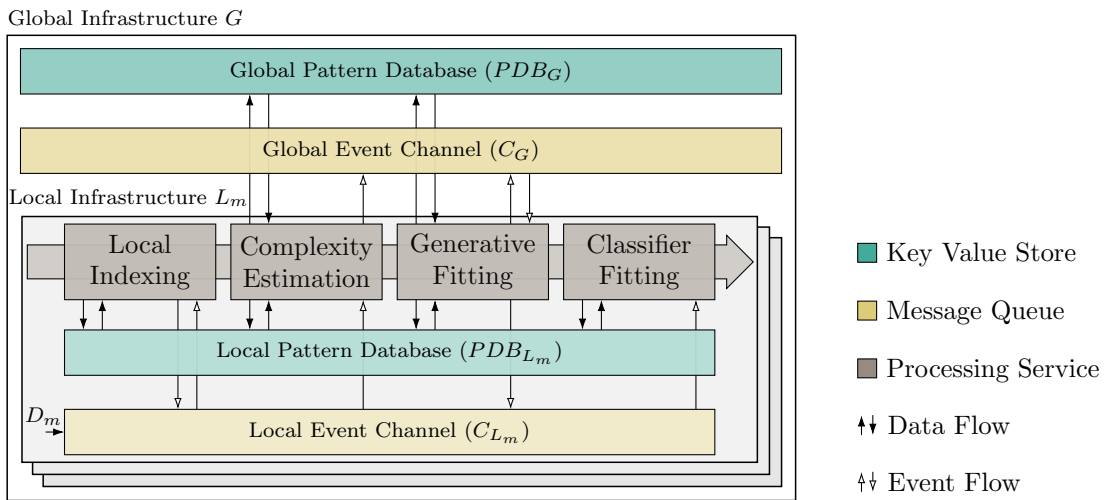


Figure 4.3: CIDS architecture illustrating the data and event flow between components within and across local infrastructure boundaries

Nonetheless, the clustering of neighbouring points into common slots is still ensured in this scenario. Each event channel C provides a topic-based publish-subscribe messaging mechanism that is mainly used to instantiate and distribute workloads among the service instances in the processing pipeline. Via the messaging system, service instances receive and emit events, on which upon the respective operations are triggered. Changes in a PDB result in responses that in turn are leveraged as the respective events. In this fashion, updates are propagated throughout the processing pipeline, ensuring a timely consistency among the pattern databases.

4.3 Service Specification

In Section 4.1, the roles of the clustering, filtering and compression operations within the architecture and the idea of the global view have been roughly explained. These concepts are implemented within the processing pipeline that has been referred to in Section 4.2 as four consecutive and event-based services, which are described in detail by focusing on a single service in each subsection.

4.3.1 Local Indexing

The local indexing service is responsible for the preprocessing and local storage of D_m . As already described in Section 4.1.2, the data is organized in regions. This means that individual data points are first assigned to a region using a GRP. By doing that, a hash of the data point is computed. Based on the generated hash value, a key is constructed that is used to persist that data point in the respective PDB_{L_m} . According to the properties of a locality-sensitive hash function, similar data points are assigned to a common region and thus form a closed processing unit for subsequent operation steps. If a region is initialized or an update is made to an existing region, e.g., due to the occurrence of new data, events are emitted to inform the subsequent service.

First, an intrusion detection dataset D_m is sent to one or more service processors via the C_{L_m} . Second, the incoming stream of pairs of data points and labels $(\mathbf{x}_n, y_n) \in D_m$ is ingested and buffered until a batch $X = (\mathbf{x}_1, y_1), \dots, (\mathbf{x}_B, y_B)$ of size $B \in \mathbb{N}$ has been accumulated. Then, X is preprocessed and inserted into the PDB_{L_m} as described in Algorithm 3. In words, a flow-feature vector \mathbf{x} is scaled to the range $[-1, 1]$ by applying a feature-wise min-max normalization given by

$$\mathbf{x}' = (b - a) \frac{\mathbf{x} - \min \mathbf{x}}{\max \mathbf{x} - \min \mathbf{x}} + a \quad (4.1)$$

where $a = -1$ and $b = 1$. After that, the scaled data point \mathbf{x}' is subject to both a locality-sensitive hashing function h and a non-cryptographic hashing function g . In this particular architecture, h is a GRP with a global seed for the initialization of the projection plane \mathbf{M} (see Section 2.2.3), such that regions $r = h(\mathbf{x}')$ across local infrastructures are comparable and consistent.¹ Since the data is organized in regions, a nested scheme is applied for the insertion of pairs of datapoints and labels as depicted in Figure 4.4.

¹Here, the words hash value and region are used synonymously

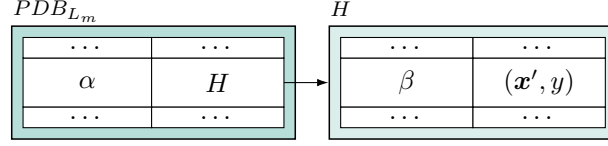


Figure 4.4: Nested indexing in a local pattern database.

In fact, the pairs within a region are further partitioned into disjoint subsets according to the true class label y . This means that for each subset of the data of a particular label within a region, a separate hashtable is initialized and inserted into the PDB_{L_m} as a second level. Thus, for the persistence of a pair (\mathbf{x}', y) , two keys α, β are constructed (see Lines 6-7 in Algorithm 3). The key α is a concatenation of the prefix constant p_x , the bit-string r and the label y . This way, the data is partitioned primarily by its region and secondarily by its label as described above. The key β is the result of the non-cryptographic hashing function $g(\mathbf{x}')$, which serves as a mechanism for deduplicating identical \mathbf{x}' . Additionally, a third key γ is constructed by concatenating the prefix constant p_y and the bit-string r . As it is important to retrieve all existing labels within a region efficiently in a processing step of the subsequent service, γ is used for storing the set of labels within a region as auxiliary metadata. Next, if not already present, a hash table is initialized and inserted into PDB_{L_m} using α . Likewise, if PDB_{L_m} at slot γ is empty, a new set² is initialized and inserted. After that, it is checked if the slot β of the hash table placed at α in PDB_{L_m} , is empty. In the positive case, the pair (\mathbf{x}', y) is inserted into that slot and the region r is inserted into the set \mathcal{R} . Otherwise, no data is inserted into the local pattern database and no region is added to \mathcal{R} . After processing a batch, the set of updated regions \mathcal{R} is emitted as events into C_{L_m} .

Input: Batch X

Output: Regions \mathcal{R}

```

1:  $\mathcal{R} \leftarrow$  new Set
2:  $\min \mathbf{x}, \max \mathbf{x} \leftarrow$  extract feature ranges from  $X$ 
3: for each  $(\mathbf{x}, y)$  in a batch do
4:    $\mathbf{x}' \leftarrow \text{normalize}(\mathbf{x})$  ► see Equation 4.1
5:    $r \leftarrow h(\mathbf{x}')$ 
6:    $\alpha \leftarrow \text{concatenate}(p_x, r, y)$ 
7:    $\beta \leftarrow g(\mathbf{x}')$ 
8:    $\gamma \leftarrow \text{concatenate}(p_y, r)$ 
9:   if  $PDB_{L_m}[\alpha]$  is None then
10:     $PDB_{L_m}[\alpha] \leftarrow$  new hash table  $H$ 
11:   if  $PDB_{L_m}[\gamma]$  is None then
12:     $PDB_{L_m}[\gamma] \leftarrow$  new set  $\mathcal{S}_r$ 
13:   if  $PDB_{L_m}[\alpha][\beta]$  is None then
14:     $PDB_{L_m}[\alpha][\beta] \leftarrow (\mathbf{x}', y)$ 
15:    insert  $y$  into the set at  $PDB_{L_m}[\gamma]$ 
16:    insert  $r$  into  $\mathcal{R}$ 
17: return  $\mathcal{R}$ 

```

Algorithm 3: Preprocessing and inserting $B \subset D_m$ into PDB_{L_m}

²A set is a data structure describing an unordered collection with no duplicate elements.

4.3.2 Complexity Estimation

As described in Section 4.1.4, a region is said to be complex if it contains more than one unique label. Otherwise, a region is simple. Since the data within a region already represents a cluster created by a locality-sensitive hashing function h , the existence of multiple classes within a single region indicates a non-linear decision boundary. On that basis we differentiate how a region is processed in the subsequent services of the pipeline. Furthermore, the complexity state of a region may vary, depending on the scope it is observed. Note that since the projection matrix \mathbf{M} that is used to construct h is initialized with the same values in every L_m , all hashes that were computed by h are globally comparable. This means that similar data points from different datasets, e.g., $\mathbf{x}_i \in D_1$ and $\mathbf{x}_j \in D_2$, $\mathbf{x}_i \sim \mathbf{x}_j$ may be hashed to the same region $h(\mathbf{x}_i) = h(\mathbf{x}_j)$. However, it is also possible that the corresponding labels $y_i \in D_1$ and $y_j \in D_2$ are not equal. Thus, a certain region may contain only a single unique label in both local scopes but multiple unique labels in the global scope and therefore lead to a different global view on that region's complexity state. Given that, the complexity estimation service acts as a bridge between the local and global components and answers the question, which regions are considered to be complex in a global scope.

First, a set of incoming regions \mathcal{R}_{in} is received on the C_{L_m} . Then, for each region $r \in \mathcal{R}_{\text{in}}$ the following operations are executed (see Algorithm 4). The set of unique labels \mathcal{S}_r for a particular region within a local scope has been stored in Algorithm 3 as auxiliary metadata, which is now retrieved from the PDB_{L_m} by constructing the corresponding key γ . In the next step, \mathcal{S}_r has to be stored in the PDB_G . Therefore, another key δ is constructed by concatenating the prefix constant p_y , the region r and the current local infrastructure identifier m , which prevents the collision of information from different infrastructures. After \mathcal{S}_r is stored on a global level at $PDB_G[\delta]$, the label set information for that region from all members in the CIDS is aggregated. That aggregated view is essentially the global complexity state for that region. By iterating over all member identifiers in the CIDS, multiple keys δ are constructed. Each key retrieves the specific label set \mathcal{S}_r of a member and inserts its content into the temporary set \mathcal{S}_t , collecting the local label sets.

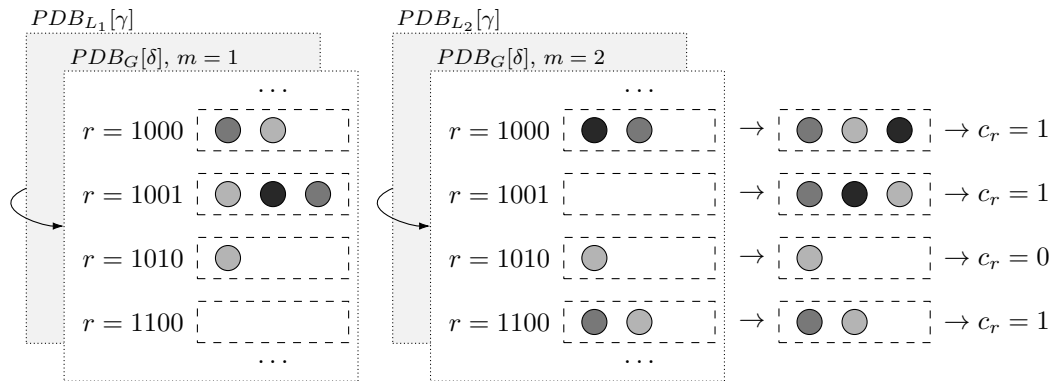


Figure 4.5: Illustration of the complexity estimation algorithm with two local infrastructures. Each local label set at $PDB_{L_m}[\kappa]$ is synchronized into the global pattern database at $PDB_G[\delta]$, where δ is constructed with m . Per region, the union operation is applied on the global label sets, whereupon the complexity is derived from.

After collecting all label sets in \mathcal{S}_t , the complexity state is obtained by simply evaluating the cardinality $|\mathcal{S}_t|$. If there is more than one class in a region on a global scope, that is $|\mathcal{S}| > 1$, then assign a true value to the global complexity variable c_r . Otherwise, assign a false value. In order to store c_r , the key κ is created by concatenating the prefix constant p_c and the region r . Note, that $PDB_G[\kappa]$ is only updated, if storing c_r changes the state that is already persisted. This is because, if an update is executed, this information has to be propagated to the next service. Thus, in that case, the region r is inserted into \mathcal{R}_{out} , which is subsequently sent into the global event channel C_G in order to inform services in all local infrastructures about the update.

Input: Regions \mathcal{R}_{in}

Output: Regions \mathcal{R}_{out}

```

1:  $\mathcal{R}_{out} \leftarrow$  new Set
2:  $m \leftarrow \text{getID}()$  ► current local infrastructure identifier
3: for each  $r$  in  $\mathcal{R}$  do
4:    $\gamma \leftarrow \text{concatenate}(p_y, r)$ 
5:    $\mathcal{S}_r \leftarrow PDB_{L_m}[\gamma]$ 
6:    $\delta \leftarrow \text{concatenate}(p_y, r, m)$ 
7:    $PDB_G[\delta] \leftarrow \mathcal{S}_r$ 
8:    $\mathcal{S}_t \leftarrow \emptyset$ 
9:   for each  $m$  in  $\{1, \dots, M\}$  do
10:     $\delta \leftarrow \text{concatenate}(p_y, r, m)$ 
11:     $\mathcal{S}_t \leftarrow \mathcal{S}_t \cup PDB_G[\delta]$ 
12:   if  $|\mathcal{S}_t| > 1$  then
13:      $c_r \leftarrow 1$ 
14:   else
15:      $c_r \leftarrow 0$ 
16:    $\kappa \leftarrow \text{concatenate}(p_c, r)$ 
17:   if  $PDB_G[\kappa] \neq c_r$  then
18:      $PDB_G[\kappa] \leftarrow c_r$ 
19:     add  $r$  to  $\mathcal{R}_{out}$ 
20: return  $\mathcal{R}_{out}$ 

```

Algorithm 4: Creating a global complexity state by combining local complexity states

4.3.3 Generative Fitting

The generative fitting service is the most demanding procedure in the context of processing resources. The service represents the filtering and compression operations presented in Section 4.1. There are two scenarios based on the region's complexity. If the region is not complex, no further actions are taken except it formally was complex. Then, existing models have to be deleted, since they are not longer used. And if the region is complex, generative models are provided, which represent the medium for exchanging information on attacks. More specifically, multiple Gaussian Mixture Model (GMM) are fitted on each label-subset of a region's data, which was stored in the indexing step in Section 4.3.1. According to a model selection process that evaluates the efficacy of each GMM, the best model is stored in the global pattern database, accessible to every member in the CIDS to sample synthetic data from.

This way, every member has access to the global knowledge from all local infrastructures in order to enhance the local dataset that is used for fitting a classifier. Thus, this service is the key for providing *privacy* and *minimal overhead* while exchanging information. Considering the length and complexity of the complete algorithm, the main procedure is outlined first in Algorithm 5 and then the details on important sub-routines are elaborated subsequently.

Regions that have been updated in the preceding service are received as events $r \in \mathcal{R}_{\text{in}}$. Since the data is further organized per label within a region, the label set for a region \mathcal{S}_r is retrieved. Additionally, the complexity state of the region c_r is checked. Then, if the region is not complex, no model fitting is executed. Instead, potentially existing models are deleted from storage. This is the case, if the complexity status of the region has been changed from complex to simple. But if the region is currently complex, the generative model fitting procedure is triggered where new models are created and already existing models are updated. For that, from every hash table within a region, the original flow samples are extracted and collected in \mathcal{X}_α , which is then stored in T with the corresponding label as the key. The goal is to fit a model on each \mathcal{X}_α within a region, such that the collection of models for a region can be used in combination for sampling the synthetic data. Note that this is a specific process for the employed generative algorithm. Since GMMs cannot be conditioned on multiple labels.

Input: Regions \mathcal{R}_{in}

Output: Regions \mathcal{R}_{out}

```

1:  $\mathcal{R}_{\text{out}} \leftarrow \emptyset$ 
2:  $m \leftarrow \text{getID}()$ 
3: for each  $r$  in  $\mathcal{R}_{\text{in}}$  do
4:    $\kappa \leftarrow \text{concatenate}(p_c, r)$ 
5:    $\delta \leftarrow \text{concatenate}(p_y, r, m)$ 
6:    $c_r \leftarrow PDB_G[\kappa]$ 
7:    $\mathcal{S}_r \leftarrow PDB_G[\delta]$ 
8:   if  $c_r = 0$  then
9:     for each  $y$  in  $\mathcal{S}_r$  do
10:       $\omega \leftarrow \text{concatenate}(p_d, r, y, m)$ 
11:      delete model in  $PDB_G[\omega]$ 
12:   else
13:      $T \leftarrow \text{new hash table}$ 
14:     for each  $y$  in  $\mathcal{S}_r$  do
15:        $\alpha \leftarrow \text{concatenate}(p_x, r, y)$ 
16:        $\mathcal{X}_\alpha \leftarrow \text{extract values (flows) from } PDB_{L_m}[\alpha]$ 
17:        $T[y] \leftarrow \mathcal{X}_\alpha$ 
18:      $T \leftarrow \text{upsampling}(T)$ 
19:     for each  $(y, F_y)$  in  $T_F$  do
20:        $\text{GMM} \leftarrow \text{modelSelection}(y, F_y)$ 
21:        $\omega \leftarrow \text{concatenate}(p_d, r, y, m)$ 
22:        $PDB_G[\omega] \leftarrow \text{GMM}$ 
23:     add  $r$  to  $\mathcal{R}_{\text{out}}$ 
24: return  $\mathcal{R}_{\text{out}}$ 

```

Algorithm 5: Generative Fitting (Main Procedure)

Note that this is a specific process for the employed generative algorithm. Since GMMs cannot be conditioned on multiple labels, multiple single label models have to be fitted. Subsequently, upsampling operations prepare the collected region data in T for the model fitting (see Algorithm 6). After that, the model selection process is started sequentially for each available label in the region (see Algorithm 7). Finally, the best fitted model is stored in the PDB_G .

So far, the main procedure has been outlined. Next, the details on the upsampling are elaborated (see Algorithm 6). As each \mathcal{X}_α is used for the fitting of a GMM and since some of these flow data subsets of a region potentially exhibit a low number of samples, an upsampling process may need to be applied. The upsampling process ensures that the fitting algorithm for the GMM is able to work. For that, the number of samples has to be at least equal to the number of components of the GMM which in turn is at most equal to the number of dimensions of the training dataset \mathcal{X}_α . And since different parameters for the number of components are tried during the model selection, the upper limit for the parameter is used as a comparison value. In this case the upper limit for the number of components is the number of dimensions of the training data. If this is not the case, the upsampling fills the lacking samples artificially.

For the initialization of the responsibilities of the mixture components within the fitting procedure of the GMM the k-means algorithm is used to find distinct clusters within \mathcal{X}_α . The resulting cluster assignments for each $\mathbf{x} \in \mathcal{X}_\alpha$ are then used as initial values for the responsibilities. A supersampling process results in duplicate points that could lead to a smaller number of distinct clusters found by the k-means algorithm than the number of components specified in the model. Therefore, the upsampling is realized by generating near neighbours per sample.

First, the number of neighbours to generate per sample N_Δ is determined by dividing the difference of the dimensionality of the flow data $\dim(\mathcal{X}_\alpha)$ and the number of data points $|\mathcal{X}_\alpha|$ by $|\mathcal{X}_\alpha|$ using an integer division. This ensures that each original data point \mathbf{x} contributes an equal share to the total amount of newly sampled points $\hat{\mathbf{x}}$. In case, the result of the integer division is zero, one is added to the result. Then for each data point $\mathbf{x} = [x_1, \dots, x_D]^\top$, nearest neighbours are generated by sampling from a uniform distribution $\mathcal{U}(a, b)$.

Input: Hash table T with labels y as keys and sets of flows \mathcal{X} as values

Output: Hash table T with upsampled sets of flows

```

1: for each  $(y, \mathcal{X}_\alpha)$  in  $T$  do
2:   if  $y \neq 0$  and  $|\mathcal{X}_\alpha| < \dim(\mathcal{X}_\alpha)$  then
3:      $\hat{\mathcal{X}} \leftarrow \emptyset$ 
4:      $N_\Delta \leftarrow \lfloor \dim(\mathcal{X}_\alpha) - |\mathcal{X}_\alpha| / |\mathcal{X}_\alpha| \rfloor + 1$ 
5:     for each  $\mathbf{x}$  in  $\mathcal{X}_\alpha$  do
6:       for each  $n$  in  $\{1 \leq n \leq N_\Delta\}$  do
7:          $\hat{\mathbf{x}} \leftarrow [s(x_1), \dots, s(x_D)]^\top$  with  $s(x_d) \sim \mathcal{U}(a, b)$ 
8:         add  $\hat{\mathbf{x}}$  to  $\hat{\mathcal{X}}$ 
9:      $\mathcal{X}_\alpha \leftarrow \mathcal{X}_\alpha \cup \hat{\mathcal{X}}$ 
10:     $T[y] \leftarrow T[y] \cup \mathcal{X}_\alpha$ 
11: return  $T$ 

```

Algorithm 6: Binary Splitting and Upsampling of Region Data

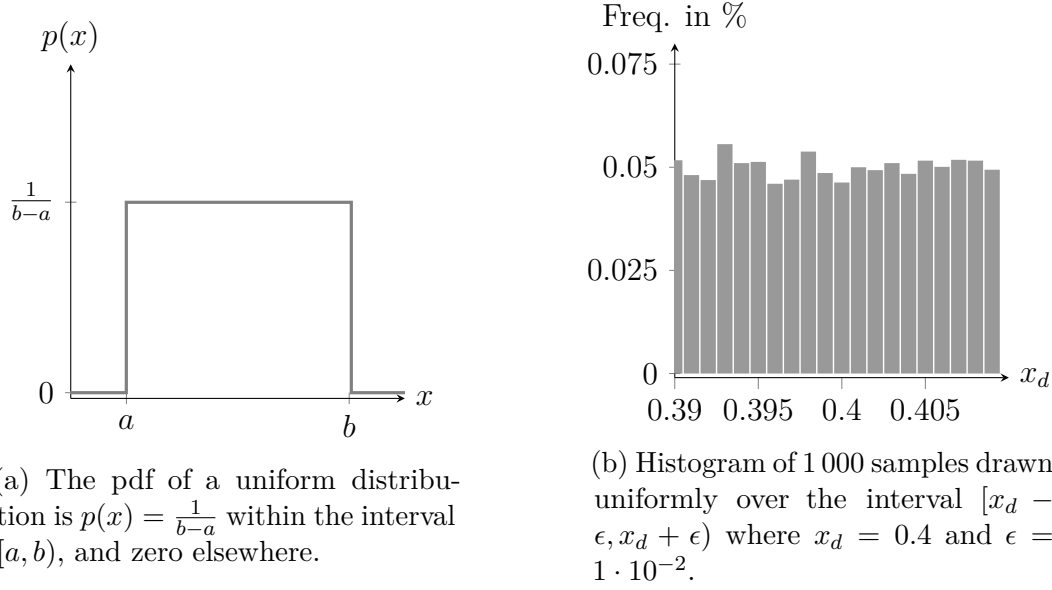


Figure 4.6: Nearest neighbours are generated by sampling each feature value from a the uniform distribution.

That way, the nearest neighbour of \mathbf{x} is the concatenation of the sampled feature values as $\hat{\mathbf{x}} = [s(x_1), \dots, s(x_D)]^\top$, where $s(x_d) \sim \mathcal{U}(a, b)$ is defined as the value sampled from the uniform distribution within the interval $[x_d - \epsilon, x_d + \epsilon)$. The value ϵ controls the size of the interval of the uniform distribution. The larger the value for ϵ , the further the newly generated values deviate from the original feature values. In Figure 4.6b the value for a single feature x_d is drawn uniformly at random. The original value of the feature was $x_d = 4$, which was extended by $\epsilon = 1 \cdot 10^{-2}$. By choosing a relatively small value for ϵ , it is ensured that the generated nearest neighbours do not alter the original data distribution significantly, while enabling a more ideal fitting of the GMM for that set of data points. Finally, the generated neighbours and the original data points are combined. After processing each pair (y, \mathcal{X}_α) , the hash table T is returned to the main procedure (Algorithm 5) for the subsequent model selection.

In the next phase of the algorithm, one GMM is selected per unique label within a region. During the selection process multiple models are fitted with different model parameters using a flow data subset \mathcal{X}_α . Since the resource demands of the Expectation Maximization Algorithm (EM Algorithm) for fitting a GMM are relatively high, the dimensionality of the training data is reduced by applying a dimensionality reduction via Principal Component Analysis (PCA). Later in the pipeline, when sampling data from the GMMs, the inverse operation of the corresponding PCA is applied on the synthetic data in order to restore the original feature space. Therefore, the parameters of the PCA have to be stored in the PDB_G along with the parameters of the GMM.

Note, that during the application of PCA in the first place, information within the data is lost by only keeping the components that describe most of the variance of the data. Of course, the result of the inverse transformation would then only be an approximation of the original data. However, the input for the inverse transformation is going to be the synthetic data. Thus, we accept the loss and focus on the fact that the synthetic data is transformed back into the original feature space, such that the synthetic data resembles more the original data as it was captured, increasing its compatibility.

The model selection is specified in Algorithm 7. First PCA is applied on \mathcal{X}_α resulting in a set of flows \mathcal{X}'_α with a reduced feature set. The number of components of the PCA has to be set heuristically or a threshold has to be set, which defines the minimum amount of variance that needs to be explained by a specific number of components. After the compression, the parameter search for the GMM is started. In general, there is no exact method to determine the optimal parameters for a GMM, such that different parameter settings have to be evaluated. For that, the search space is defined by two dimensions, namely the number of components and the type of covariance matrix that is used for each component. The set of numbers that is used for specifying the number of components is defined as $\mathcal{C} = \{4c \mid c \in \mathbb{N}, 1 \leq c \leq \dim(\mathcal{X}_1)\}$. The covariance matrix can either be a standard covariance matrix with a full set of entries or can be an approximation with entries only on the diagonal of the matrix, i.e., we define $\Sigma = \{\text{"full"}, \text{"diagonal"}\}$. The reason behind the choice of both types of covariance matrix is also motivated by heuristical optimization. The full covariance matrix can result in overfitting, especially on small datasets, whereas the diagonal matrix acts as a type of regularization to the model. However, depending on the data the diagonal type sometimes also leads to an underfitting of the model.

After fitting a GMM on \mathcal{X}'_1 the first metric for the selection is calculated. Precisely, the bayesian information criterion (BIC) is calculated as in Equation ?? (see Section 2.3.3). Note, that for the case of a diagonal covariance matrix, the number of entries of the covariance matrix to estimate changes from $\frac{D(D+1)}{2}$ to D . Thus, given a GMM with K mixture components, each exhibiting a diagonal covariance matrix, and a dataset \mathcal{X}_1 consisting of N data points and D features, the BIC is defined as

$$\text{BIC}(\text{GMM}|\mathcal{X}_1) = (KD + D + K - 1) \ln(N) - 2 \ln(\hat{L}). \quad (4.2)$$

After that, a second evaluation metric is calculated (see Algorithm 8). The process that is used to gather that metric is called adversary evaluation and is based on the principles of Generative Adversarial Networks (GANs).

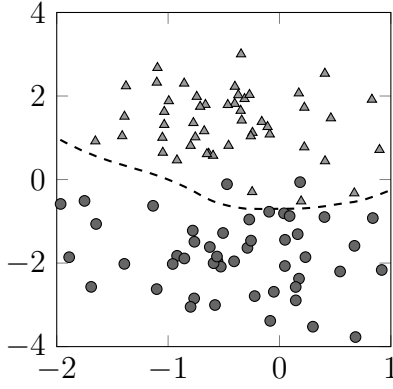
Input: Dataset \mathcal{X}_1

Output: Tuple (GMS , GMM, PCA)

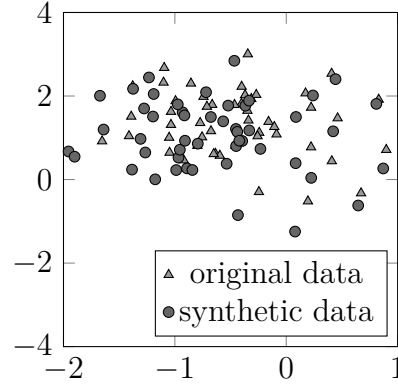
```

1:  $\mathcal{X}'_1 \leftarrow \text{PCA}(\mathcal{X}_1)$ 
2:  $\mathcal{C} \leftarrow \{4c \mid c \in \mathbb{N}, 1 \leq c \leq \dim(\mathcal{X}_1)\}$ 
3:  $\Sigma \leftarrow \{\text{"full"}, \text{"diagonal"}\}$ 
4:  $L \leftarrow$  new list
5: for each  $c$  in  $\mathcal{C}$  do
6:   for each  $\Sigma$  in  $\Sigma$  do
7:      $\text{GMM} \leftarrow \text{fitGaussianMixture}(\mathcal{X}'_1, c, \Sigma)$ 
8:      $\text{BIC} \leftarrow \text{BIC}(\text{GMM}, \mathcal{X}'_1)$ 
9:      $\text{ACC} \leftarrow \text{AdversaryEvaluation}(\mathcal{X}_1, \text{GMM}, \text{PCA})$ 
10:     $GMS \leftarrow \text{GMS}(\text{BIC}, \text{ACC})$ 
11:    add ( $GMS$ , GMM, PCA) to  $L$ 
12: sort  $L$  according to the values of  $GMS$ 
13: return ( $GMS$ , GMM, PCA) with the lowest value for  $GMS$ 
```

Algorithm 7: Model Selection



(a) A poor fitted generative model: The original data (triangles) and the synthetic data (circles) can be easily separated by a classifier.



(b) A well fitted generative model: The synthetic data resemble the original data well, such that a separation is not easy.

Figure 4.7: Adversary evaluation: separate original and fake data.

Fitting a Generative Adversarial Network (GAN) involves a discriminator function, i.e., classifier that tries to distinguish between the original and synthetic data. In other words, the generative algorithm synthesizes fake data, which resembles the original data. Based on that, a dataset is assembled by combining fake data labeled as the positive class (1) and original data labeled as the negative class (0) or vice versa. This dataset is shuffled and split into a training and test proportion.

Then, a discriminative model is trained on the training proportion, trying to find distinguishing features within both classes, allowing a distinction to be made. Within the evaluation step, the discriminator is tested on its ability to separate fake and original data. The lower the score of the discriminator, the better the generative model. Figure 4.7 illustrates two scenarios. In the first scenario (a), the generative model has been fitted poorly, because the synthetic data can be easily separated from the original data as indicated by the decision boundary (dashed line). In the second scenario (b), the generative model performs well by creating synthetic data that could not be separated from the original data.

Input: \mathcal{X}_1 , GMM, PCA

Output: ACC from decision tree model DT

- 1: $\tilde{\mathcal{X}}'_1 \leftarrow \text{sample } |\mathcal{X}_1| \text{ data points from GMM}$
- 2: $\tilde{\mathcal{X}}_1 \leftarrow \text{PCA}^{-1}(\tilde{\mathcal{X}}'_1)$
- 3: $\mathcal{Y} \leftarrow \{1\}$
- 4: $\tilde{\mathcal{Y}} \leftarrow \{0\}$
- 5: $\mathcal{D} \leftarrow \text{concatenate}(\mathcal{X}_1 \times \mathcal{Y}, \tilde{\mathcal{X}}_1 \times \tilde{\mathcal{Y}})$
- 6: $\mathcal{D}_{\text{train}}, \mathcal{D}_{\text{test}} \leftarrow \text{shuffleSplit}(\mathcal{D})$
- 7: $DT \leftarrow \text{fitDecisionTree}(\mathcal{D}_{\text{train}})$
- 8: $\hat{\mathcal{Y}} \leftarrow \text{predict } \mathcal{X}_{\text{test}} \subset \mathcal{D}_{\text{test}} \text{ with } DT$
- 9: $ACC \leftarrow ACC(\mathcal{Y}_{\text{test}}, \hat{\mathcal{Y}})$
- 10: **return** ACC

Algorithm 8: Adversary Evaluation

In order to quantify the performance of the discriminator within the adversary evaluation, a classification metric is calculated. Since the original and synthetic data is equal in size and the posed problem is binary the accuracy score (ACC) is chosen, which is defined as

$$ACC = \frac{TP + TN}{TP + TN + FP + FN} \quad (4.3)$$

For each iteration in the model selection process, both the BIC and the ACC are stored. After all parameter combinations have been exhausted and all resulting models have been evaluated a combined metric that we call generative model selection (GMS) is calculated from the BIC and ACC for each model. For that, the value range of both metrics must be aligned, such that the BIC is normalized into the range $[0, 1]$ by applying the min-max-normalization from Equation 4.1. After that, the mean is calculated for each metric pair as defined in Equation 4.4. Finally, the model with the lowest combined GMS is selected.

$$GMS = \frac{1 - ACC + BIC}{2}. \quad (4.4)$$

The model parameters of both the GMM and the PCA are stored in the PDB_G . In numbers, these can range, depending on which type of covariance matrix is chosen for the GMM. PCA on the other hand, requires a $D \times M$ projection matrix, with D being the dimensions of the original data space and M being the number of dimensions in the projected subspace. Note that $|\mathcal{S}_y|$ defines the number of unique labels within a region, which effectively determines the number of model pairs (GMM, PCA) that are to be stored per region. Therefore, per region, the number of parameters to store is at least

$$|\mathcal{S}_y| (2KD + K - 1 + MD)$$

and at most

$$|\mathcal{S}_y| \left((KD + K \frac{D(D+1)}{2} + K - 1) + MD \right).$$

4.3.4 Classifier Fitting

4.4 Summary

Chapter 5

Experimental Evaluation

5.1 Flow Feature Analysis

5.1.1 Datasets

5.1.2 Feature Extraction and Preprocessing

5.2 Experimental Setup

5.2.1 Implementation Details

5.2.2 Methodologies

5.3 Evaluation Results

5.3.1 Classification Improvement

5.3.2 Overhead Reduction

5.4 Summary and Discussion

Chapter 6

Conclusion and Outlook

6.1 Conclusion

6.2 Outlook

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List of Abbreviations

<i>ACC</i>	accuracy score
<i>GMS</i>	generative model selection
<i>c</i> -ANN	<i>c</i> -approximate nearest-neighbour problem
<i>cr</i> -ANN	<i>cr</i> -approximate nearest-neighbour problem
BIC	bayesian information criterion
CIDS	Collaborative Intrusion Detection System
CIDSM	Collaborative Intrusion Detection System Message
DGM	Deep Generative Models
DoS	Denial of Service
DPI	Deep Packet Inspection
DR	Detection Rate
EM Algorithm	Expectation Maximization Algorithm
FPF	Flow Processing Format
FPR	False Postive Rate
GAN	Generative Adversarial Network
GMM	Gaussian Mixture Model
GRP	gaussian random projection
HIDS	Host-based Intrusion Detection System
IDS	Intrusion Detection System
IETF	Internet Enginnering Task Force
IPFIX	IP Flow Information Export
LSH	locality-sensitive hashing
LVM	Latent Variable Model
MLE	Maximum Likelihood Estimation
NIDS	Network-based Intrusion Detection System
NN	nearest-neighbour search problem
ONB	Orthonormal Basis
PCA	Principal Component Analysis
QoS	Quality of Service
R2L	Remote to Local
SPoF	single point of failure
U2R	User to Root

List of Symbols

General Mathematical Notation

\mathbb{N}	natural numbers
\mathbb{R}	real numbers
\mathbb{R}^n	n -dimensional vector space of real numbers
a, b, c	scalars are lowercase
$\mathbf{x}, \mathbf{y}, \mathbf{z}$	vectors are bold lowercase
$\mathbf{A}, \mathbf{B}, \mathbf{C}$	matrices are bold uppercase
$\mathcal{A}, \mathcal{B}, \mathcal{C}$	sets
$\mathbf{x}^\top, \mathbf{A}^\top$	transpose of a vector or matrix
\mathbf{A}^{-1}	inverse of a matrix
$\mathbf{x}^\top \mathbf{y}$	dot product of \mathbf{x} and \mathbf{y}
$B = (\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3)$	(ordered) tuple
$\mathbf{B} = [\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3]$	matrix of column vectors stacked horizontally
$\mathcal{B} = \{\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3\}$	set of vectors
$a \in \mathcal{A}$	a is element of the set \mathcal{A}
$a \notin \mathcal{A}$	a is not element of the set \mathcal{A}
$\{a \in \mathcal{A} \mid \phi\}$	set containing all $a \in \mathcal{A}$ meeting condition ϕ
$ \mathcal{A} $	cardinality of the set \mathcal{A}
$a \gg b$	a is much greater than b

Architecture Specification

$N \in \mathbb{N}$	number of data points; indexed by $n = 1, \dots, N$
$D \in \mathbb{N}$	number of dimensions; indexed by $d = 1, \dots, D$
$M \in \mathbb{N}$	number of members in the CIDS; indexed by $m = 1, \dots, M$
\mathcal{X}	input space

\mathcal{Y}	space of true targets, i.e., classes
\mathcal{D}	training dataset

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